

Design & Reinforcement of Frames.

نسألكم الدعاء

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إذا حملت تطبيق **RC Structures**  على تليفونك المحمول أو اللوح السطحي ستستطيع أن تشغل أفلام شرح للمقاطع التي تحتوى على رمز 

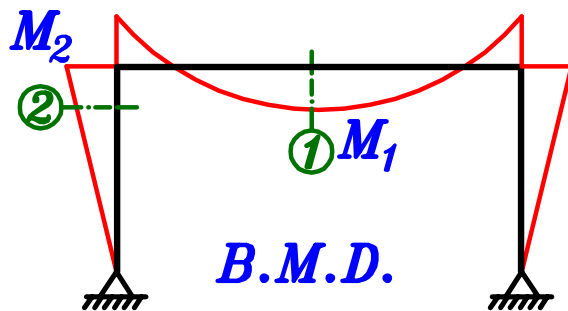
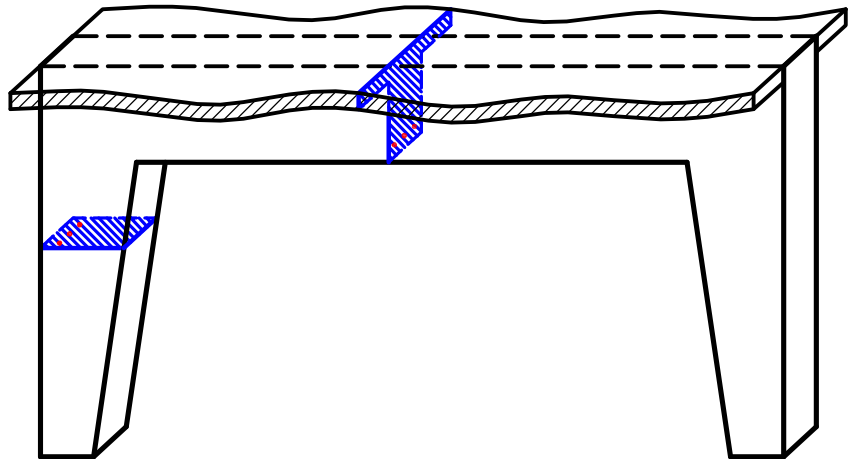
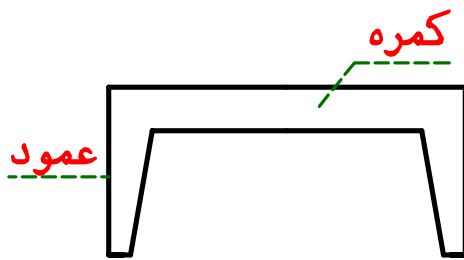
Design & Reinforcement of Frames. Table of Contents.

Design of Sections Subjected to M, P	Page 2
Design of Sections Subjected to M, T	Page 27
Design of Sec. Subjected to Bi-Axial Moment.	Page 35
Stiffness of members.	Page 63
Real Hinge.	Page 66
Columns concrete Dimensions.	Page 67
Reinforcement splices.	Page 69
Reinforcement of Frames.	Page 74
Reinforcement of columns and supports.	Page 76
Reinforcement of Joints.	Page 81
RFT. of Three member Joint.	Page 87
RFT. of Four member Joint.	Page 95
Variable Depth.	Page 97
Critical Sections.	Page 98
Stirrups.	Page 101
Cross Sections.	Page 103
Steps to design a Frame.	Page 104
Steps to draw Frame Concrete Dimensions.	Page 108
Steps to Draw Frame Reinforcement.	Page 111
Example on Design and RFT. of Frames.	Page 119
RFT. of max-max Bending moment for Frames.	Page 269

Design of Frames Sections.

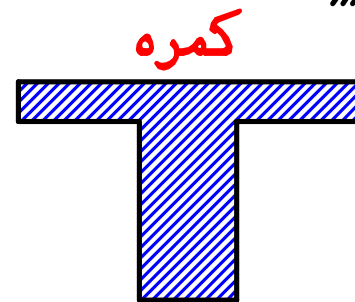
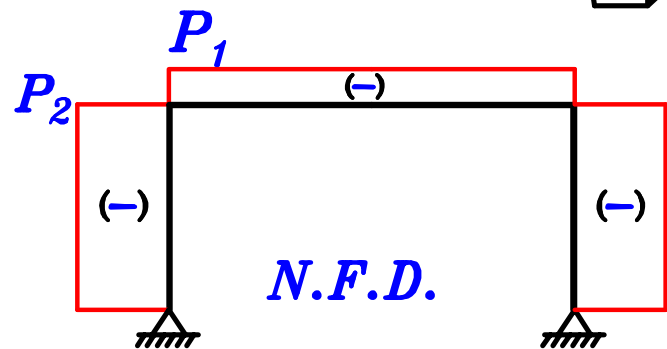
Design of Sections Subjected to M, P

تتعرض القطاعات في ال **Frames** إلى **Moment & Normal** و يمكن أن تكون هذه القطاعات إما في كمّرات أو في أعمده .



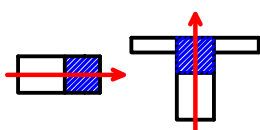
Sec. (2-2)

Designed on M_2, P_2



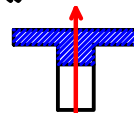
Sec. (1-1)

Designed on M_1, P_1



في حاله وجود M, P يجب عمل تصميم للقطاع على أنه **R-Sec.**
أما في حاله وجود M فقط فيجب مراعاة إذا ما كان القطاع

R-Sec. or T-Sec. or L-Sec.



Steps of Design :

- 1 – Get Dimensions of the section. ($b \times t$)
- 2 – Check *IF P* neglected or not.
- 3 – Get Reinforcement A_s, A_s'

1 – Get Dimensions of the section. ($b \times t$)

Take $b = (300 \text{ mm or } 350 \text{ mm or } 400 \text{ mm})$

To get t get the bigger value of t_1 (Bending), t_2 (Normal)

– Get $d_1 = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}}$ take $C_1 = 3.5$, $J = 0.78$ (as R-Sec.)

$$t_1 = d_1 + \text{cover} \quad \text{where cover} = 50 \text{ mm IF } t \leq 1000 \text{ mm} \\ = 100 \text{ mm IF } t > 1000 \text{ mm}$$

– Get $t_2 \xrightarrow{\text{Take}} \mu = \frac{A_s}{b t_2} = 1.0 \% \rightarrow A_s = \frac{b t_2}{100}$

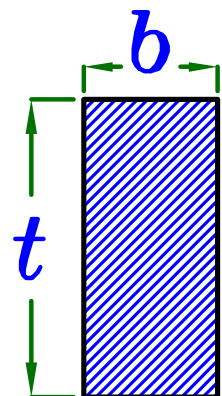
From $P_{u.L.} = 0.35 A_c F_{cu} + 0.67 A_s F_y$

$$\therefore P_{u.L.} = 0.35 b t_2 F_{cu} + 0.67 \frac{b t_2}{100} F_y$$

$$\therefore P_{u.L.} = \left(0.35 b F_{cu} + 0.67 \frac{b}{100} F_y \right) t_2$$

– $t_o =$ The bigger value of t_1 & t_2

– $t = (1.1 \rightarrow 1.3) t_o$



2- Check:

$$\checkmark \checkmark \text{ IF } K = \frac{P_{U.L.}}{F_{cu} b t} \leq 0.04 \rightarrow \text{neglect } P_{U.L.}$$

and Design the Sec. on B.M. only as Beams.

$$\therefore d = d_1 = C_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \quad \begin{array}{l} \text{take } C_1 = 3.5, J = 0.78 \text{ (R-Sec.)} \\ \text{take } C_1 = 6.0, J = 0.826 \text{ (T-Sec., L-Sec.)} \end{array}$$

ملحوظه هامه :

فى بدايه التصميم نعمل تصميم على M, P على أن القطاع **R-sec.**
و لكن اذا أهملنا ال P فنعمل تصميم على M فقط فيجب مراعاة
اذا كان القطاع **R-sec. or T-sec.**

Get
$$e = \frac{M_{U.L.}}{P_{U.L.}}$$

$$\text{IF } \frac{e}{t} \leq 0.05 \rightarrow \text{neglect } M_{U.L.}$$

and Design the Sec. on N.F. only as Columns.

$$P_{U.L.} = 0.35 A_c F_{cu} + 0.67 A_s F_y \quad \text{Take } \mu = 1.0 \%$$

$$\therefore P_{U.L.} = 0.35 A_c F_{cu} + 0.67 \frac{A_c}{100} F_y$$

Get A_c, A_s

يمكن إهمال هذه الخطوه

IF $K = \frac{P_{u.L.}}{F_{cu} b t} > 0.04$ Design the Sec. on both **B.M.** & **N.F.**

3- Get Reinforcement A_s, A_s'

لحساب كميه الحديد طريقتين : ١ - طريقه دقيقه (صعبه)

٢ - طريقه تقريبيه (المعمول بها فى هذا الملف)

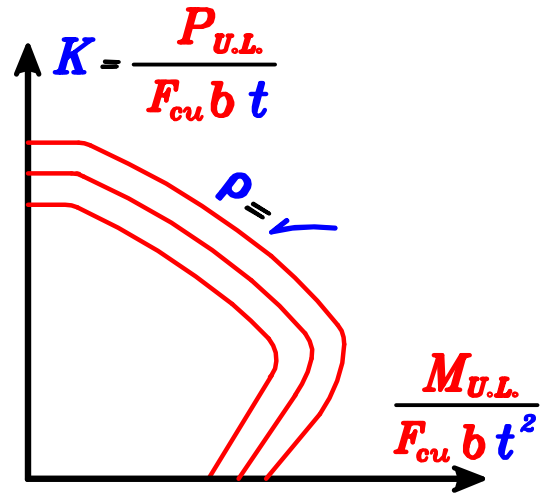
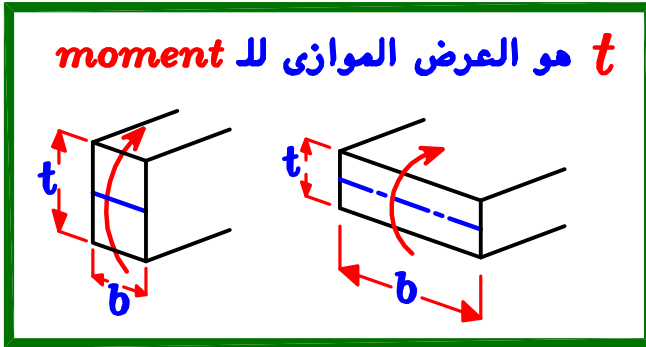
1- Exact Method.

١ - طريقه دقيقه (صعبه)

Use Interaction Diagram

ECCS Page (4-20) → (4-63)

Interaction Diagram. (I.D.)



لتحديد الصفحه المطلوبه نحدد ثلاثه قيم F_y, α, ζ

Chart Key مفتاح الجدول

Chart Key

يوجد فى كل صفحه من صفحات ال **I.D.** فى الجداول مفتاح للجدول لتحديد أى جدول سوف نستخدمه

$F_y = \checkmark$
$\zeta = \checkmark$
$\alpha = \frac{A_s'}{A_s} = 1$

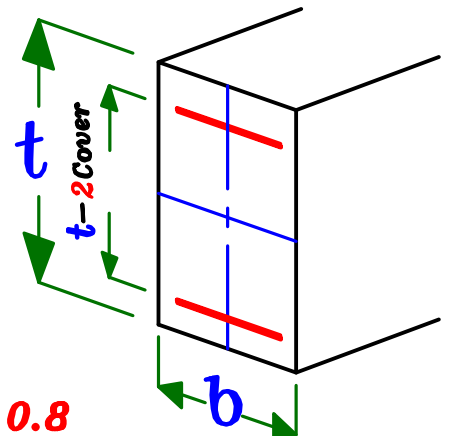
- $F_y = \text{Type of Steel}$ $\begin{cases} 240 \\ 280 \\ 360 \checkmark \\ 400 \checkmark \end{cases}$

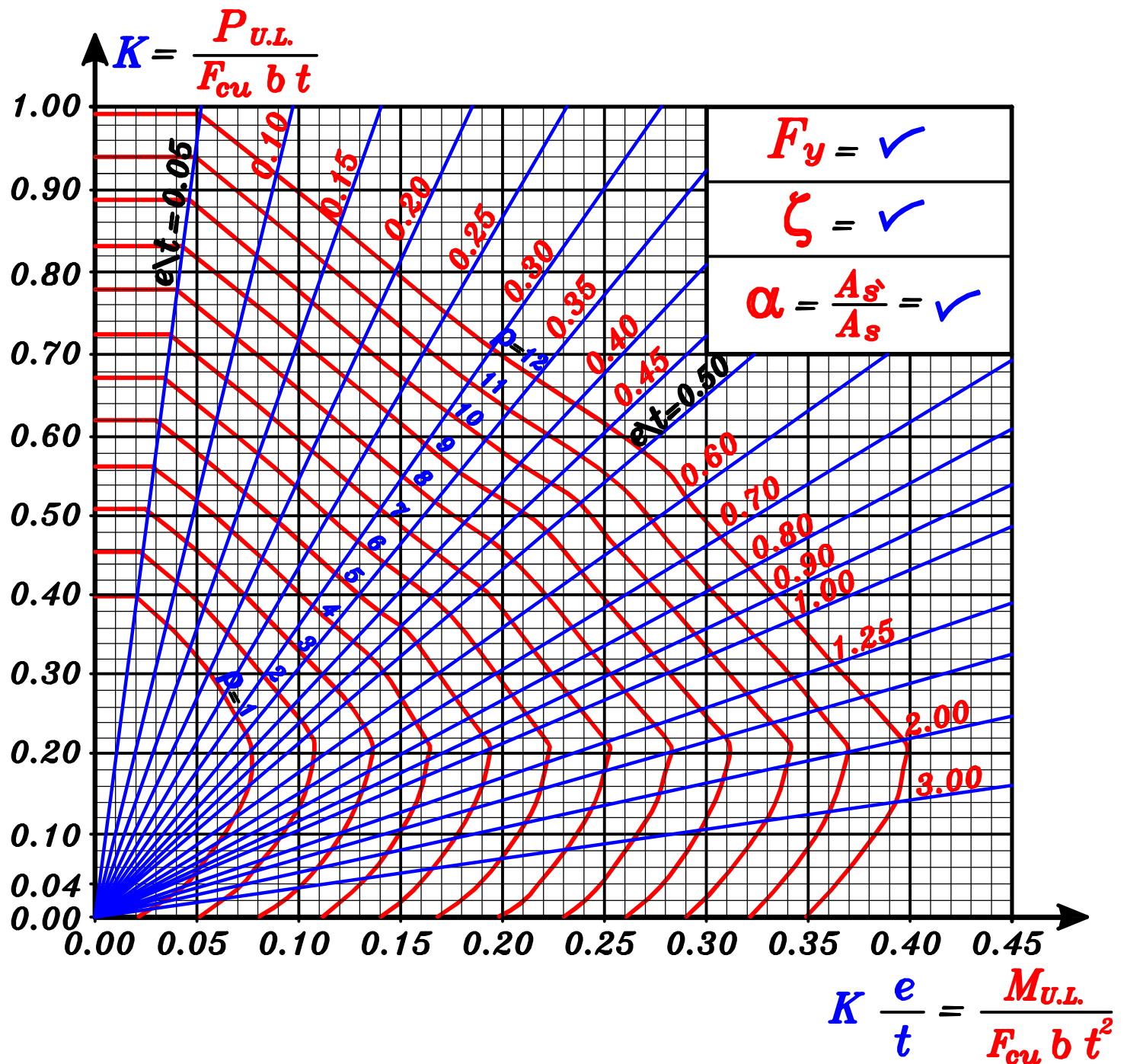
- $\alpha = \frac{A_s'}{A_s} \begin{cases} 0.8 \\ 1.0 \checkmark \end{cases}$ **Design** نسبة تحدد قبل بدء ال
و تؤخذ عادة تساوى ١

- $\zeta = \frac{t - 2\text{Cover}}{t} = \frac{\text{المسافه بين الحديد}}{\text{التخانه الكليه}}$ و تقرب للرقم الأصغر

Example: $t = 800 \text{ mm}$

$$\therefore \zeta = \frac{800 - 100}{800} = \frac{700}{800} = 0.875 \xrightarrow{\text{Take}} \zeta = 0.8$$





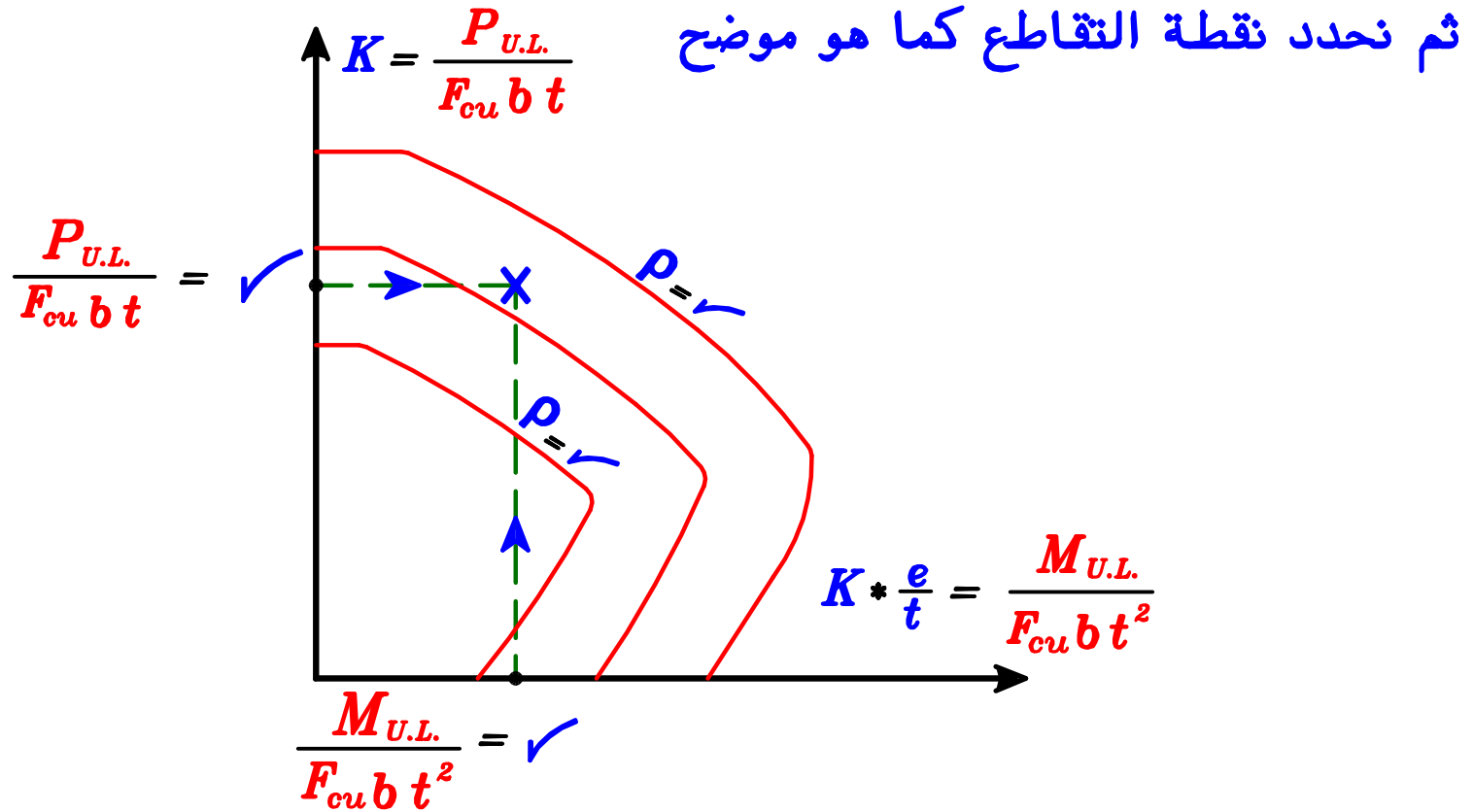
$$\mu = \rho * F_{cu} * 10^{-4}$$

$$A_s = \mu * b * t$$

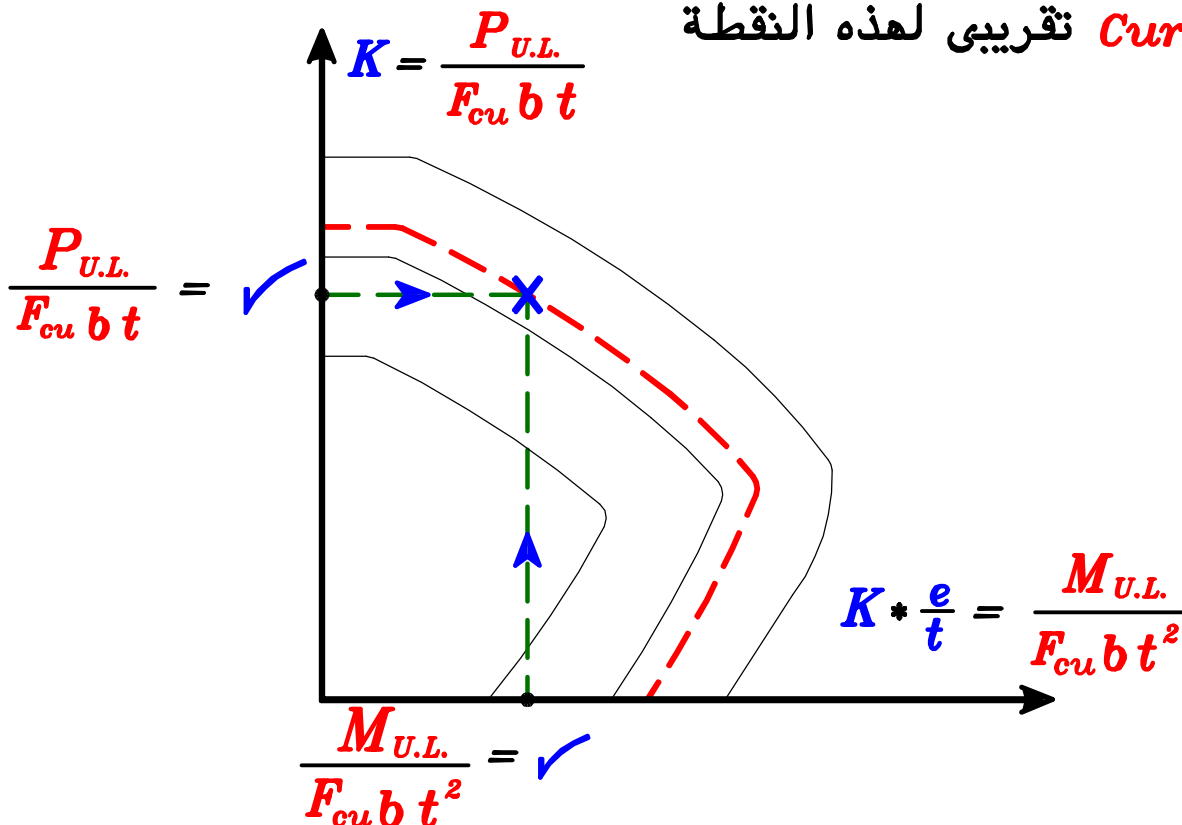
$$A_{s'} = \alpha * A_s$$

١- بعد تحديد ال *Curve* بمعرفة كل من F_y , α , ζ

٢- نحدد قيمة كل من $K = \frac{P_{U.L.}}{F_{cu} b t}$, $K * \frac{e}{t} = \frac{M_{U.L.}}{F_{cu} b t^2}$

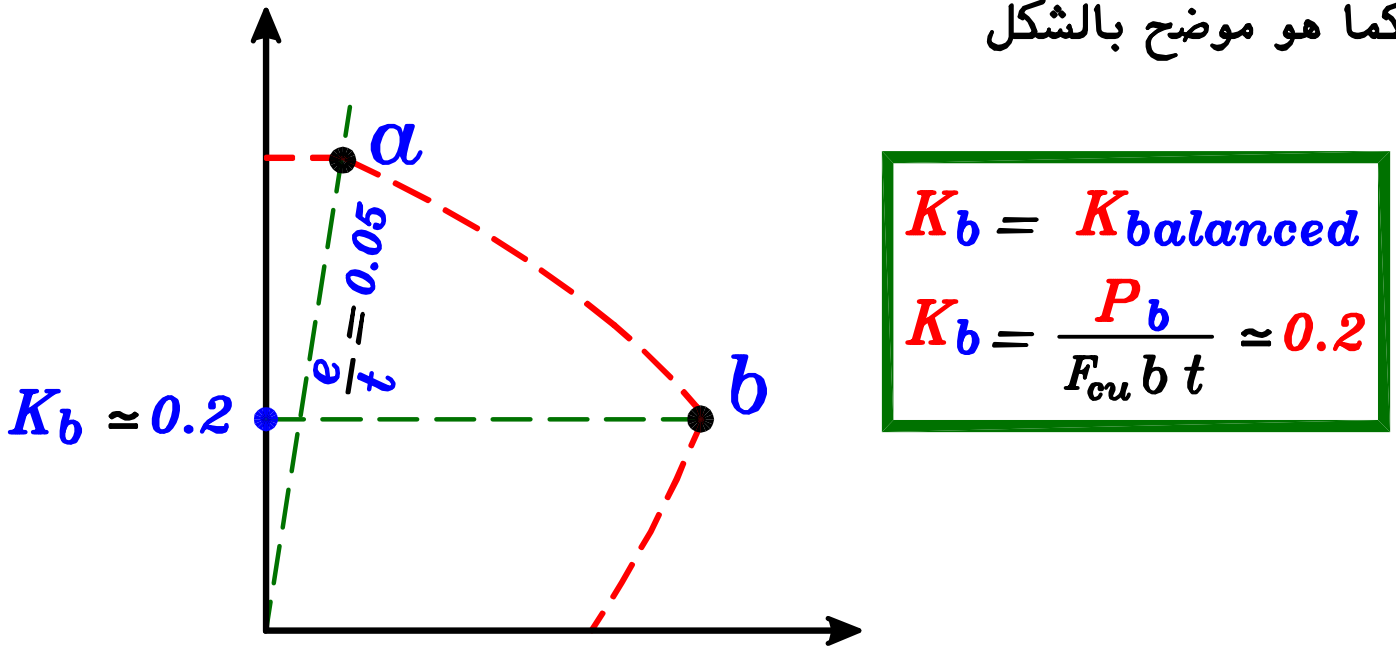


٣- ثم نرسم *Curve* تقريبي لهذه النقطة



٤- نحدد النقطتين a و b على هذا ال *Curve*

كما هو موضح بالشكل



حيث a هي نقطة *min eccentricity*

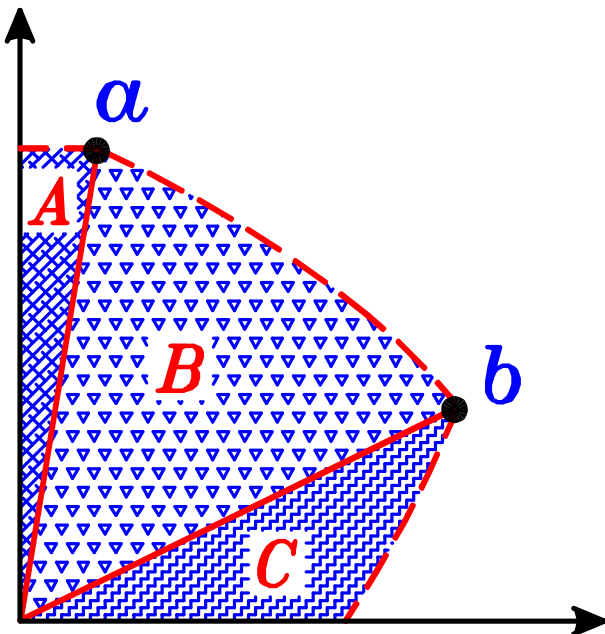
و عند هذه النقطة تكون $\frac{e}{t} = 0.05$

و نقطة b هي نقطة ال *Balanced Failure*

٥- من النقطتين a و b نوصل خطين الى نقطة ال *origin (0,0)*

و نقسم المساحة الى *Zones*

و نحدد طريقة ال *Design*

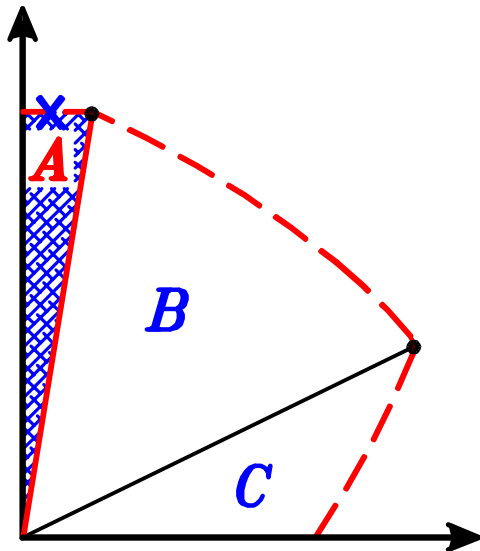


Zone A → Design as *Short Column*

Zone B → Design as *Compression Failure*

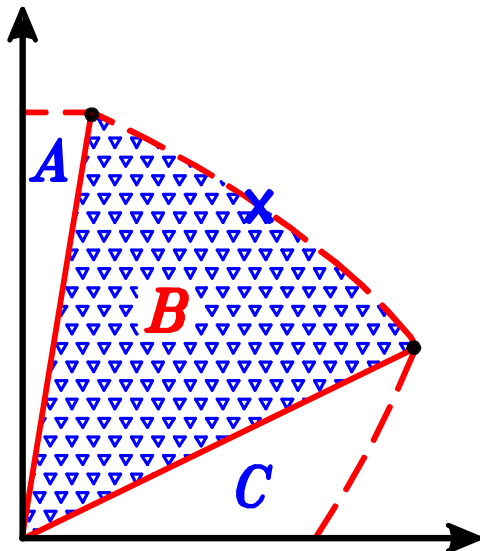
Zone C → Design as *Tension Failure*

بعد تحديد نقطة تقاطع $K = \frac{P_{U.L.}}{F_{cu} b t}$, $K * \frac{e}{t} = \frac{M_{U.L.}}{F_{cu} b t^2}$



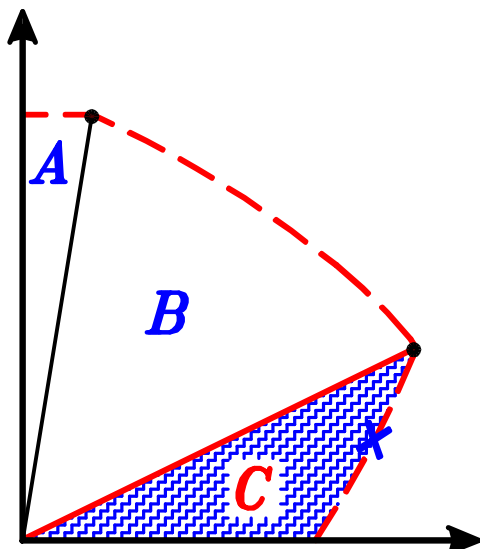
عند وجود نقطة التقاطع عند **Zone A** نهمل وجود ال **moment** و نصمم على ال **Normal** فقط

Design as Short Column using $P_{U.L.}$



عند وجود نقطة التقاطع عند **Zone B** يكون أغلب القطاع على **Compression**

Design as Compression Failure using Interaction Diagram



عند وجود نقطة التقاطع عند **Zone C** يكون أغلب القطاع على **Tension**

Design as Tension Failure using e_s

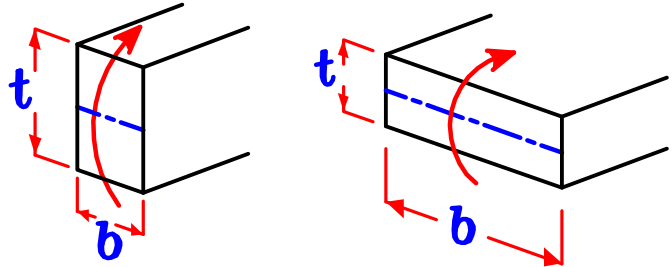
2- Approximate Method.

٢ - طريقه تقريبيه .

(المعمول بها فى هذا الملف)



t هو العرض الموازى لل $moment$



- Get $e = \frac{M_{U.L.}}{P_{U.L.}}$

- Get $\frac{e}{t}$

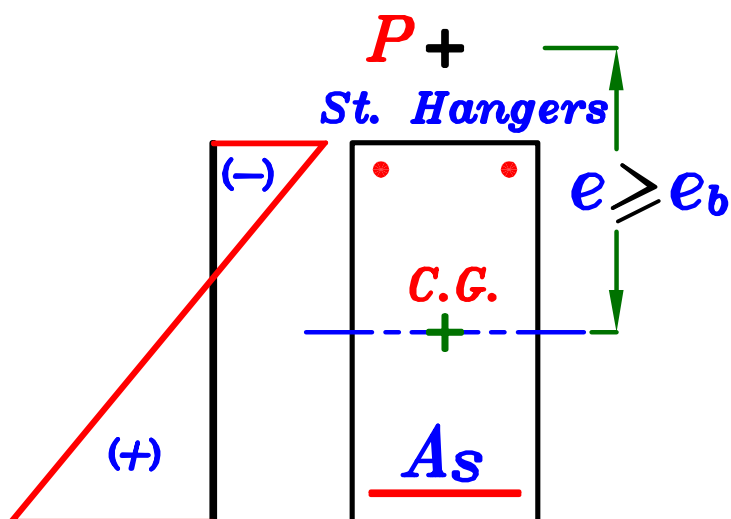
$IF \quad \frac{e}{t}$

$\frac{e}{t} \geq 0.5$

Big Eccentricity
Tension Failure

معناه أن محصله القوى تؤثر خارج القطاع

Use e_s

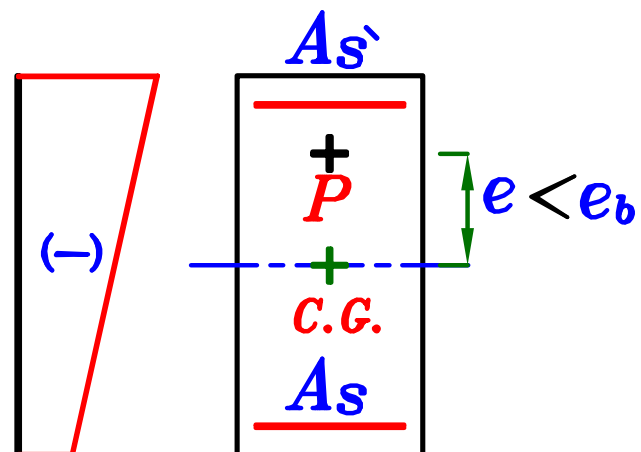


$\frac{e}{t} < 0.5$

Small Eccentricity
Compression Failure

معناه أن محصله القوى تؤثر داخل القطاع

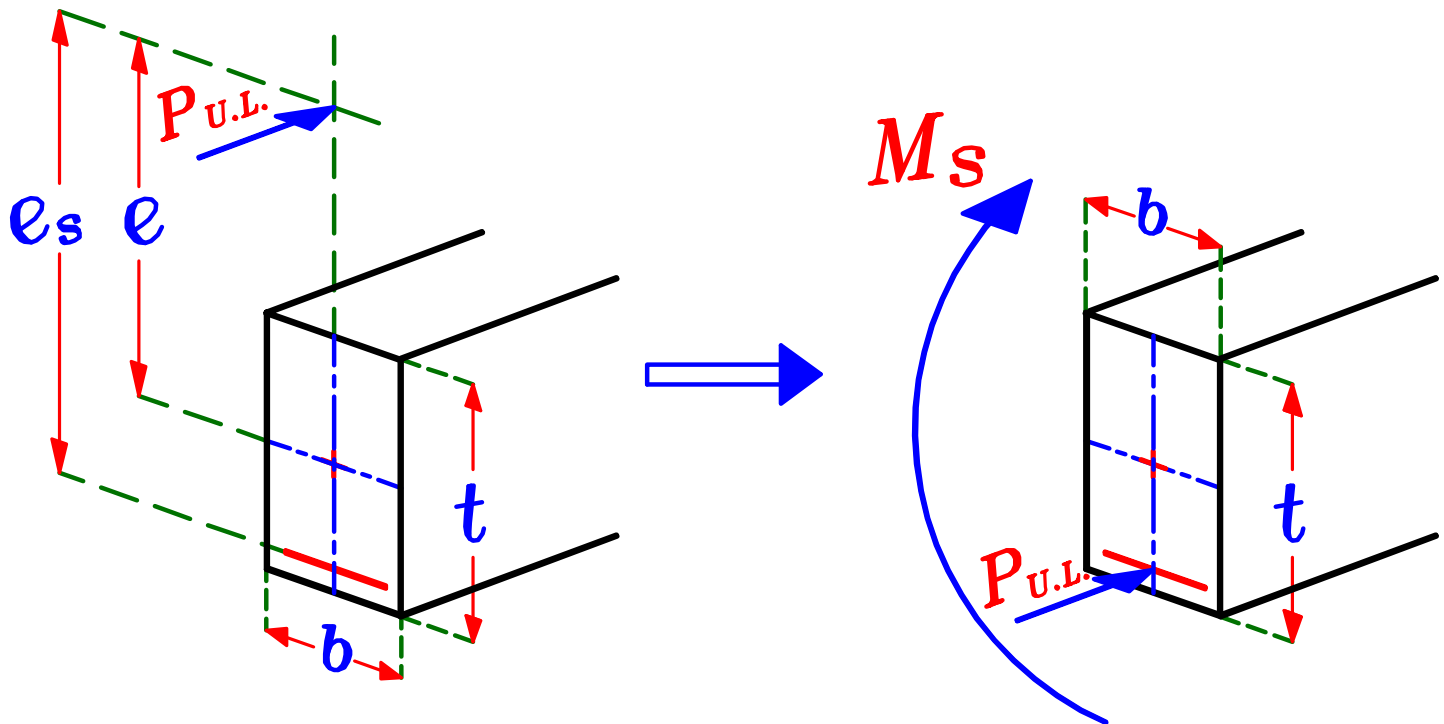
Use $I.D.$





عندما تكون قيمه $\frac{e}{t} \geq 0.5$ معناه أن محصله القوى تؤثر خارج القطاع .
القطاع أقرب لقطاع الكمره منه لقطاع العمود .

أى أن جهه من الخرسانه عليها **Compression** و جهه عليها **Tension**.



Get

$$e = \frac{M_{U.L.}}{P_{U.L.}}$$

Get

$$e_s = e + \frac{t}{2} - c$$

حيث e هى بعد المحصله عن ال **C.G.**
حيث e_s هى بعد المحصله عن ال **steel**

Where: **C** is the Cover $\begin{cases} = 50 \text{ mm} & \text{IF } t \leq 1000 \text{ mm} \\ = 100 \text{ mm} & \text{IF } t > 1000 \text{ mm} \end{cases}$

– Get the moment about Tension steel

$$M_s = P_{U.L.} * e_s$$

– From $d = c_1 \sqrt{\frac{M_s}{F_{cu} b}}$ Get $c_1 = \checkmark \xrightarrow{\text{get}} J = \checkmark$

– Get A_s From

$$A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y / \phi_s)}$$

– Check $A_{s_{min.}}$

Compare area of tension steel with $\left(0.225 * \frac{\sqrt{F_{cu}}}{F_y}\right) * b * d$

IF $A_{s_{req.}} \geq \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y}\right) * b * d \xrightarrow{\text{Take}} A_{s_{req.}}$

IF $A_{s_{req.}} < \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y}\right) * b * d \xrightarrow{\text{Take}} A_{s_{min.}}$

$$A_{s_{min.}} = \left\{ \begin{array}{l} \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y}\right) * b * d \\ 1.3 A_{s_{req.}} \end{array} \right\} \text{الأقل}$$

A_s

Stirrup Hangers.

Stirrup Hangers = $\left(0.1 \rightarrow 0.2\right) A_s$ } الأكبر
2 # 12 Frames

ملحوظه :

سواء كان ال member أفقى أو رأسى يعامل معاملة الكمره
ولكن يفضل أن لا يقل ال stirrup hangers فى ال members
الرأسيه عن $0.4 A_s$ و هذا ليس شرط.

Shrinkage Bars. (IF the sec. in Beam.)

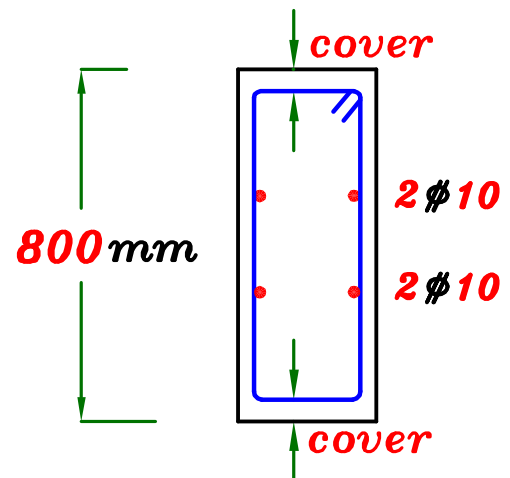
- توضع ال **Shrinkage Bars** عندما تكون $t > 700 \text{ mm}$
- وقيمة ال **Shrinkage Bars** = $2 \phi 10$ at every 300 mm

Example.

IF $t = 800 \text{ mm}$

∴ **No. of Spacings** =

$$= \frac{800 - 100}{300} = 2.33 = 3.0 \text{ Spacing}$$
$$= 2.0 \text{ Bars}$$



Buckling Bars. (Longitudinal Bars)

(IF the sec. in Column.)

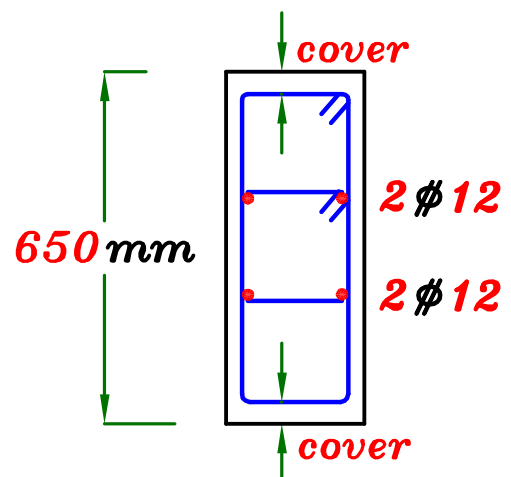
- في الأعمدة التي يؤثر عليها **M & P**.
- يجب وضع أسياخ جانبيه تسمى **Buckling Bars**.
- و توضع أيضاً عندما تكون $t < 700 \text{ mm}$ (ليس مثل ال **Shrinkage Bars**)
- و قيمه ال **Buckling Bars** = $2 \phi 12$ at every 250 mm
- و توضع كانات داخلية بحيث لا تزيد المسافه بين كل فرع كانه و الفرع الذى يليه عن ٣٠٠ مم

Example.

IF $t = 650 \text{ mm}$

∴ **No. of Spacings** =

$$= \frac{650 - 100}{250} = 2.20 = 3.0 \text{ Spacing}$$
$$= 2.0 \text{ Bars}$$



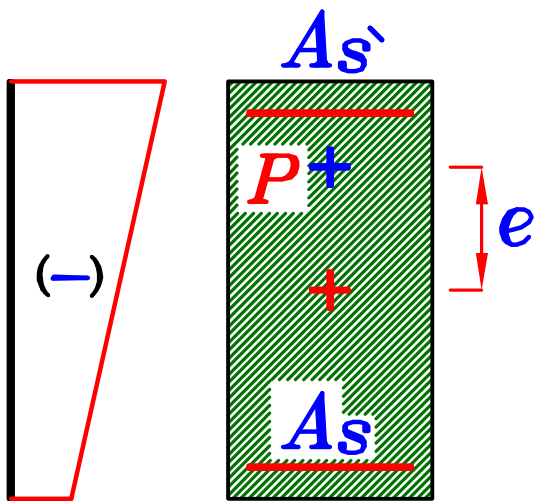
Compression Failure.



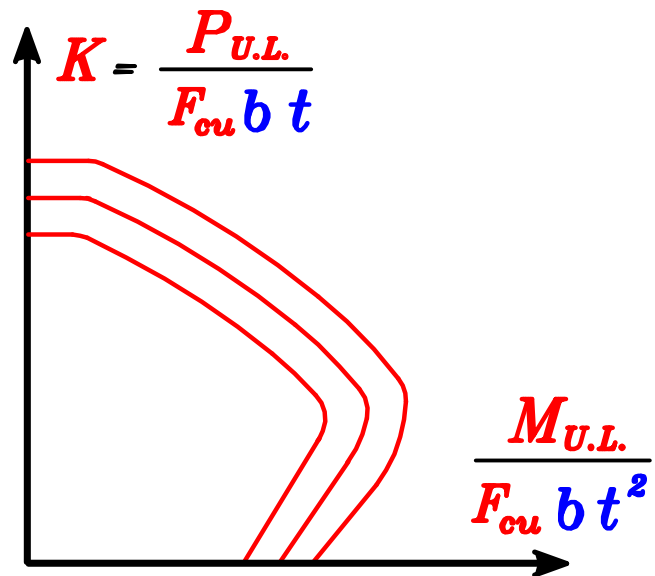
عندما تكون قيمه $\frac{e}{t} < 0.5$ معناه أن محصله القوى تؤثر داخل القطاع .

القطاع أقرب لقطاع العمود منه لقطاع الكمره .

أى يوجد **Compression** على كل القطاع .



سنحتاج لوضع تسليح فى الاتجاهين A_s , A_s' و نستخدم **Interaction Diagram (I.D.)**



و ممكن من ال **(I.D.)** تصميم قطاعات

Big eccentricity or small eccentricity

أى عندما تكون $\frac{e}{t} > 0.5$ or $\frac{e}{t} < 0.5$

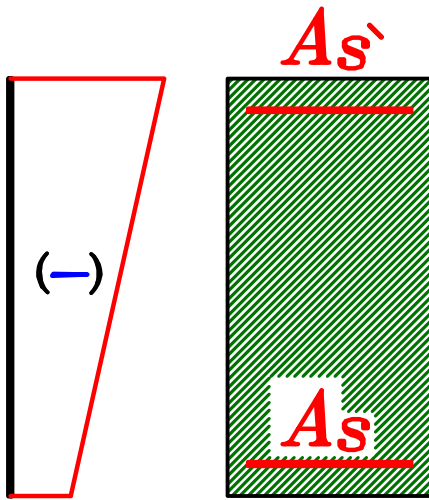
و لكنه فى حاله **Big eccentricity** أى $\frac{e}{t} > 0.5$ يكون غير دقيق و يعطى كميات تسليح كبيره و مكلفه .

لذا يفضل استخدام ال **Interaction Diagram (I.D.)** عندما

يكون القطاع **small eccentricity** أى $\frac{e}{t} < 0.5$

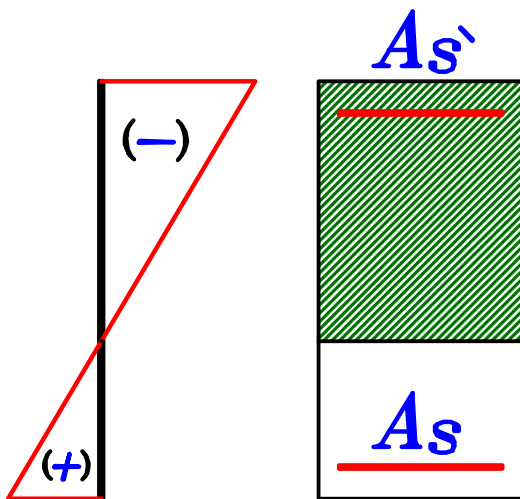
Interaction Diagram الانسب و الاوفر عند استخدام

ان نختار قيم α حيث $\alpha = \frac{A_{s'}}{A_s}$



$$IF \frac{e}{t} < 0.5$$

يفضل اختيار $\alpha = \frac{A_{s'}}{A_s} = (0.8 \rightarrow 1.0)$



$$IF \frac{e}{t} > 0.5$$

يفضل اختيار $\alpha = \frac{A_{s'}}{A_s} = (0.4 \rightarrow 1.0)$

و ان كان الافضل حساب التسليح بطريقة e_s

ملحوظه

الموجود فى كتاب **ECCS** $\alpha = 0.8 \& 1.0$ فقط

لذا فى هذه الملفات سنستخدم قيمه $\alpha = 0.8$ or $\alpha = 1.0$ فقط

مع العلم انه فى العمل توجد جداول $\alpha = 0.0 \rightarrow 1.0$

To get A_s , $A_{s'}$ using Interaction Diagram.

ECCS Pages (4-20) → (4-63)

لتحديد الصفحة المطلوبه نحدد ثلاثه قيم F_y , α , ζ .

Chart Key

$$F_y = \checkmark$$

$$\zeta = \checkmark$$

$$\alpha = \frac{A_{s'}}{A_s}$$

مفتاح الجدول Chart Key

يوجد فى كل صفحه من صفحات ال I.D. فى الجداول
مفتاح للجدول لتحديد أى جدول سوف نستخدمه

- $F_y = \text{Type of Steel}$

	240
	280
	360 ✓✓
	400 ✓✓

- $\alpha = \frac{A_{s'}}{A_s}$

	0.8
	1.0 ✓✓

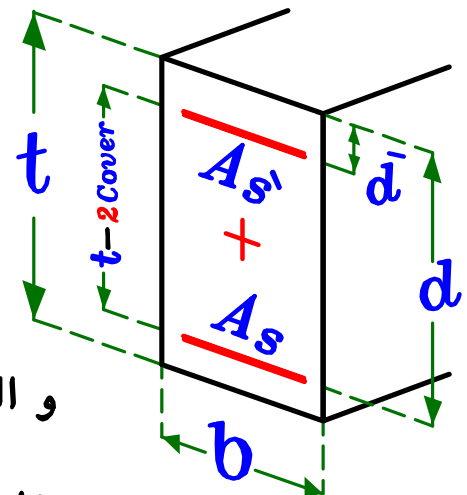
و تؤخذ عادة تساوى 1

- $\zeta = \frac{d - d'}{t} = \frac{\text{المسافه بين الحديد}}{\text{التخانه الكليه}}$

$$\zeta = \frac{t - 2\text{Cover}}{t}$$

$\zeta = 0.7 \text{ or } 0.8 \text{ or } 0.9$ و الموجود فى الجداول

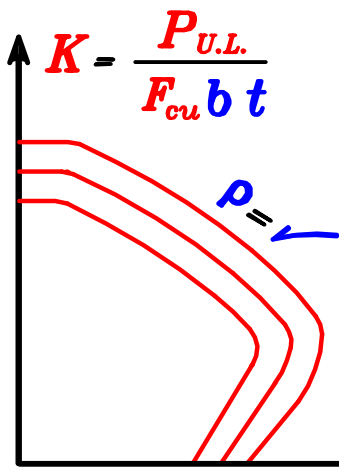
بعد حساب قيمه ζ اذا كانت بين رقمين تقرب للرقم الأصغر



Example. $t = 800 \text{ mm}$

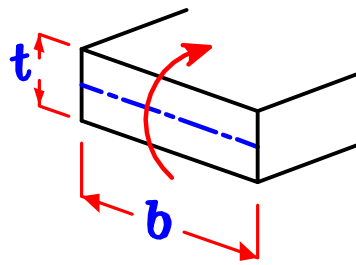
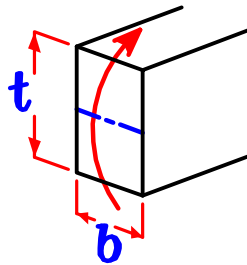
$$\therefore \zeta = \frac{800 - 100}{800} = \frac{700}{800} = 0.875 \xrightarrow{\text{Take}} \zeta = 0.8$$

بعد تحديد ال **I.D.** المطلوب



نحدد قيمه كلا من $\frac{P_{U.L.}}{F_{cu} b t}$, $\frac{M_{U.L.}}{F_{cu} b t^2}$

حيث t هو العرض المقاوم لل **moment** اي العرض الموازي لل **moment**



$$\frac{P_{U.L.}}{F_{cu} b t}$$

$$\frac{P_{U.L.}}{F_{cu} b t}$$

$$\frac{M_{U.L.}}{F_{cu} b t^2}$$

نحدد نقطه تقاطع كلا من

ثم نحدد قيمه ρ كما هو موضح

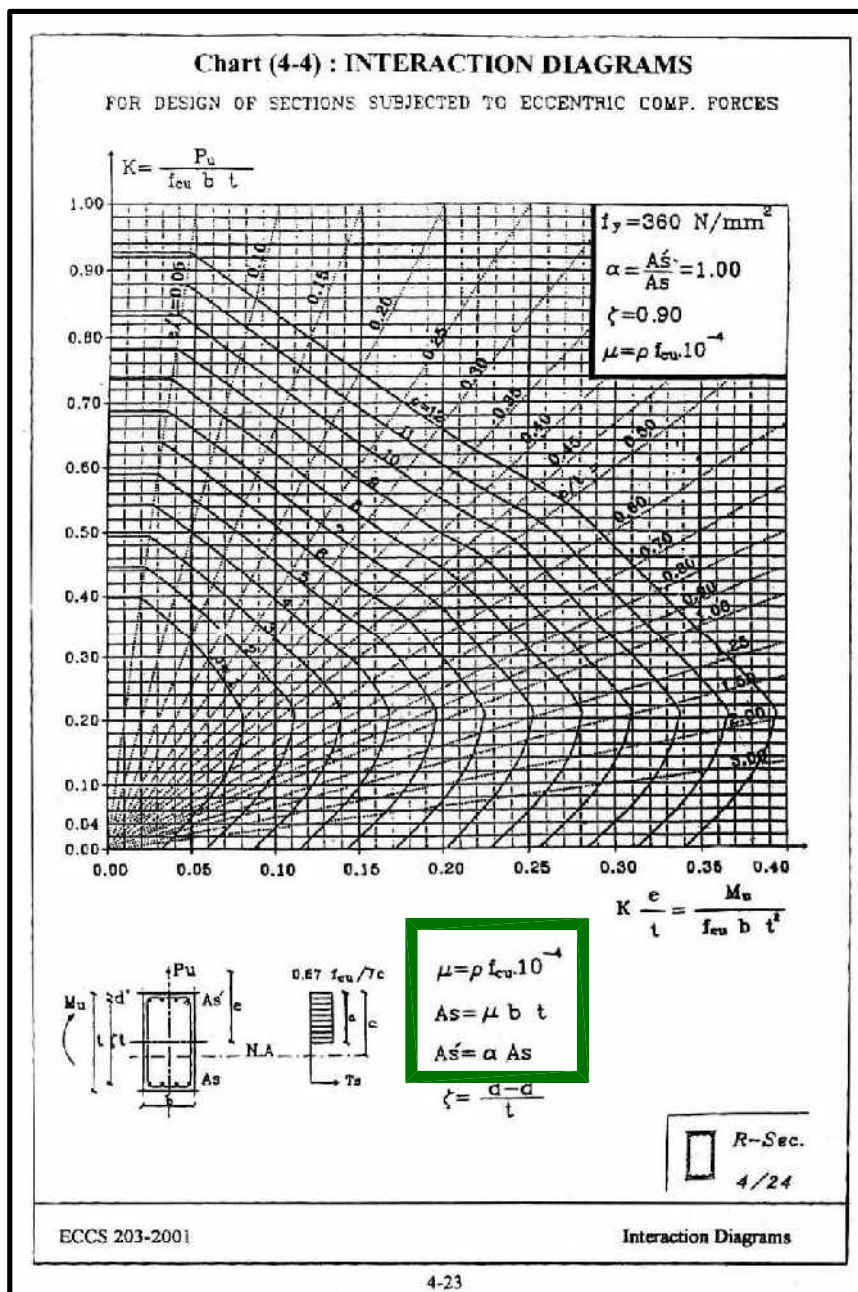
Note.

IF $\rho < 1.0$ Take $\rho = 1.0$

$$\frac{P_{U.L.}}{F_{cu} b t} = \checkmark$$

$$\frac{M_{U.L.}}{F_{cu} b t^2} = \checkmark$$

$$\frac{M_{U.L.}}{F_{cu} b t^2}$$



ثم نعوض فى المعادلات الآتية لتحديد قيمه A_s , $A_{s'}$

$$\mu = \rho * F_{cu} * 10^{-4}$$

$$A_s = \mu * b * t$$

$$A_{s'} = \alpha * A_s$$

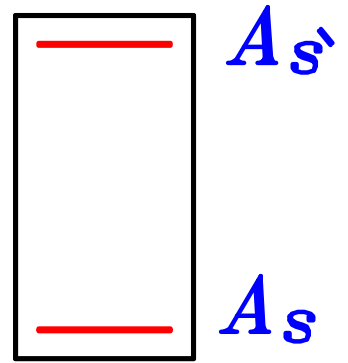
– Check $A_{s_{min.}}$

Calculate $A_{s_{Total}} = A_s + A_{s'}$

Calculate $A_{s_{min.}} = \frac{0.8}{100} * b * t$

IF $A_{s_{Total}} \geq A_{s_{min.}} \therefore o.k.$

IF $A_{s_{Total}} < A_{s_{min.}} \xrightarrow{\text{take}} A_s = A_{s'} = \frac{A_{s_{min.}}}{2}$



Shrinkage Bars. (IF the sec. in Beam)

- توضع ال **Shrinkage Bars** عندما تكون $t > 700 \text{ mm}$
- و قيمه ال **Shrinkage Bars** = $2 \phi 10$ at every 300 mm

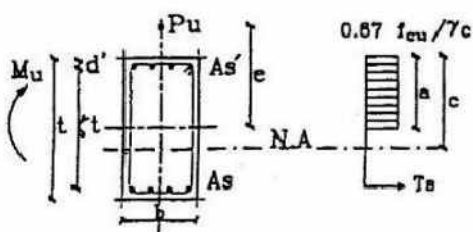
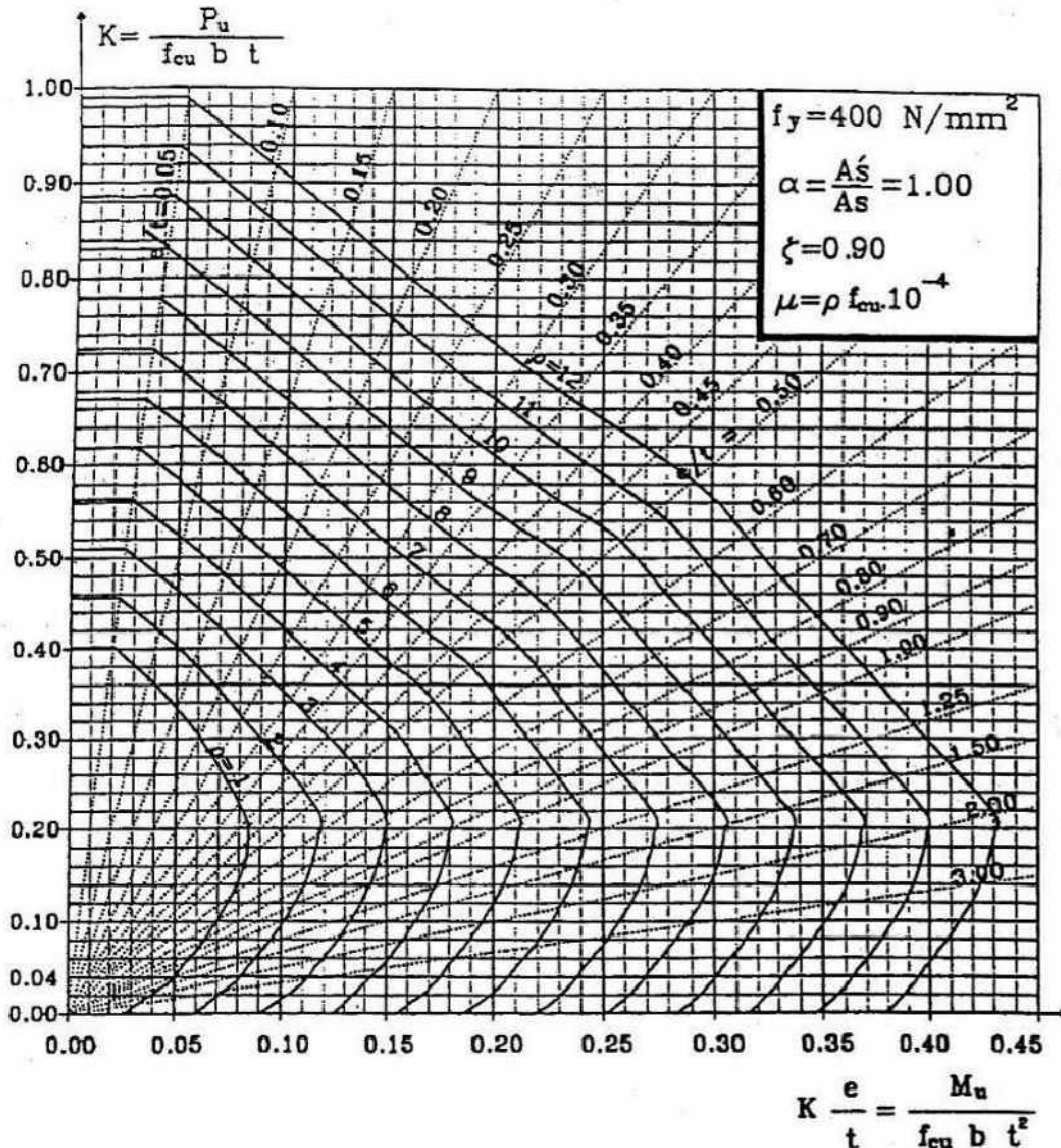
Buckling Bars. (Longitudinal Bars)

(IF the sec. in Column.)

- فى الأعمده التى يؤثر عليها M & P .
- يجب وضع أسياخ جانبيه تسمى **Buckling Bars**.
- و توضع أيضاً عندما تكون $t < 700 \text{ mm}$ (ليس مثل ال **Shrinkage Bars**)
- و قيمه ال **Buckling Bars** = $2 \phi 12$ at every 250 mm
- و توضع كانات داخلية
- بحيث لا تزيد المسافه بين كل فرع كانه و الفرع الذى يليه عن 300 mm

Chart (4-1) : INTERACTION DIAGRAMS

FOR DESIGN OF SECTIONS SUBJECTED TO ECCENTRIC COMP. FORCES



$$\mu = \rho f_{cu} \cdot 10^{-4}$$

$$A_s = \mu b t$$

$$A_s' = \alpha A_s$$

$$\zeta = \frac{d - d'}{t}$$

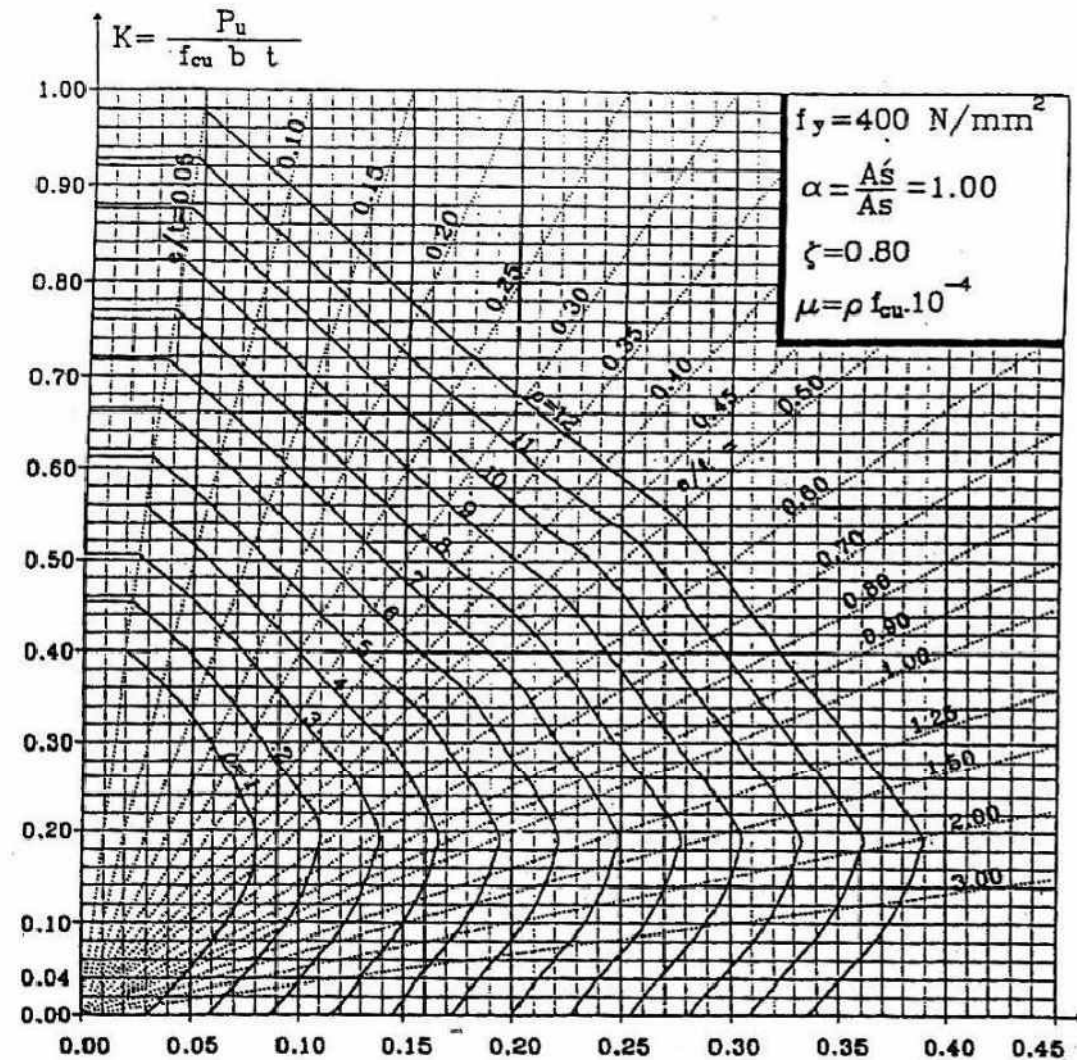
R-Sec.
 1/24

ECCS 203-2001

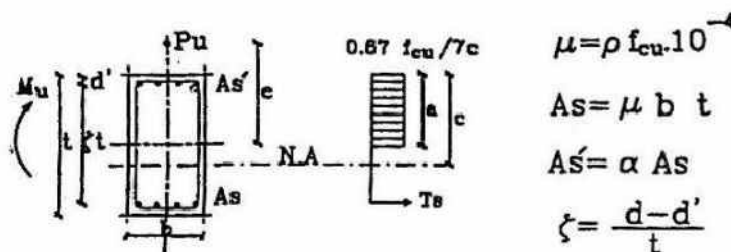
Interaction Diagrams

Chart (4-2) : INTERACTION DIAGRAMS

FOR DESIGN OF SECTIONS SUBJECTED TO ECCENTRIC COMP. FORCES



$$K \frac{e}{t} = \frac{M_u}{f_{cu} b t^2}$$



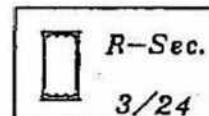
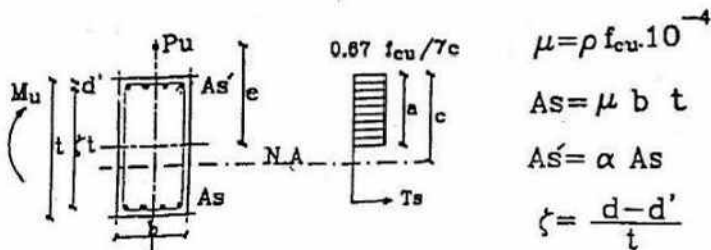
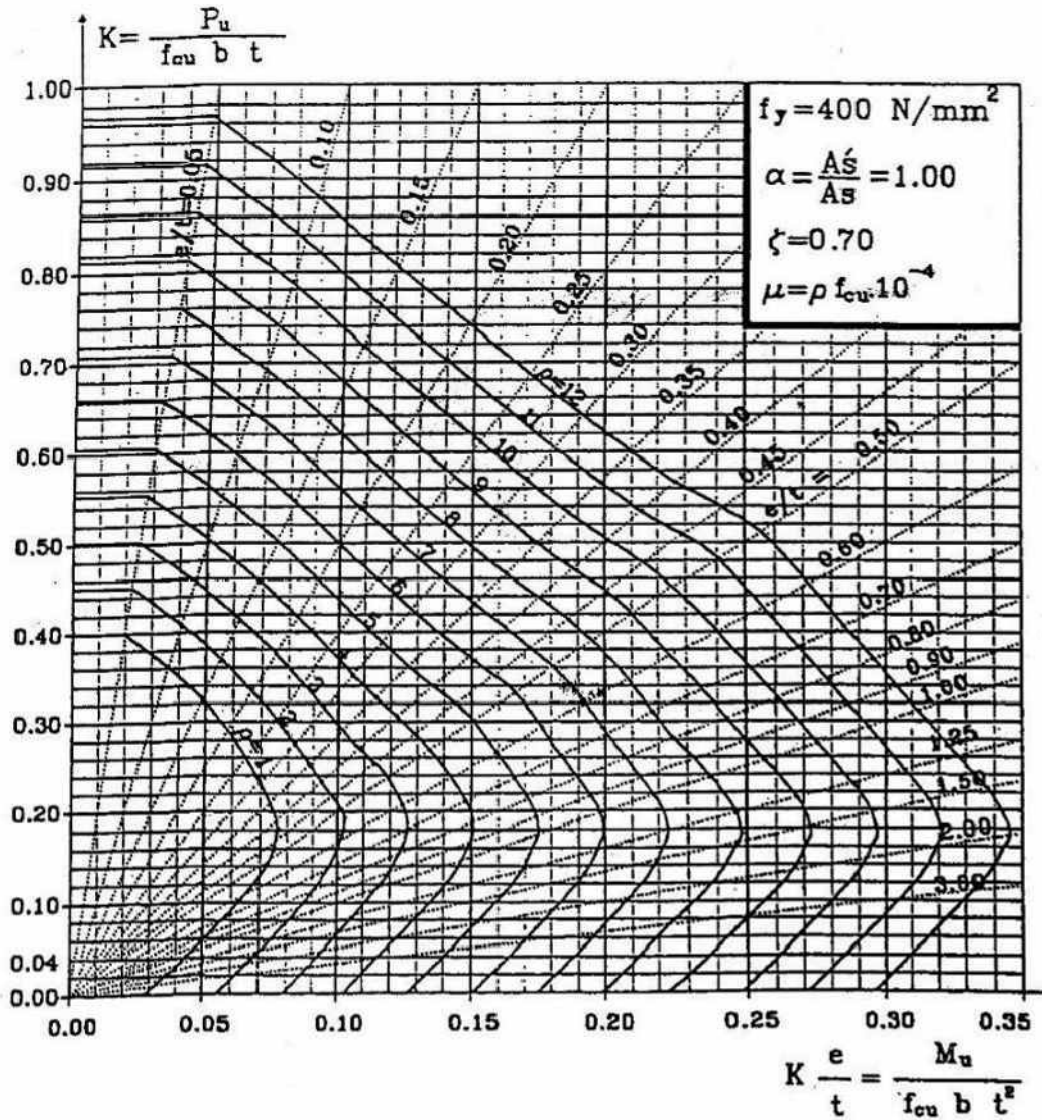
R-Sec.
 2 / 24

ECCS 203-2001

Interaction Diagrams

Chart (4-3) : INTERACTION DIAGRAMS

FOR DESIGN OF SECTIONS SUBJECTED TO ECCENTRIC COMP. FORCES

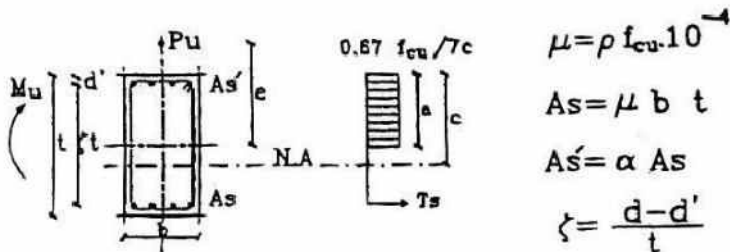
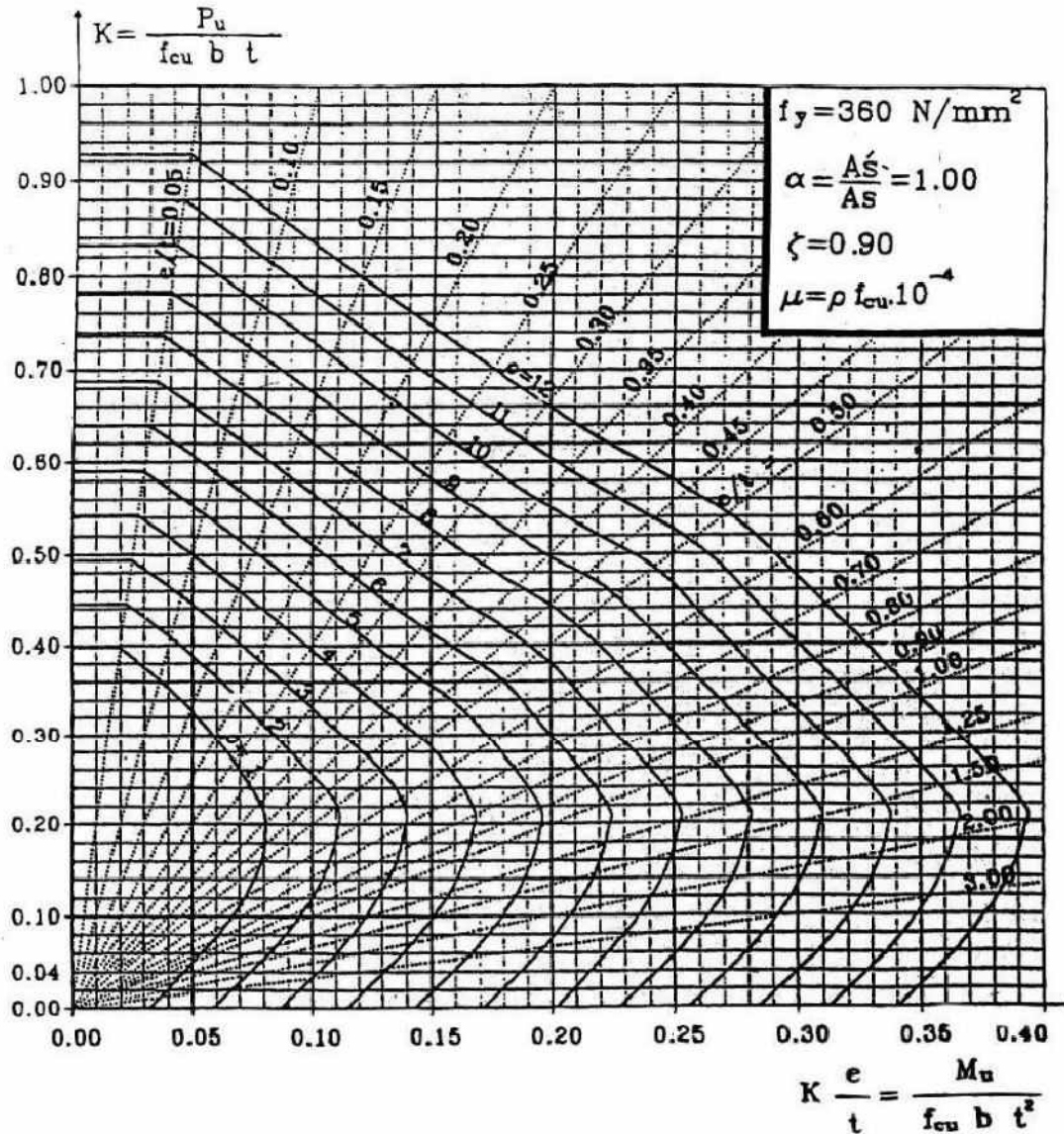


ECCS 203-2001

Interaction Diagrams

Chart (4-4) : INTERACTION DIAGRAMS

FOR DESIGN OF SECTIONS SUBJECTED TO ECCENTRIC COMP. FORCES



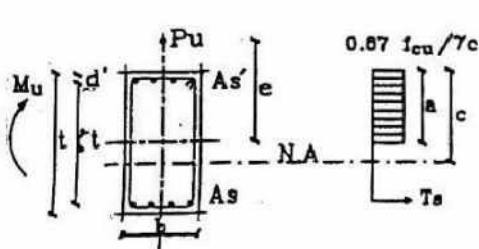
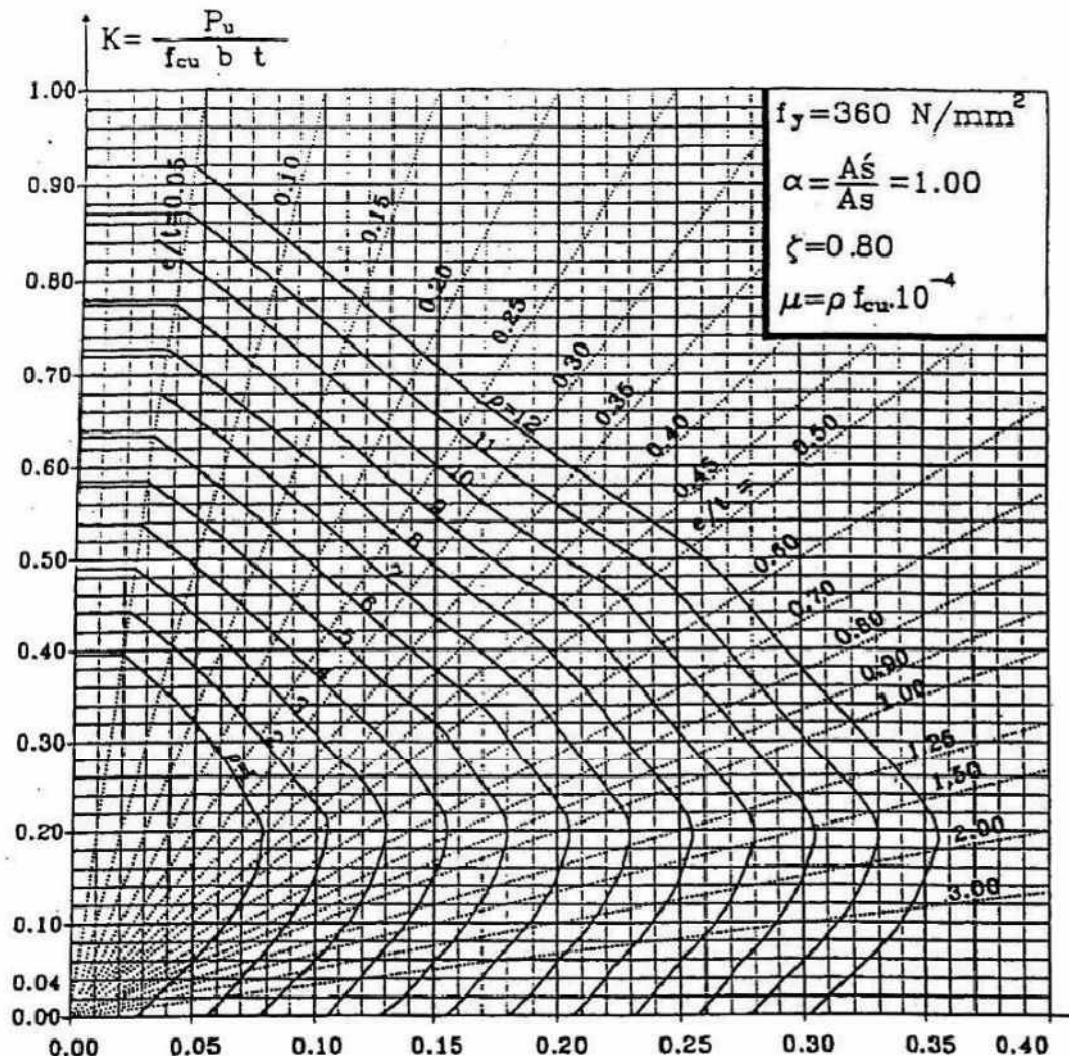
R-Sec.
4/24

ECCS 203-2001

Interaction Diagrams

Chart (4-5) : INTERACTION DIAGRAMS

FOR DESIGN OF SECTIONS SUBJECTED TO ECCENTRIC COMP. FORCES



$$\mu = \rho f_{cu} \cdot 10^{-4}$$

$$A_s = \mu b t$$

$$A_s' = \alpha A_s$$

$$\zeta = \frac{d - d'}{t}$$

$$K \frac{e}{t} = \frac{M_u}{f_{cu} b t^2}$$

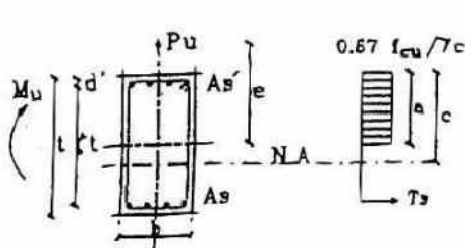
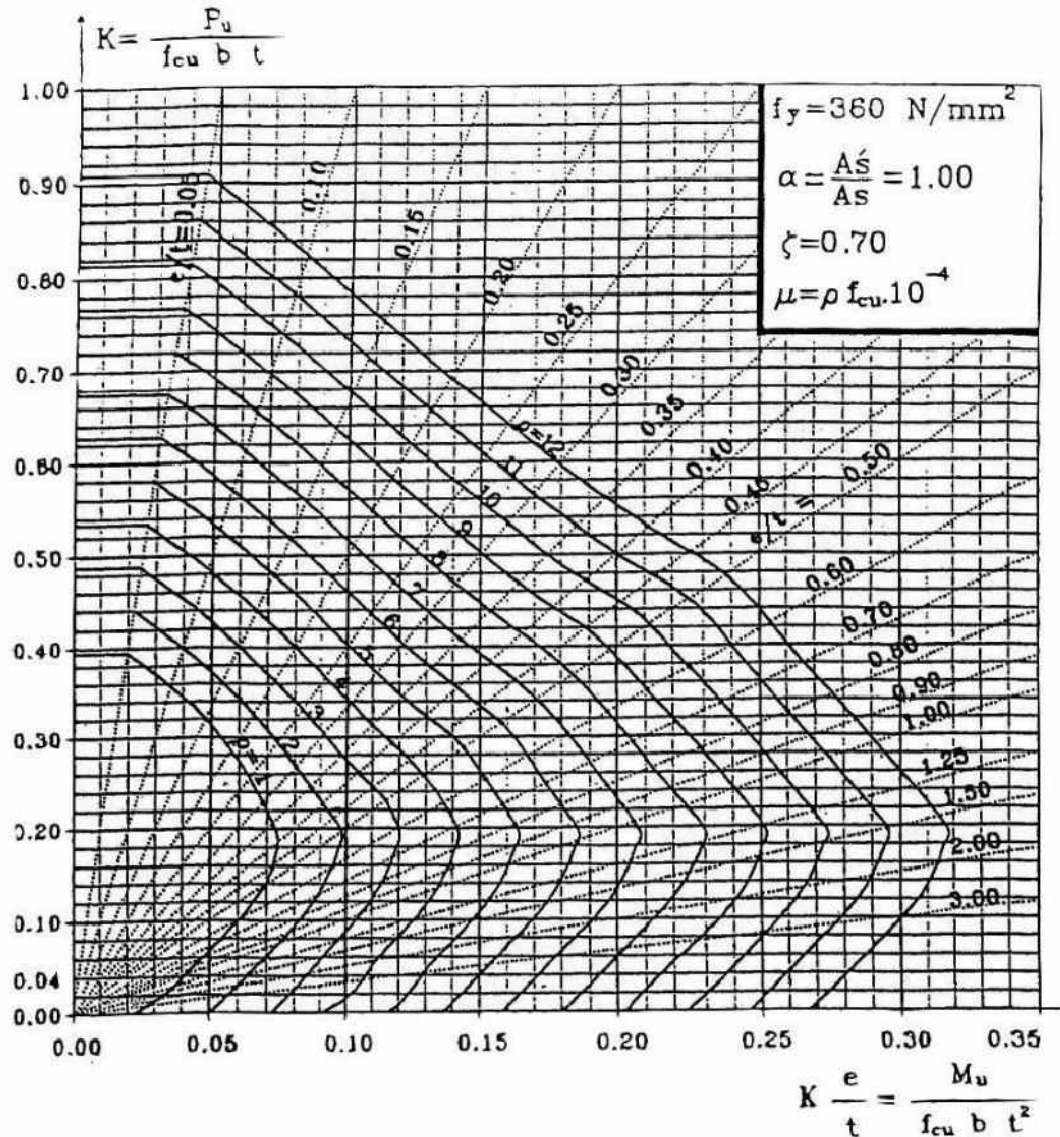
R-Sec.
5/24

ECCS 203-2001

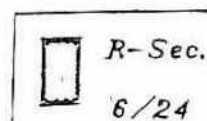
Interaction Diagrams

Chart (4-6) : INTERACTION DIAGRAMS

FOR DESIGN OF SECTIONS SUBJECTED TO ECCENTRIC COMP. FORCES



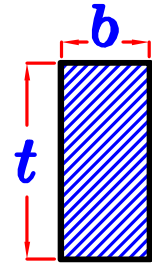
$\mu = \rho f_{cu} \cdot 10^{-4}$
 $A_s = \mu b t$
 $A_s' = \alpha A_s$
 $\zeta = \frac{d - d'}{t}$



① Get Dimensions of the section. ($b \times t$) اذا كانت الابعاد غير موجوده

- Take $b = (300 \text{ mm or } 350 \text{ mm or } 400 \text{ mm})$

Get $t_1 = d_1 + \text{cover}$ where $d_1 = 3.5 \sqrt{\frac{M_{U.L.}}{F_{cu} b}}$



Get t_2 From $P_{U.L.} = 0.35 (b t_2) F_{cu} + 0.67 \frac{(b t_2)}{100} F_y$

- Take $t = (1.1 \rightarrow 1.3) t_o$ where $t_o =$ The bigger value of t_1 & t_2

② Check IF « P » neglected or not.

Calculate $K = \frac{P_{U.L.}}{F_{cu} b t}$ IF $K \leq 0.04$ neglect P

$$d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} (b \text{ or } B)}}$$

$$A_s = \frac{M_{U.L.}}{J F_y d}$$

IF $K > 0.04$ don't neglect P

Design the Sec. on both M, P

- Take the same b, t From step ①

③ Get Reinforcement A_s, A_s'

- Get $e = \frac{M_{U.L.}}{P_{U.L.}}$

- Get $\frac{e}{t}$ moment لا العرض الموازي

IF $\frac{e}{t} \geq 0.5$

Big Eccentricity $\rightarrow e_s$

$$e_s = e + \frac{t}{2} - c$$

$$M_s = P_{U.L.} * e_s$$

$$\text{From } d = c_1 \sqrt{\frac{M_s}{F_{cu} b}} \rightarrow c_1 \& J$$

$$A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y / \phi_s)}$$

$$\text{Check } A_{smin} = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d$$

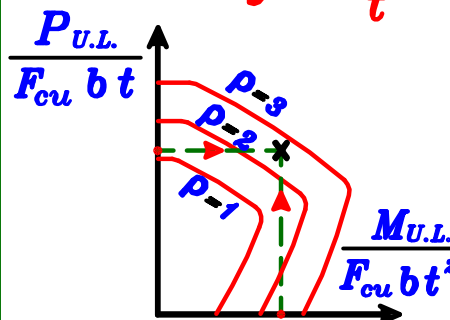
IF $\frac{e}{t} < 0.5$

small Eccentricity $\rightarrow I.D.$

نحدد ال $I.D.$ المناسب من كتاب الجداول على حسب كل من

$$F_y, \quad \zeta = \frac{t - 2\text{Cover}}{t}, \quad \alpha = \frac{A_s'}{A_s} = 1$$

نحدد قيمه ρ



$$\begin{aligned} \mu &= \rho * F_{cu} * 10^{-4} \\ A_s &= \mu * b * t \\ A_s' &= \alpha * A_s \end{aligned}$$

$$\text{Check } A_{sTotal} = A_s + A_s'$$

$$\text{with } A_{smin} = \frac{0.8}{100} * b * t$$

Design of Sections Subjected to Bending Moment & Axial Tension Force (M, T)

Steps of Design :

- 1 – Get Dimensions of the section. ($b \times t$)*
- 2 – Get Reinforcement A_{s1}, A_{s2}*

Solution:

- 1 – Get Dimensions of the section. ($b \times t$)*
-

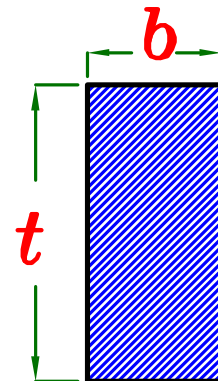
Take $b = (250 \text{ mm or } 300 \text{ mm or } 350 \text{ mm or } 400 \text{ mm})$

Get $d_o = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}}$ take $c_1 = 3.5, J = 0.78$

Then take $d = (0.9 \rightarrow 1.0) d_o$

$t = d + 50 \text{ mm}$ IF $t \leq 1000 \text{ mm}$

$t = d + 100 \text{ mm}$ IF $t > 1000 \text{ mm}$



2 - Get Reinforcement A_{s1}, A_{s2}



Then get $e = \frac{M_{U.L.}}{T_{U.L.}}$ Then get $\frac{e}{t}$

- IF $\frac{e}{t} \leq 0.05 \rightarrow$ neglect $M_{U.L.}$

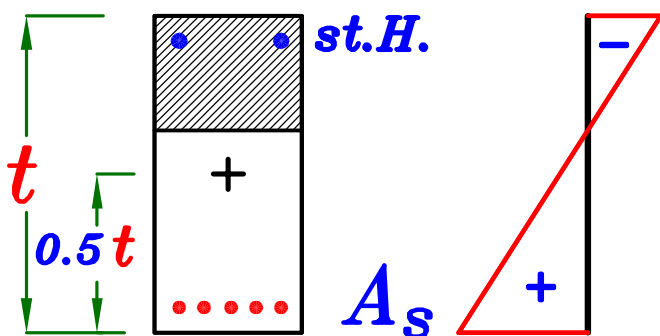
and Design the Sec. on Tension Force only as Tie.

IF $\frac{e}{t}$

$$\frac{e}{t} \geq 0.5$$

Big Eccentricity

$$e \geq 0.5 t$$

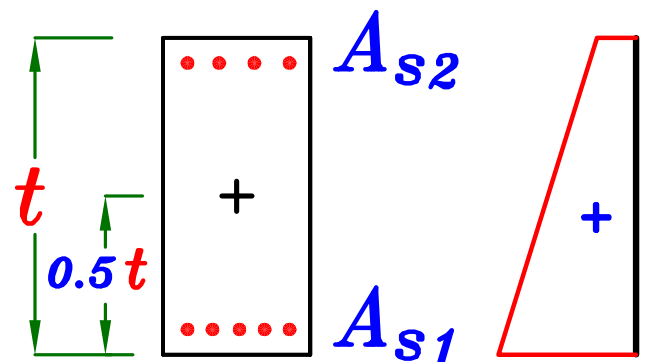


القطاع أقرب لقطاع الكمره منه
لقطاع ال Tie .

$$\frac{e}{t} < 0.5$$

Small Eccentricity

$$e < 0.5 t$$



القطاع أقرب لقطاع ال Tie
منه الى قطاع الكمره .

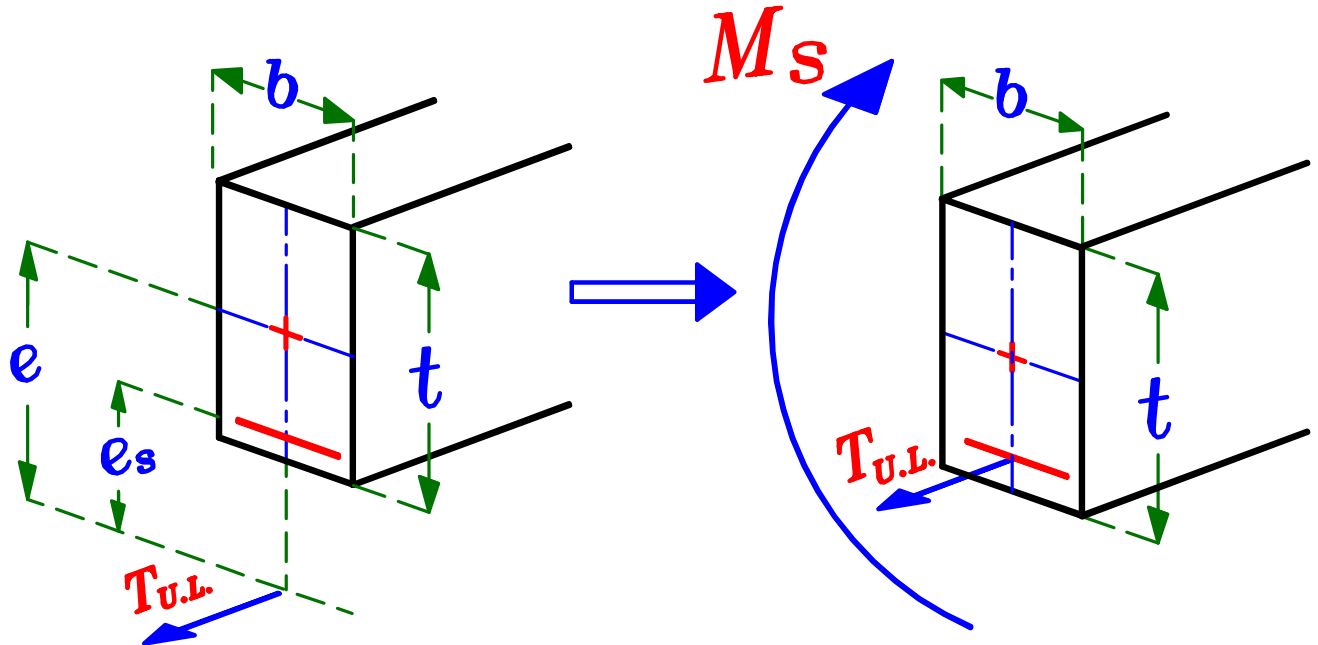


① $\frac{e}{t} \geq 0.5$ Big Eccentricity.

∴ محصلة القوى العموديه تكون خارج القطاع.

القطاع أقرب لقطاع الكمره منه لقطاع ال Tie .

أى أن جهه من الخرسانه عليها **Compression** و جهه عليها **Tension**.



Get

$$e_s = e - \frac{t}{2} + c$$

Get

$$M_s = T_{u.L.} * e_s$$

From $d = c_1 \sqrt{\frac{M_s}{F_{cu} b}}$ Get $c_1 = \checkmark \xrightarrow{\text{get}} J = \checkmark$

$$A_s = \frac{M_s}{J F_y d} + \frac{T_{u.L.}}{(F_y / \phi_s)}$$

Check $A_{smin} = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d$

Example.

$$F_{cu} = 25 \text{ N/mm}^2 \quad \text{st. } 360/520$$

$$M_{u.L.} = 300 \text{ kN.m} , \quad T_{u.L.} = 300 \text{ kN} , \quad b = 300 \text{ mm}$$

Req. Design the Sec.

Solution.

$$\text{Take } d_o = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}} \quad C_1 = 3.5 , J = 0.78$$

$$\therefore d_o = 3.5 \sqrt{\frac{300 * 10^6}{25 * 300}} = 700 \text{ mm}$$

$$d = (0.9 \rightarrow 1.0) d_o = (0.9 \rightarrow 1.0) (700) = (630 \rightarrow 700) \text{ mm}$$

$$\text{Take } d = 650 \text{ mm} , \quad t = 650 + 50 = 700 \text{ mm}$$

$$e = \frac{M}{T} = \frac{300}{300} = 1.0 \text{ m}$$

$$\therefore \frac{e}{t} = \frac{1.0}{0.7} = 1.428 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e - \frac{t}{2} + c = 1.0 - \frac{0.70}{2} + 0.05 = 0.70 \text{ m}$$

$$M_s = T * e_s = 300 * 0.70 = 210 \text{ kN.m}$$

$$\therefore d = c_1 \sqrt{\frac{M_s}{F_{cu} b}}$$

$$\therefore 650 = c_1 \sqrt{\frac{210 * 10^6}{25 * 300}} \rightarrow C_1 = 3.884 \rightarrow J = 0.798$$

$$\therefore A_s = \frac{M_s}{J F_y d} + \frac{T_{u.L.}}{(F_y \backslash \delta_s)}$$

$$= \frac{210 * 10^6}{0.798 * 360 * 650} + \frac{300 * 10^3}{(360 \backslash 1.15)} = 2082.9 \text{ mm}^2$$

– Check $A_{s_{min.}}$ $A_{s_{req.}} = 2082.9 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 300 * 650 = 609.3 \text{ mm}^2$$

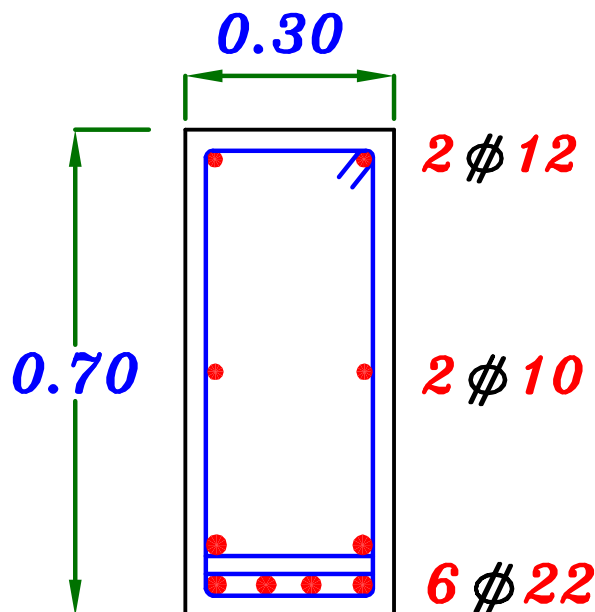
$$\therefore A_{s_{req.}} > \mu_{min.} b d$$

$$\therefore \text{Take } A_s = A_{s_{req.}} = 2082.9 \text{ mm}^2 \quad (6 \phi 22)$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{300 - 25}{22 + 25} = 5.85 = 5.0$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 2082.9$$

$$(2 \phi 12)$$



② $\frac{e}{t} < 0.5$ Small Eccentricity.



∴ محصلة القوى العمودية تكون داخل القطاع.

القطاع أقرب لقطاع ال **Tie** منة لقطاع الكمره .

أى أن الخرسانه عليها **Tension** من الجهتين .

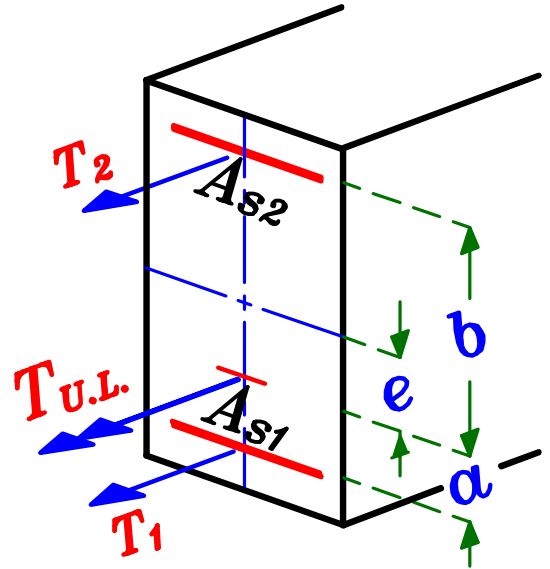
و تكون الخرسانه مشرخه من الجهتين و يقاوم الحديد كل ال **Tension** .

$$a = \frac{t}{2} - c - e$$

a هى بعد المحصلة عن الحديد الاقرب لها

$$b = \frac{t}{2} - c + e$$

b هى بعد المحصلة عن الحديد الابدع عنها

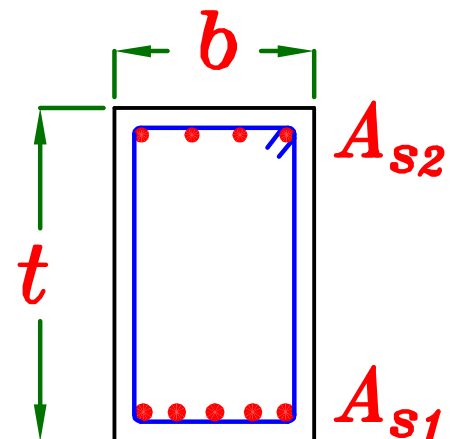


نحسب مركبتين الشد T_1 و T_2 عند الحديد القريب و البعيد عن المحصلة
و منهم نحسب مساحه الحديد المطلوبه لحمل هذه القوى A_{s1} و A_{s2}

بأخذ العزم عند T_2

$$\therefore T_1 (a + b) = T (b) \xrightarrow{\text{Get}} T_1$$

$$\therefore T = T_1 + T_2 \xrightarrow{\text{Get}} T_2$$



$$A_{s1} = \frac{T_1}{(F_y / \phi_s)}$$

$$A_{s2} = \frac{T_2}{(F_y / \phi_s)}$$

دائما ال T_1 الكبيره جهه ال **moment**

Example.

$$F_{cu} = 25 \text{ N/mm}^2 \quad \text{st. } 360/520$$

$$M_{u.L} = 100 \text{ kN.m} , \quad T_{u.L} = 600 \text{ kN} , \quad b = 300 \text{ mm} , \quad t = 500 \text{ mm}$$

Req. Design the Sec.

Solution.

$$e = \frac{M}{T} = \frac{100}{600} = 0.1667 \text{ m}$$

$$\therefore \frac{e}{t} = \frac{0.1667}{0.50} = 0.333 < 0.5 \longrightarrow \text{Small Eccentricity.}$$

$$a = \frac{t}{2} - c - e = \frac{0.50}{2} - 0.05 - 0.1667 = 0.033 \text{ m}$$

$$b = \frac{t}{2} - c + e = \frac{0.50}{2} - 0.05 + 0.1667 = 0.3667 \text{ m}$$

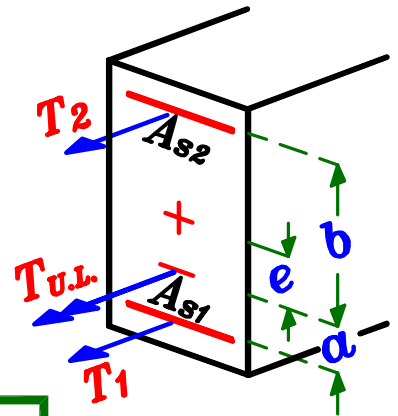
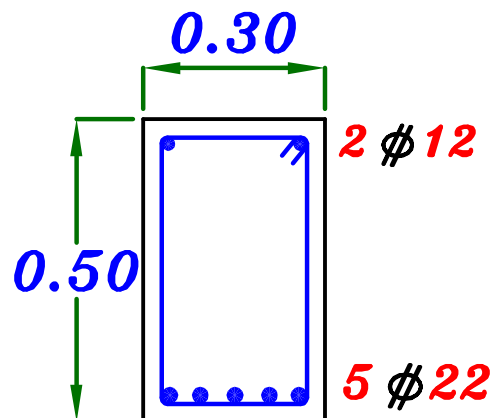
$$\therefore T_1 (a + b) = T (b) \quad \boxed{\text{بأخذ العزم عند } T_2}$$

$$T_1 (0.40) = 600 (0.366) \longrightarrow \boxed{T_1 = 550 \text{ kN}}$$

$$\therefore T = T_1 + T_2 \quad \therefore 600 = 550 + T_2 \longrightarrow \boxed{T_2 = 50 \text{ kN}}$$

$$A_{s1} = \frac{T_1}{(F_y / \phi_s)} = \frac{550 * 10^3}{(360 / 1.15)} = 1757 \text{ mm}^2 \quad \boxed{5 \phi 22}$$

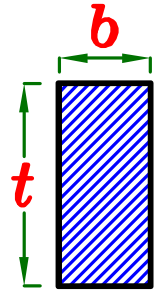
$$A_{s2} = \frac{T_2}{(F_y / \phi_s)} = \frac{50 * 10^3}{(360 / 1.15)} = 159.7 \text{ mm}^2 \quad \boxed{2 \phi 12}$$



① Get Dimensions of the section. ($b \times t$) اذا كانت الابعاد غير معطاه

- Take $b = (250 \text{ mm or } 300 \text{ mm or } 350 \text{ mm or } 400 \text{ mm})$

Get $t = d_o + \text{cover}$ where $d_o = 3.5 \sqrt{\frac{M_{U.L.}}{F_{cu} b}}$



② Get Reinforcement A_{s1}, A_{s2}

- Get $e = \frac{M_{U.L.}}{T_{U.L.}}$

- Get $\frac{e}{t}$

t هو العرض الموازي للمoment

IF $\frac{e}{t} \geq 0.5$

Big Eccentricity $\rightarrow e_s$

$$- e_s = e - \frac{t}{2} + c$$

$$- M_s = T_{U.L.} * e_s$$

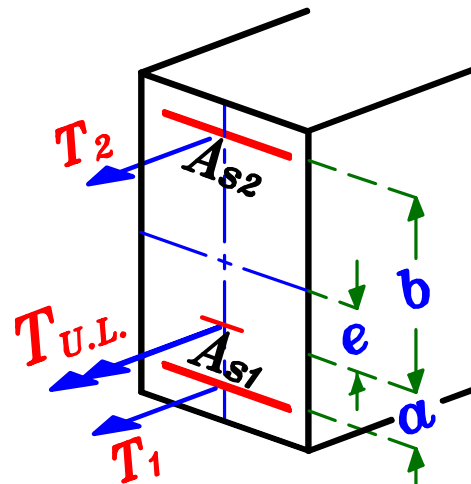
$$- \text{From } d = c_1 \sqrt{\frac{M_s}{F_{cu} b}} \rightarrow c_1 \& J$$

$$- A_s = \frac{M_s}{J F_y d} + \frac{T_{U.L.}}{(F_y / \phi_s)}$$

$$\text{Check } A_{smin} = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d$$

IF $\frac{e}{t} < 0.5$

small Eccentricity



$$a = \frac{t}{2} - c - e$$

$$b = \frac{t}{2} - c + e$$

$$T_1 (a + b) = T (b) \rightarrow T_1$$

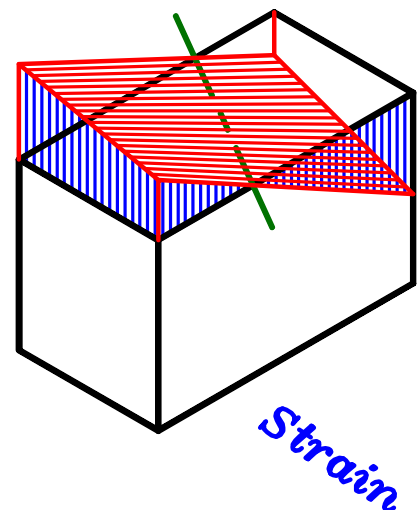
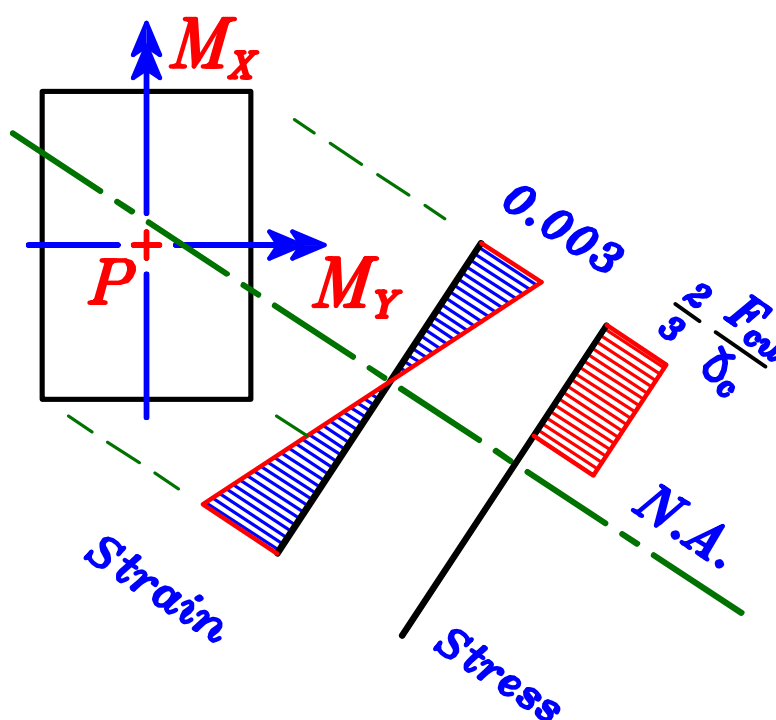
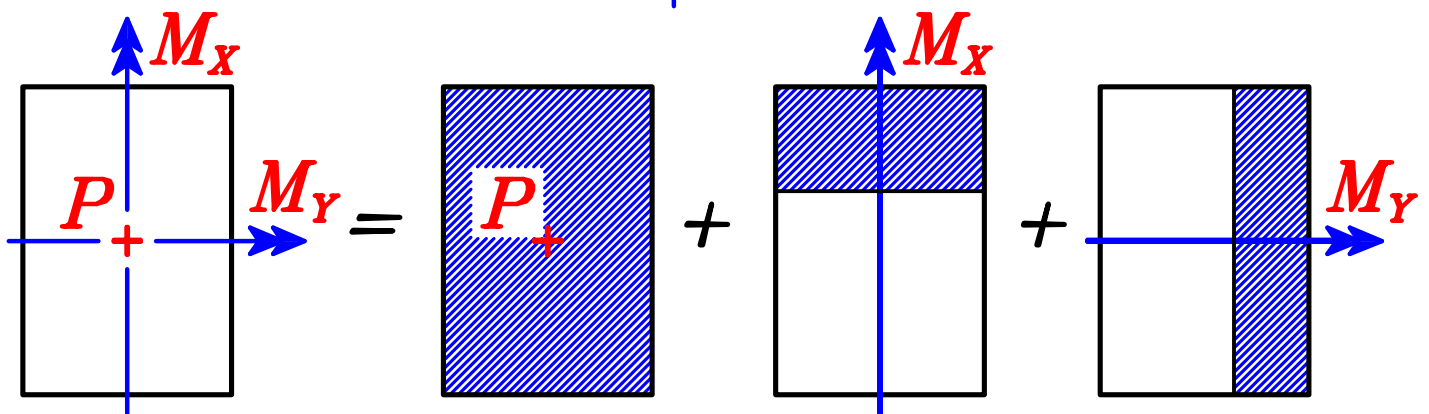
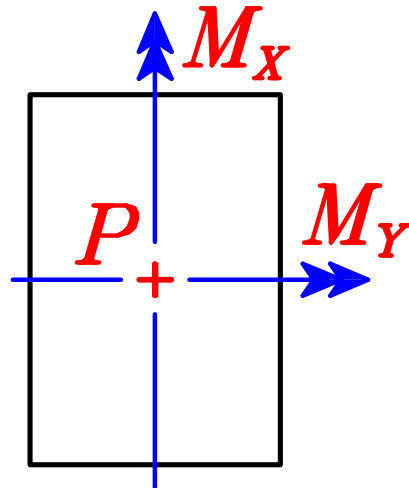
$$T = T_1 + T_2 \rightarrow T_2$$

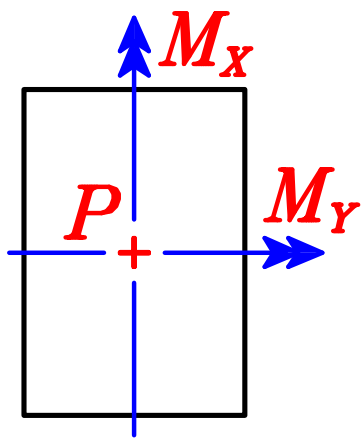
$$A_{s1} = \frac{T_1}{(F_y / \phi_s)}$$

$$A_{s2} = \frac{T_2}{(F_y / \phi_s)}$$

Introduction.

Bi-Axial Moment هو قطاع معرض لقوى ضغط و عزم فى الاتجاهين





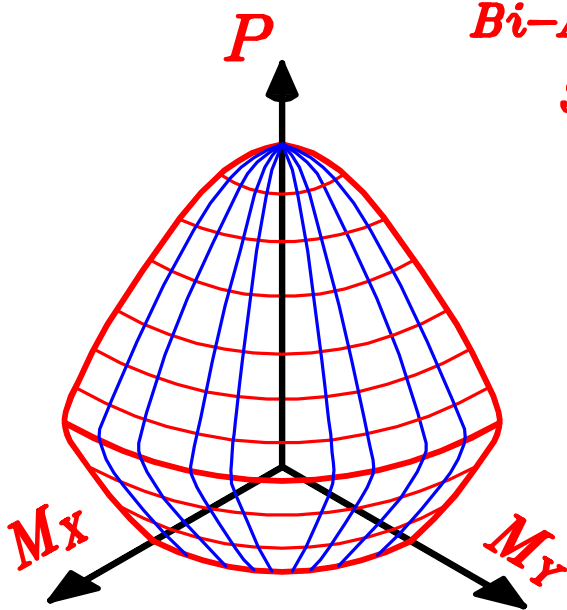
لتصميم قطاع *Bi-Axial Moment*

توجد عدة طرق :

منها التصميم بـ *First Principles*

و هي صعبة جدا و لن يتم دراستها في هذا الملف .

و سندرس فقط التصميم بال *Interaction Diagram (I.D.)*



ال *(I.D.)* للقطاعات ال *Bi-Axial Moment*

المفروض أن يكون ثلاثي الابعاد *3-D (I.D.)*

بحيث ان كل نقطه تتكون من P, M_x, M_y

اذا كانت موجوده داخل ال *3-D (I.D.)*

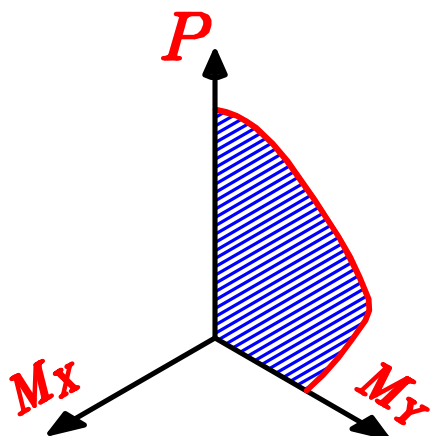
يكون القطاع *Safe*

و اذا كانت النقطه التي تتكون

من P, M_x, M_y خارج ال *3-D (I.D.)*

يكون القطاع *Unsafe*

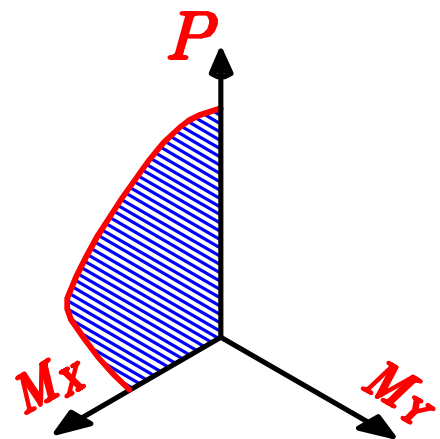
3 Dimensional (I.D.)



عندما يؤثر على القطاع P, M_x فقط

أي $M_y = \text{Zero}$ سنحتاج لـ *(I.D.)*

يسمى *Uniaxial (I.D.)*

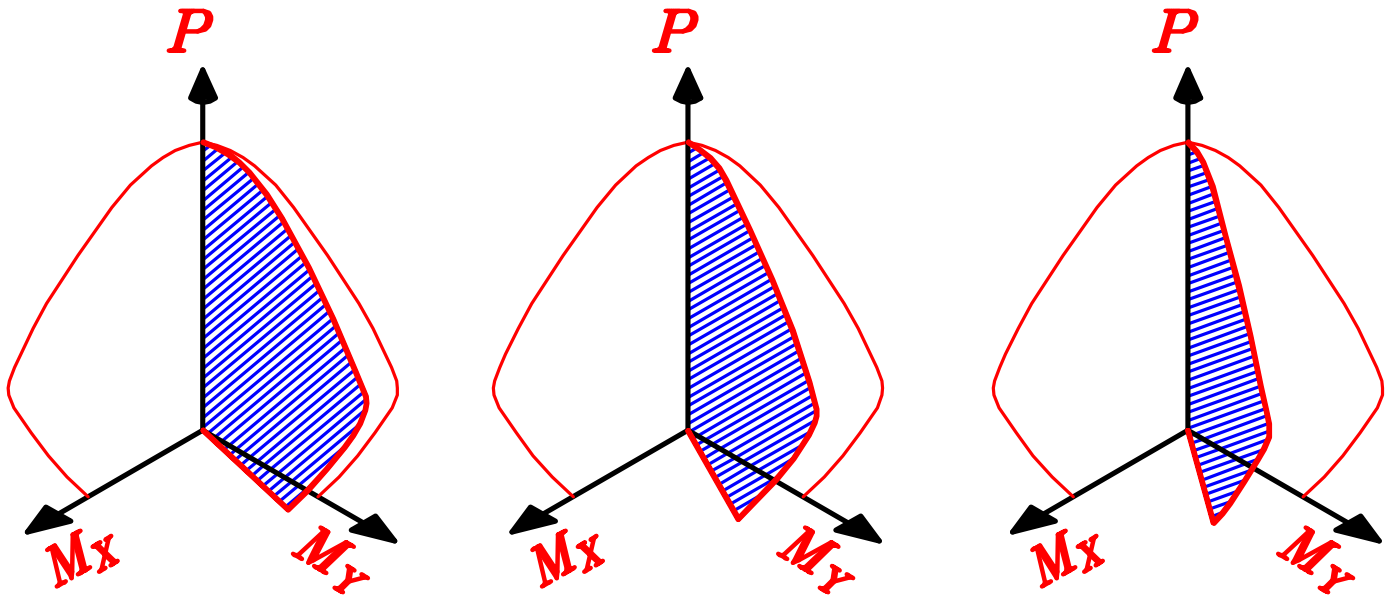


عندما يؤثر على القطاع P, M_y فقط

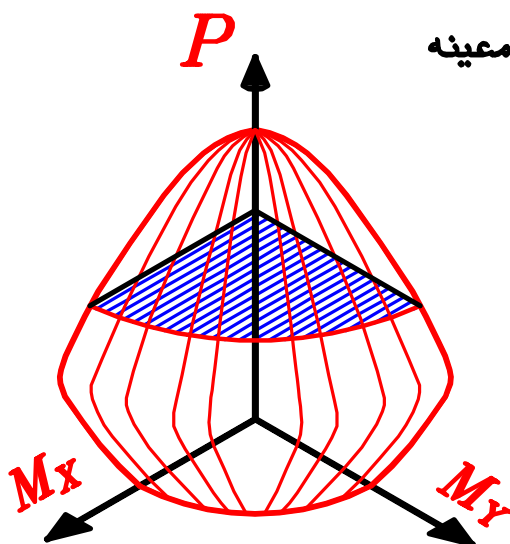
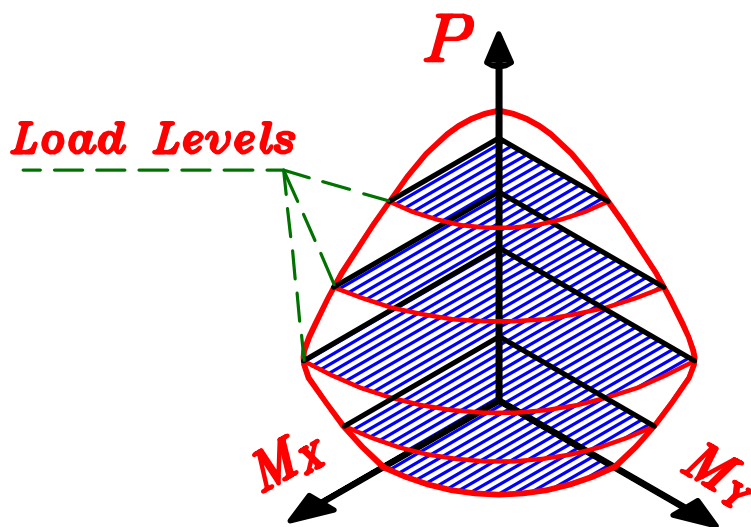
أي $M_x = \text{Zero}$ سنحتاج لـ *(I.D.)*

يسمى *Uniaxial (I.D.)*

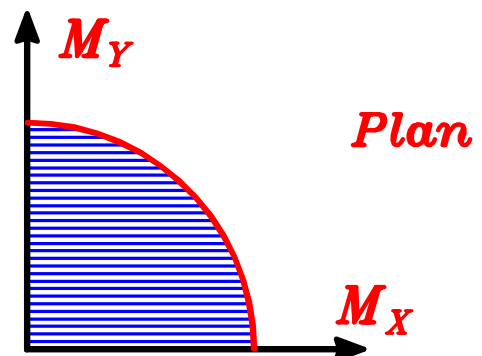
ستتغير زاویه ال **I.D.** مع تغير قيمه كلا من M_x و M_y



لكي نستطيع استخدام ال **(I.D.)** لتصميم مقاطعات ال **Bi-Axial Moment** يتم قطع ال **3-D (I.D.)** بمستويات أفقيه أي مع كل تغير لقيمه P و تسمى **Load Levels**



بحيث عند قيمه P معينه أي عند **Load Level** معينه مع أخذ مقطع أفقي سيكون سيكون شكله



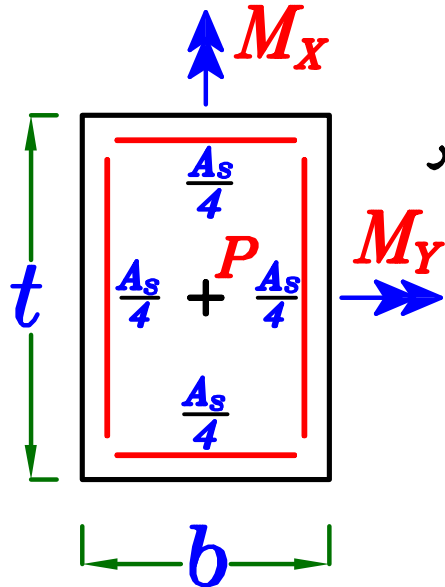
لتصميم قطاع *Bi-Axial Moment* بال *Inter Action Diagram*

يوجد حالتان .

1 – Symmetrical RFT.

و فيها يتم تقسيم التسليح الكلى على الاربعة جهات بالتساوى .

و يفضل ان نستخدم هذه الحالة عندما يكون :



و عندما يكون العرض الكبير يقاوم ال *moment* الكبير
و العرض الصغير يقاوم ال *moment* الصغير

او عندما

Load Level

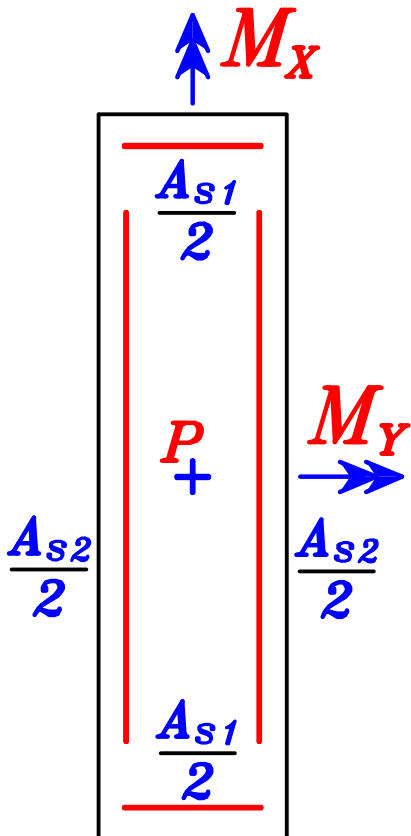
$$R_b = \frac{P}{F_{cu} b t} \geq 0.5$$

2 – Unsymmetrical RFT.

و فيها يتم حساب كميه تسليح كل *moment*

على حده و تقسيم هذا التسليح الى نصفين

و يفضل ان نستخدم هذه الحالة عندما يكون :



Load Level

$$R_b = \frac{P}{F_{cu} b t} \leq 0.5$$

عندما

و عندما يكون العرض الكبير لا يقاوم ال *moment* الكبير

أو عندما يكون الفرق كبير بين طول و عرض القطاع

فلا يكون من المناسب ان نضع التسليح متساوى فى الاربعة جهات .

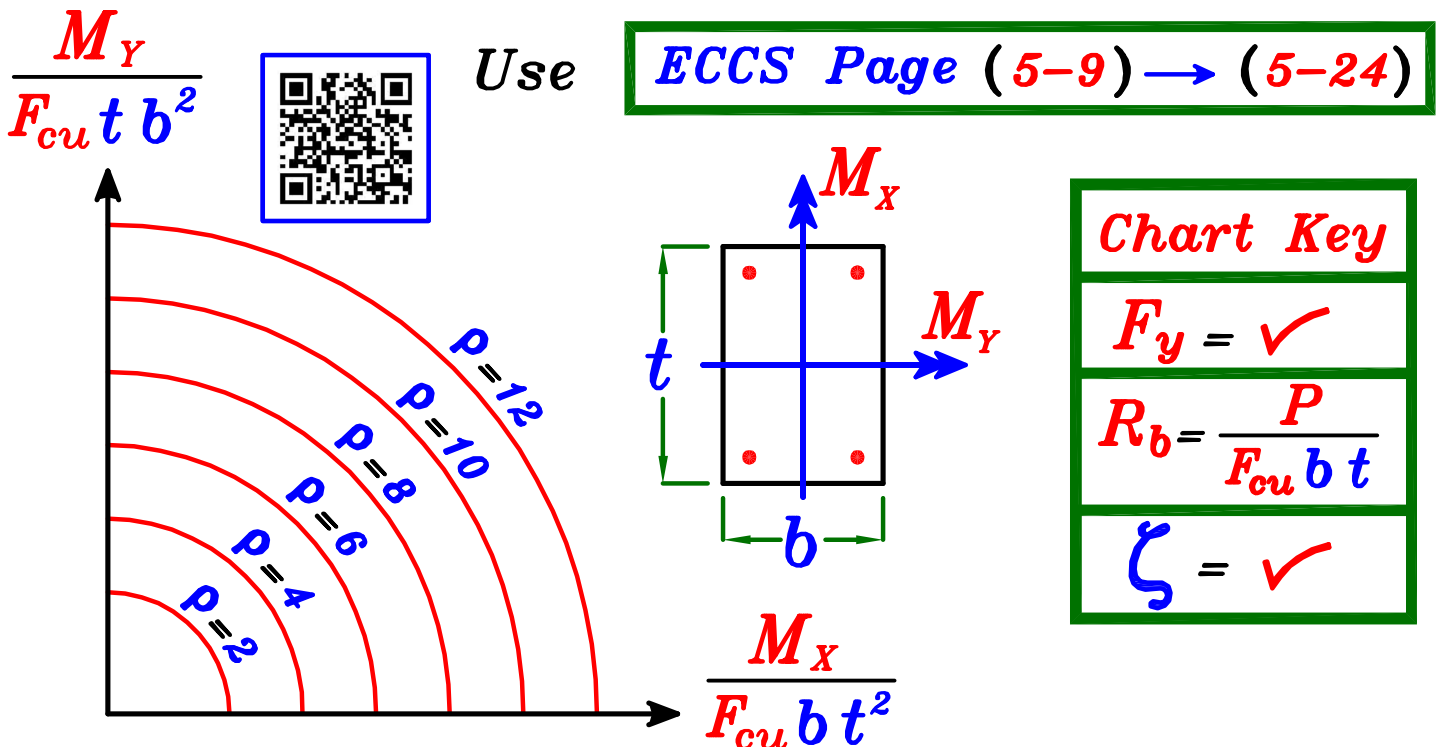
1 – Symmetrical RFT.

و يوجد طريقتان لتصميم القطاع ال **Biaxial** و يكون **Symmetrical RFT.**

1 – Use **Biaxial I.D.**

2 – Use **Uniaxial I.D.**

Design using (**Biaxial Bending Interaction Diagram**)
(**Symmetrical arrangement of reinforcement**)



لتحديد أى **Chart** سيستخدم نحدد قيمة كل من F_y , R_b , ζ

$$R_b = \frac{P}{F_{cu} b t}$$

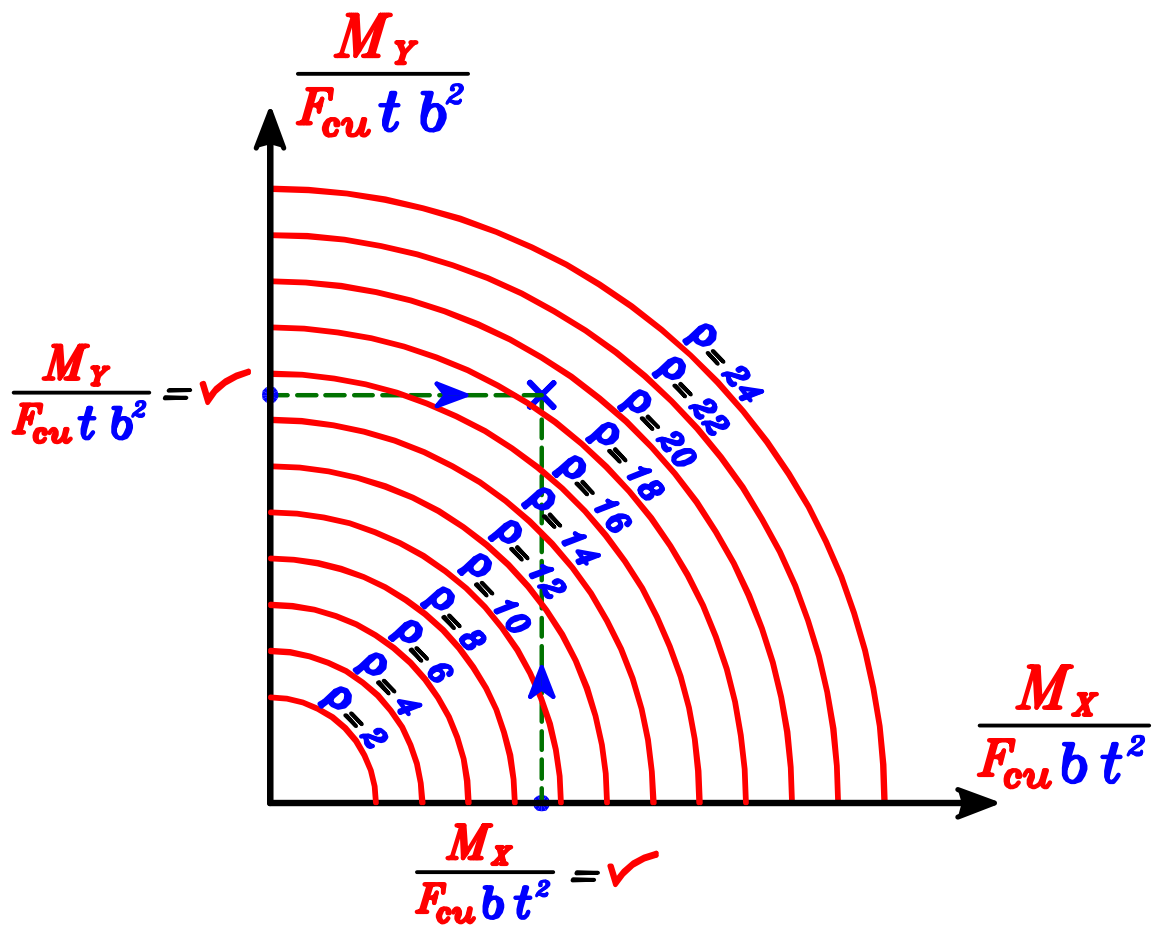
لأنها القيمة الوحيدة الموجودة فى الجداول $\zeta = \frac{t - 2\text{Cover}}{t} = 0.9$

بعد تحديد ال **Curve** بمعرفه كل من F_y , R_b , ζ

$$\frac{M_x}{F_{cu} b t^2}$$

$$\frac{M_y}{F_{cu} t b^2}$$

نحدد قيمة كل من



ثم نحدد قيمة ρ كما هو موضح

ثم نعوض فى المعادلات الآتية لتحديد قيمه $A_{s\text{total}}$

$$\mu = \rho * F_{cu} * 10^{-4}$$

$$A_{s\text{total}} = \mu * b * t$$

$$A_{s\text{min}} = \frac{0.8}{100} * b * t$$

نقارن $A_{s\text{total}}$ بال $A_{s\text{min}}$ و نضع القيمه الاكبر.

و يجب أن يكون عدد الاسياخ يقبل القسمة على ٤

نضع أربع أسياخ فى الركان

ثم يقسم باقى الحديد بالتساوى على الاربعة جهات

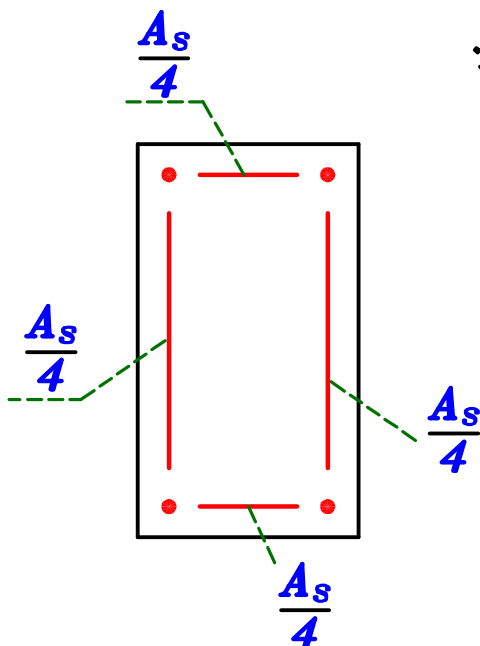
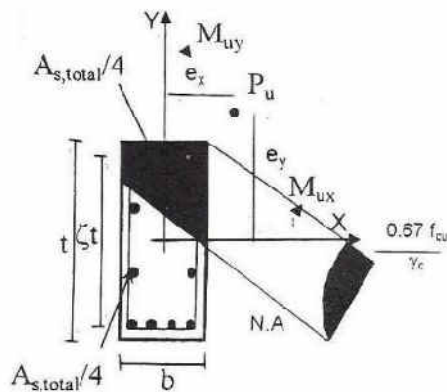
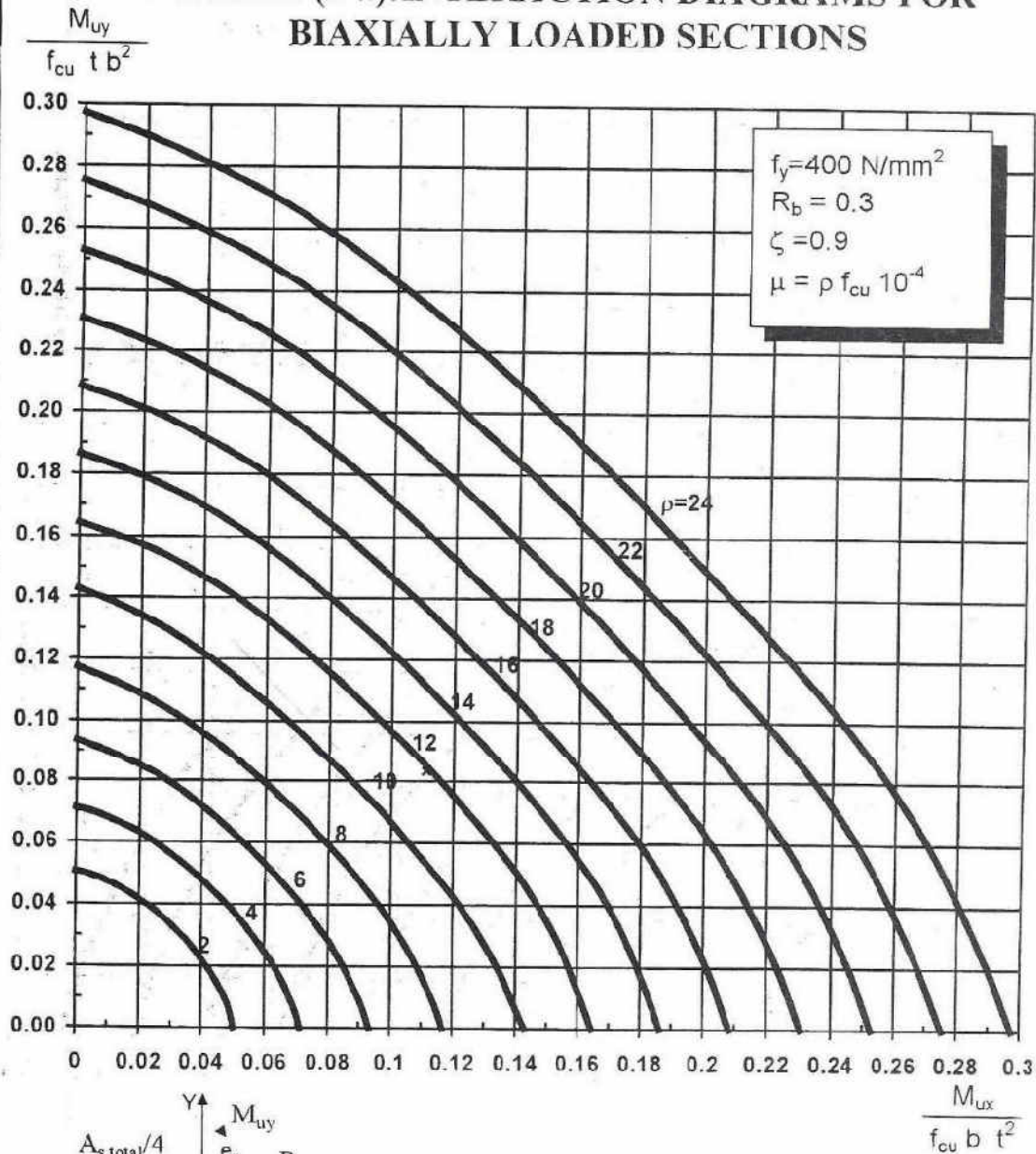


CHART (5-1): INTERACTION DIAGRAMS FOR BIAXIALLY LOADED SECTIONS



$$R_b = \frac{P_u}{f_{cu} b t}$$

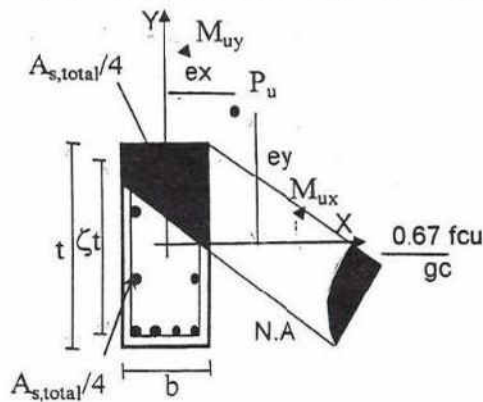
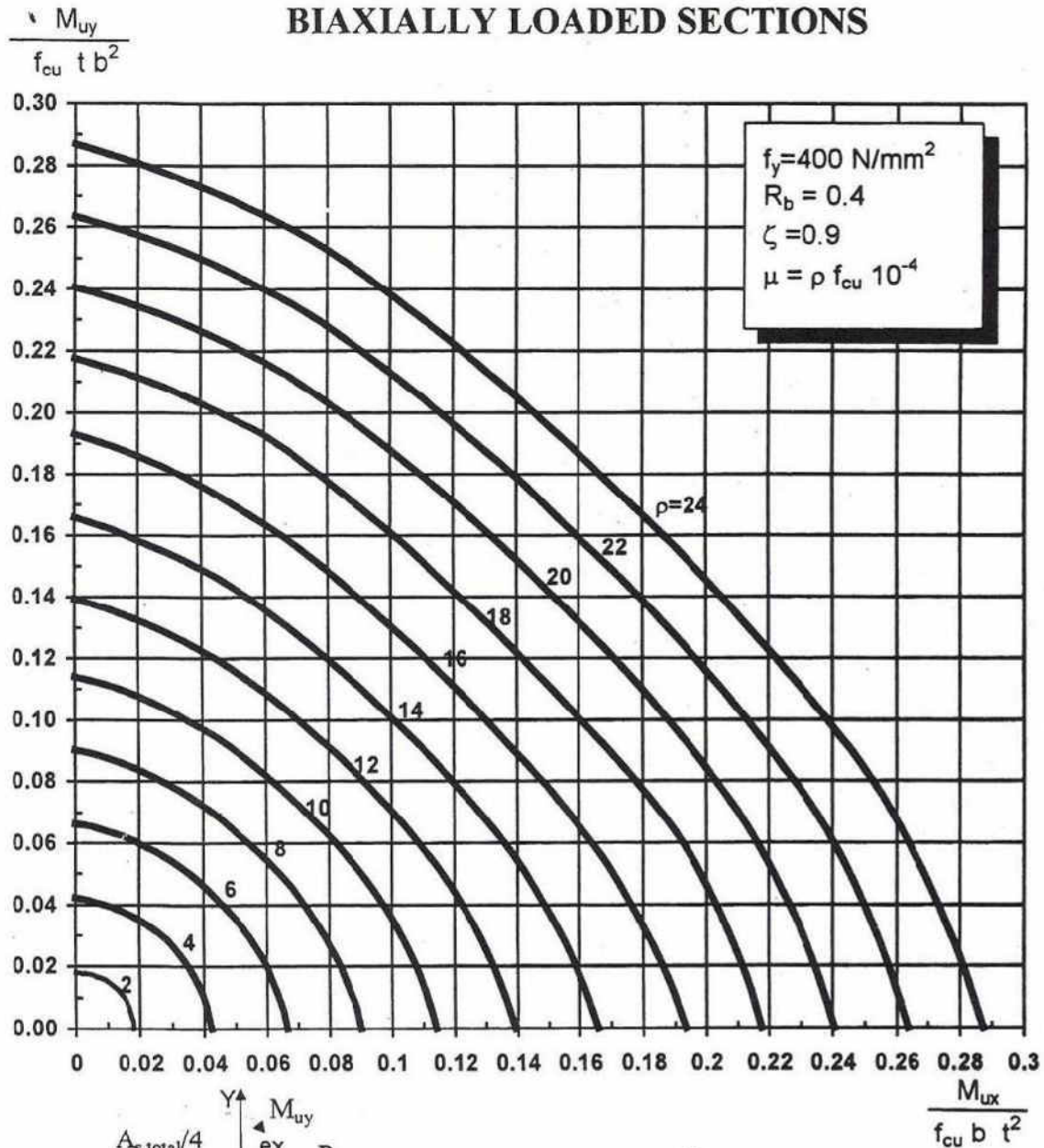
$$\mu = \rho f_{cu} 10^{-4}$$

$$A_{s, \text{total}} = \mu b t$$

ECCS 203-2001 Design Aids

Biaxial Bending

**CHART (5-2): INTERACTION DIAGRAMS FOR
BIAXIALLY LOADED SECTIONS**

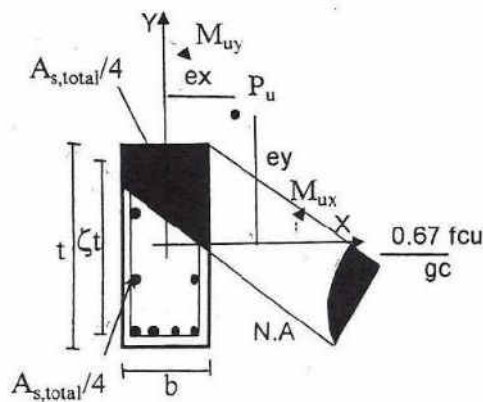
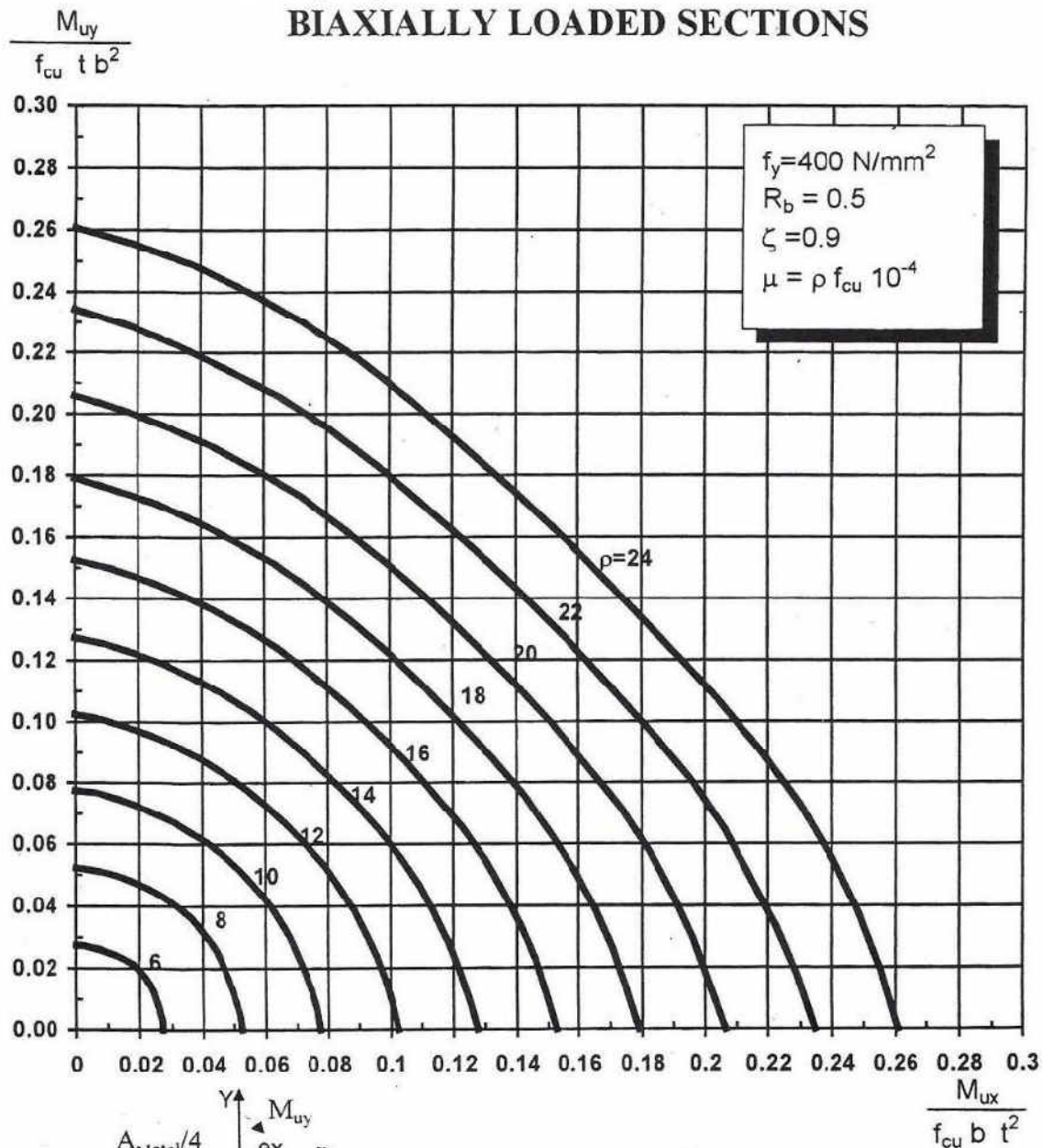


$$R_b = \frac{P_u}{f_{cu} b t}$$

$$\mu = \rho f_{cu} 10^{-4}$$

$$A_{s,total} = \mu b t$$

**CHART (5-3): INTERACTION DIAGRAMS FOR
BIAXIALLY LOADED SECTIONS**

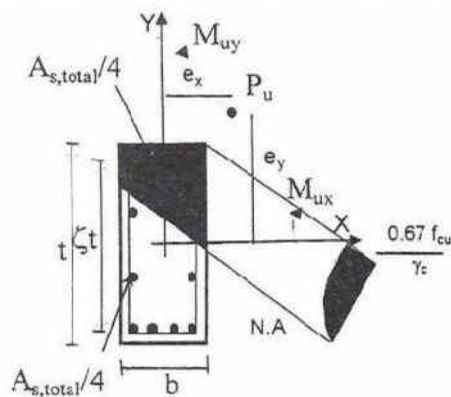
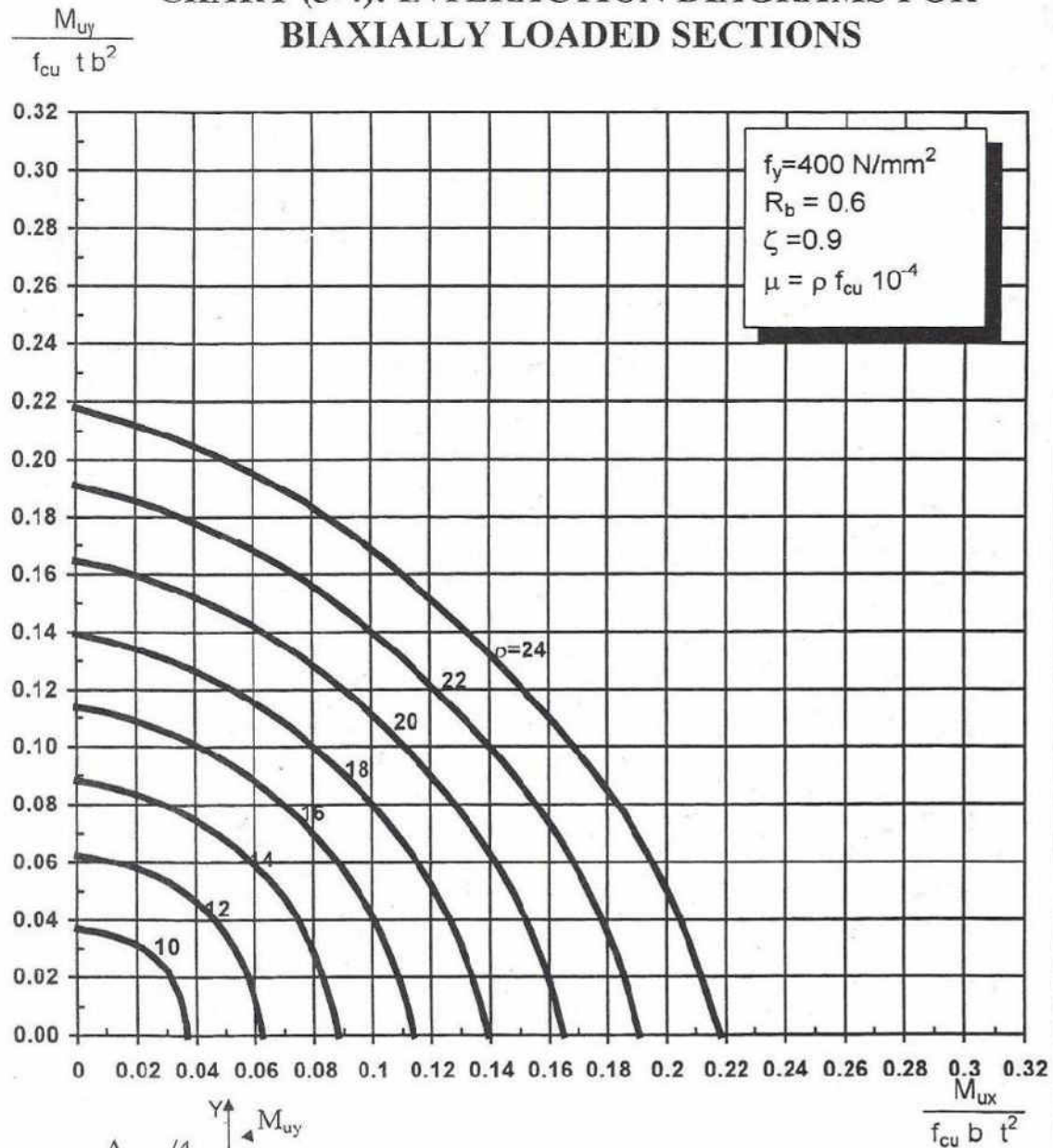


$$R_b = \frac{P_u}{f_{cu} b t}$$

$$\mu = \rho f_{cu} 10^{-4}$$

$$A_{s,total} = \mu b t$$

**CHART (5-4): INTERACTION DIAGRAMS FOR
BIAXIALLY LOADED SECTIONS**

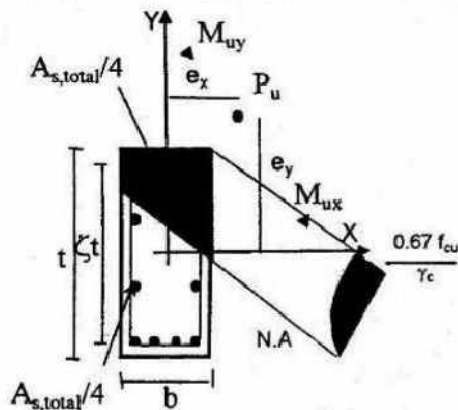
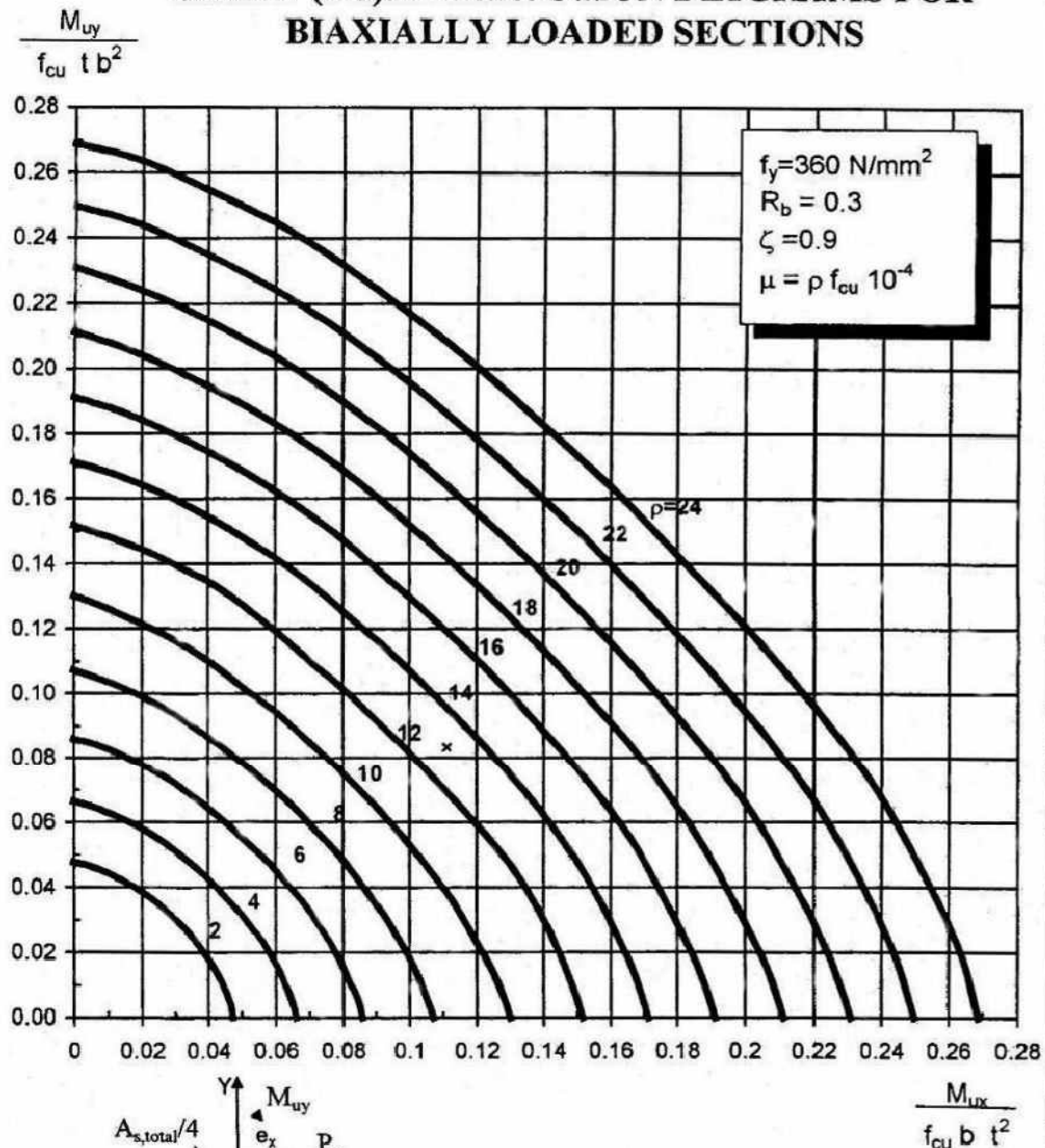


$$R_b = \frac{P_u}{f_{cu} b t}$$

$$\mu = \rho f_{cu} 10^{-4}$$

$$A_{s, \text{total}} = \mu b t$$

**CHART (5-5): INTERACTION DIAGRAMS FOR
BIAXIALLY LOADED SECTIONS**

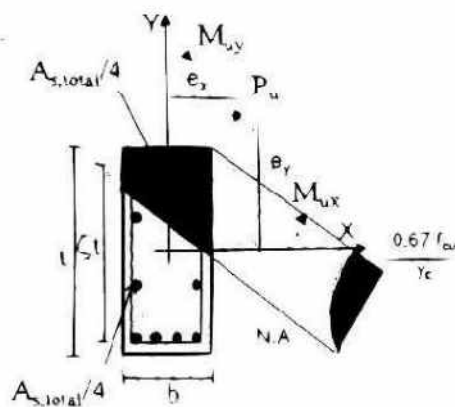
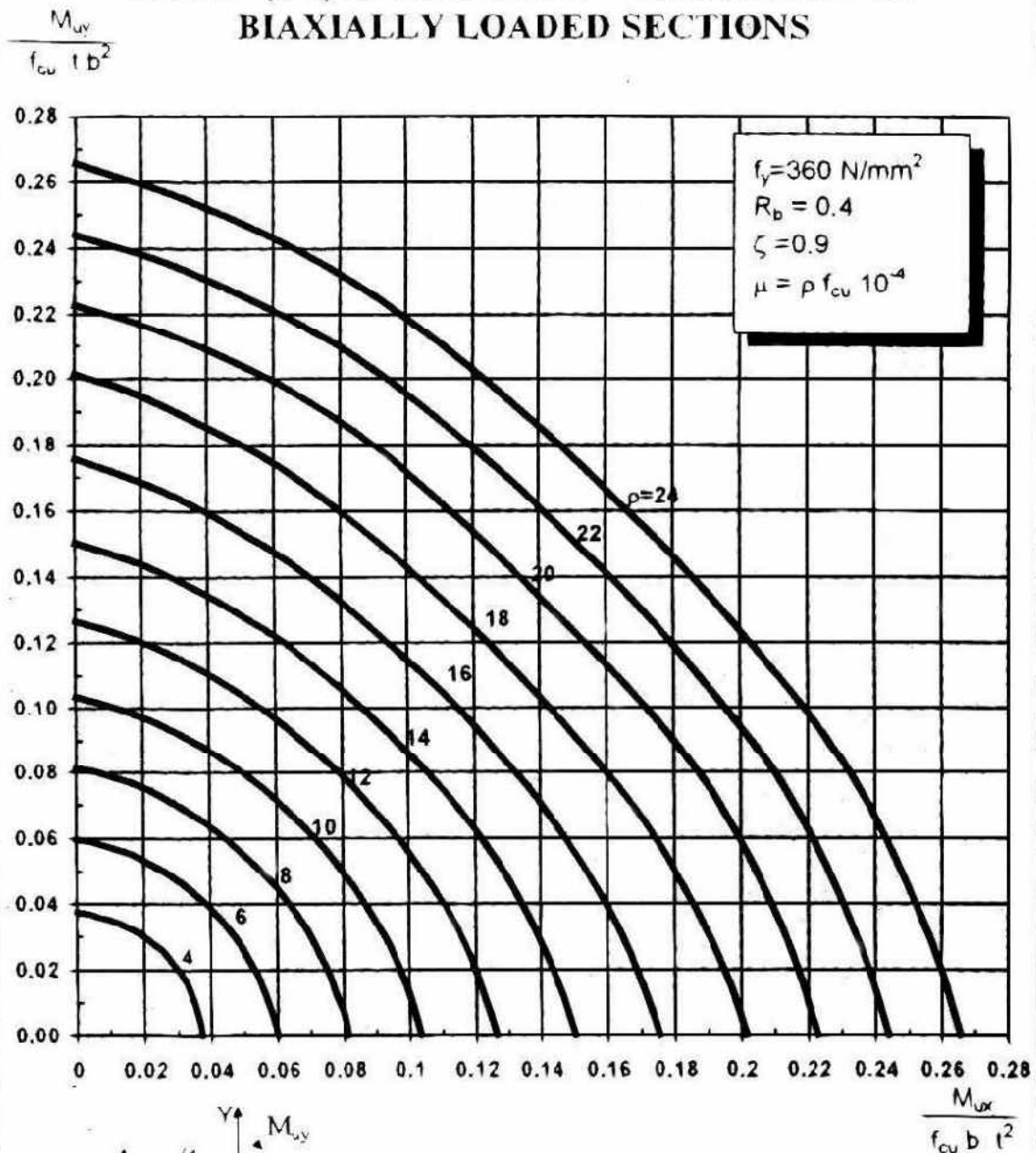


$$R_b = \frac{P_u}{f_{cu} b t}$$

$$\mu = \rho f_{cu} 10^{-4}$$

$$A_{s,total} = \mu b t$$

**CHART (5-6): INTERACTION DIAGRAMS FOR
BIAXIALLY LOADED SECTIONS**

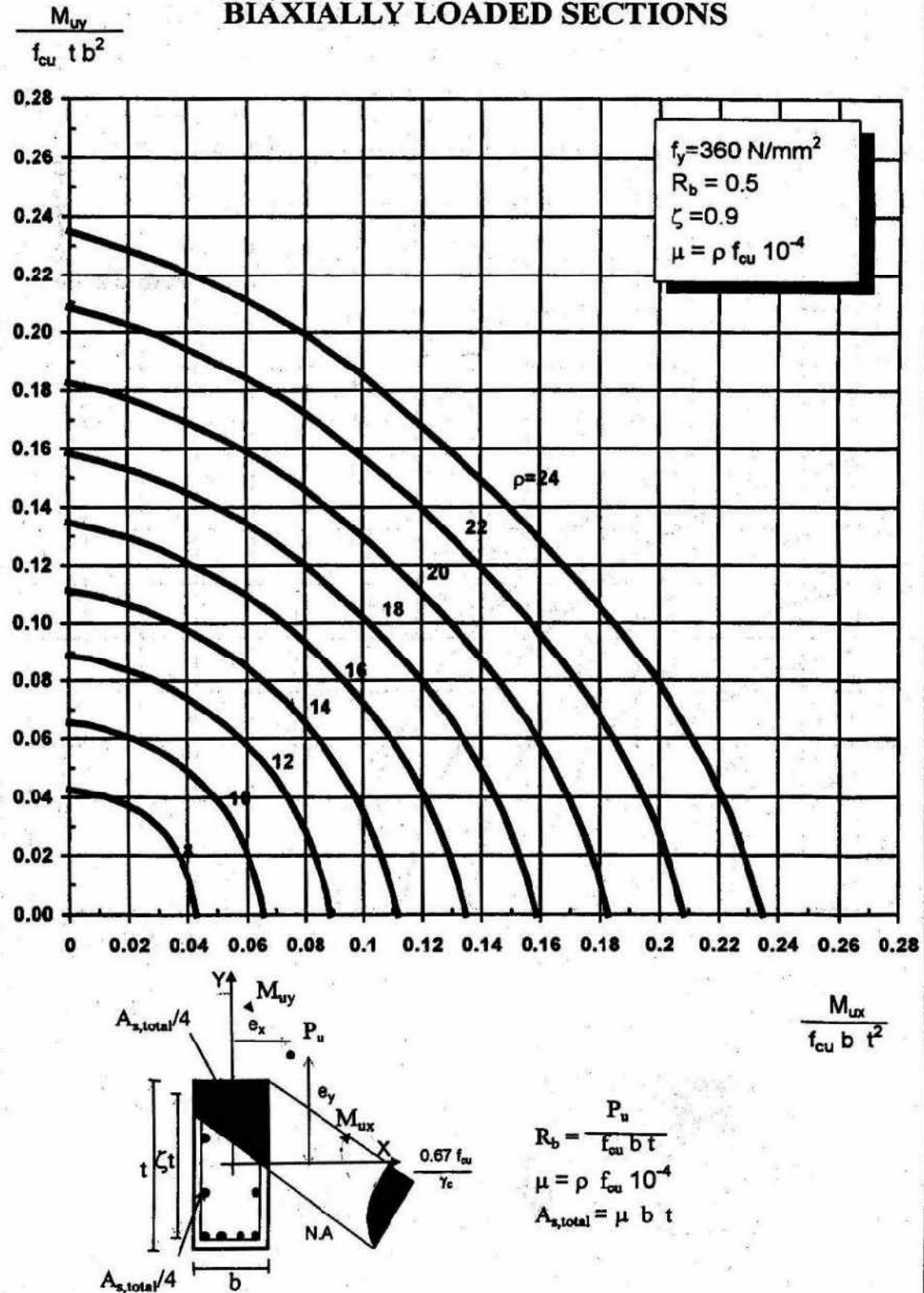


$$R_b = \frac{P_u}{f_{cu} b t}$$

$$\mu = \rho f_{cu} 10^{-4}$$

$$A_{s, total} = \mu b t$$

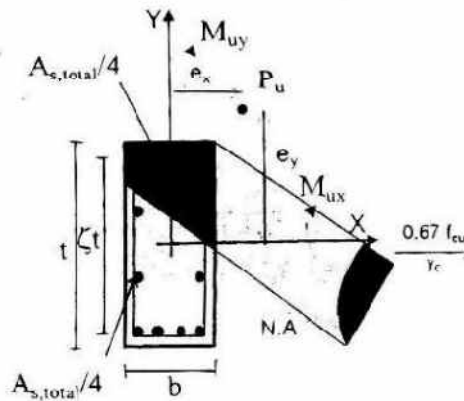
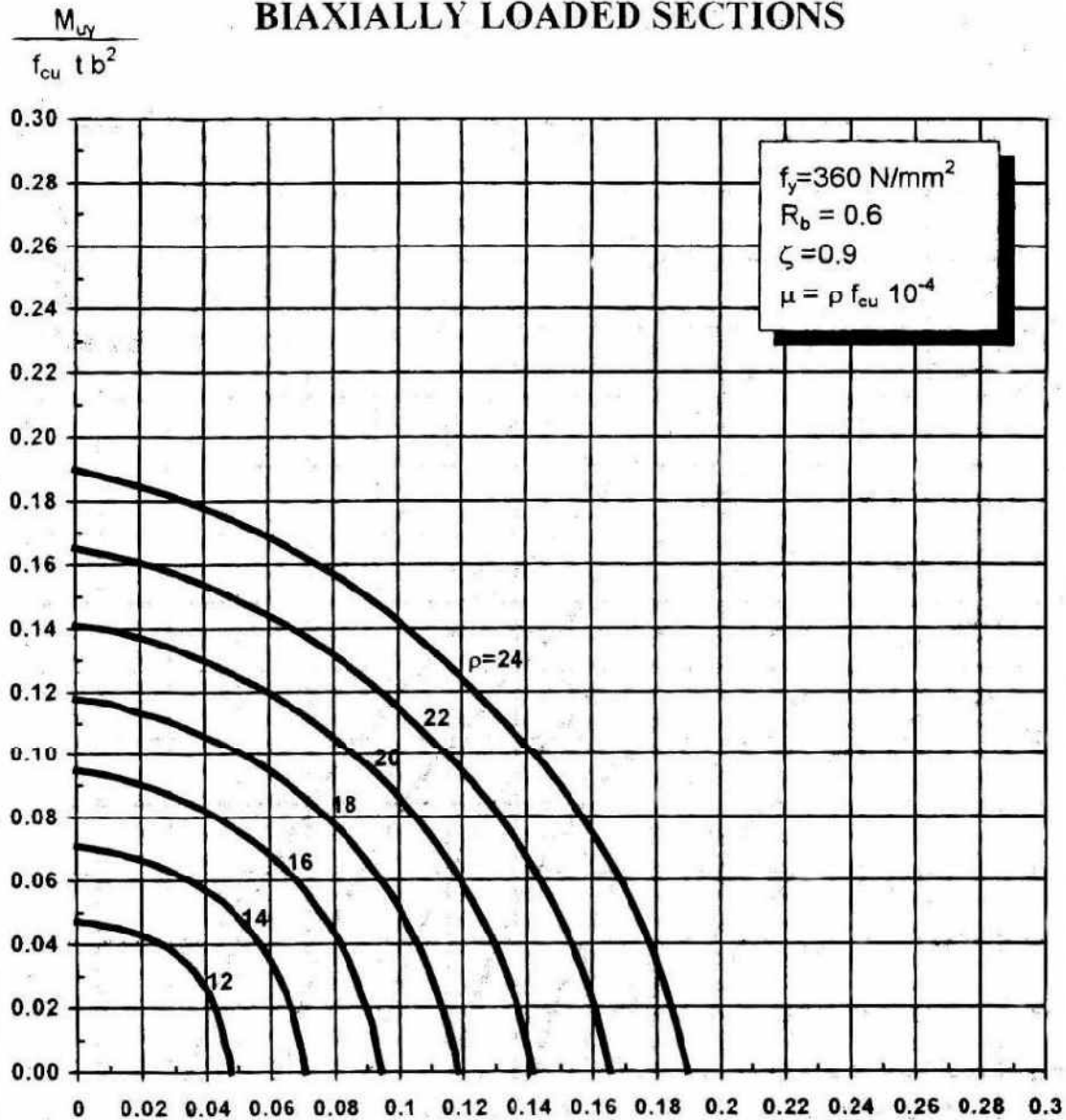
**CHART (5-7): INTERACTION DIAGRAMS FOR
BIAXIALLY LOADED SECTIONS**



ECCS 203-2001 Design Aids

Biaxial Bending

**CHART (5-8): INTERACTION DIAGRAMS FOR
BIAXIALLY LOADED SECTIONS**



$$R_b = \frac{P_u}{f_{cu} b t}$$

$$\mu = \rho f_{cu} 10^{-4}$$

$$A_{s,total} = \mu b t$$

Example.

Data:

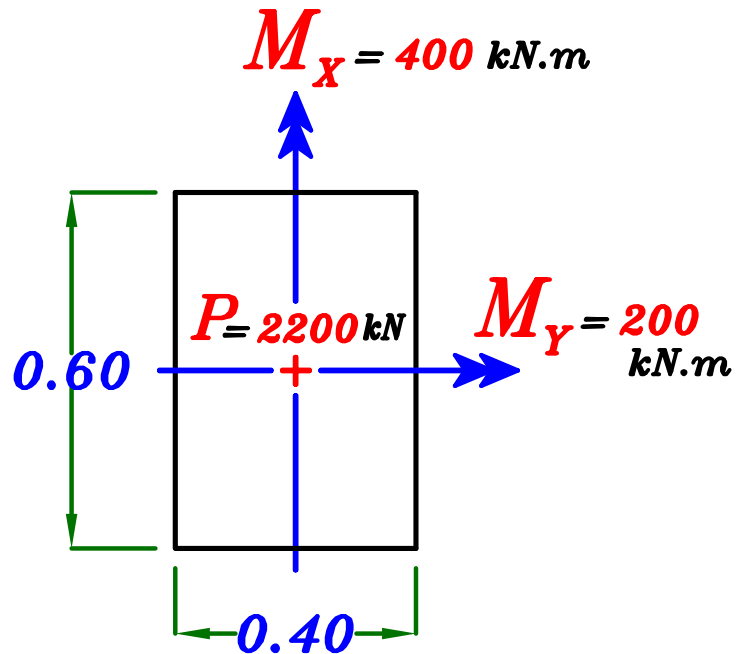
$$F_{cu} = 25 \text{ N/mm}^2$$

$$F_y = 360 \text{ N/mm}^2$$

$$P_{U.L.} = 2200 \text{ kN}$$

$$M_x (U.L.) = 400 \text{ kN.m}$$

$$M_y (U.L.) = 200 \text{ kN.m}$$



Req:

Design the Section.

assume $\zeta = 0.90$ ----- *ECCS* لا توجد قيمة غيرها في ال

$$R_b = \frac{P}{F_{cu} b t} = \frac{2200 \cdot 10^3}{25 \cdot 400 \cdot 600} = 0.366 \longrightarrow \text{Not in } ECCS$$

لانه لا توجد قيمة لـ $R_b = 0.366$ في كتاب *ECCS* فيتم حساب قيمتين لـ ρ مره عند $R_b = 0.30$ و مره عند $R_b = 0.40$ ثم أخذ قيمة لـ ρ بينهم

For $R_b = 0.30 \longrightarrow$ *ECCS* Page (5-13)

$$\frac{M_x}{F_{cu} b t^2} = \frac{400 \cdot 10^6}{25 \cdot 400 \cdot 600^2} = 0.111$$

$$\frac{M_y}{F_{cu} t b^2} = \frac{200 \cdot 10^6}{25 \cdot 600 \cdot 400^2} = 0.083$$

$$\rho = 12.8$$

For $R_b = 0.40 \longrightarrow$ *ECCS* Page (5-14)

$$\frac{M_x}{F_{cu} b t^2} = \frac{400 \cdot 10^6}{25 \cdot 400 \cdot 600^2} = 0.111$$

$$\frac{M_y}{F_{cu} t b^2} = \frac{200 \cdot 10^6}{25 \cdot 600 \cdot 400^2} = 0.083$$

$$\rho = 15$$

نأخذ ρ قيمة بينهم

To get value of ρ For $R_b = 0.366$

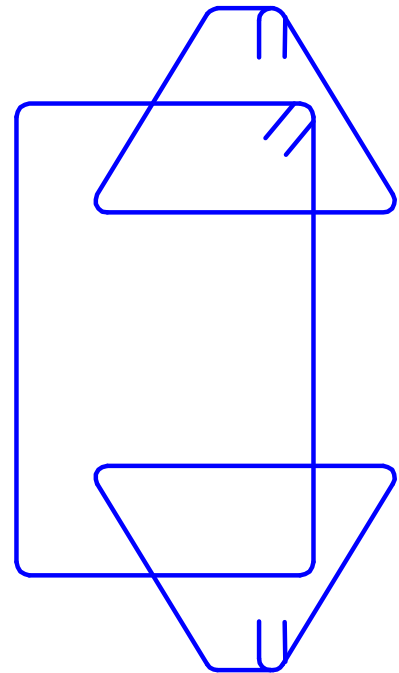
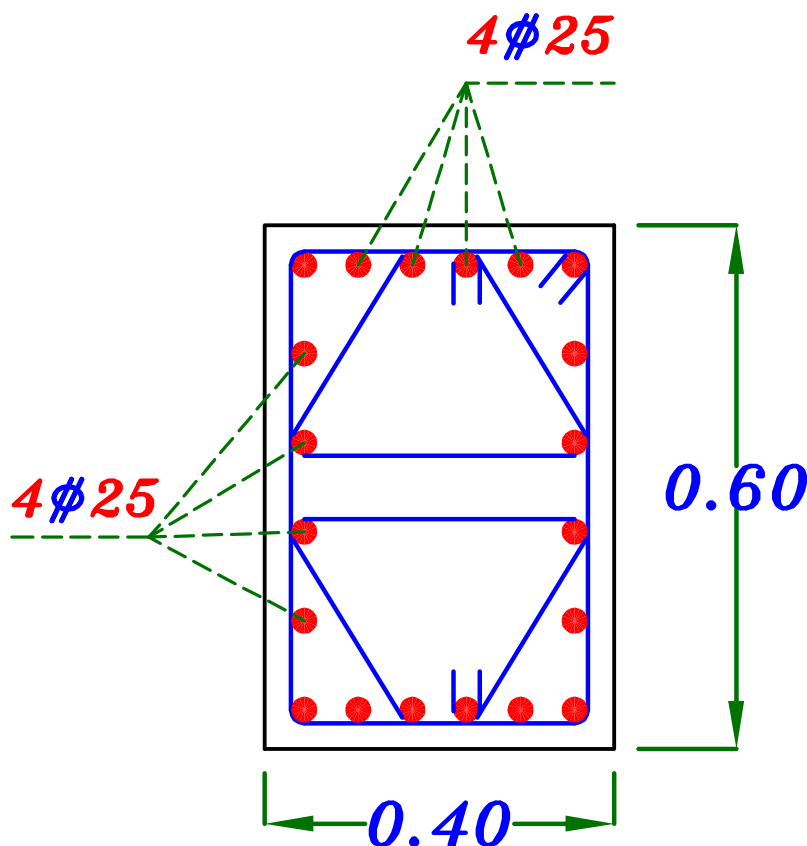
$$\begin{array}{l} R_b = 0.30 \longrightarrow \rho = 12.8 \\ R_b = 0.40 \longrightarrow \rho = 15 \end{array} \left. \vphantom{\begin{array}{l} R_b = 0.30 \\ R_b = 0.40 \end{array}} \right\} \rho = 13.9 \text{ نأخذ قيمه بينهم}$$

$$\mu = \rho * F_{cu} * 10^{-4} = 13.9 * 25 * 10^{-4} = 0.03475$$

$$A_{s_{total}} = \mu * b * t = 0.03475 * 400 * 600 = 8340 \text{ mm}^2$$

– Check $A_{s_{min.}} = \frac{0.8}{100} * b * t = \frac{0.8}{100} * 400 * 600 = 1920 \text{ mm}^2$

$$A_s = A_{s_{total}} = 8340 \text{ mm}^2 \quad \textcircled{20 \phi 25}$$





2- Design using (Uniaxial Bending Interaction Diagram) (Symmetrical arrangement of reinforcement)

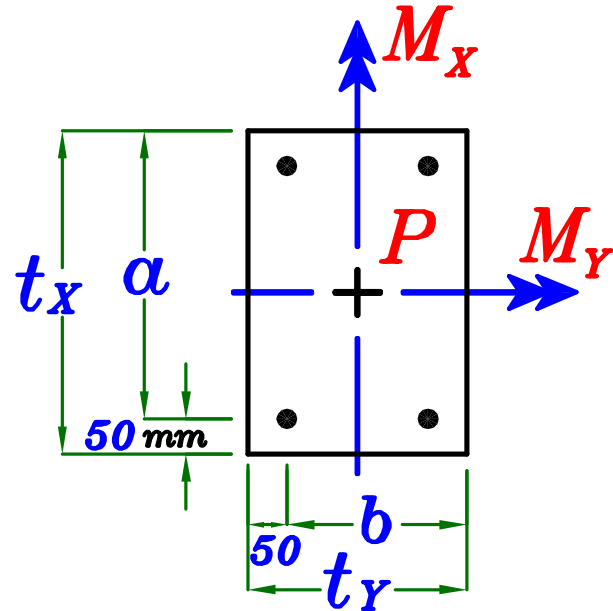
طريقه أخرى تعتمد على تحويل تأثير العزمين الى عزم واحد فقط مكافئ لهم.

نحدد قيمه d التى تقاوم M_x و تسمى مثلاً a

$$a = t_x - 50 \text{ mm}$$

نحدد قيمه d التى تقاوم M_y و تسمى مثلاً b

$$b = t_y - 50 \text{ mm}$$



نحدد العزم الذى سيكون تأثيره اقل على القطاع و نهمله و نأخذ العزم الذى تأثيره اكبر على القطاع و نعمل على تكبيره لكن يكون مكافئ للعزمين معا .
و لمعرفة اى عزم سيتم اهماله و ايه سيتم تكبيره نحسب نسبة كل عزم على ال d التى ستقاومه .

Calculate $\frac{M_x}{a}$, $\frac{M_y}{b}$

We have two cases:

① IF $\frac{M_x}{a} > \frac{M_y}{b}$ Neglect M_y And Calculate M_x'

② IF $\frac{M_y}{b} > \frac{M_x}{a}$ Neglect M_x And Calculate M_y'

① IF $\frac{M_x}{a} > \frac{M_y}{b}$ $\xrightarrow{\text{Neglect } M_y}$ M_x $\xrightarrow{\text{And Calculate}}$ $M_{x'}$

Where:

$$M_{x'} = M_x + \beta \frac{a}{b} M_y$$

$$\beta = 0.9 - \frac{R_b}{2}$$

$$0.6 \leq \beta \leq 0.8$$

IF $\beta < 0.6 \rightarrow \text{Take } \beta = 0.6$

IF $\beta > 0.8 \rightarrow \text{Take } \beta = 0.8$

Where R_b is the Load Level $R_b = \frac{P}{F_{cu} b t}$

Or we can use table in Code Page (6-59)

R_b	≤ 0.2	0.3	0.4	0.5	≥ 0.6
β	0.80	0.75	0.70	0.65	0.60

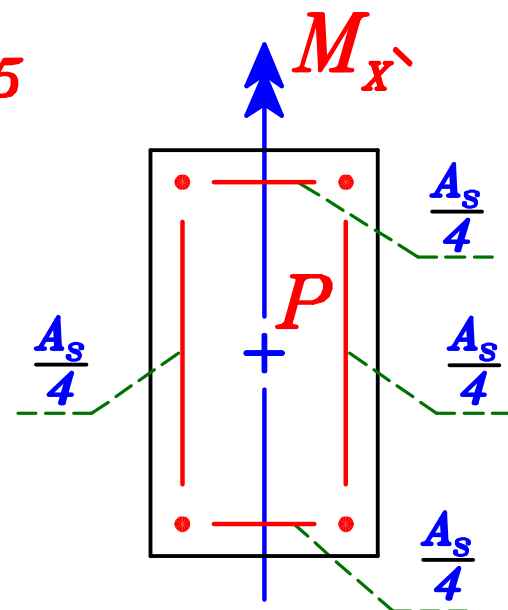
design the section on $P, M_{x'}$

Using Uniaxial I.D. even IF $\frac{e}{t} > 0.5$

Then get $A_s = A_{s'}$

$$A_{s \text{ total}} = A_s + A_{s'}$$

Check $A_{s \text{ total}}$ with $A_{s \text{ min}} = \frac{0.8}{100} * b * t$



نضع أربع أسياخ فى الاركان

ثم يقسم باقى الحديد بالتساوى على الاربع جهات

② IF $\frac{M_Y}{b} > \frac{M_X}{a}$ $\xrightarrow{\text{Neglect}}$ M_X $\xrightarrow{\text{And Calculate}}$ $M_{Y'}$

Where: $M_{Y'} = M_X + \beta \frac{b}{a} M_X$

β is the same as before.

design the section on $P, M_{X'}$

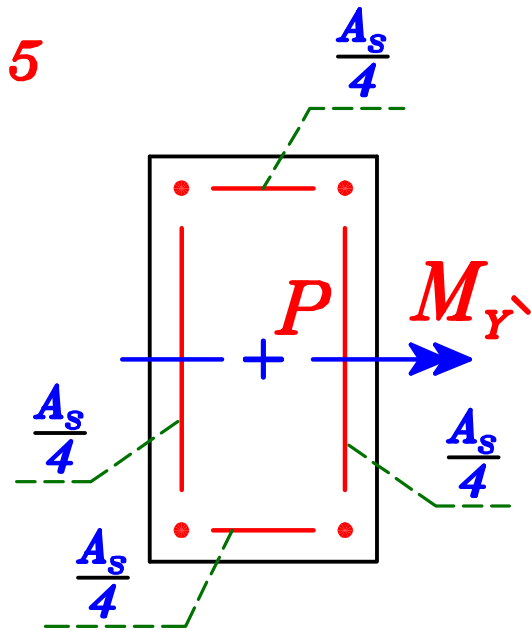
Using *Uniaxial I.D.* even IF $\frac{e}{t} > 0.5$

Then get $A_s = A_{s'}$

$$A_{s \text{ total}} = A_s + A_{s'}$$

Check $A_{s \text{ total}}$ with $A_{s \text{ min}} = \frac{0.8}{100} * b * t$

نضع أربع أسياخ فى الاركان



Example.

Data:

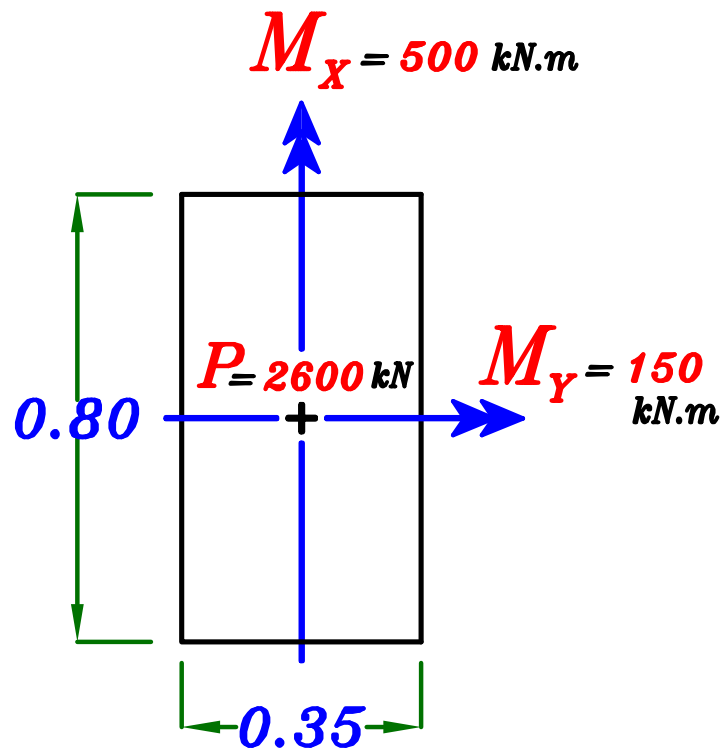
$$F_{cu} = 30 \text{ N/mm}^2$$

$$F_y = 360 \text{ N/mm}^2$$

$$P_{U.L.} = 2600 \text{ kN}$$

$$M_X (U.L.) = 500 \text{ kN.m}$$

$$M_Y (U.L.) = 150 \text{ kN.m}$$



Req: Design the Section with symmetric RFT.

$$a = t_x - 50 \text{ mm} = 800 - 50 = 750 \text{ mm} = 0.75 \text{ m}$$

$$b = t_y - 50 \text{ mm} = 350 - 50 = 300 \text{ mm} = 0.30 \text{ m}$$

$$\frac{M_X}{a} = \frac{500}{0.75} = 666.6, \quad \frac{M_Y}{b} = \frac{150}{0.30} = 500$$

$$\frac{M_X}{a} > \frac{M_Y}{b} \longrightarrow \text{Neglect } M_Y \text{ and design the Sec. on } M_X$$

$$R_b = \frac{P}{F_{cu} b t} = \frac{2600 * 10^3}{30 * 350 * 800} = 0.31$$

$$\beta = 0.9 - \frac{R_b}{2} = 0.9 - \frac{0.31}{2} = 0.745 > 0.6 < 0.8$$

$$M_{X'} = M_X + \beta \left(\frac{a}{b} \right) M_Y$$

$$M_{X'} = 500 + 0.745 \left(\frac{0.75}{0.30} \right) 150 = 779.37 \text{ kN.m}$$

Using *Uniaxial I.D.*

$$M_{x'} = 779.37 \text{ kN.m}$$

$$e = \frac{M}{P} = \frac{779.37}{2600} = 0.299 \text{ m}$$

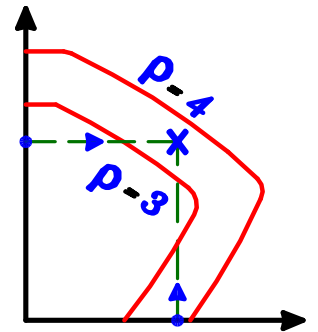
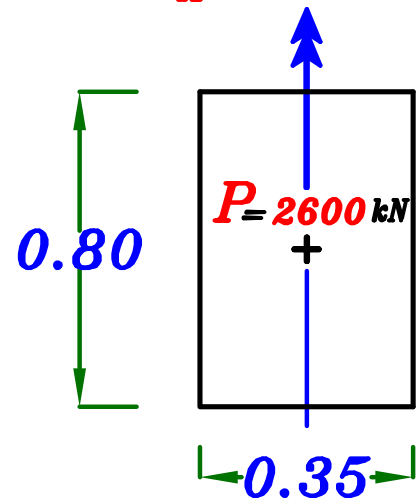
$$\zeta = \frac{800 - 100}{800} = 0.87 = 0.80$$

use *ECCS Design Aids Page 4-24*

$$\frac{P_U}{F_{cu} b t} = \frac{2600 * 10^3}{30 * 350 * 800} = 0.31$$

$$\frac{M_U}{F_{cu} b t^2} = \frac{779.37 * 10^6}{30 * 350 * 800^2} = 0.116$$

$$\rho = 3.6$$



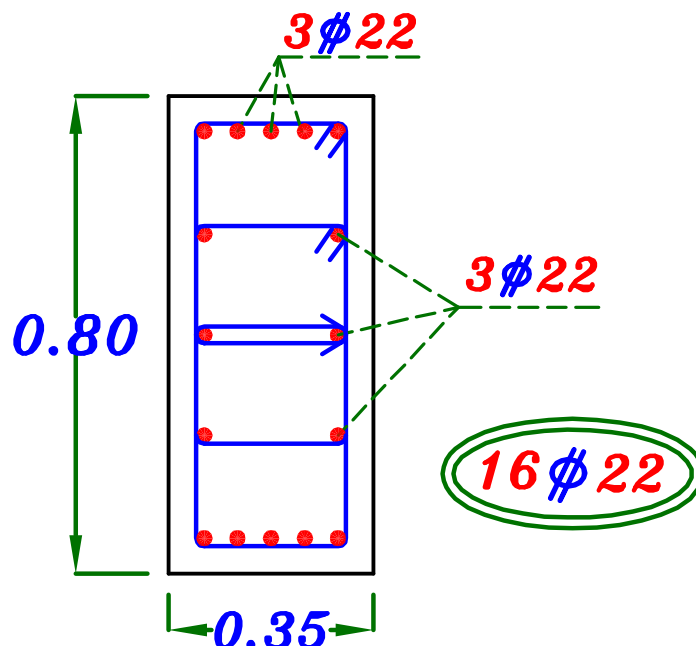
$$\mu = \rho * F_{cu} * 10^{-4} = 3.6 * 30 * 10^{-4} = 0.0108$$

$$A_s = A_{s'} = \mu * b * t = 0.0108 * 350 * 800 = 3024 \text{ mm}^2$$

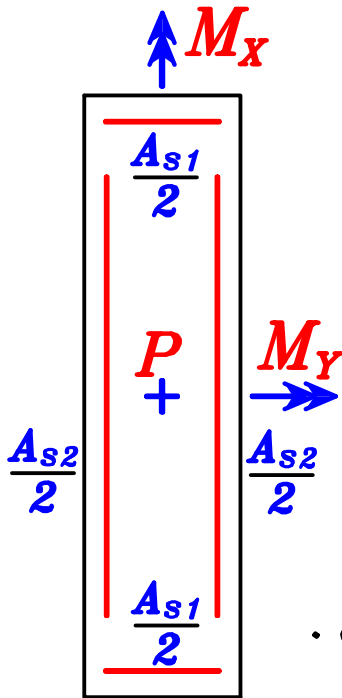
$$A_{s_{Total}} = A_s + A_{s'} = 2 * 3024 = 6048 \text{ mm}^2$$

$$A_{s_{min}} = \frac{0.80}{100} * b * t = \frac{0.80}{100} * 350 * 800 = 2240 \text{ mm}^2 < A_{s_{total}}$$

$$\text{Take } A_s = A_{s_{Total}} = 6048 \text{ mm}^2 \quad \text{16 } \phi 22$$



2 – Unsymmetrical RFT.



و فيما يتم حساب كميه تسليح كل *moment* على حده و تقسيم هذا التسليح الى نصفين و ممكن ان نستخدم هذه الحاله عندما يكون :

Load Level $R_b = \frac{P}{F_{cu} b t} \leq 0.5$

و عندما يكون العرض الكبير لا يقاوم ال *moment* الكبير أو عندما يكون الفرق كبير بين طول و عرض القطاع فلا يكون من المناسب ان نضع التسليح متساوى فى الاربع جهات .

تعتمد هذه الطريقه على ضرب قيمه كلا من M_x و M_y فى معامل α_b

$$M_x' = \alpha_b * M_x , \quad M_y' = \alpha_b * M_y$$

To calculate α_b

- Calculate $R_b = \frac{P}{F_{cu} b t}$ يجب ان لا تزيد قيمه R_b عن 0.5
- Calculate the Ratio $\frac{M_x \backslash \alpha}{M_y \backslash b}$
- Calculate α_b From Table at Code **page 6-61**

$R_b \backslash \frac{M_x \backslash \alpha}{M_y \backslash b}$	∞	3.0	2.0	1.0	0.5	0.33	Zero
$R_b \leq 0.1$	1.0	1.20	1.25	1.30	1.25	1.20	1.0
$R_b = 0.2$	1.0	1.35	1.50	1.75	1.50	1.35	1.0
$R_b = 0.3$	1.0	1.25	1.35	1.40	1.35	1.25	1.0
$R_b = 0.4$	1.0	0.95	0.95	0.95	0.95	0.95	1.0
$R_b \geq 0.5$	1.0	0.65	0.70	0.75	0.70	0.65	1.0

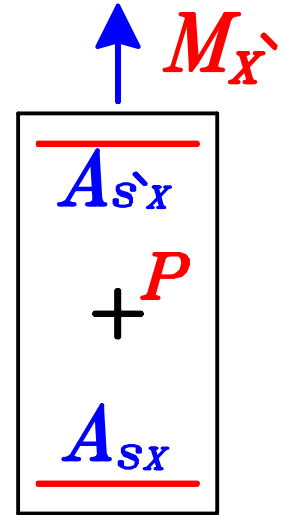
① Design on P, M_x'

Using **Uniaxial I.D.**

Get $A_{sx} = A_{s'x}$

ثم يتم وضع التسليح $A_{sx} + A_{s'x}$

فى الاتجاه الرأسى لمقاومه M_x'



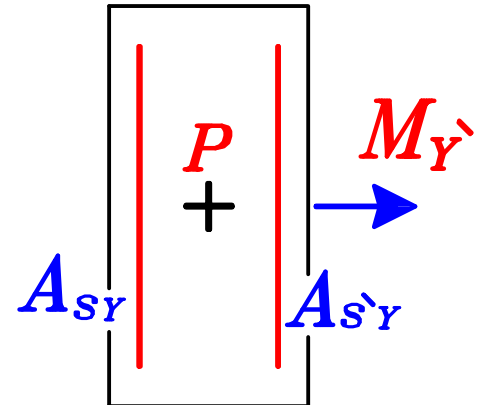
② Design on P, M_y'

Using **Uniaxial I.D.**

Get $A_{sy} = A_{s'y}$

ثم يتم وضع التسليح $A_{sy} + A_{s'y}$

فى الاتجاه الافقى لمقاومه M_y'



Check A_{smin}

يتم حساب $A_{sT} = A_{sx} + A_{s'x} + A_{sy} + A_{s'y}$

و حساب $A_{smin} = \frac{0.80}{100} * b * t$

IF $A_{sT} > A_{smin}$ $\xrightarrow{\text{use}}$ $A_{sx}, A_{s'x}, A_{sy} \& A_{s'y}$

IF $A_{sT} < A_{smin}$ $\xrightarrow{\text{use}}$ A_{smin}

يتم تقسيم قيمه A_s الكليه التى ستوضع فى القطاع على الاربع اتجاهات لكن بنسبه

$$\frac{A_{sx}}{A_{sy}} = \frac{\text{مساحه الحديد الذى سيوضع فى اتجاه } M_x}{\text{مساحه الحديد الذى سيوضع فى اتجاه } M_y} \text{ نسبه}$$

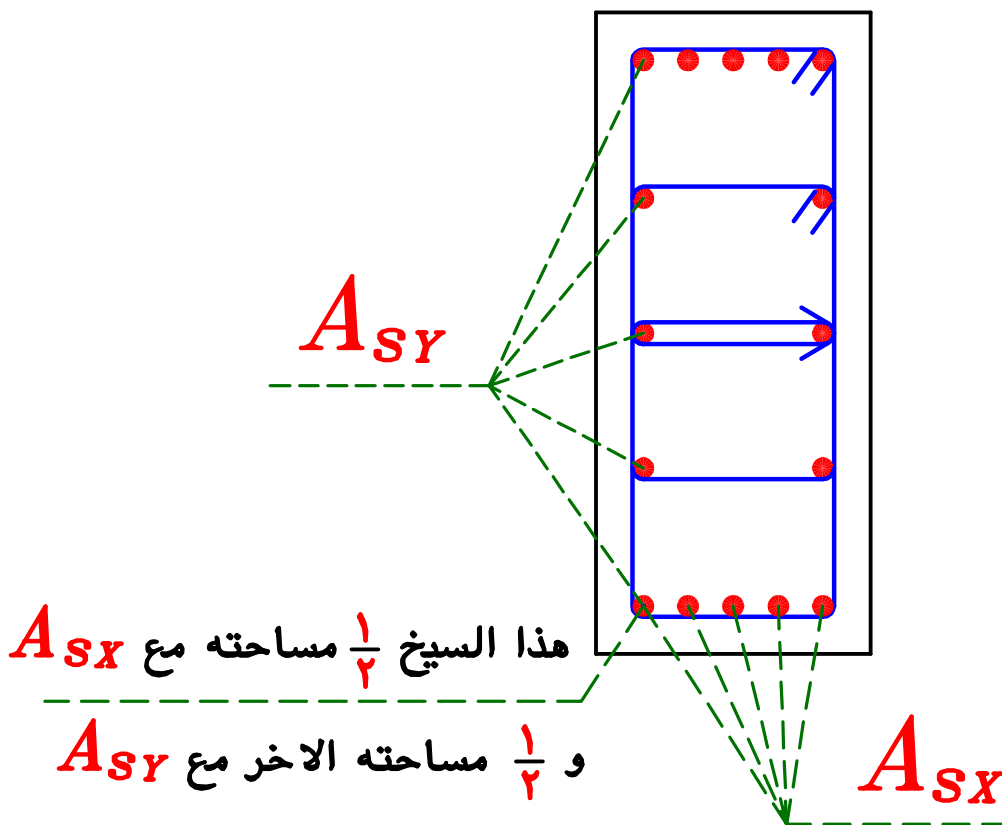
مع اخذ السيخ الذى سيوضع فى الركن نصف مساحته مع A_{sx} و النصف الاخر مع A_{sy}

$$\text{No. of Bars to resist } M_x = \frac{A_{sx}}{A_{sx} + A_{sy}} * \text{Total No. of bars}$$

و يتم تقسيم الحديد الى نصفين نصف اسفل القطاع و نصف اعلى

$$\text{No. of Bars to resist } M_y = \frac{A_{sy}}{A_{sx} + A_{sy}} * \text{Total No. of bars}$$

و يتم تقسيم الحديد الى نصفين نصف جهه اليمين و نصف جهه اليسار .



Example.

Data:

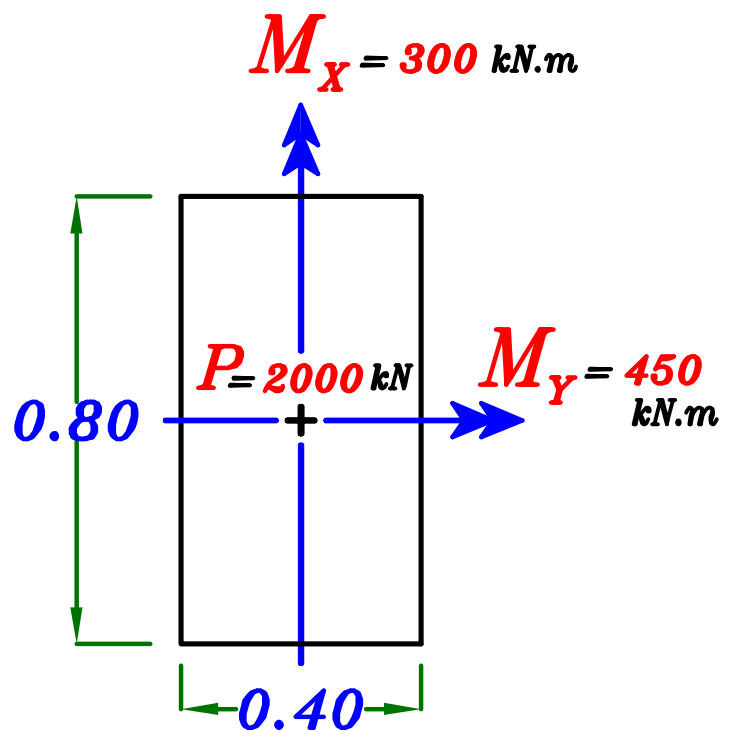
$$F_{cu} = 30 \text{ N/mm}^2$$

$$F_y = 360 \text{ N/mm}^2$$

$$P_{U.L.} = 2000 \text{ kN}$$

$$M_x (U.L.) = 300 \text{ kN.m}$$

$$M_y (U.L.) = 450 \text{ kN.m}$$



Req:

Design the Section with unsymmetric RFT.

$$R_b = \frac{P}{F_{cu} b t} = \frac{2000 * 10^3}{30 * 400 * 800} = 0.208 < 0.5 \therefore \text{o.k.}$$

$$\alpha = t_x - 50 \text{ mm} = 800 - 50 = 750 \text{ mm} = 0.75 \text{ m}$$

$$b = t_y - 50 \text{ mm} = 400 - 50 = 350 \text{ mm} = 0.35 \text{ m}$$

$$\frac{M_x}{\alpha} = \frac{300}{0.75} = 400, \quad \frac{M_y}{b} = \frac{450}{0.30} = 1500$$

$$\therefore \frac{M_x \backslash \alpha}{M_y \backslash b} = \frac{400}{1500} = 0.267$$

Calculate α_b From Table at Code page 6-61

$R_b \backslash \frac{M_x \backslash \alpha}{M_y \backslash b}$	∞	3.0	2.0	1.0	0.5	0.33	Zero
$R_b \leq 0.1$	1.0	1.20	1.25	1.30	1.25	1.20	1.0
$R_b = 0.2$	1.0	1.35	1.50	1.75	1.50	1.35	1.0
$R_b = 0.3$	1.0	1.25	1.35	1.40	1.35	1.25	1.0
$R_b = 0.4$	1.0	0.95	0.95	0.95	0.95	0.95	1.0
$R_b \geq 0.5$	1.0	0.65	0.70	0.75	0.70	0.65	1.0

From Interpolation

$$\alpha_b = 1.24$$

$$M_{X'} = \alpha_b * M_X = 1.24 * 300 = 372 \text{ kN.m}$$

$$M_{Y'} = \alpha_b * M_Y = 1.24 * 450 = 558 \text{ kN.m}$$

ثم يتم تصميم القطاع مرتين باستخدام *Uniaxial I.D.*

① Design on $P, M_{X'}$

$$\zeta = \frac{800 - 100}{800} = 0.87 = 0.80$$

use *ECCS Design Aids* Page 4-24

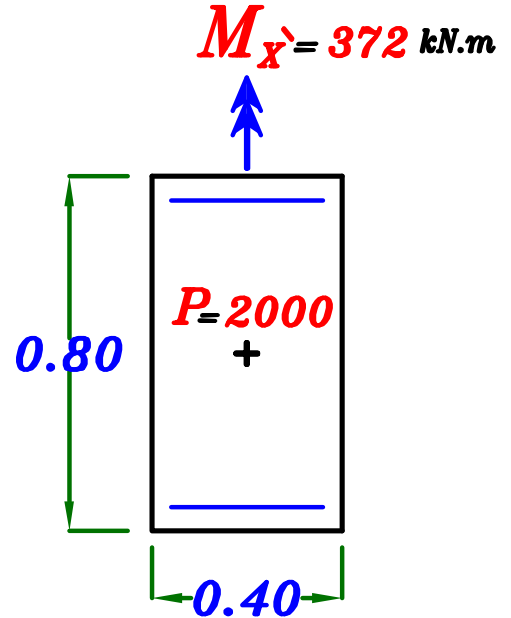
$$\frac{P_u}{F_{cu} b t} = \frac{2000 * 10^3}{30 * 400 * 800} = 0.208$$

$$\frac{M_{X'}}{F_{cu} b t^2} = \frac{372 * 10^6}{30 * 400 * 800^2} = 0.048$$

$$\rho < 1.0 \rightarrow \rho = 1.0$$

$$\mu = \rho * F_{cu} * 10^{-4} = 1.0 * 30 * 10^{-4} = 0.003$$

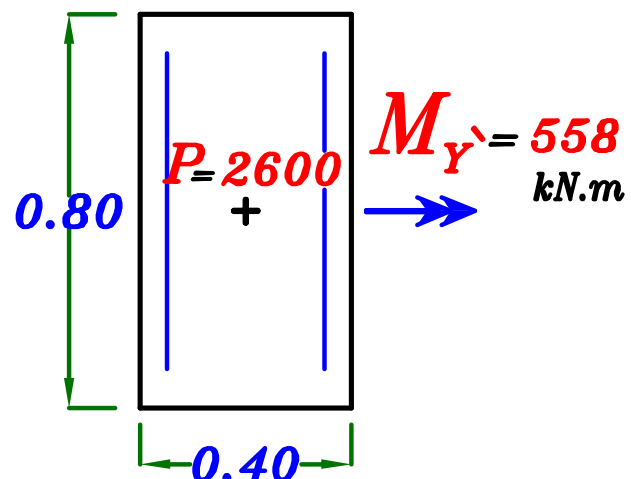
$$A_{sx} = A_{s'x} = \mu * b * t = 0.003 * 400 * 800 = 960 \text{ mm}^2$$



② Design on $P, M_{Y'}$

$$\zeta = \frac{400 - 100}{400} = 0.75 = 0.70$$

use *ECCS Design Aids* Page 4-25



$$\left. \begin{aligned} \frac{P_u}{F_{cu} b t} &= \frac{2000 * 10^3}{30 * 800 * 400} = 0.208 \\ \frac{M_Y}{F_{cu} b t^2} &= \frac{558 * 10^6}{30 * 800 * 400^2} = 0.145 \end{aligned} \right\} \rho = 4.0$$

$$\mu = \rho * F_{cu} * 10^{-4} = 4.0 * 30 * 10^{-4} = 0.012$$

$$A_{sY} = A_{s'Y} = \mu * b * t = 0.012 * 800 * 400 = 3840 \text{ mm}^2$$

Check A_{smin}

$$A_{sT} = A_{sX} + A_{s'X} + A_{sY} + A_{s'Y} = 2 * 960 + 2 * 3840 = 9600 \text{ mm}^2$$

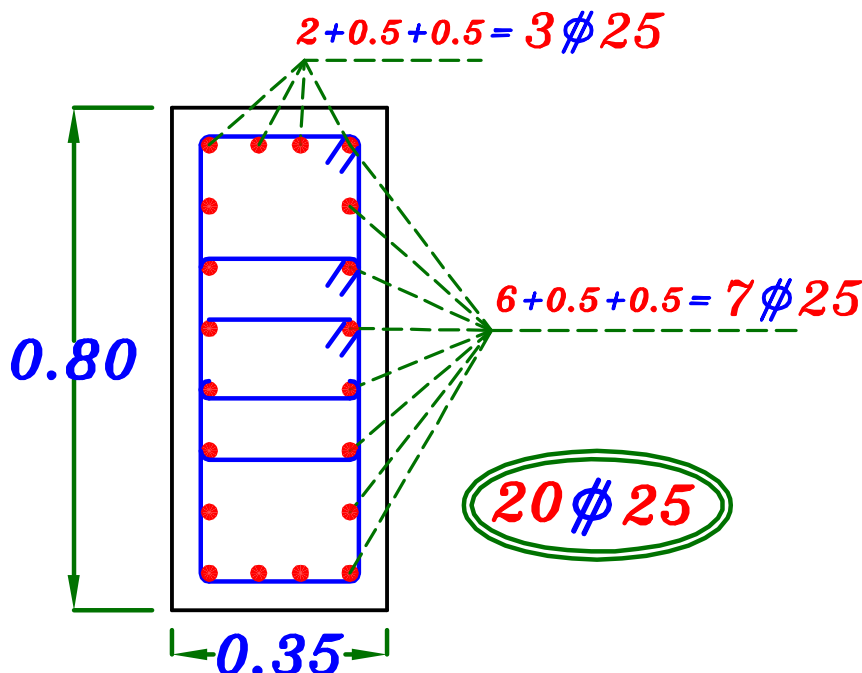
$$A_{smin} = \frac{0.80}{100} * b * t = \frac{0.80}{100} * 400 * 800 = 2560 \text{ mm}^2$$

$$\therefore A_{sT} > A_{smin} \therefore \text{Take } A_{sT} = 9600 \text{ mm}^2 = \textcircled{20 \phi 25}$$

نأخذ ٤ أسياخ فى الاركاب و ال ١٦ سيخ المتبقية سيتم توزيعهم على اتجاهى M_Y و M_X على التوالى بنفس نسبة $A_{sY} : A_{sX}$ أى بنسبة 1596 : 2604

$$\text{No. of Bars to resist } M_X = \frac{960}{960 + 3840} * 16 = 3.2 = 4.0 \text{ bars}$$

$$\text{No. of Bars to resist } M_Y = \frac{4416}{2604 + 3840} * 16 = 12.8 = 12.0 \text{ bars}$$



Special Case.

إذا كانت الكمره يؤثر عليها M_X , M_Y و لا يؤثر عليها P أى $R_b = \text{Zero}$
فمن المسموح أن نأخذ قيمه $\alpha_b = 1.0$
أى نصمم على قيم M_X و M_Y كما هم .

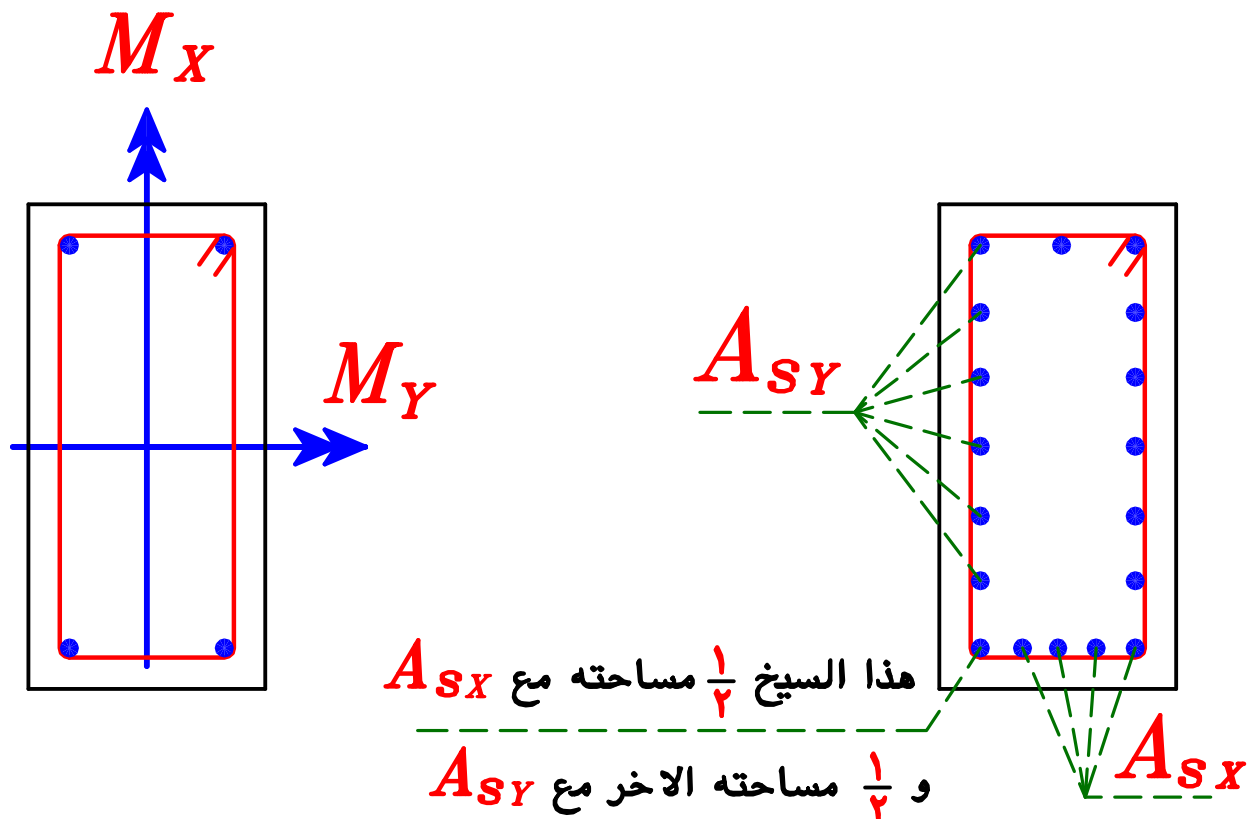
و يتم تصميم قطاع الكمره مرتين :

١- يتم تصميم قطاع الكمره على M_X فقط و تحديد قيمه A_{sx}

Check $A_{sx} > A_{smin} = \mu_{min.} b d \xrightarrow{\text{IF not}} \text{Take } A_{sx} = A_{smin}$

٢- يتم تصميم قطاع الكمره على M_Y فقط و تحديد قيمه A_{sy}

Check $A_{sy} > A_{smin} = \mu_{min.} b d \xrightarrow{\text{IF not}} \text{Take } A_{sy} = A_{smin}$



Concrete Dimensions of Frames.



Stiffness.

كلما زادت ال **Stiffness** لا **member** سواء كان كمره أو عمود كلما كان ال **member** أقوى و بالتالى يقل ال **deflection** و بالتالى يحمل هذا ال **member** جزء أكبر من الحمل .

$$K = \frac{EI}{L}$$

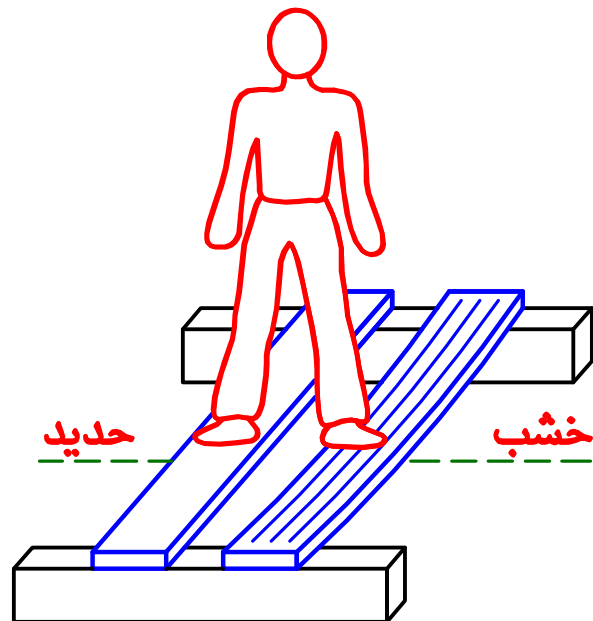
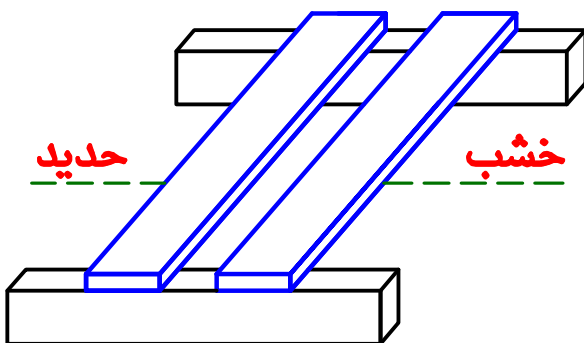
و نعبر عن ال **Stiffness** برمز **K** و **K** تعبر عن نسبة ال **Stiffness** و ليست عن القيمة الفعلية لا **Stiffness**

حيث **E** هى معايير المرونه و يعتمد على الماده المكون منها ال **member** و كلما كانت الماده أقوى كلما زادت قيمه ال **E** كلما زادت ال **Stiffness**

Example.

إذا وجد لوحان لهم نفس القطاع و نفس الطول و لكن نوع الماده مختلف مثلاً خشب و حديد إذا وضع حمل على اللوحان سيحدث للخشب **deflection** أكبر و بالتالى سيحمل الحديد الجزء الأكبر من الحمل .

$$\therefore E_{Steel} > E_{Wood}$$
$$\therefore K_{Steel} > K_{Wood}$$



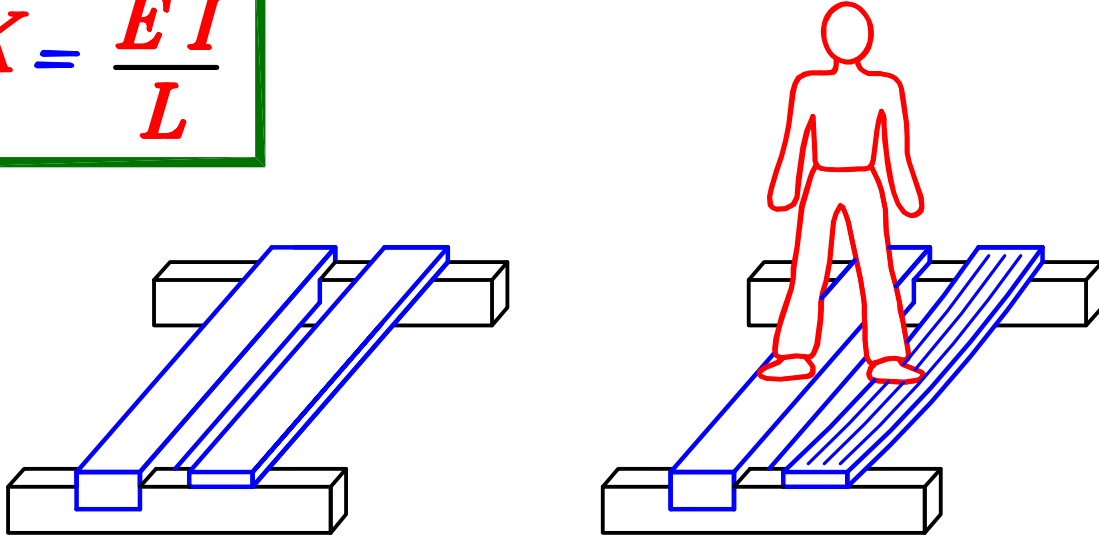
حيث I هي *moment of Inertia* لقطاع ال *member* و يعتمد على

$$I = \frac{bt^3}{12} \quad t \text{ أبعاد القطاع و خاصه ال}$$

و كلما زادت أبعاد القطاع زادت ال I كلما زادت ال *Stiffness*

Example. اذا وجد لوحان من نفس المادة و لهما نفس الطول و لكن أبعاد قطاعيهما مختلفان اذا وضع حمل على اللوحان سيحدث للوح الذي له أبعاد أقل *deflection* أكبر و بالتالي سيحمل اللوح الذي له أبعاد أكبر الجزء الأكبر من الحمل .

$$K = \frac{EI}{L}$$

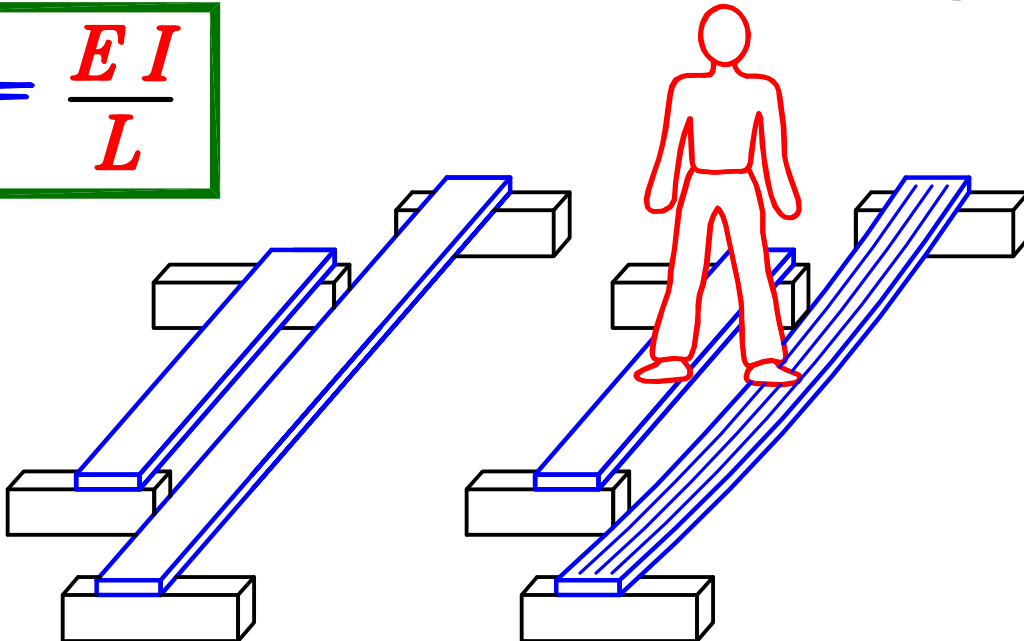


حيث L هي طول ال *member*

و كلما زاد طول ال *member* L كلما قلت ال *Stiffness*

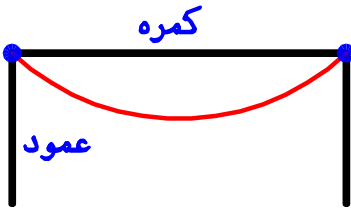
Example. اذا وجد لوحان من نفس المادة و لهما نفس القطاع و لكن طولهما مختلف اذا وضع حمل على اللوحان سيحدث للوح الاطول *deflection* أكبر و بالتالي سيحمل اللوح الاقصر الجزء الأكبر من الحمل .

$$K = \frac{EI}{L}$$



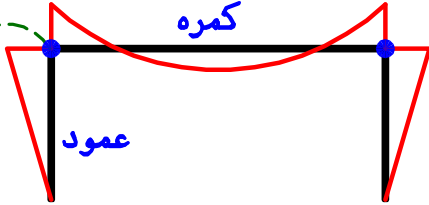
Connection between Beam & Column.

Hinged Joint

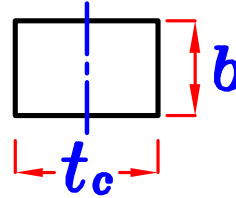
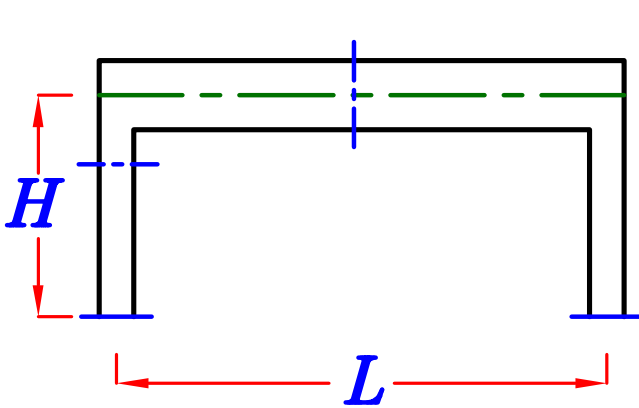


يتكون ال **B.M.** من الاحمال الموجوده على الكمره
أى أنه دائما الكمره عليها **B.M.**

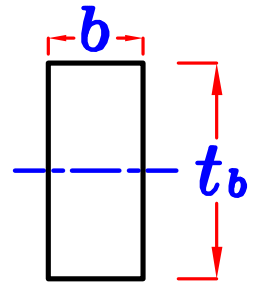
Rigid Joint



ولكن وجود **B.M.** على العمود يعتمد على ال **Joint**
بين الكمره و العمود اذا كانت **Hinged or Rigid**
و ذلك يعتمد على ال **Stiffness** بين كلا من الكمره و العمود



$$I_c = \frac{b t_c^3}{12}$$



$$I_b = \frac{b t_b^3}{12}$$

$$K_b = \frac{E I_b}{L}$$

$$K_c = \frac{E I_c}{H}$$

Relative Stiffness.

$$K_r = \frac{K_b}{K_c}$$



إذا كانت قيمه K_r كبيره نسبيا تعتبر ال **Joint** بين الكمره و العمود **Hinged**



إذا كانت قيمه K_r صغيره نسبيا تعتبر ال **Joint** بين الكمره و العمود **Rigid**



للتسهيل سنعتبر أنه عندما تكون $t_c \leq \frac{t_b}{2}$ تكون **Hinged Joint**



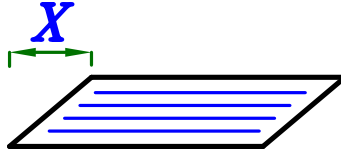
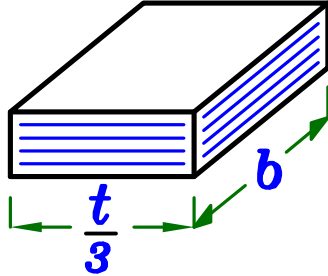
و عندما تكون $t_c \geq 0.8 t_b$ تكون **Rigid Joint**

Real Hinge.

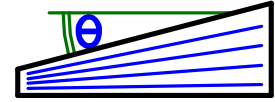


Neoprene Plate.

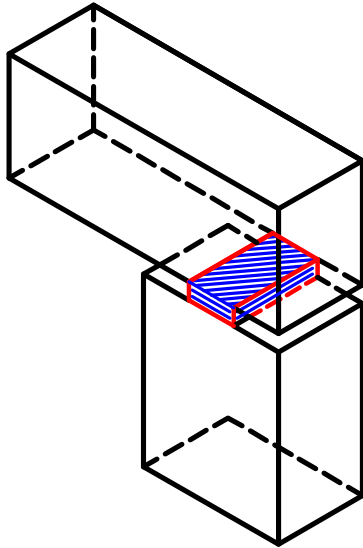
ال **Neoprene Plate** هي ألواح من الصلب بينها شرائح من المطاط المضغوط .
توضع بين العمود و الكمره أو بين العمود و القاعده لعمل **Real Hinge**
و فائدتها أنها تسمح بالحركة الأفقيه و الدوران .



الحركة الأفقيه X



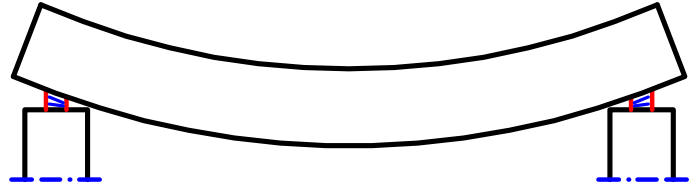
الدوران θ



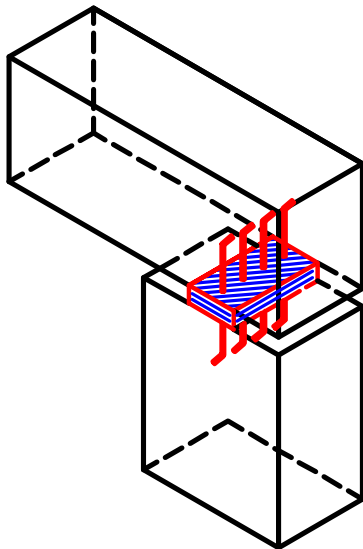
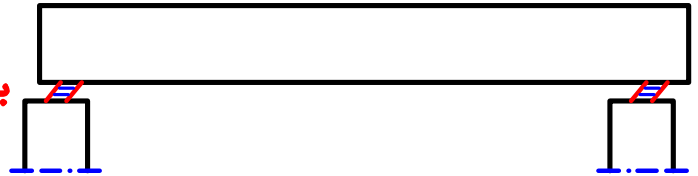
تسمح بالحركة الأفقيه و تسمح بالدوران

لذلك تعتبر **Roller support**

تسمح بالدوران
أي لا تنقل عزوم
على العمود



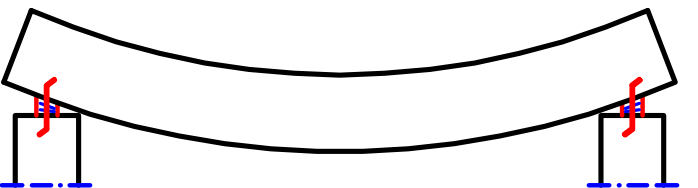
تسمح
بالحركة الأفقيه



توضع صف أسياخ حديد في المنتصف تماما
فتمنع الحركة الأفقيه و لكن لا تمنع الدوران

لذلك تعتبر **Hinged support**

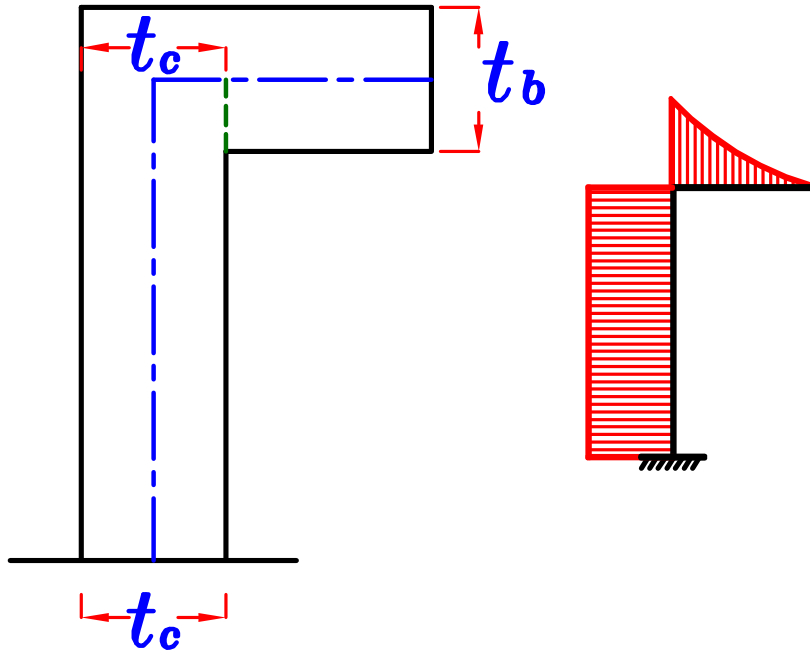
تسمح بالدوران
أي لا تنقل عزوم
على العمود



Coumns Concrete Dimensions.

توجد عدة أشكال لاعمدته الـ **Frames** يجب أولا أن نتعلم رسم الخرسانه للاعمده

Concrete Dimensions.



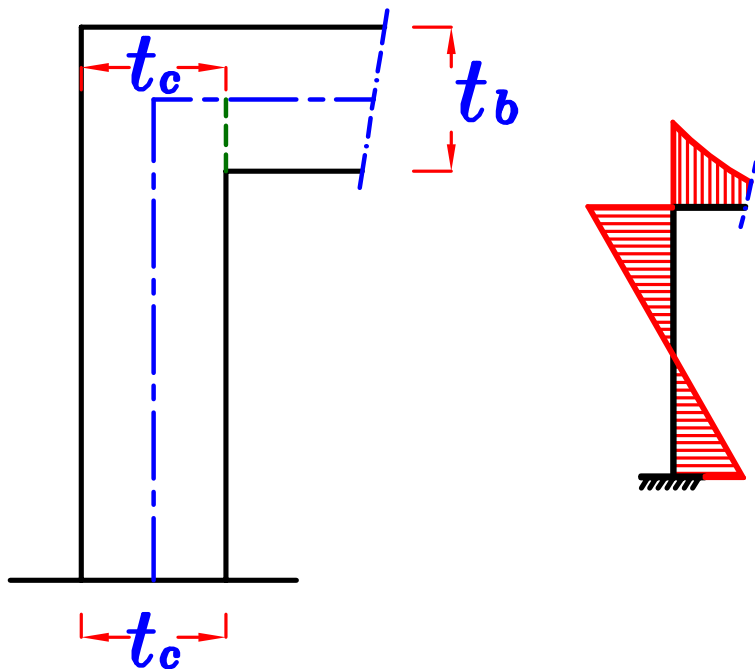
$$t_c \geq 0.8 t_b$$

حتى تكون **Rigid Joint**

ملحوظه

يمكن من التصميم

أن تكون $t_c > t_b$



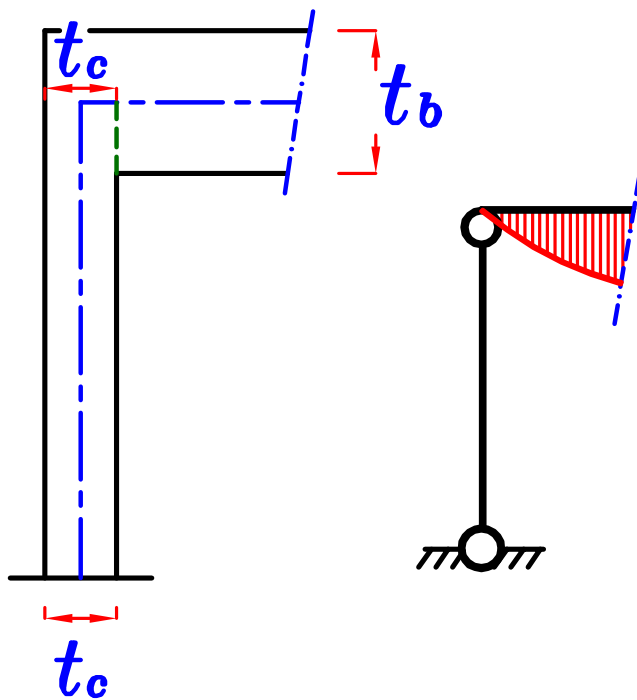
$$t_c \geq 0.8 t_b$$

حتى تكون **Rigid Joint**

ملحوظه

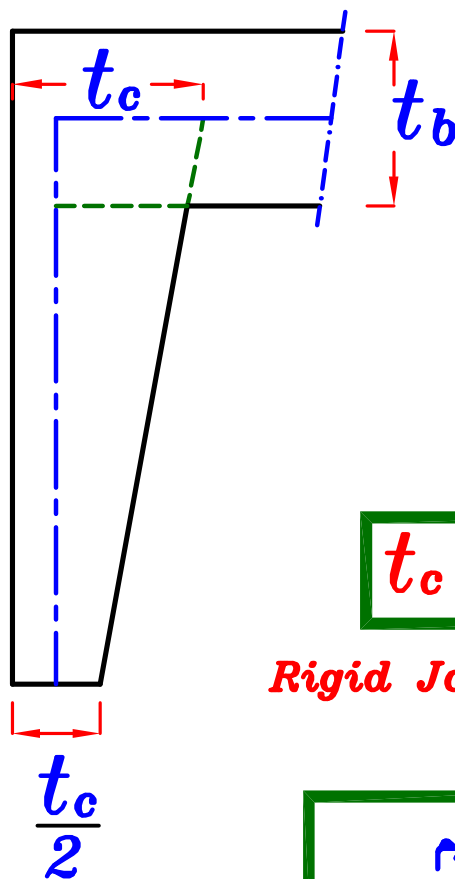
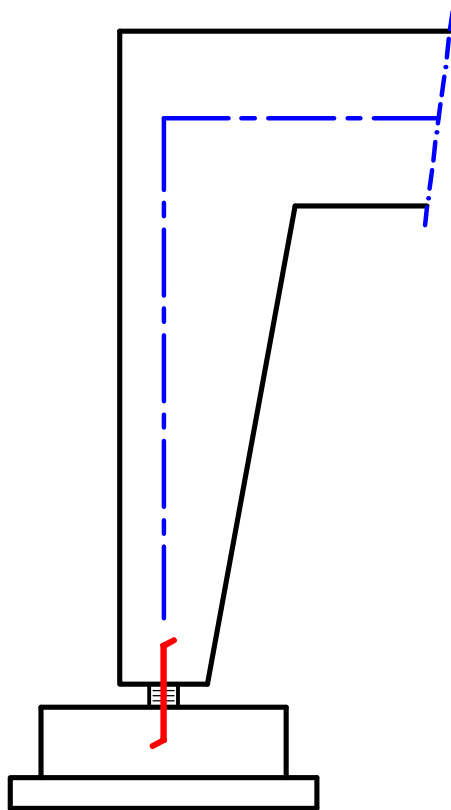
يمكن من التصميم

أن تكون $t_c > t_b$



$$t_c = \frac{t_b}{2}$$

حتى تكون Hinged Joint



$$t_c \geq 0.8 t_b$$

حتى تكون Rigid Joint

ملحوظه

يمكن من التصميم

أن تكون $t_c > t_b$

Reinforcement splices.

و وصلات التسليح

إذا زاد طول السيخ عن -١٢م المفروض أن نعمل وصله فى سيخ الحديد .

Types of splices. أنواع الوصلات

- 1- *Lap splices.* وصلات بالتراكب
- 2- *Mechanical splices.* وصلات ميكانيكية
- 3- *Welded splices.* وصلات لحام

و الاسهل فى التنفيذ اذا كان ال *member* واقع عليه
moment or compression أن تكون الوصلات بالتراكب .

أما اذا كان ال *member* واقع عليه *tension*
فيجب أن تكون الوصلة اما وصله ميكانيكية او وصله لحام

ملحوظه

فى المشاريع الكبرى ممكن عمل أسياخ خاصه للمشروع
طولها أكبر من -١٢م و تسمى *special order*
و هى لا تحتاج لوصلات .

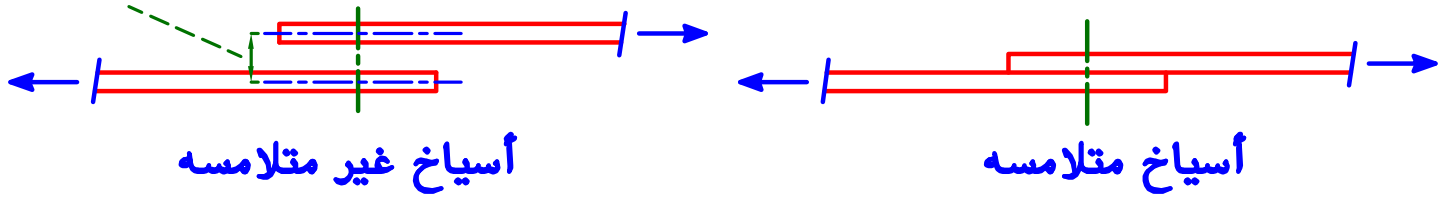
1- Lap splices. وصلات بالتراكب

و هي وصلات تعتمد على تراكب الاسياخ

تنتقل الاجهادات بين الاسياخ عن طريق نقلها اولا الى الخرسانه عن طريق قوه التماسك بين الحديد و الخرسانه و أيضا بقوه التماسك تنتقل الاجهادات الى الاسياخ الاخرى .

و تكون وصله التراكب بين اسياخ متلامسه او اسياخ غير متلامسه .

لا تزيد المسافه عن ١٥ سم
او ٢٠٪ من طول الوصله



فى حاله الـ *member* المعرضه لـ *moment*

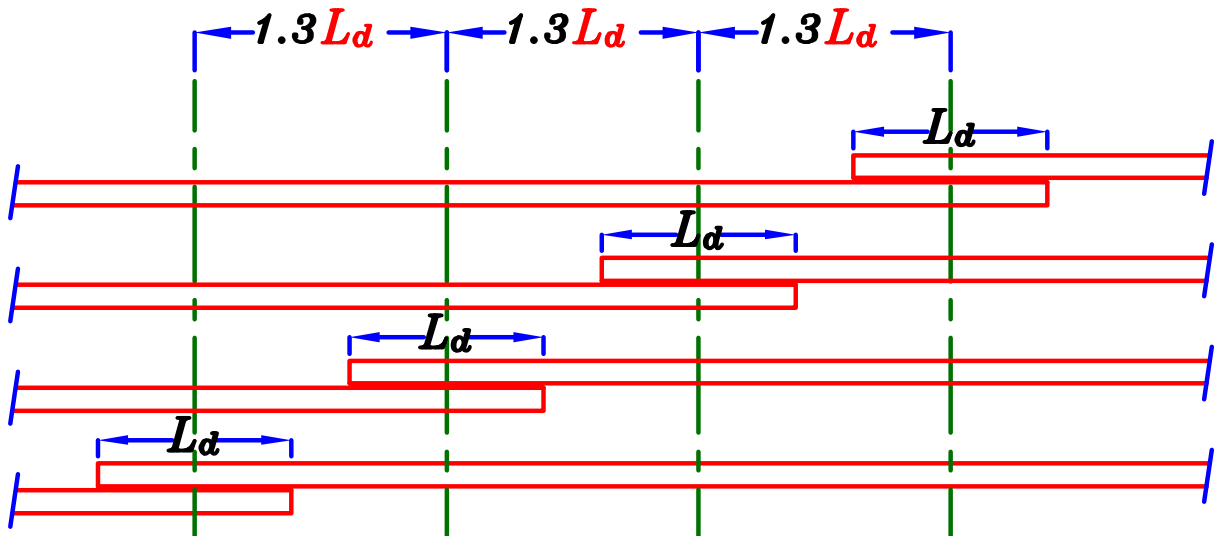
$$L_d = 60 \phi * \eta$$

حديد سفلى $\eta = 1.0$
حديد على $\eta = 1.3$

يتم حساب قيمه L_d

يجب ان لا يزيد مساحه الاسياخ الموصوله فى قطاع واحد عن ٢٥٪ من المساحه الكليه للاسياخ .
لذا يفضل عمل الوصله للحديد كله على أربع أجزاء .

المسافه من *C.L.* كل وصله و أخرى لا تقل عن $1.3 L_d$

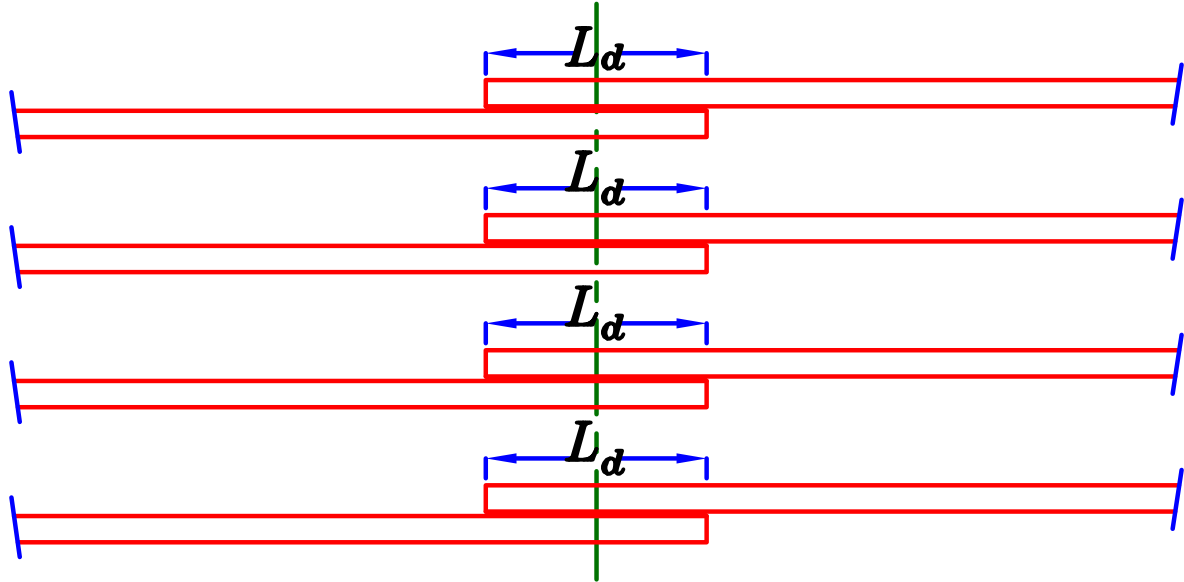


$$L_d = 40 \phi * \eta$$

حديد سفلى $\eta = 1.0$
حديد علوى $\eta = 1.3$

يتم حساب قيمه L_d

يمكن عمل كل الوصلات في قطاع واحد .



2- Mechanical splices.

الوصلات الميكانيكية

يجب أن لا يقل قطر السيخ عن ١٦ مم $\min \phi 16$

و يستخدم معها **جلب** من الحديد الصلب مواصفاته لا تقل عن مواصفات الاسياخ الموصوله

كما يجب أن لا تقل مقاومه قطاع **الجلبه** عن ١,٢٥ مره لـ F_y للاسياخ الموصوله .

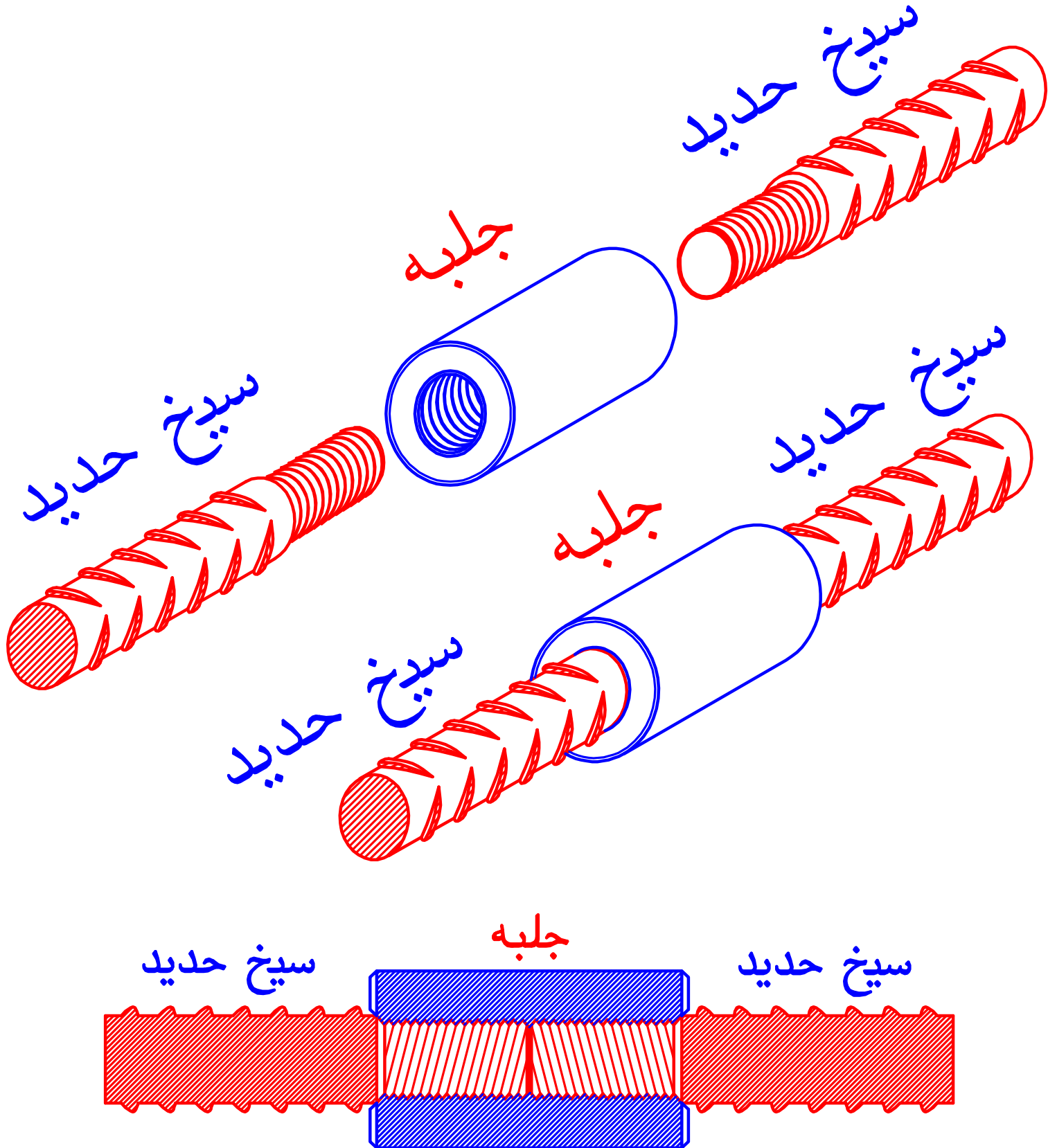
و الوصله الميكانيكيه لها طريقتين للتنفيذ :

١- بقلوظه الاسياخ من الخارج و الجلب من الداخل .

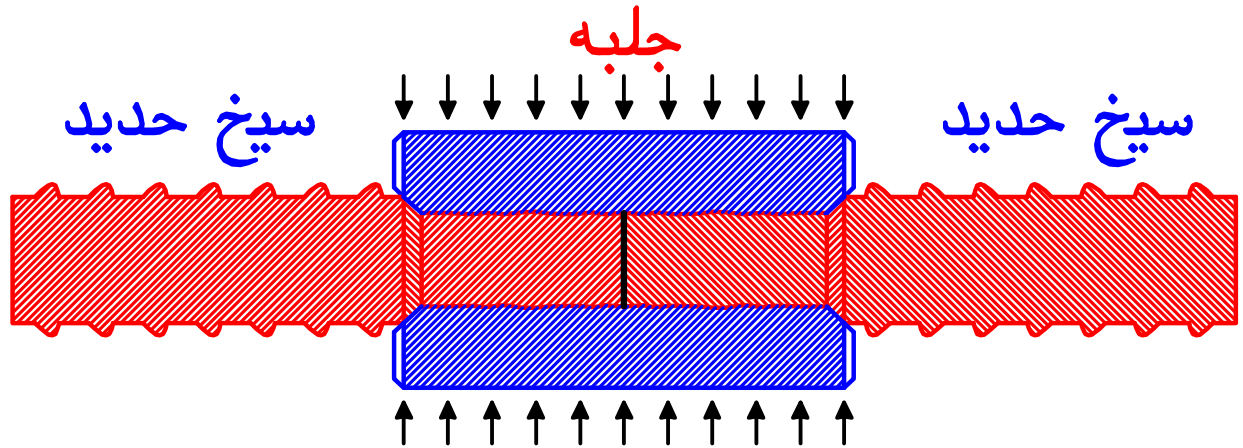
٢- بضغط الجلب في مكابس خاصه على نهايات الاسياخ ذات النتوءات .

و الوصله الميكانيكيه لها طريقتين للتنفيذ :

- ١- بقلوظه الاسياخ من الخارج و الجلب من الداخل .
تنتقل الاجهادات بين الاسياخ بواسطه الارتكاز بين اسنان قلوظ السيخ و اسنان قلوظ الجلبه .



- ٢- بضغط الجلب فى مكابس خاصه على نهايات الاسياخ ذات النتؤات
لتنقل الاجهادات بين الاسياخ بواسطه الاحتكاك بين السطح الداخلى للجلبه
مع السطح الخارجى لنهايه الاسياخ .

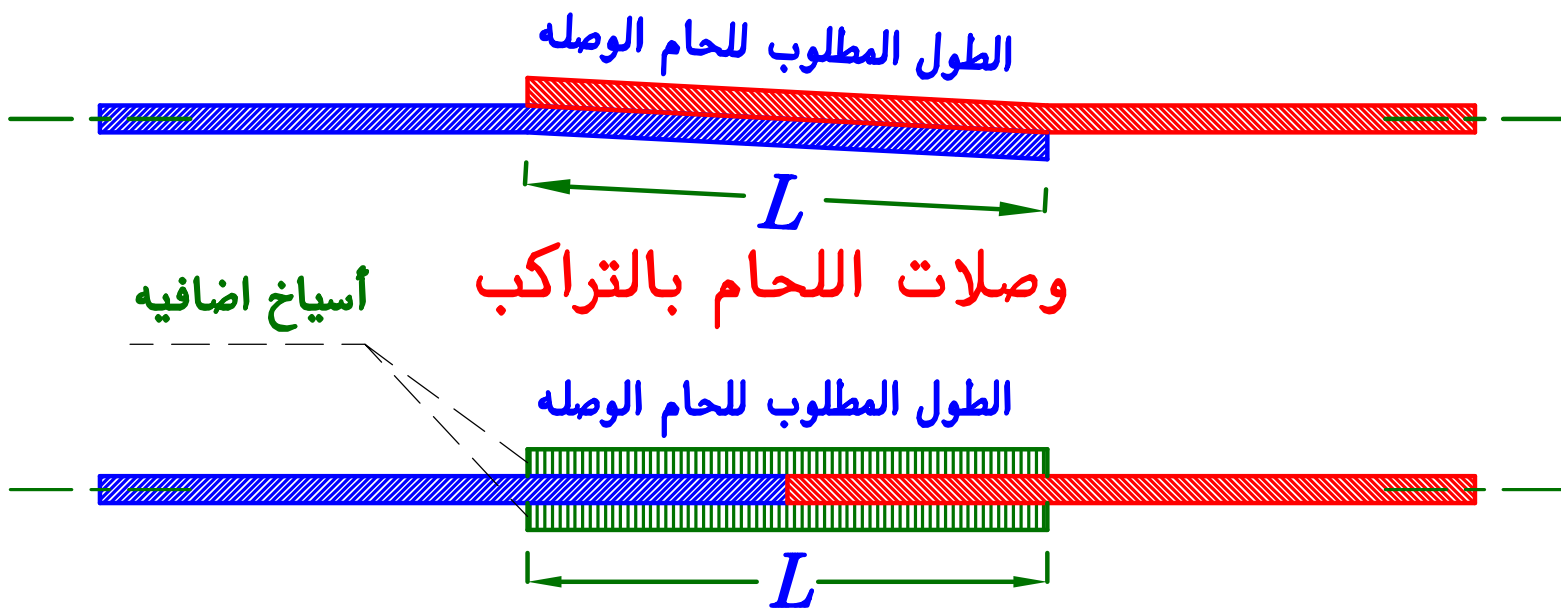


3- Welded splices.

وصلات اللحام

يجب أن لا يقل قطر السبخ عن ١٦ مم $\min \phi 16$

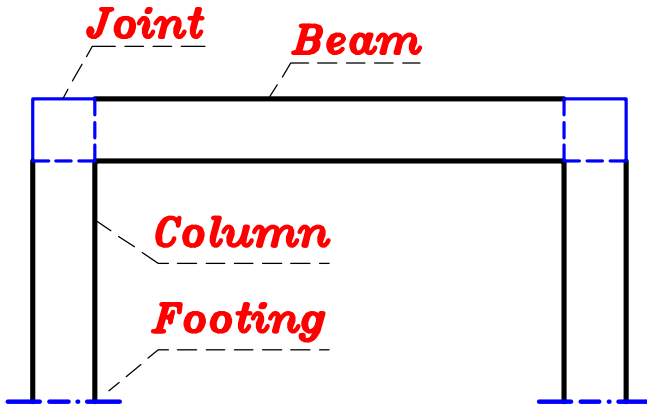
- ١- يستخدم لحام كهربائى .
- ٢- يجب أن يكون محور السبخين الملحومين على استقامه واحده .
- ٣- يجب ان لا تزيد مساحه الاسياخ الملحومه فى قطاع واحد عن ٢٥ %
و باقى الوصلات على مسافات طويله لا تقل عن ٢٠ مره قطر السبخ الملحوم .



وصلات اللحام بأستخدام أسياخ اضافيه

Reinforcement of Frames.

Introduction.



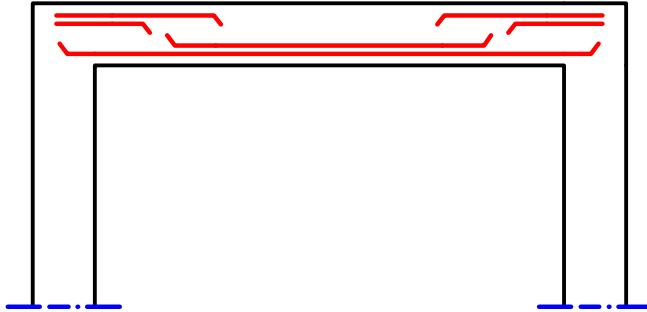
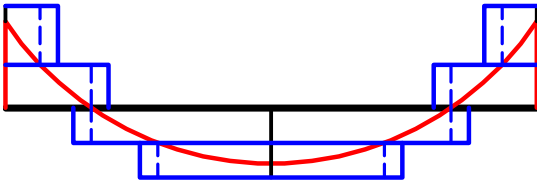
يتكون ال **Frame** من أربع عناصر أساسيه :

١- الكمرات (أفقيه أو مائمه)

٢- الاعمده (رأسيه أو مائمه)

٣- ال **Joints** و هى التى تربط العناصر ببعضها
(**Rigid Joint or Hinged Joint**)

٤- القواعد .



نرسم التسليح فى الكمرات و يقف عاده

بطريقه **Moment of Resistance (M_R)**

يفضل رسم التسليح فى الاعمده

بطريقه **Empirical Method**

لان **Normal Force** على الاعمده

كبيره و بالتالى طريقه **(M_R)**

لن تكون دقيقه .

يتم ربط تسليح الكمرات و الاعمده

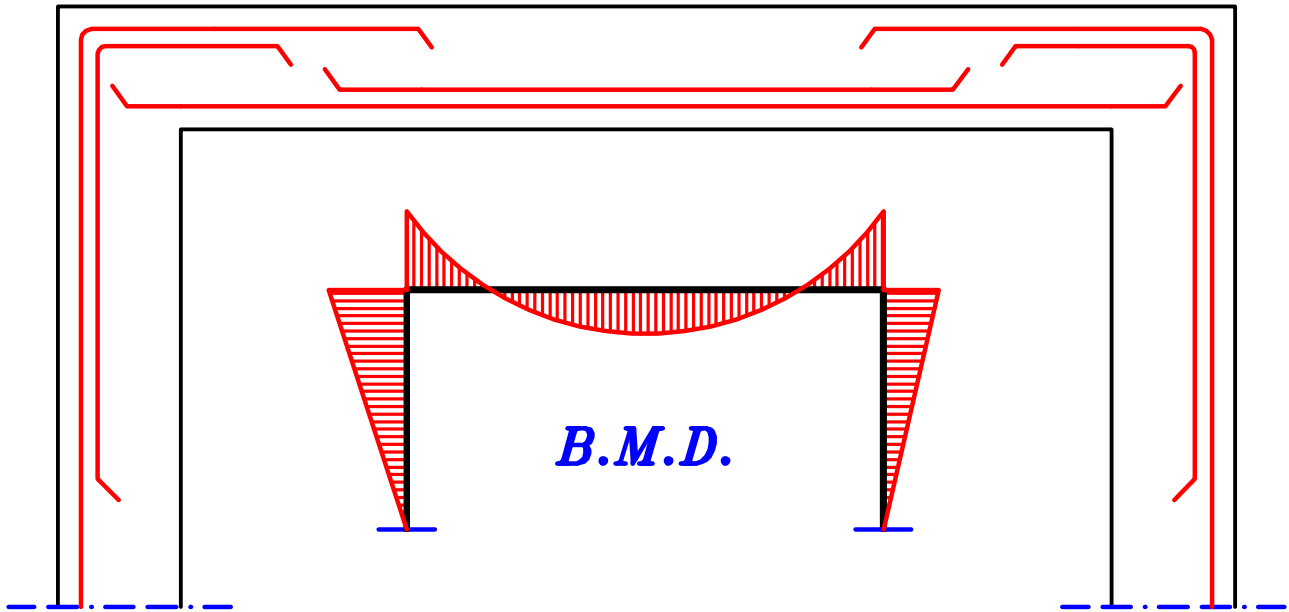
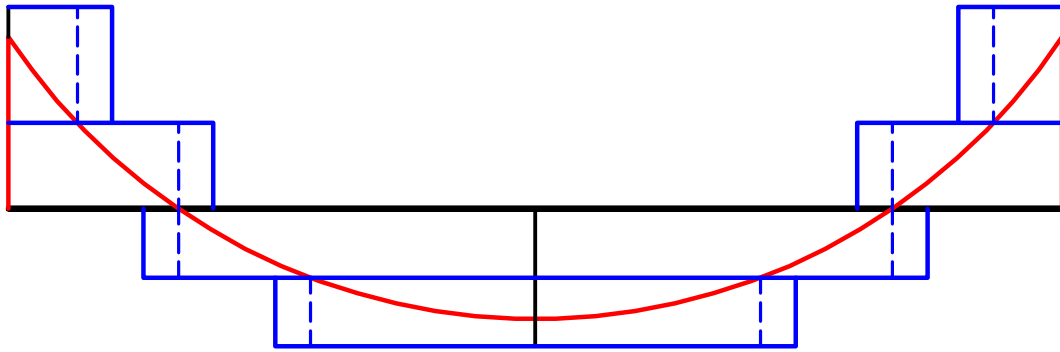
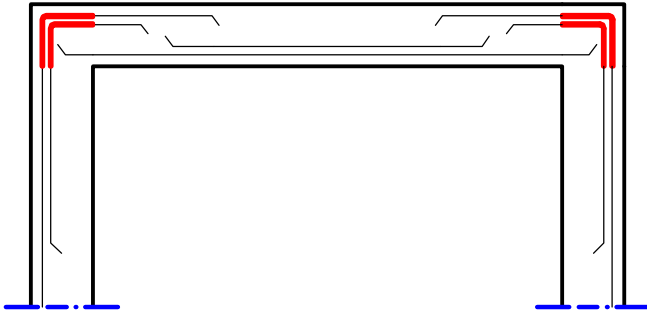
بتسليح ال **Joints**

مع ملاحظه انه سيكون هناك حديد مشترك

بين الكمرات و الاعمده

مما سيتلزم ان توحيد قطر الاسياخ ϕ

فى هذه القطاعات .

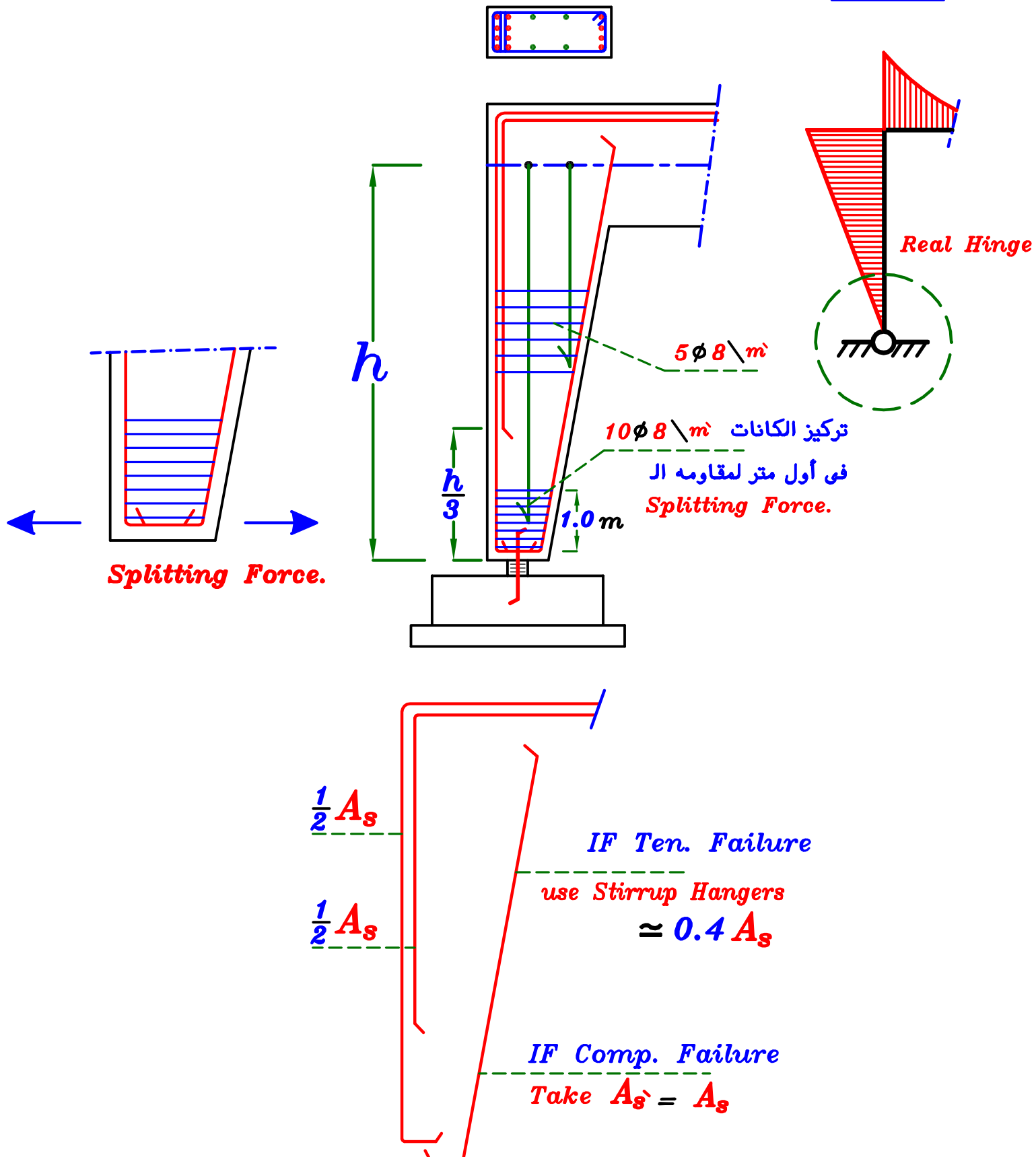


ملحوظه

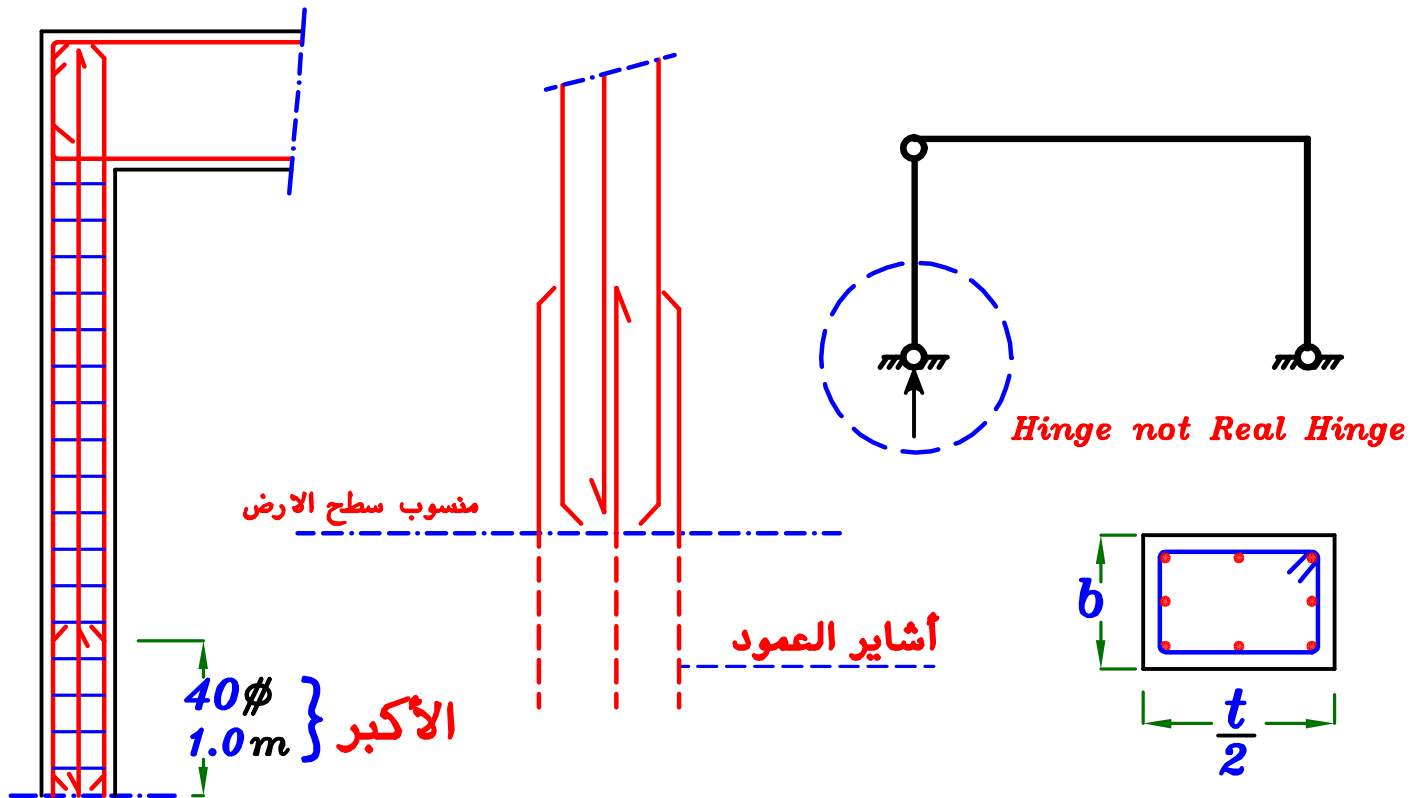
تسليح القواعد لن ندرسه فى هذا الملف و سيدرس لاحقا فى ملف آخر بأذن الله

RFT. of columns (Using Empirical Method)

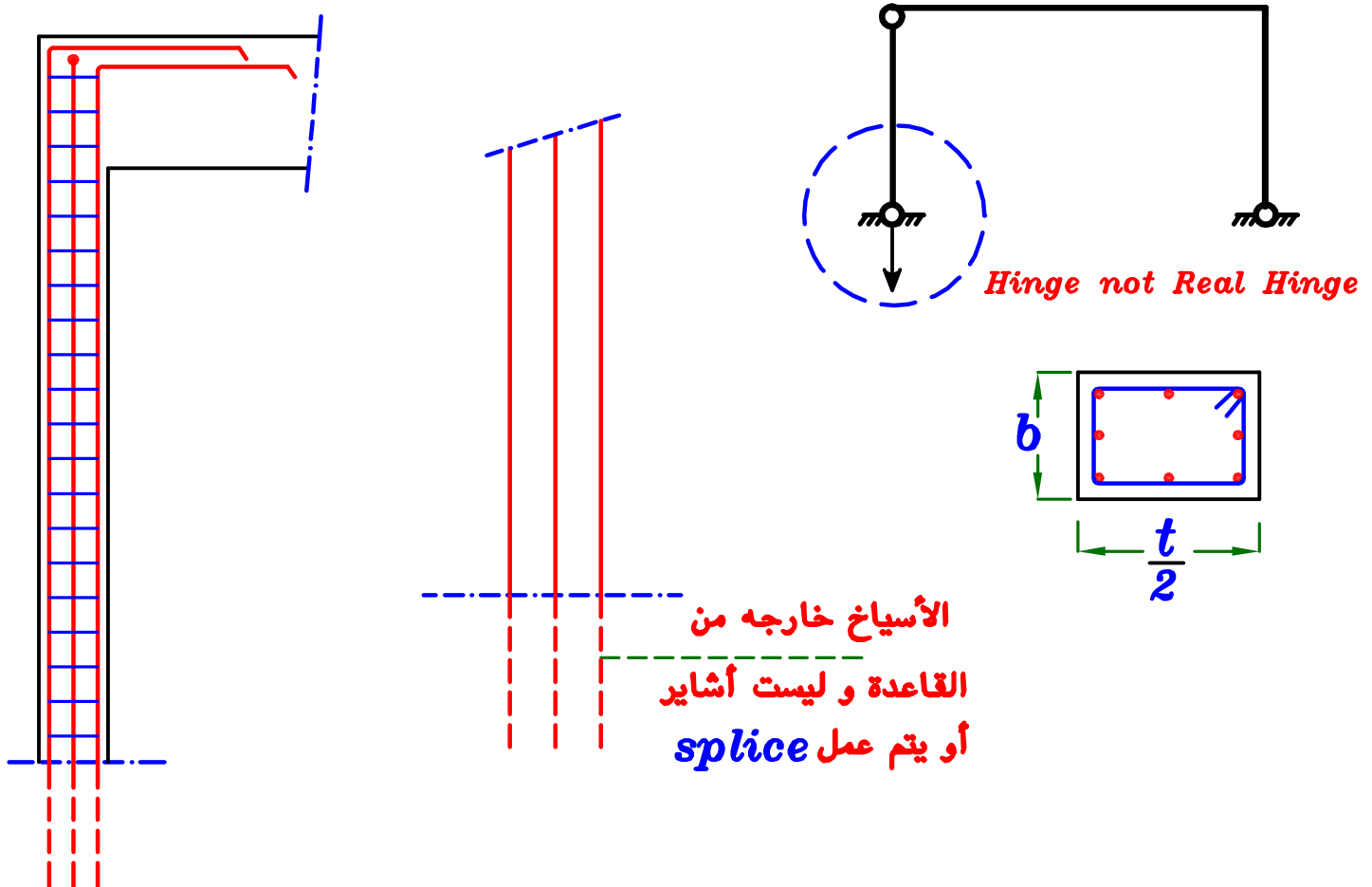
① Hinged-Rigid Column.



② Link member. (For Compression Link member)

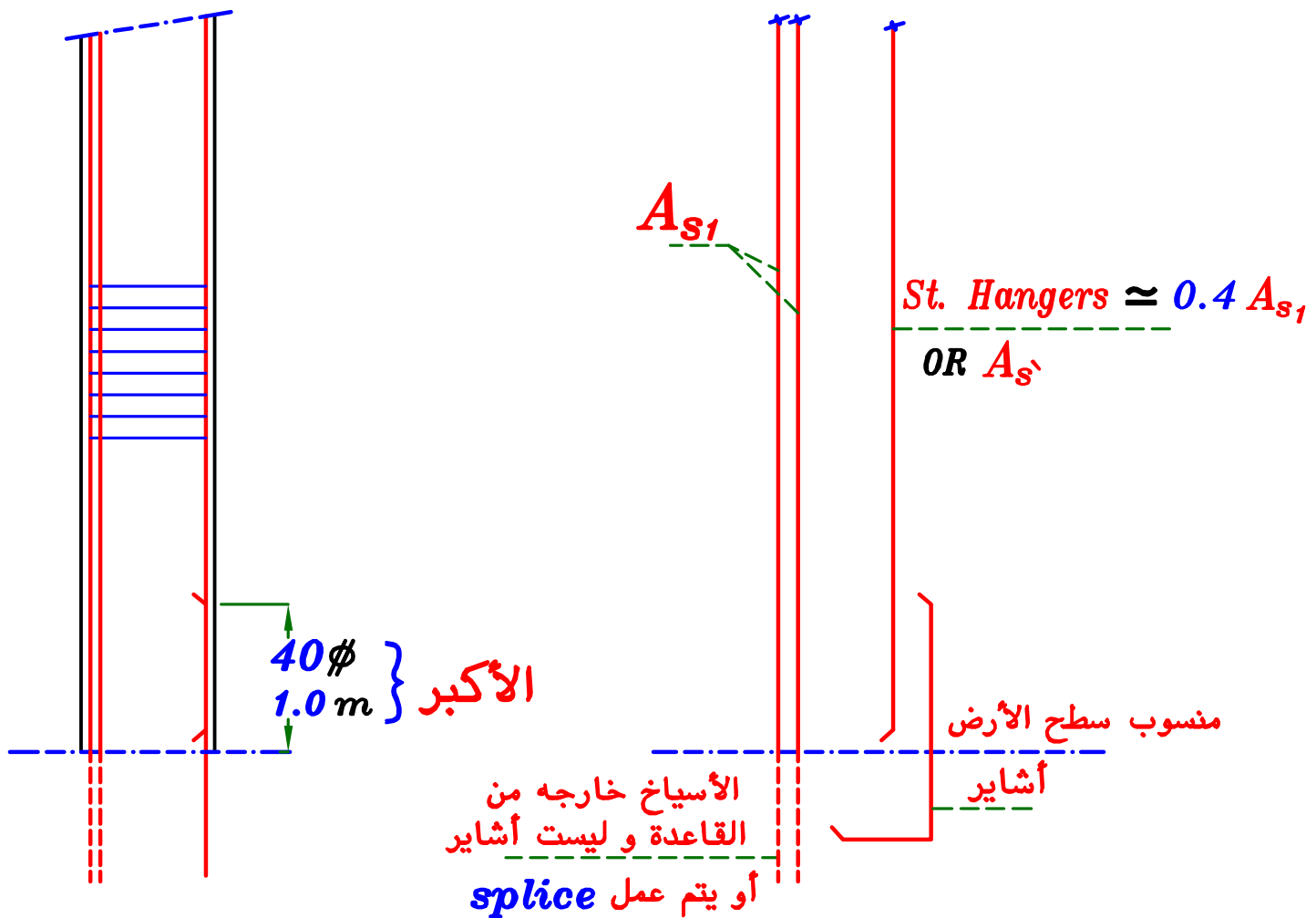
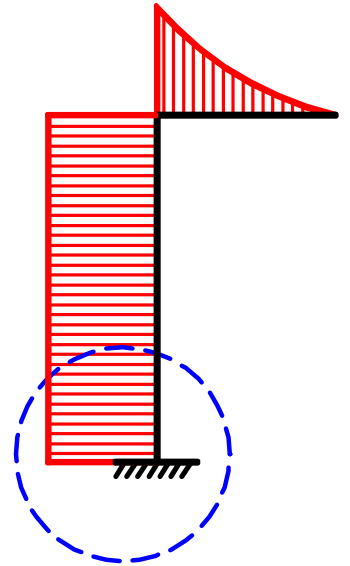


Hinged Support. (For Tension Link member)

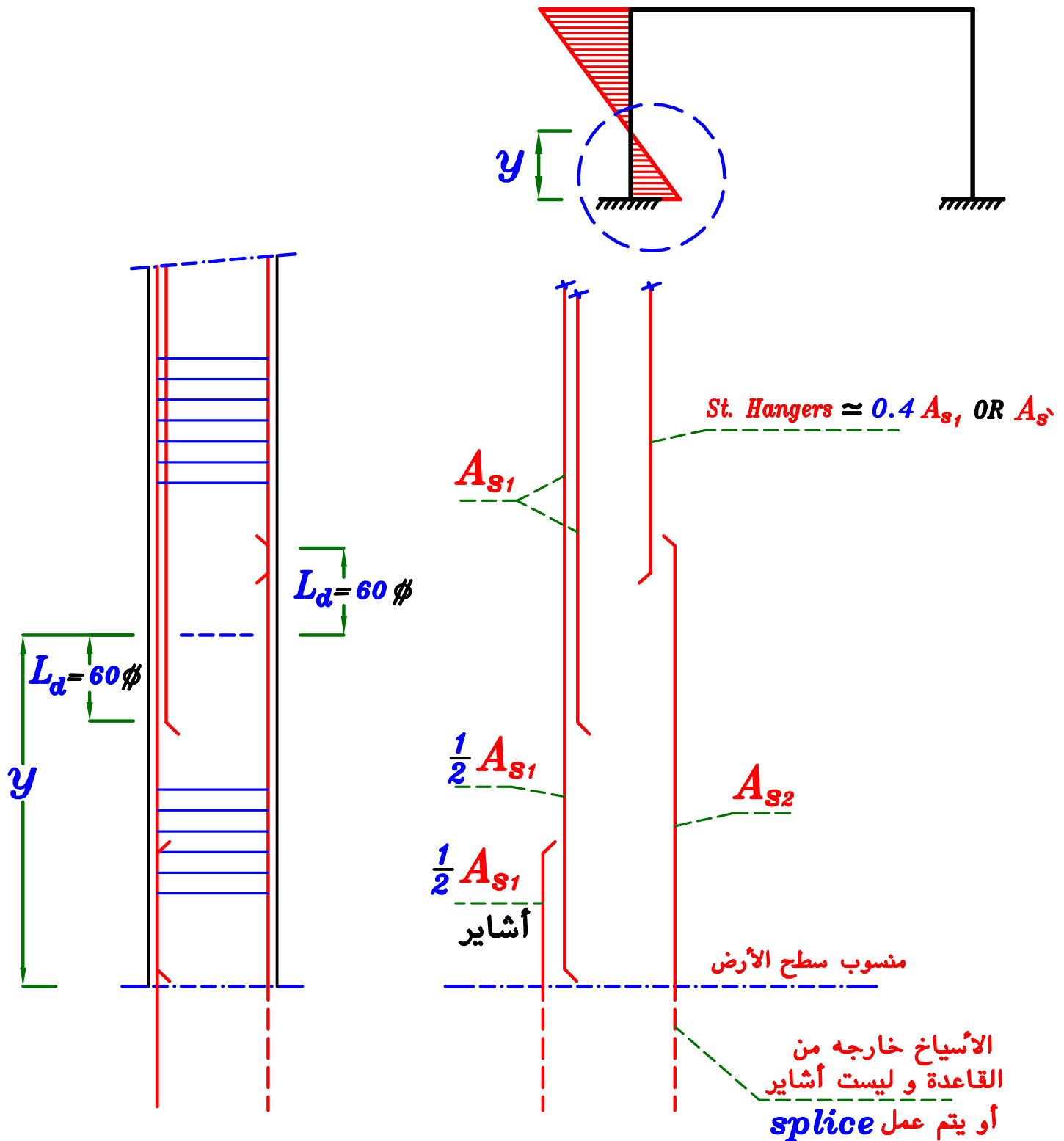


③ Rigid-Rigid Column

Ⓐ *Moment at one side only.*



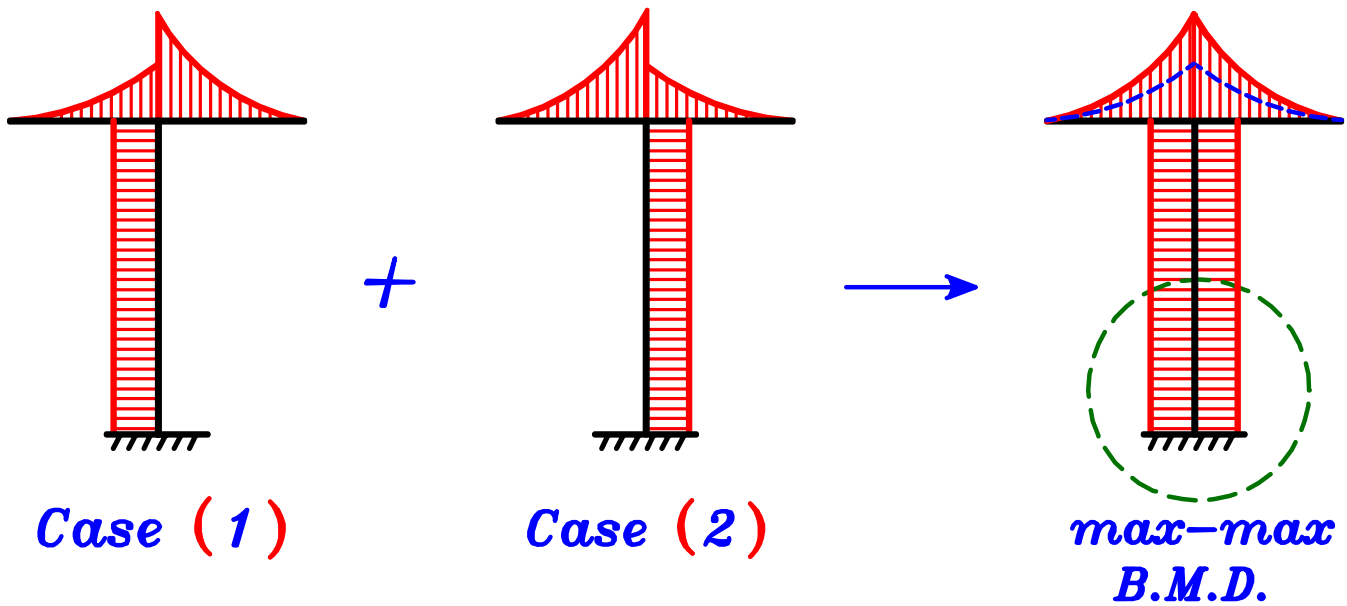
b) Moment at Two sides.



ملحوظه

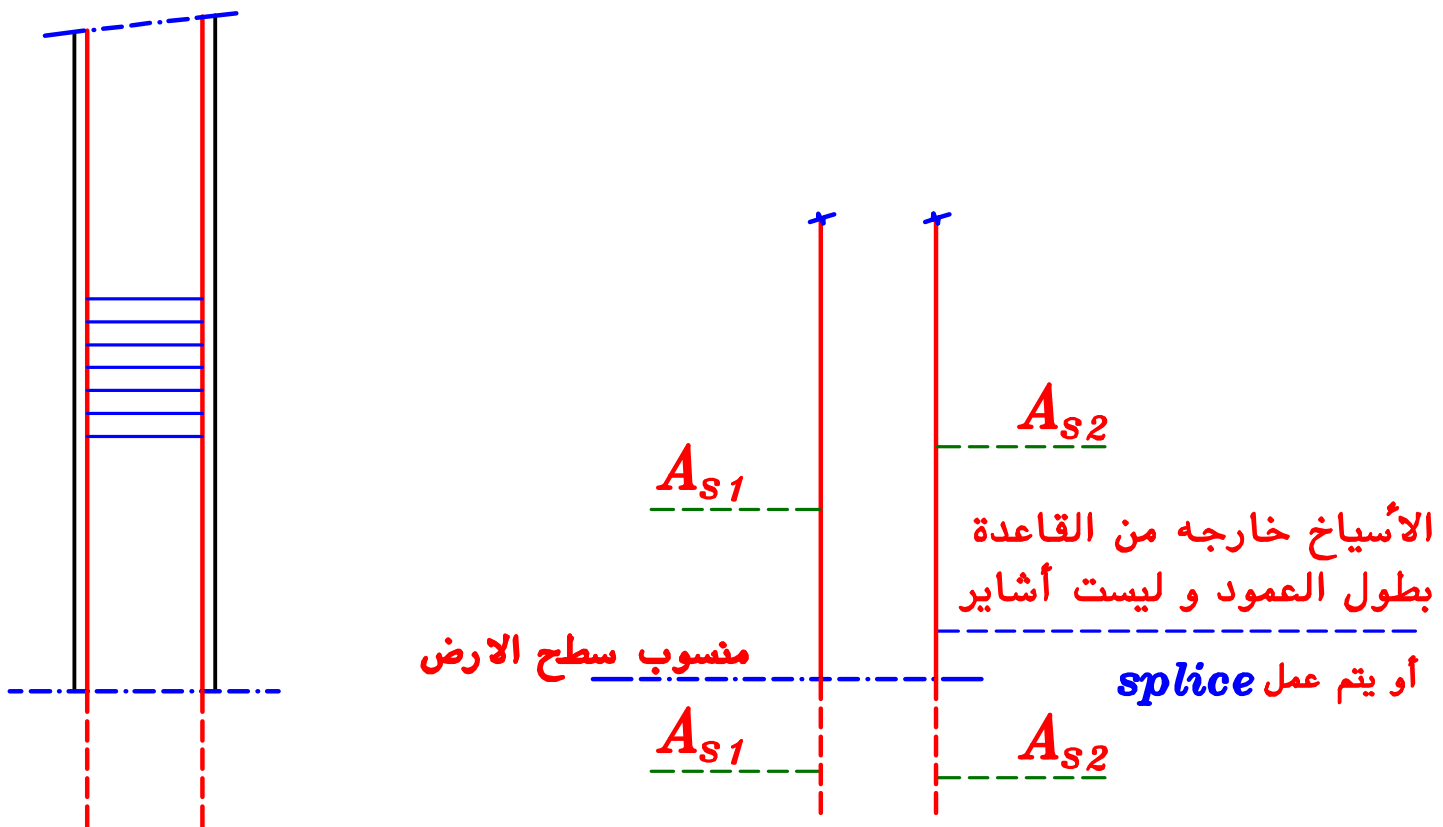
الاشاير تكون جعه ال **Compression** فقط و تكون بنفس قيمه التسليح الرئيسى
 أما جعه ال **Tension** فيجب أن يخرج التسليح الرئيسى من القاعده
 أو يتم عمل **Lap splice**

© Moment at Two sides due to Cases of Loading.



حديد متماثل لأنه *Symm.*

$$A_{s1} = A_{s2}$$

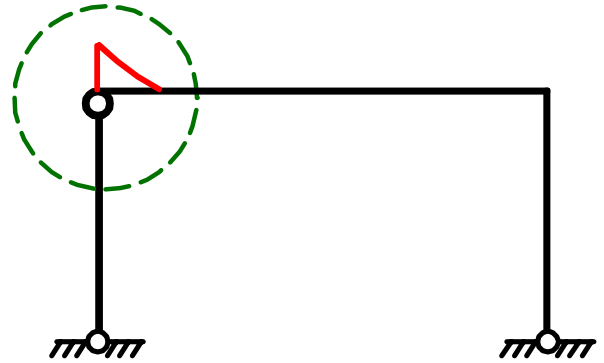


Joints RFT. (Connection between members)

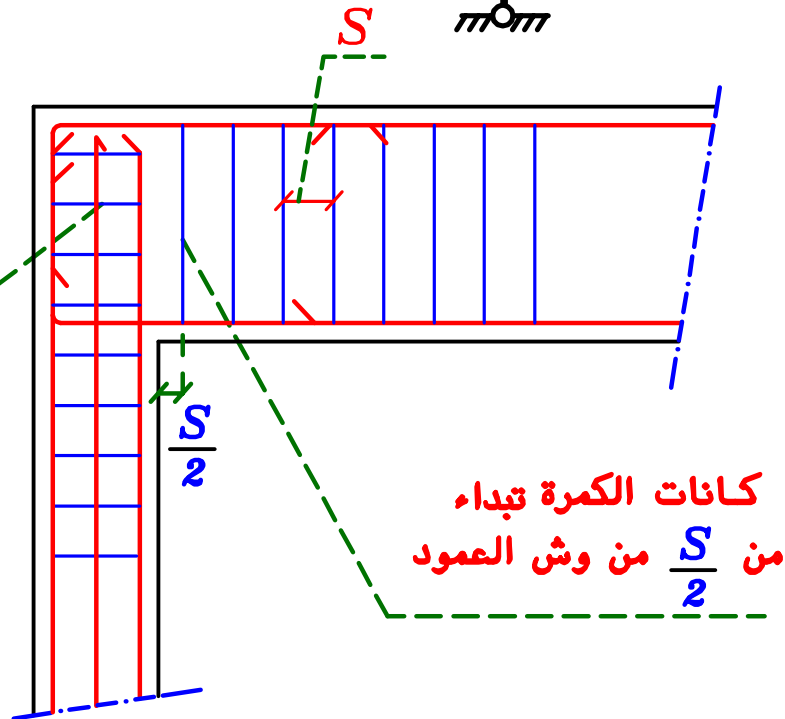


① Hinged Joints. (Joint between the beam & Link member)

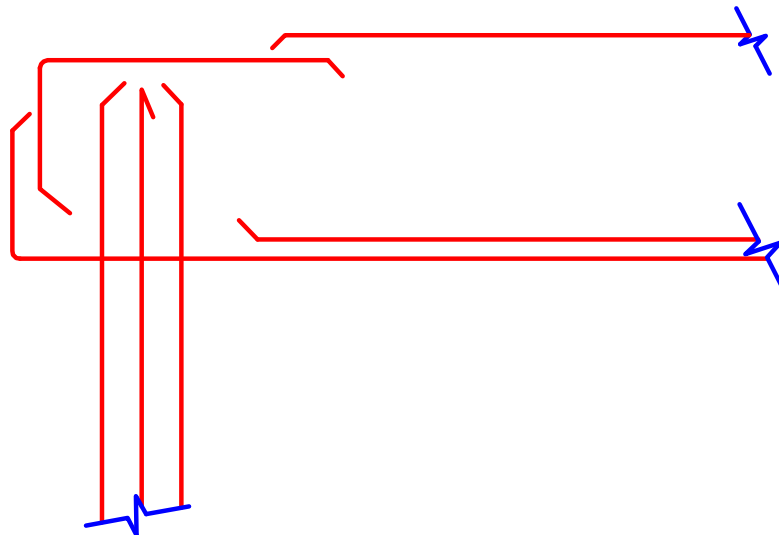
هذه ال joint لا تنقل عزوم



كانات العمود
تكمل من الأول للآخر



كانات الكمرة تبدأ
من $\frac{S}{2}$ من وش العمود

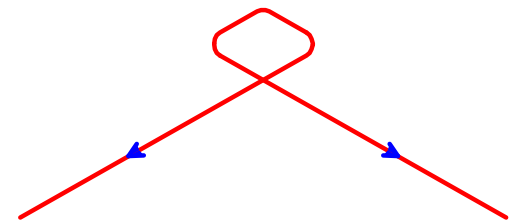
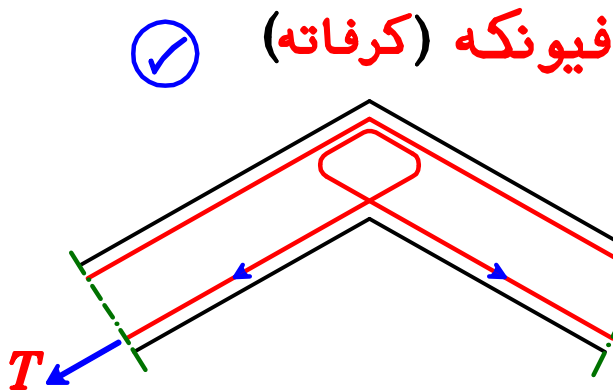
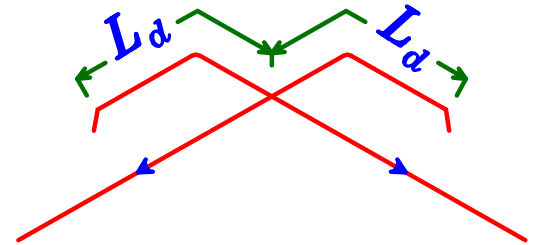
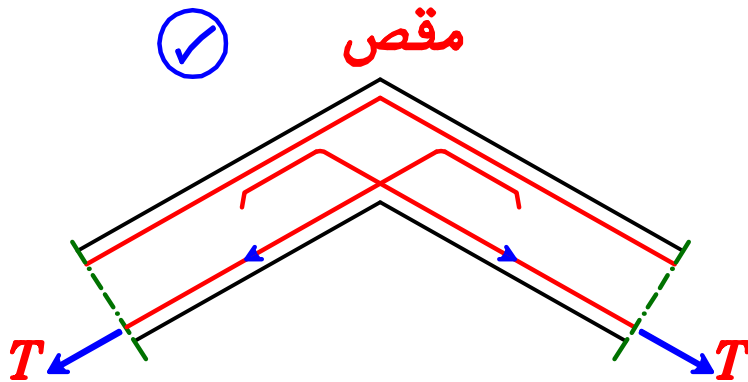
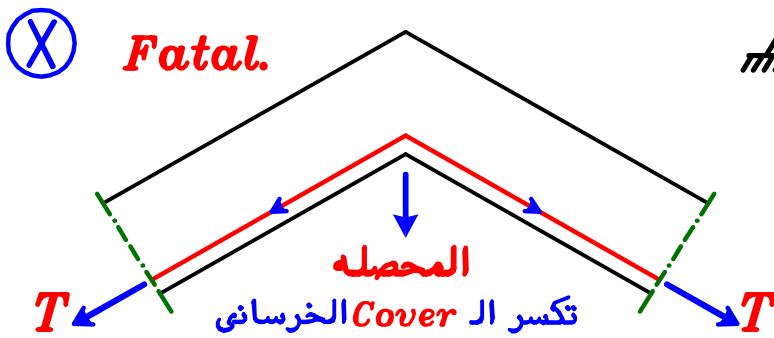
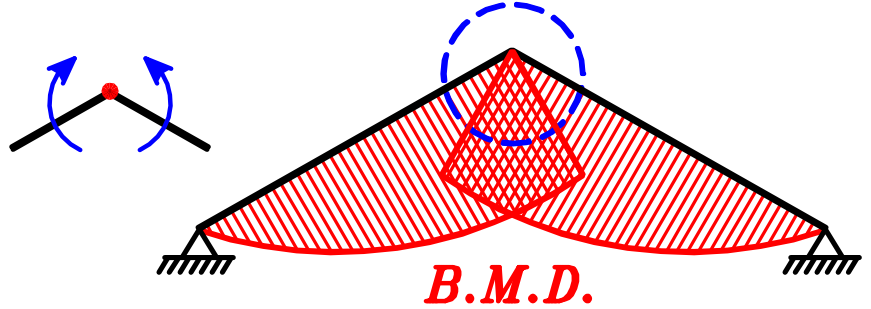


② Rigid Joints. joints تنقل عزوم



① Opening Joints joints يحدث عندها تداخل في العزوم

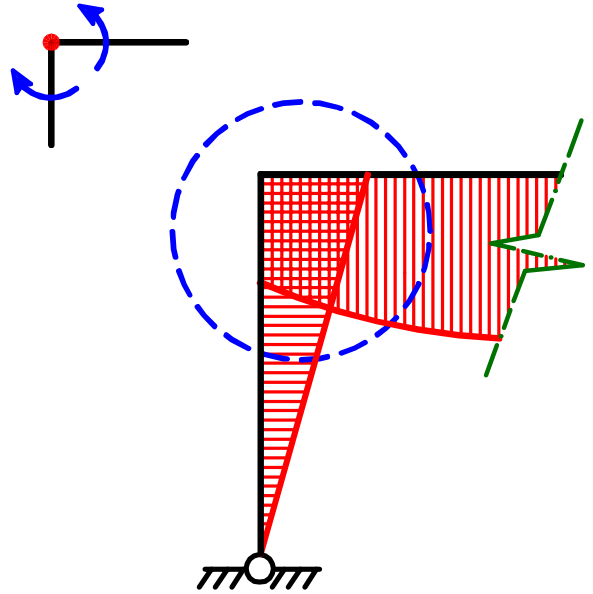
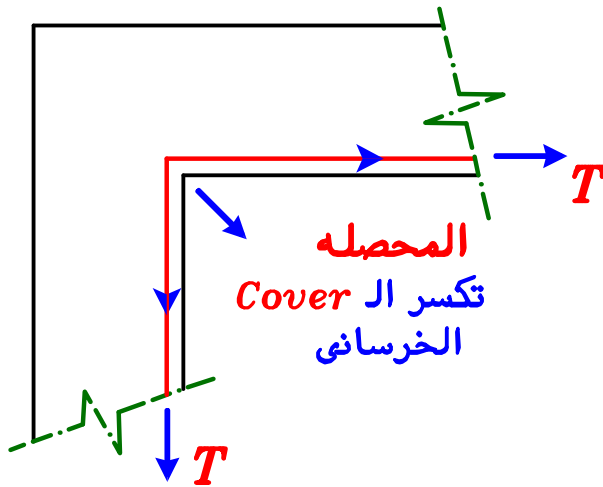
ملحوظة: إذا حدث تداخل في العزوم يجب عمل مقص أو فيونكه



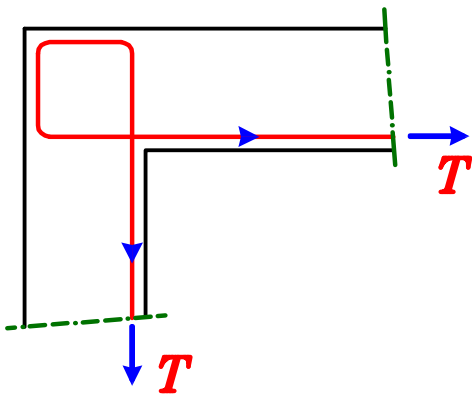
ملحوظة: يفضل عمل المقص عن الفيونكه .

يوجد تداخل فى العزوم
إذاً يجب عمل مقص أو فيونكه

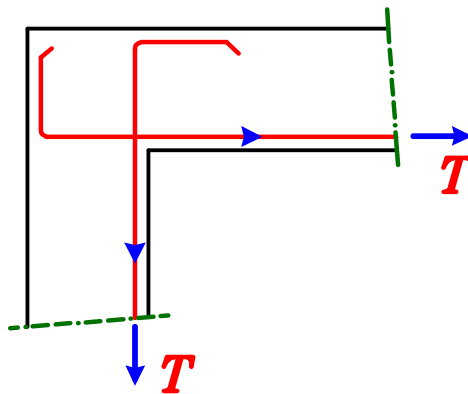
⊗ **Fatal.**



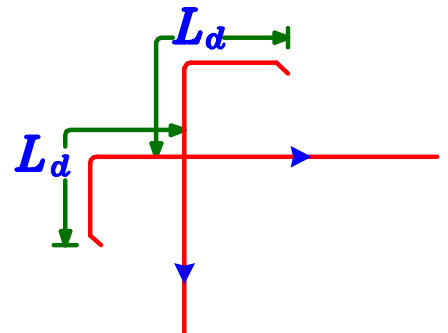
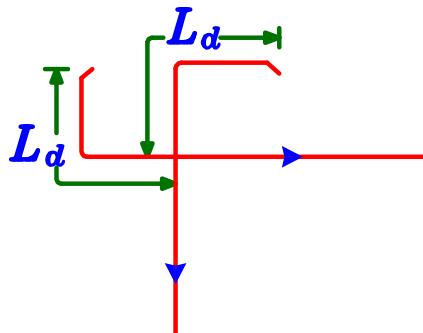
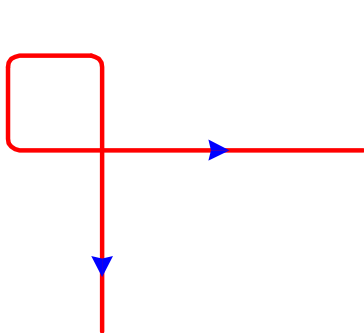
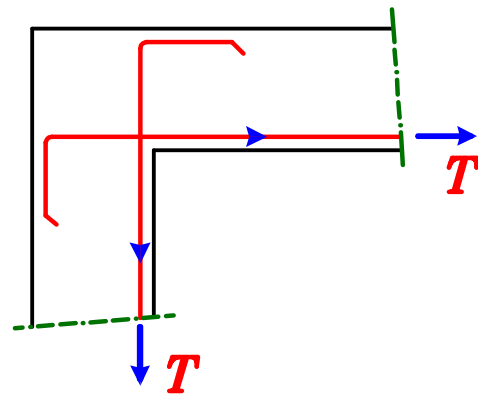
✓ فيونكه (كرفاته)



✓ مقص



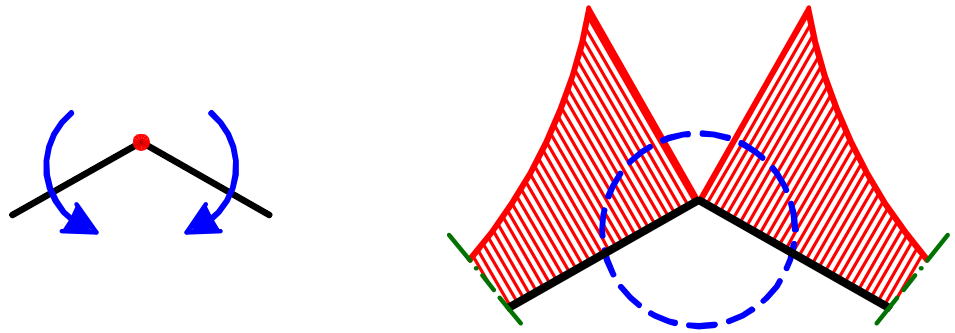
✓ مقص



يفضل هذا الحل فى التنفيذ
حيث يتم صب العمود أولاً

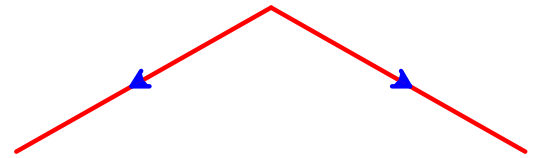
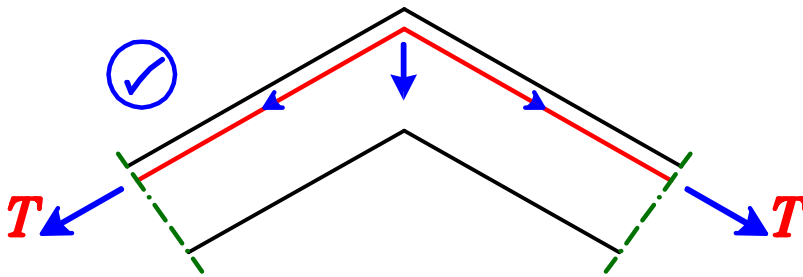


⑥ *Closing Joints* يحدث عندها تباعد فى العزوم



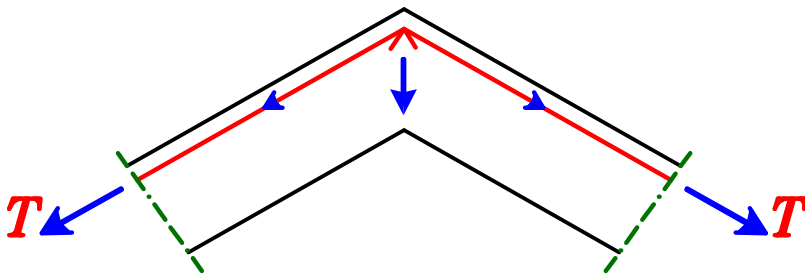
B.M.D.

لا يوجد خوف على الخرسانه لأن سمكها كبير



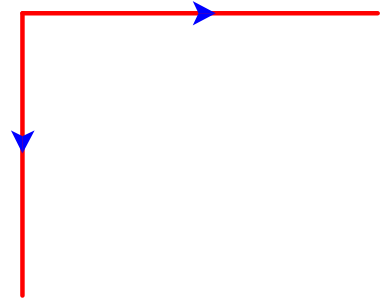
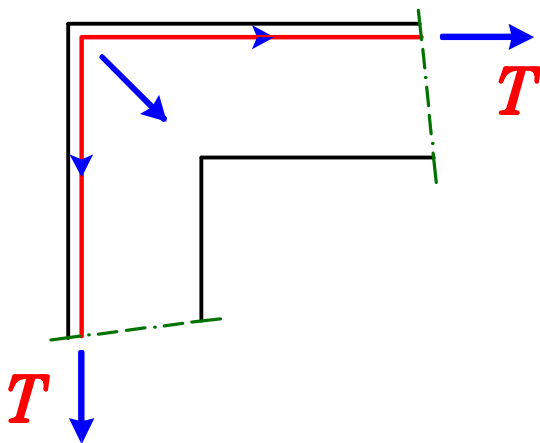
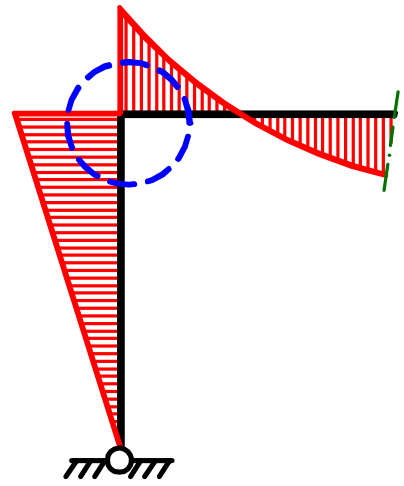
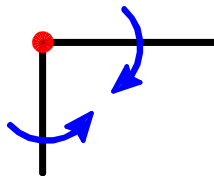
يجب أن يكمل حديد الشد دون أن ينقطع فى منطقه ال *max. moment*

⊗ *Fatal.*



Fatal

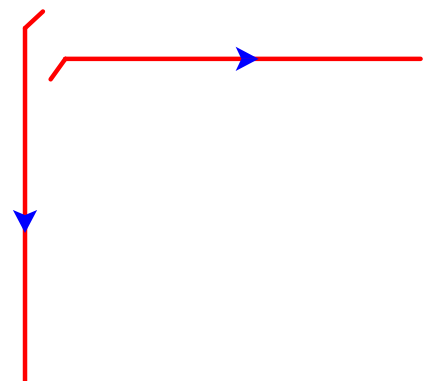
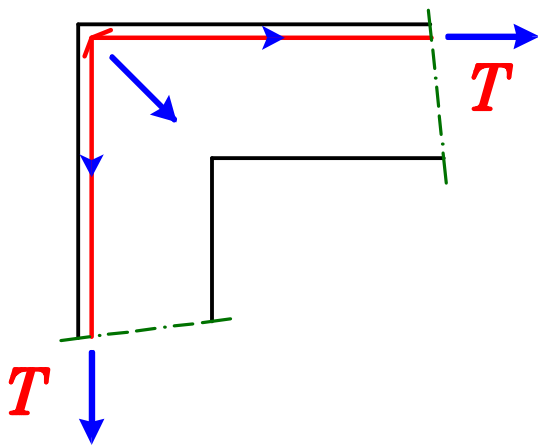
توقيف الحديد عند منطقه ال *max. moment*



يجب أن يكمل حديد الشد دون أن ينقطع في منطقه ال *max. moment*



Fatal.

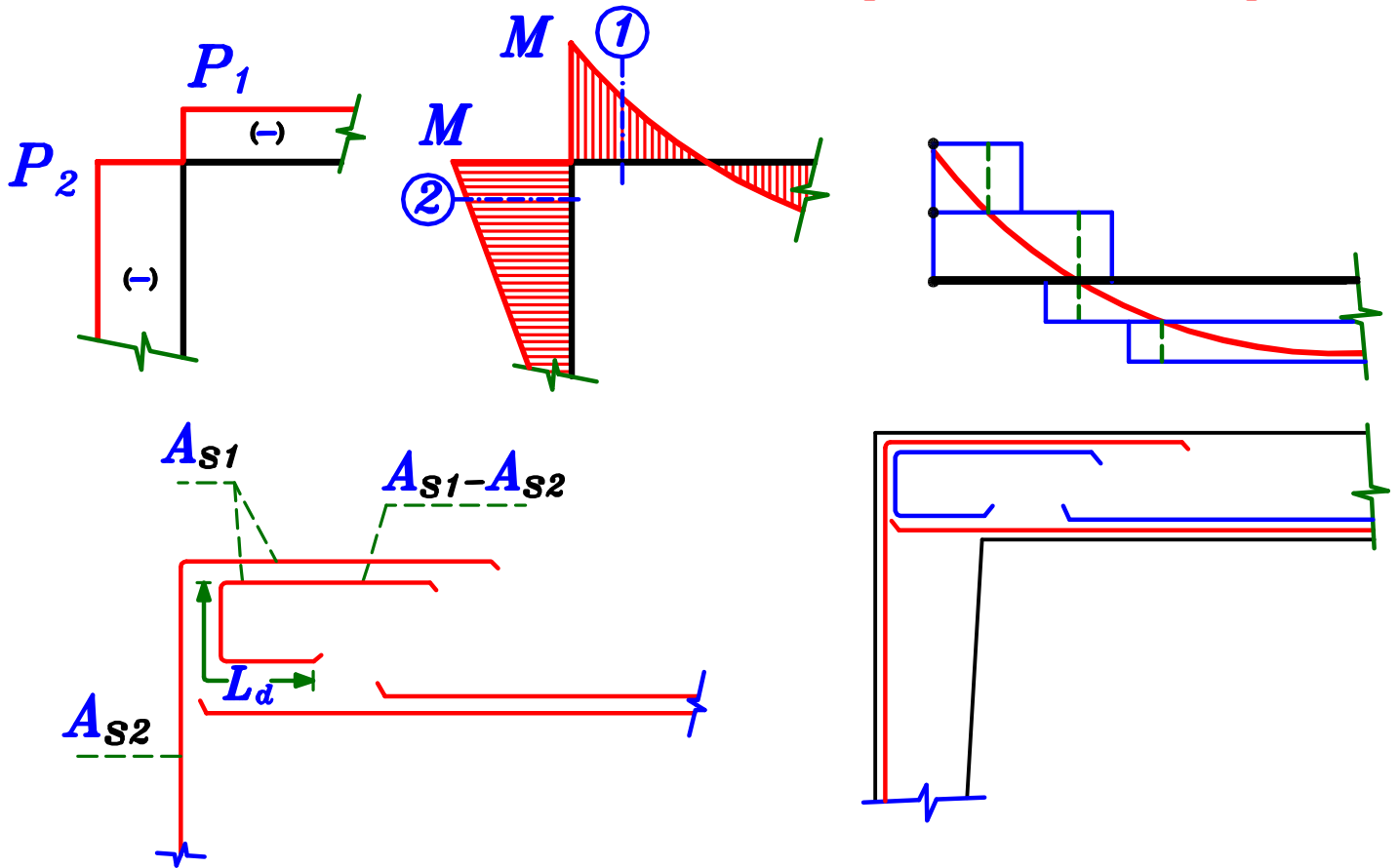


Fatal

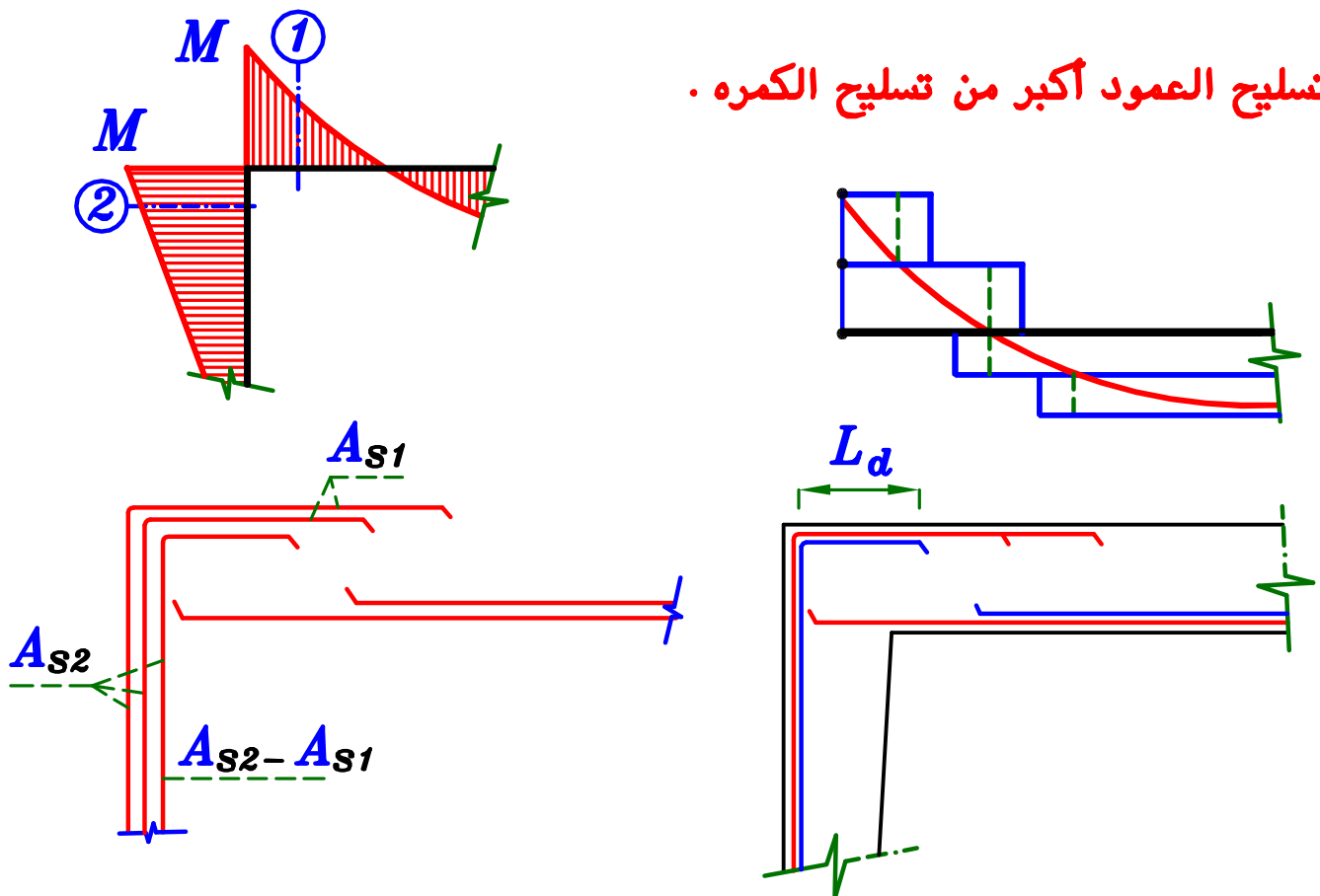
توقيف الحديد عند منطقه ال *max. moment*

في حالة إختلاف كمية الحديد في قطاعين في نفس ال Joint

① تسليح الكمره أكبر من تسليح العمود .



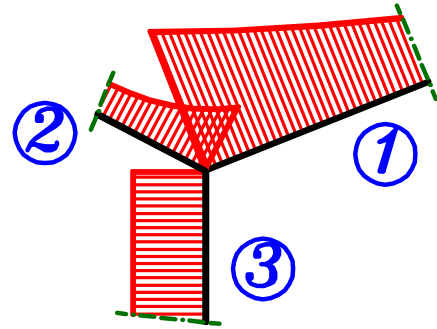
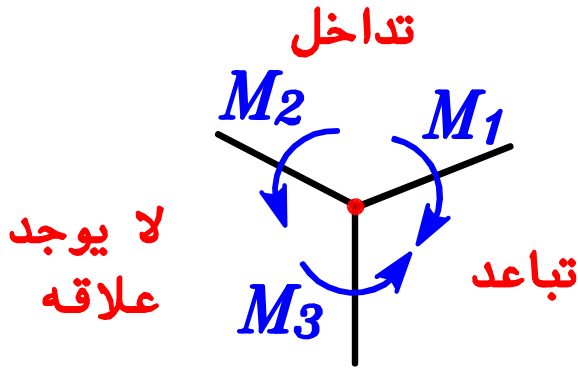
② تسليح العمود أكبر من تسليح الكمره .



Joints with 3 members.

إذا كانت أسهم العزوم تدور في نفس الاتجاه ← لا توجد علاقة بين العزوم
إذا كانت أسهم العزوم تدور في عكس الاتجاه ← توجد علاقة بين العزوم تحدد من شكل الـ **moment**

تباعداً و تداخلاً



ملحوظة هامة

عندما تكون هناك علاقة بين عزمين يجب أن ننظر الى **B.M.D.**
لكي نحدد اذا كانت هذه العلاقة تباعد أم تداخل .

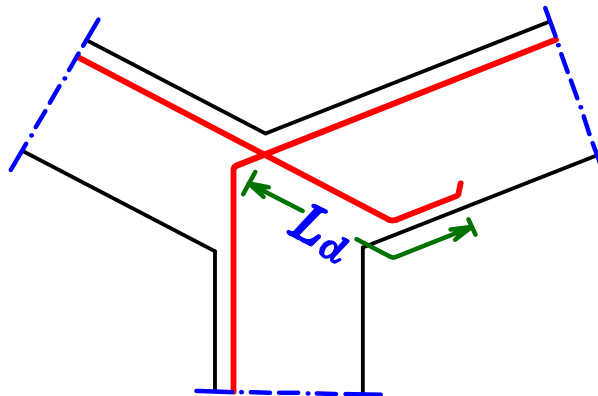
$$M_1 = M_2 + M_3$$

M_1, M_2 → تداخل

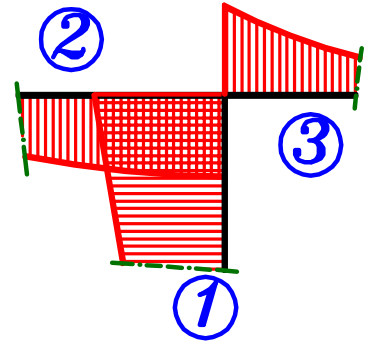
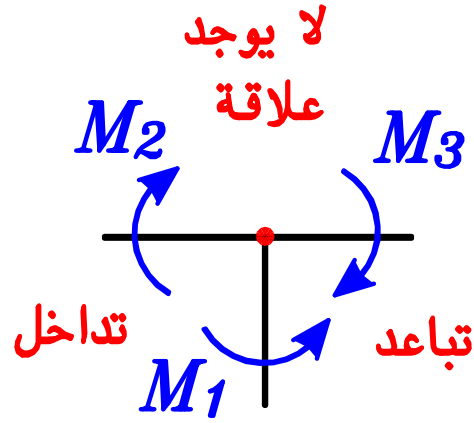
M_1, M_3 → تباعد

M_2, M_3 → لا يوجد علاقة

إذا وجد تباعد و تداخل معاً نكمل حديد التباعد أولاً ثم نعمل مقص التداخل .



تباعد و تداخل



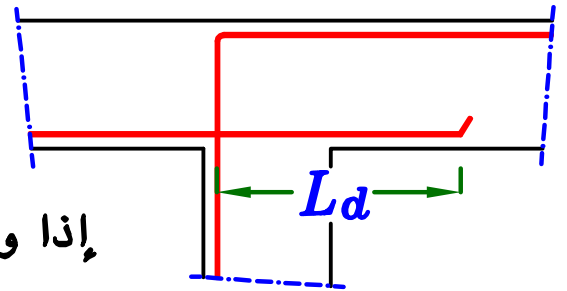
$$M_1 = M_2 + M_3$$

$M_1, M_2 \rightarrow$ تداخل

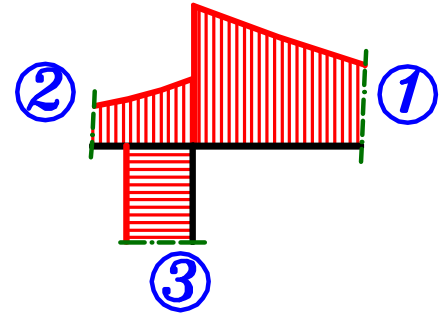
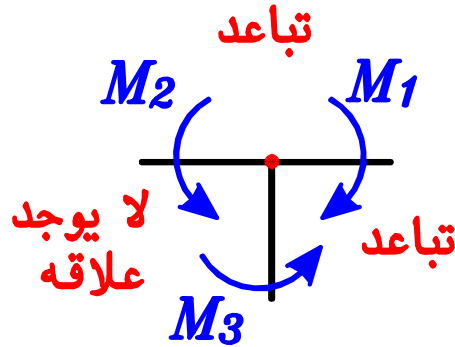
$M_1, M_3 \rightarrow$ تباعد

$M_2, M_3 \rightarrow$ لا يوجد علاقته

إذا وجد تباعد و تداخل معاً نكمل حديد التباعد أولاً ثم نعمل مقص التداخل .



تباعد و تباعد



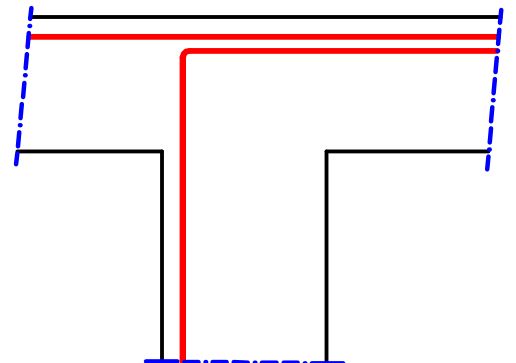
$$M_1 = M_2 + M_3$$

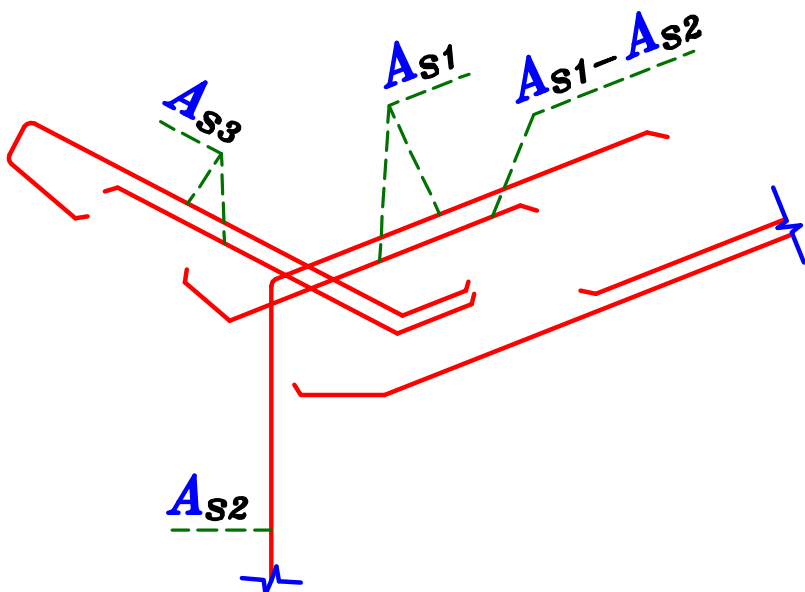
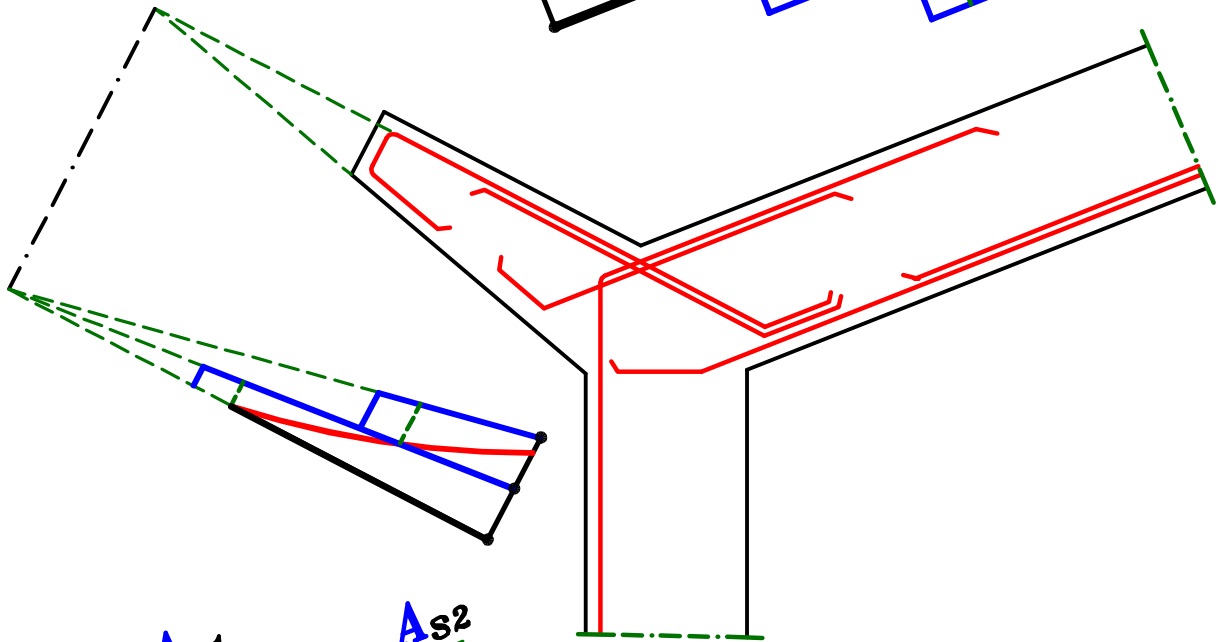
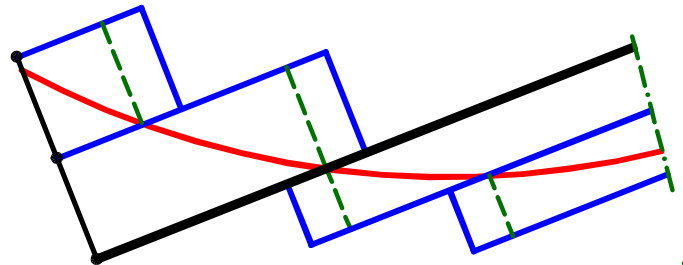
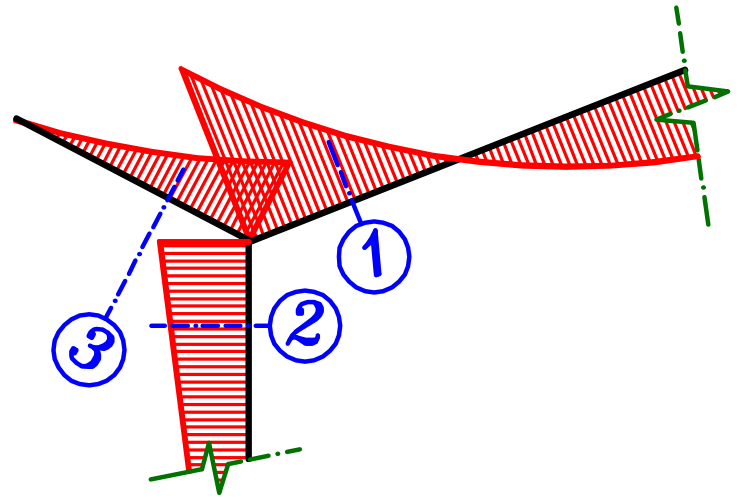
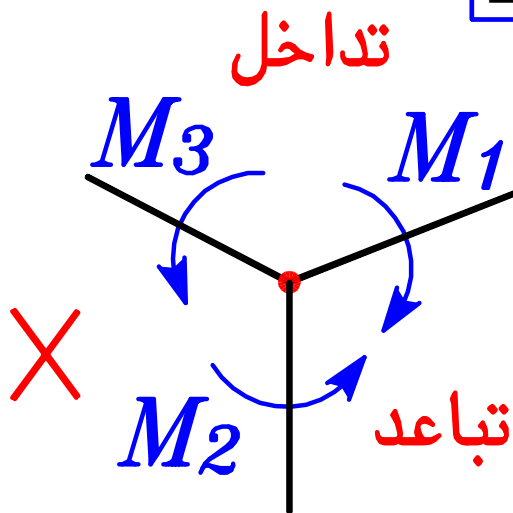
$M_1, M_2 \rightarrow$ تباعد

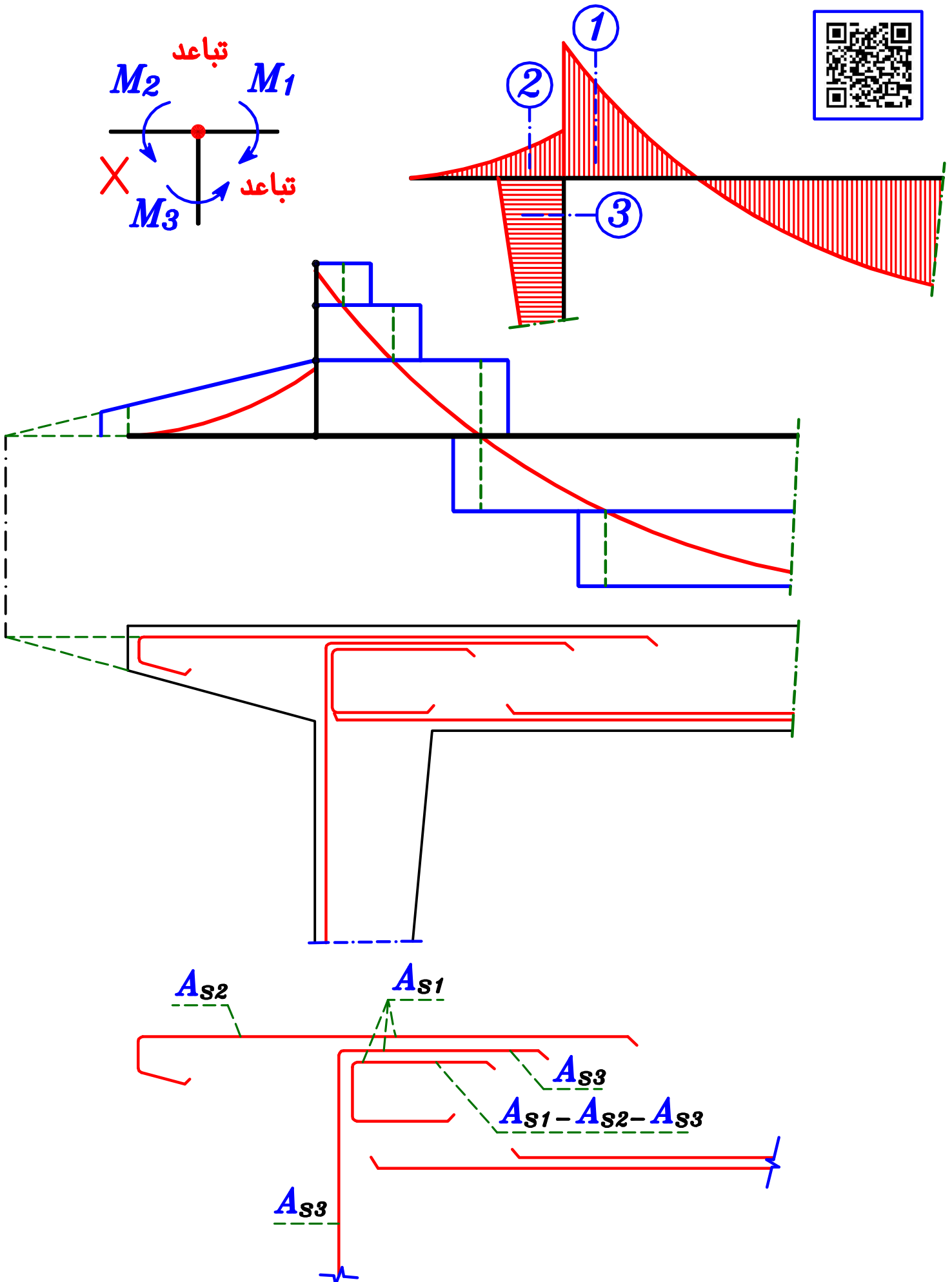
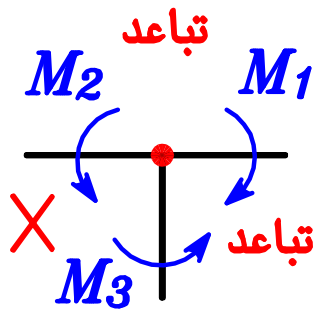
$M_1, M_3 \rightarrow$ تباعد

$M_2, M_3 \rightarrow$ لا يوجد علاقته

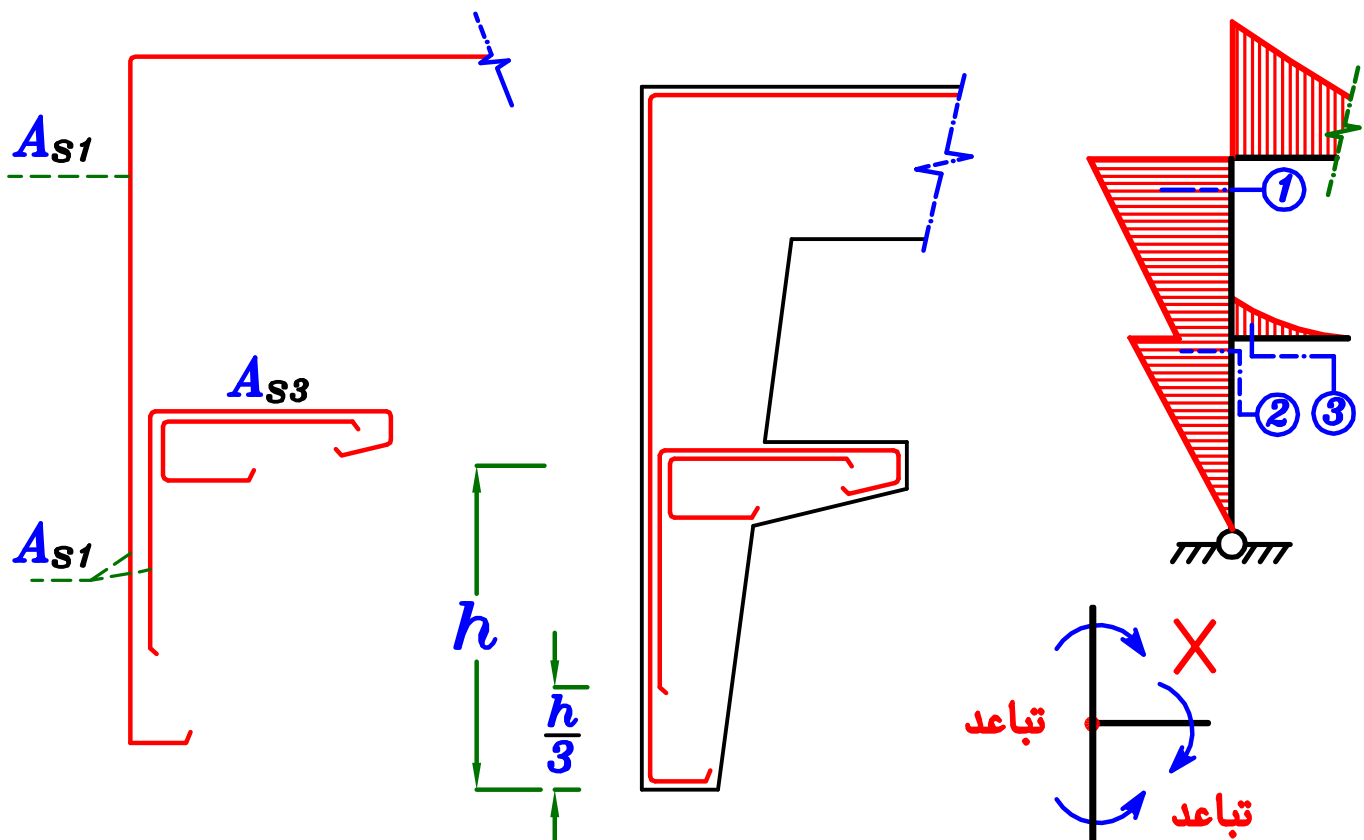
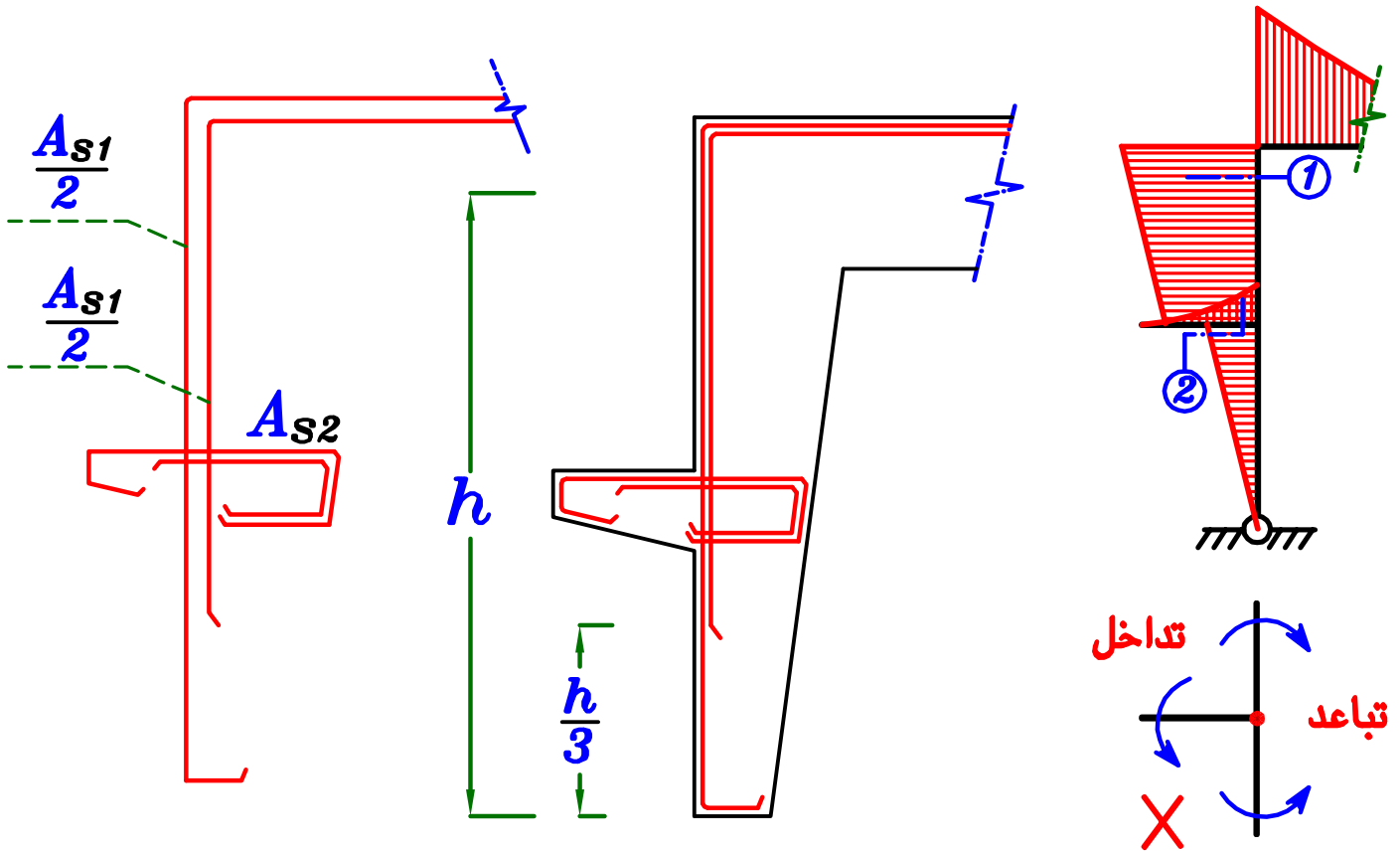
إذا وجد تباعد و تباعد نكمل الحديد الموجود على إستقامه واحده أولاً .
ثم نعمل التباعد الاخر صف ثانى .

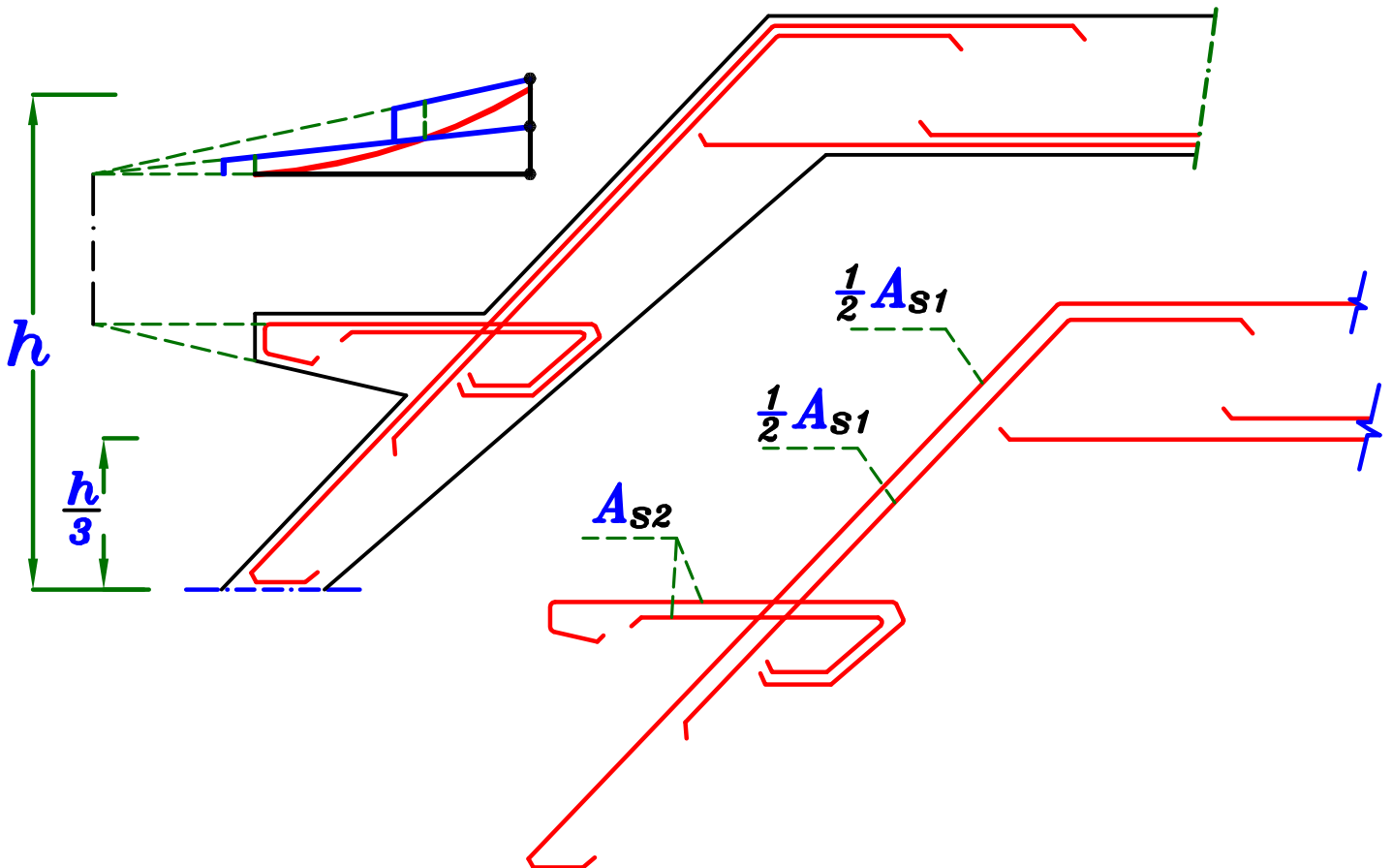
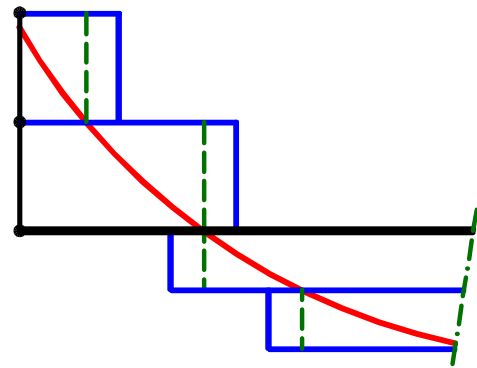
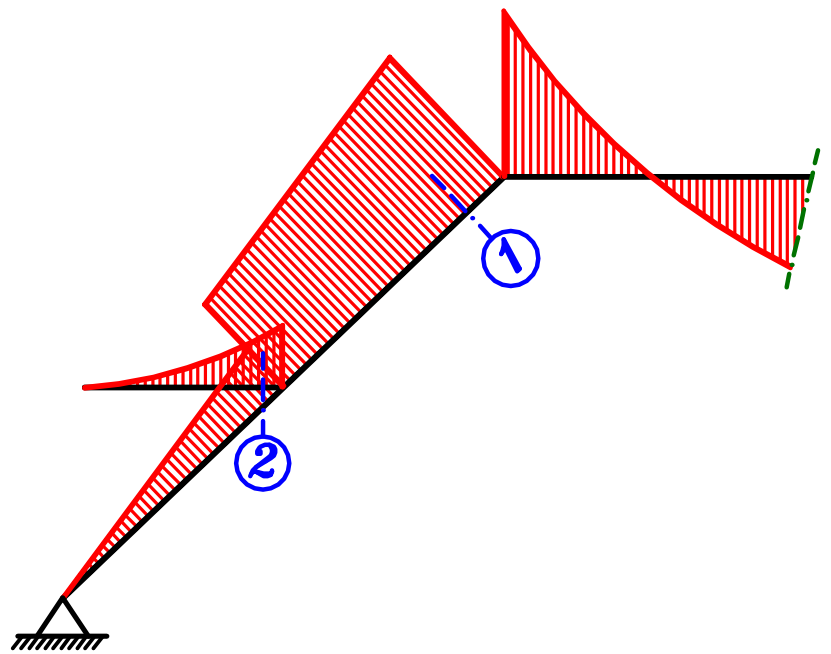
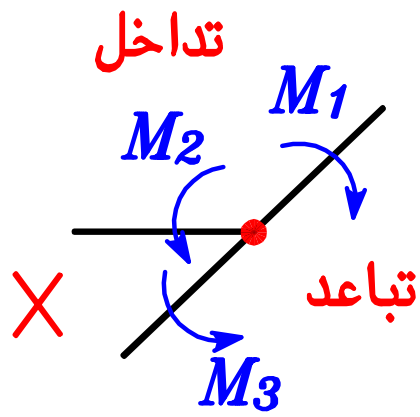


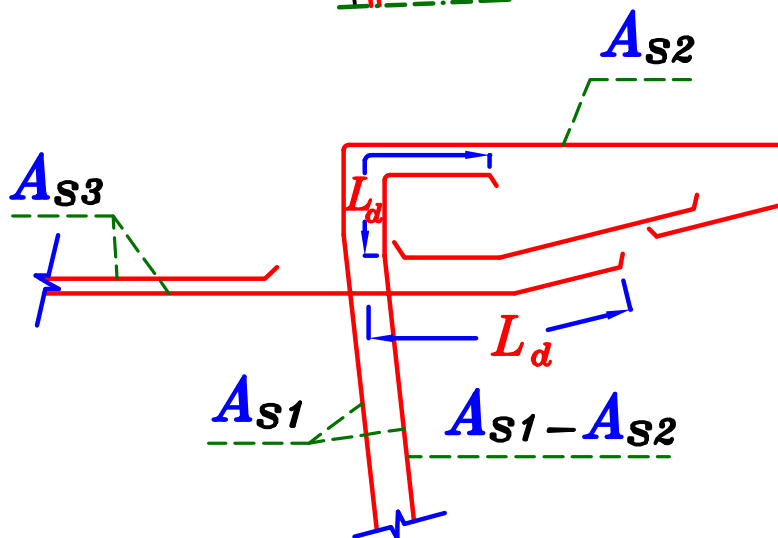
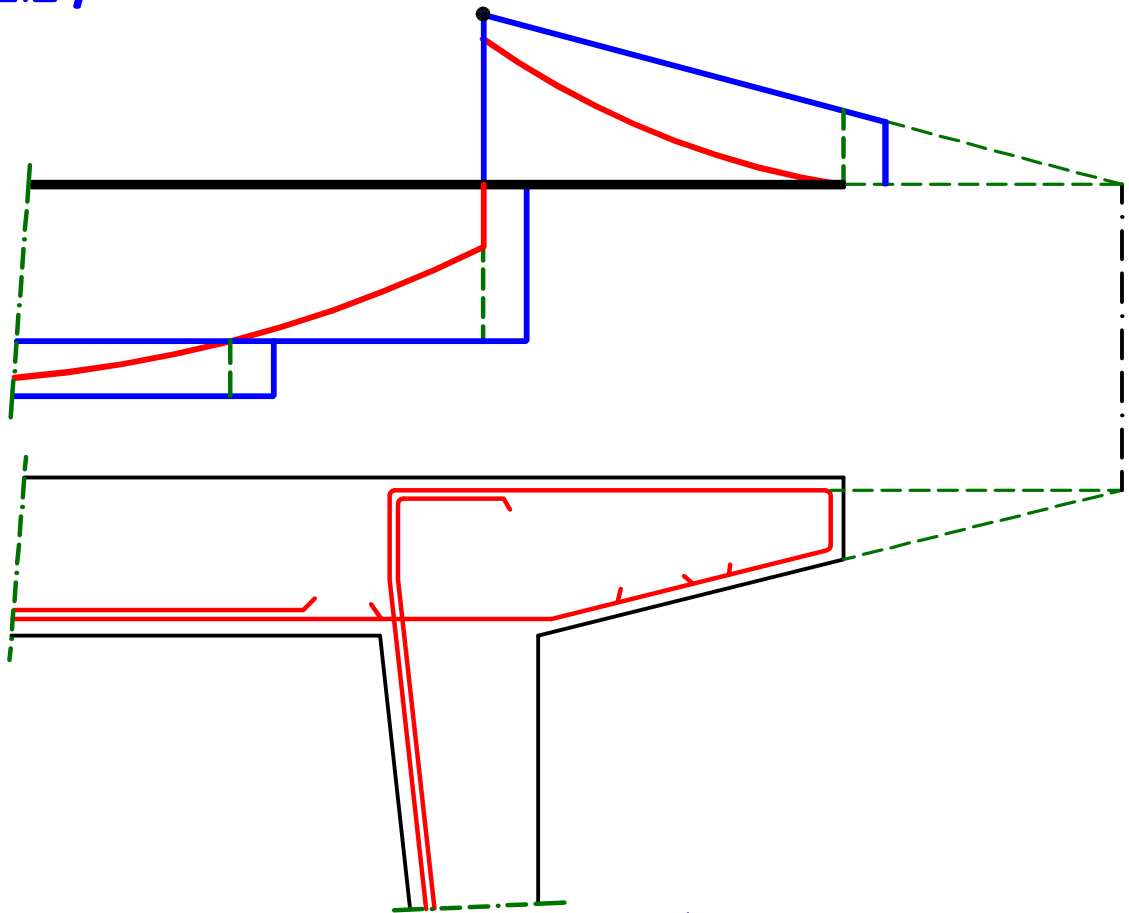
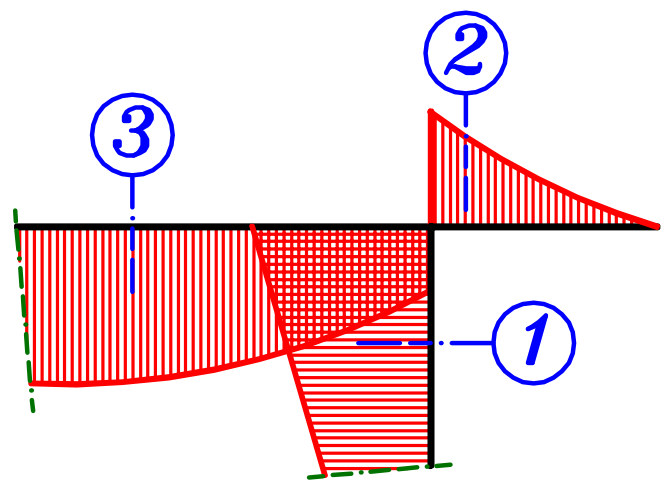
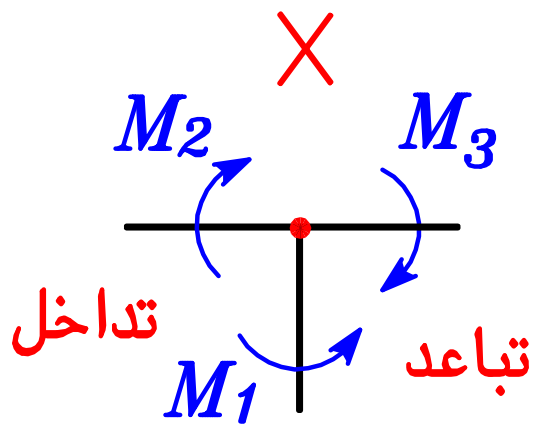




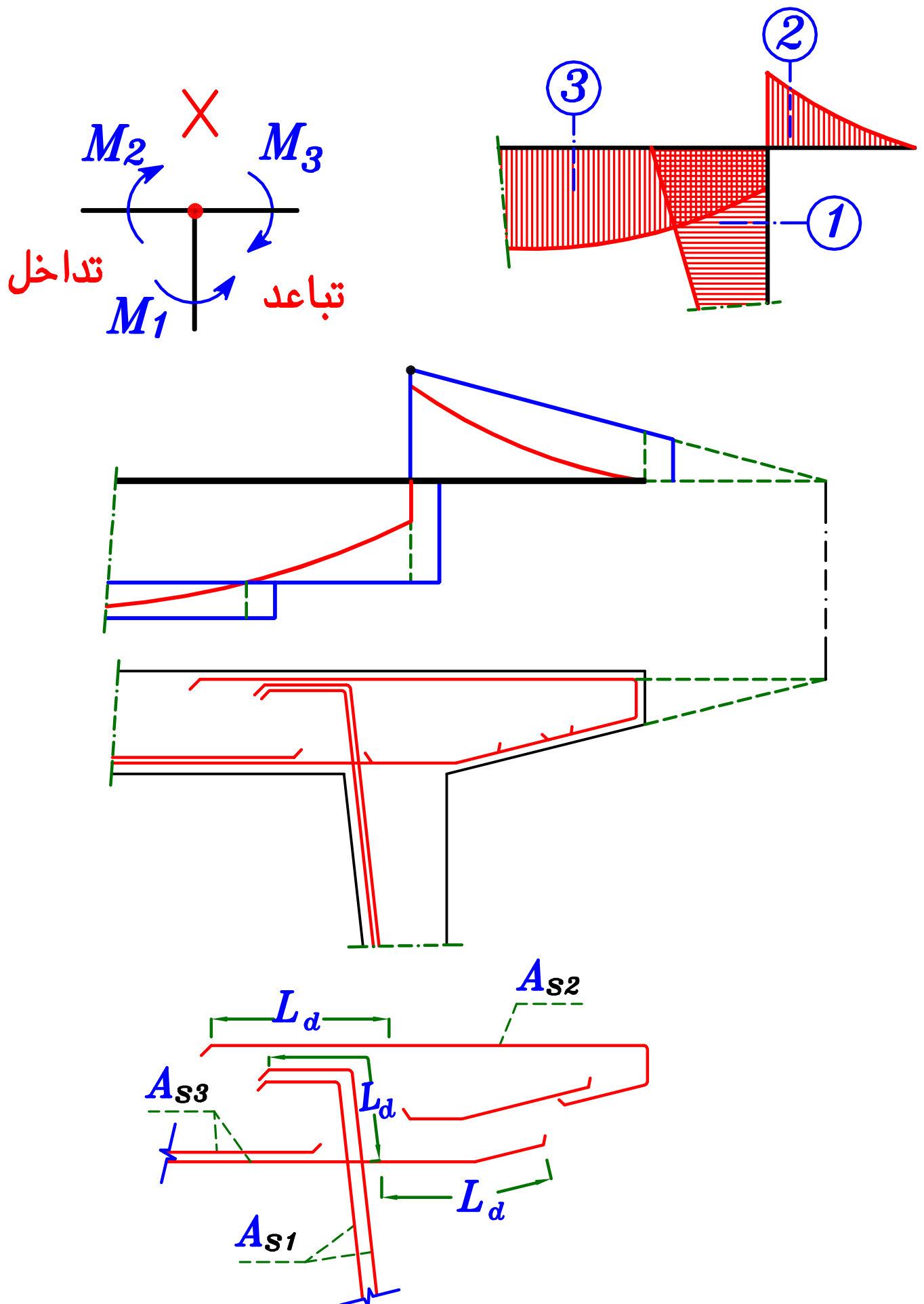
Frequent Joints.



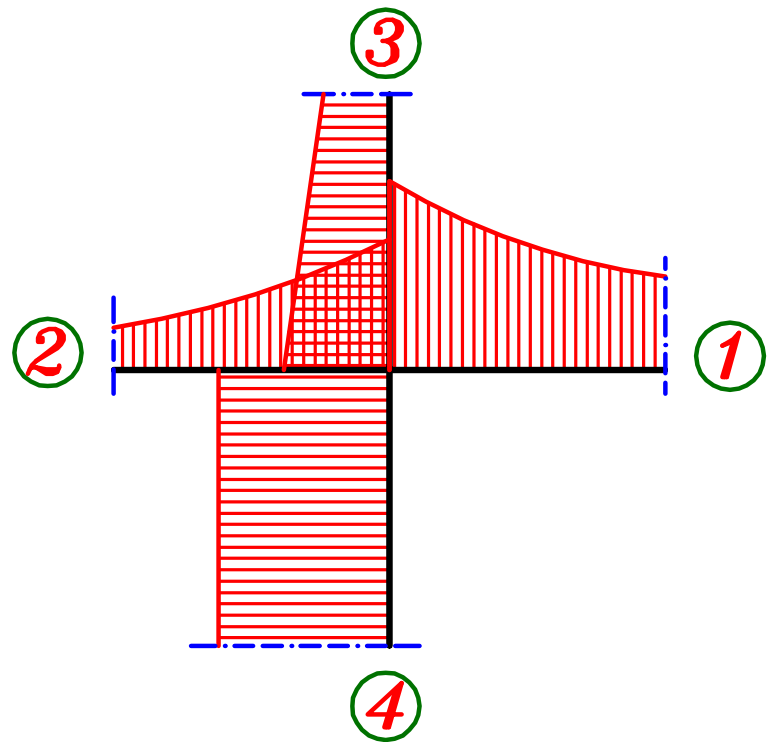
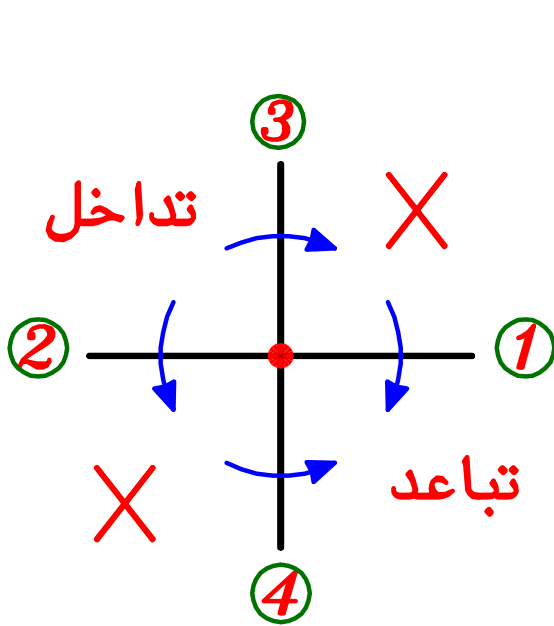




Another Concept of RFT.



RFT. of Four member Joint.



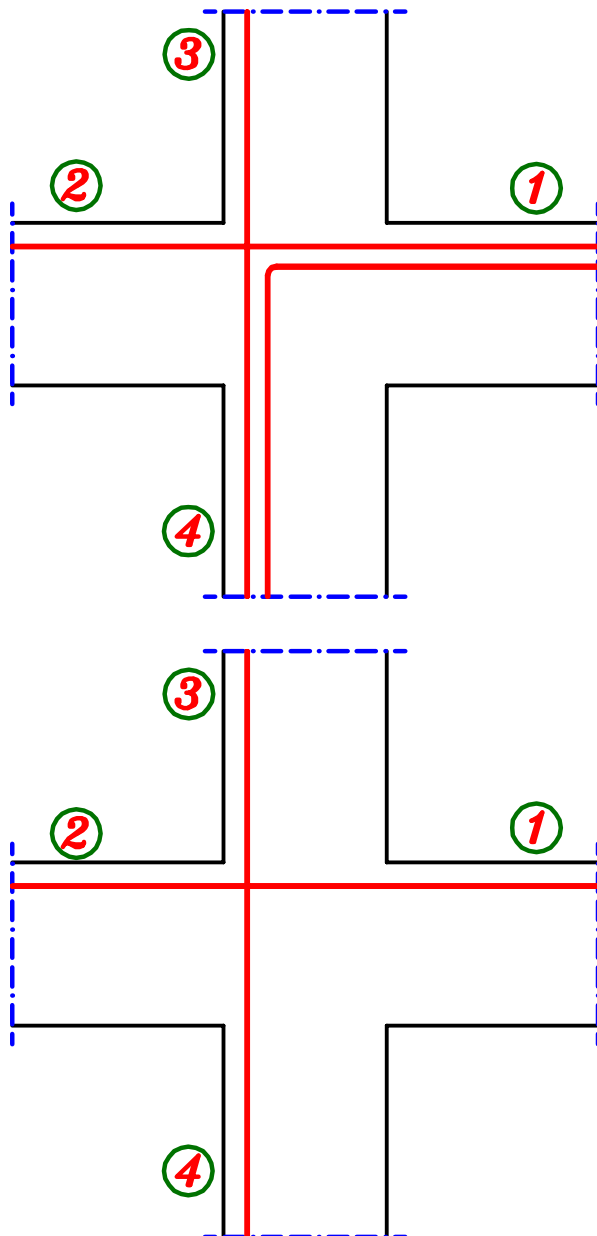
بین ① و ② وجود تبع
 بین ③ و ④ وجود تبع
 بین ① و ④ وجود تبع
 بین ② و ③ وجود تداخل
 بین ① و ③ لا وجود شیء
 بین ② و ④ لا وجود شیء

بین ① و ④ وجود تبع

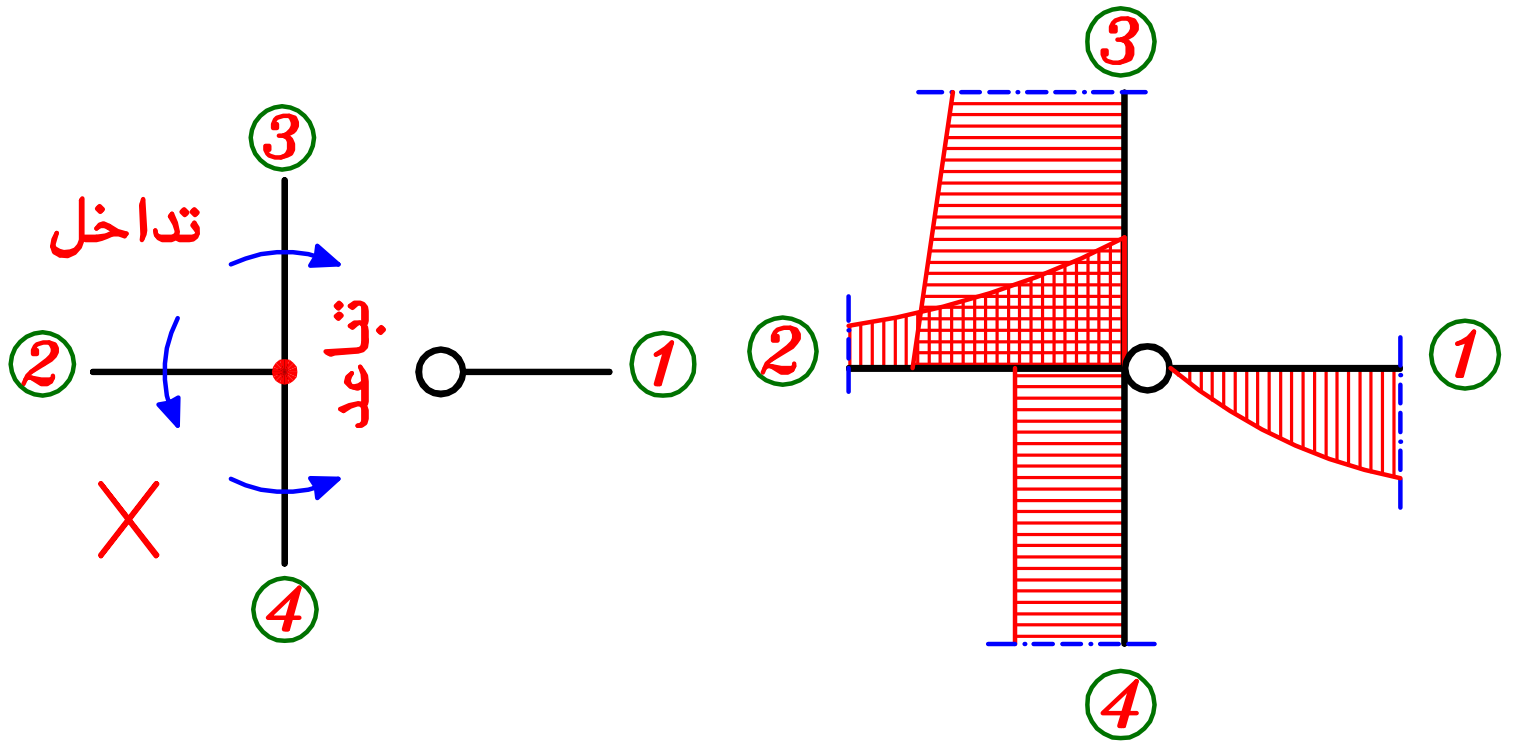
لكن اذا لم يحتاج ای member منهم

حدید من ال member الاخر

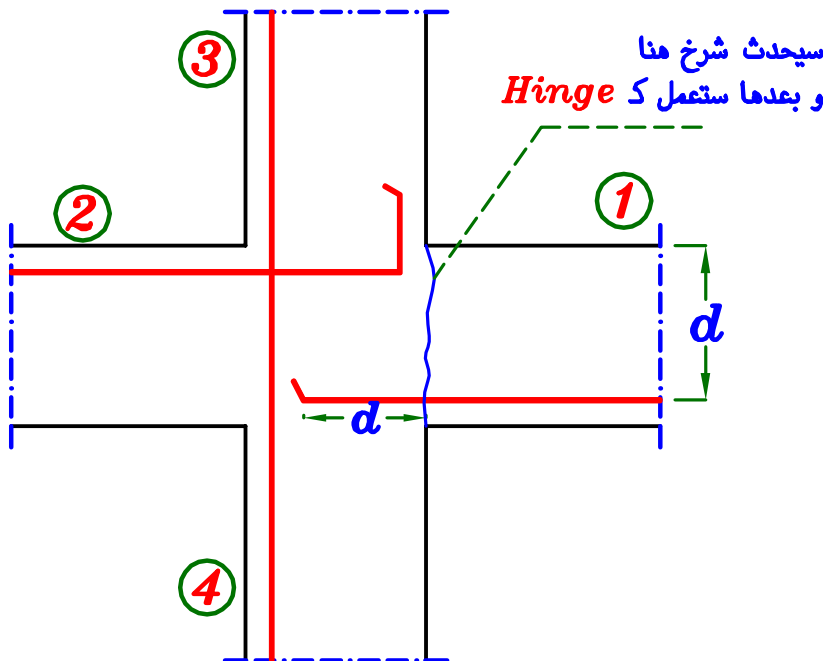
ممکن ان لا نكمل بينهم ای اسياخ مشترکه



RFT. of Four member Joint with Hinge.



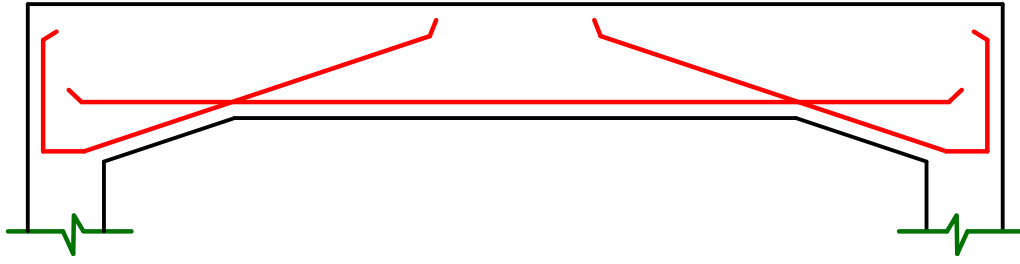
في هذه الحالة يتم تنفيذ ال **Hinge** بأن لا تكمل الحديد من **member 1** الى داخل ال **Joint** الا قيمه صغيره بمقدار d الكمره



بين ③ و ④ يوجد تباعد
بين ③ و ② يوجد تداخل
بين ② و ④ لا يوجد شيء

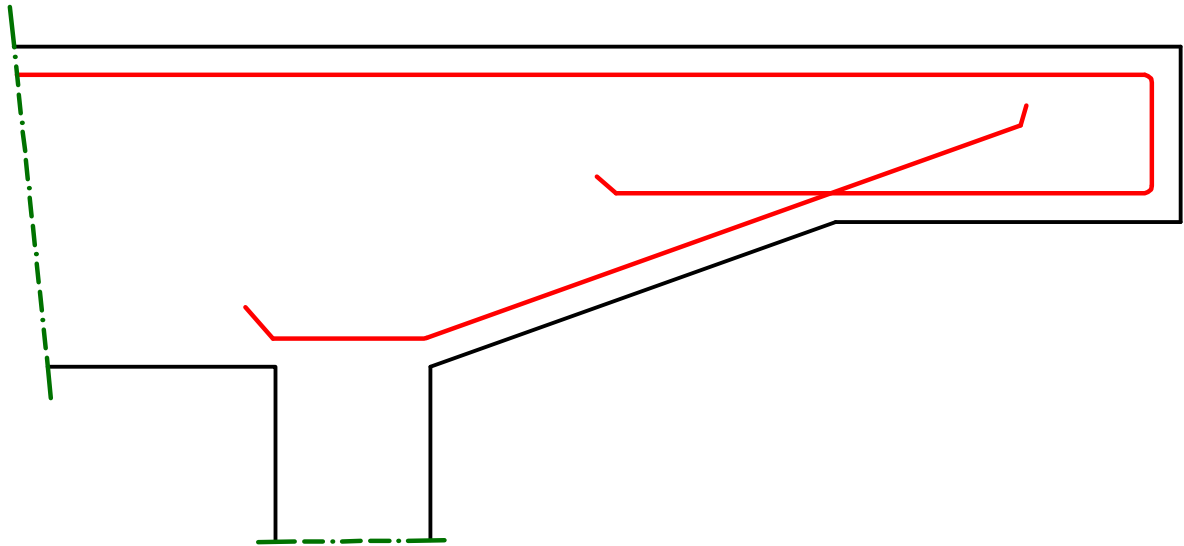
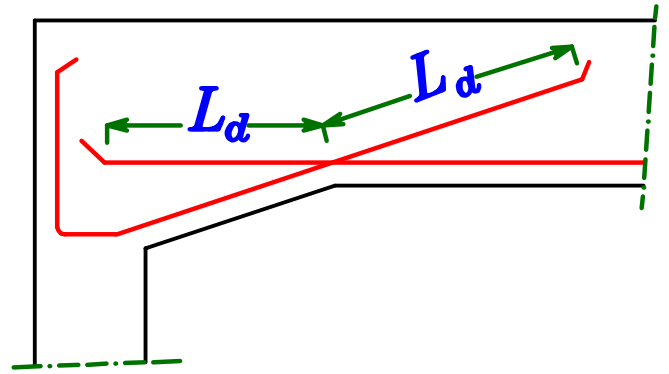
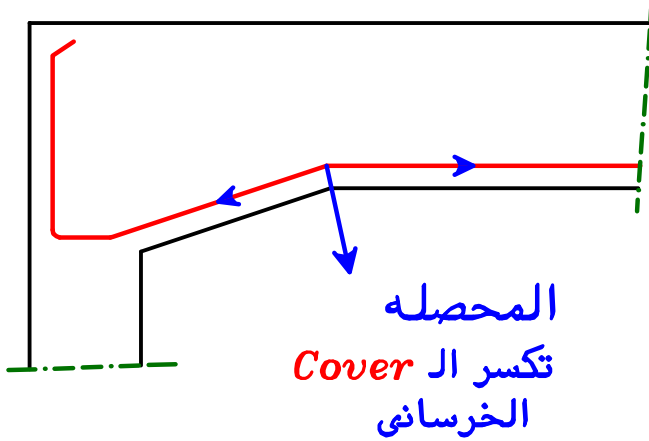
و تعتبر ال **Joint** عند التسليح كأنها **3 member joint** تباعد و تداخل

Variable Depth.



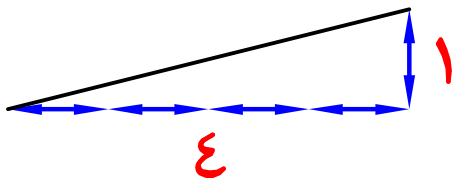
⊗ **Fatal.**

⊙ **مقص**



إذا كان ميل الخرسانه غير معطى فى المسأله

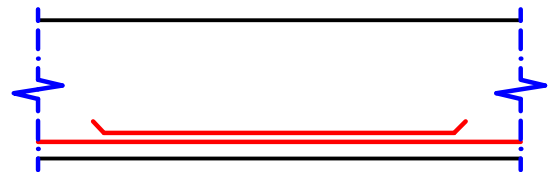
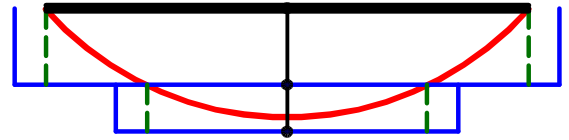
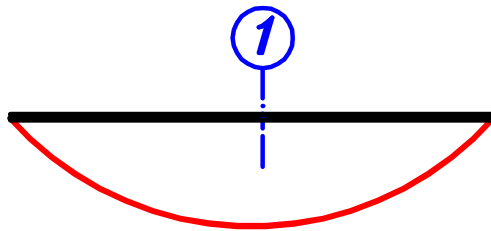
يفضل أن نأخذه بميل ١ : ٤



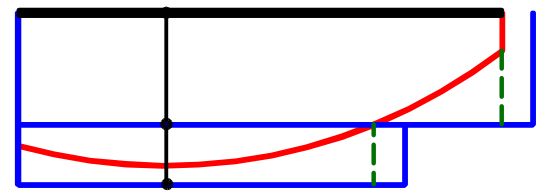
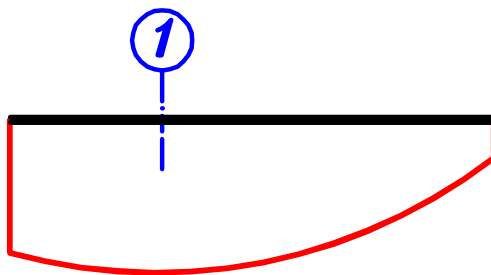
Critical Sections & Details of RFT.

For different members

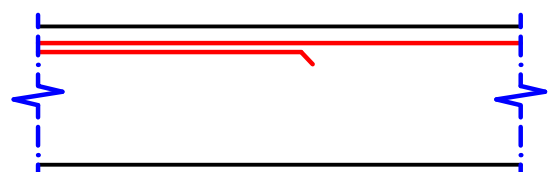
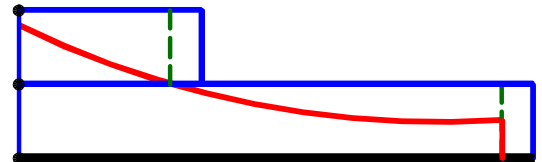
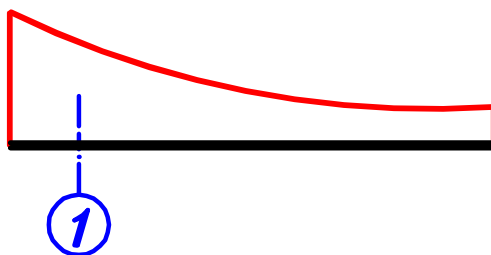
1



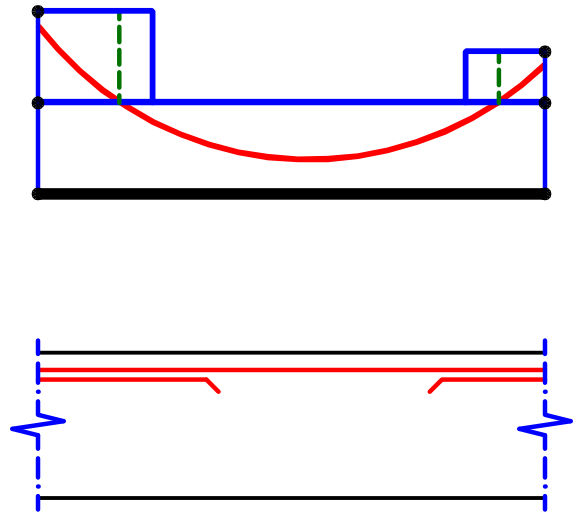
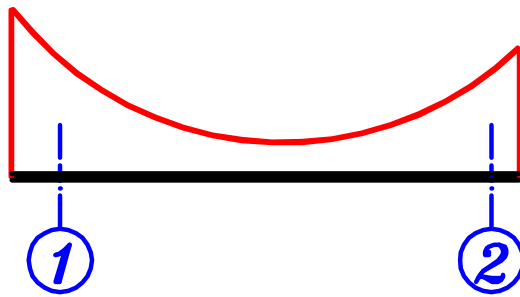
2



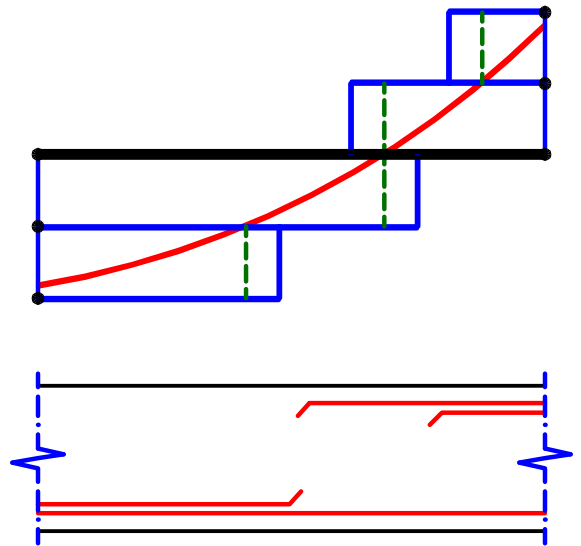
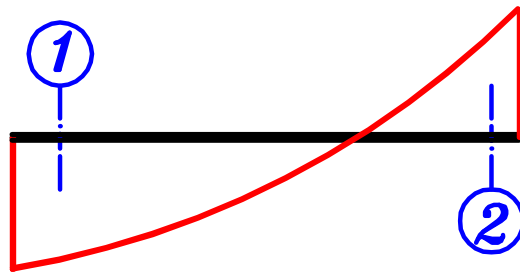
3



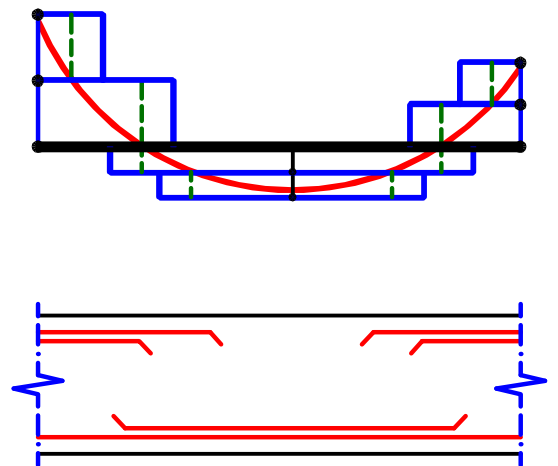
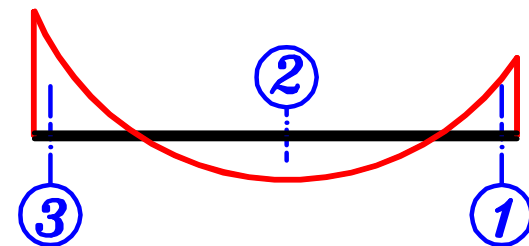
4



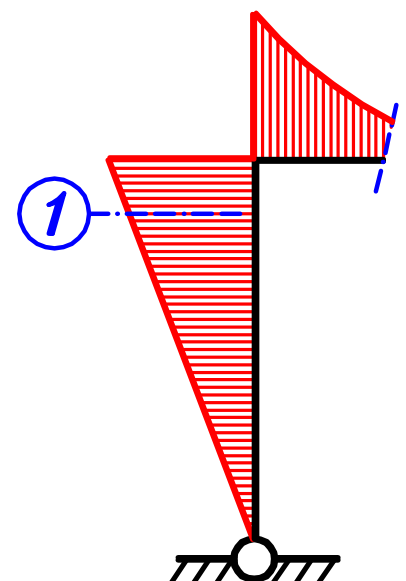
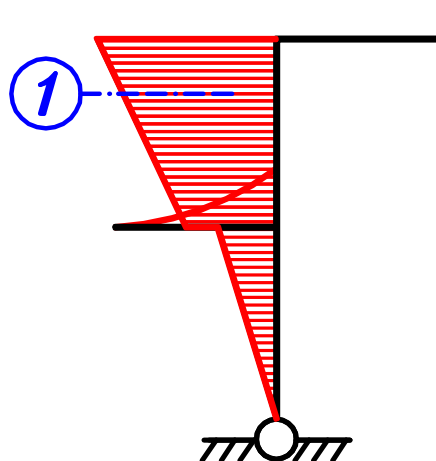
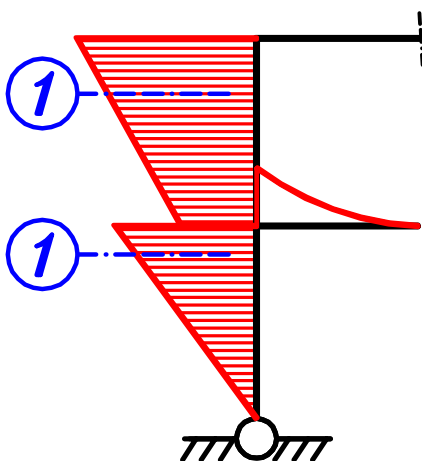
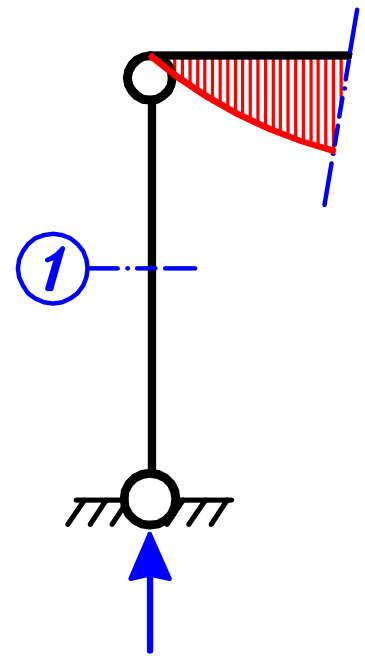
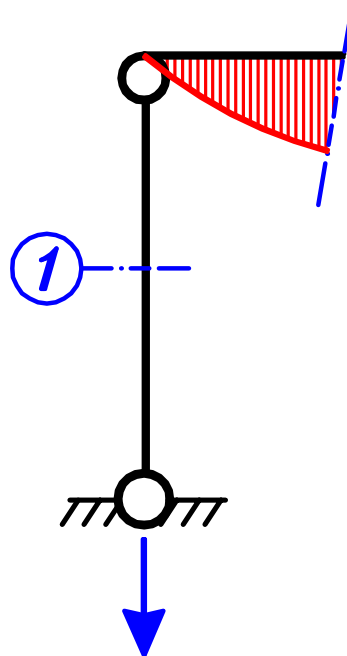
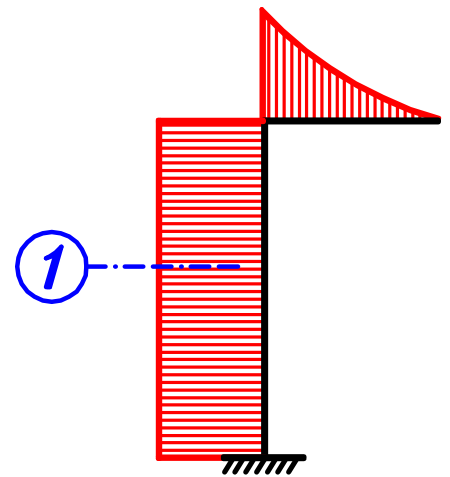
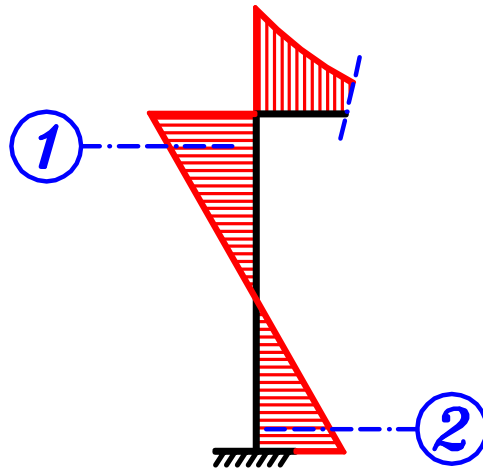
5



6



Columns Critical Sections.

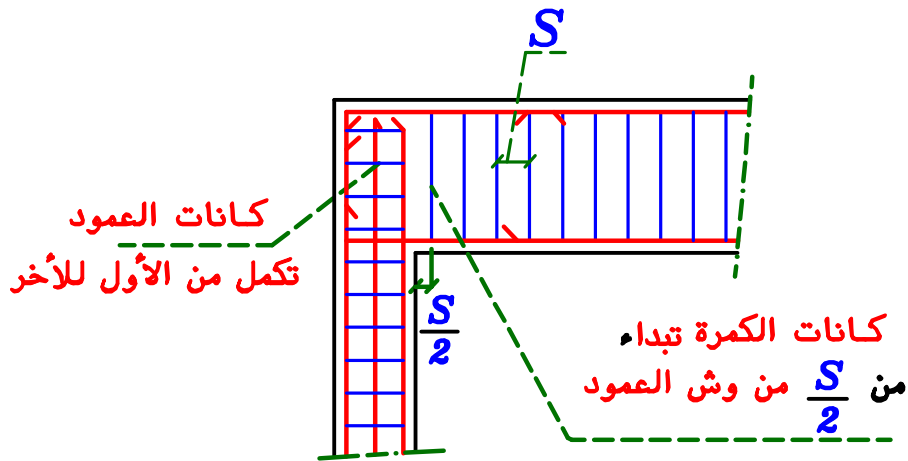
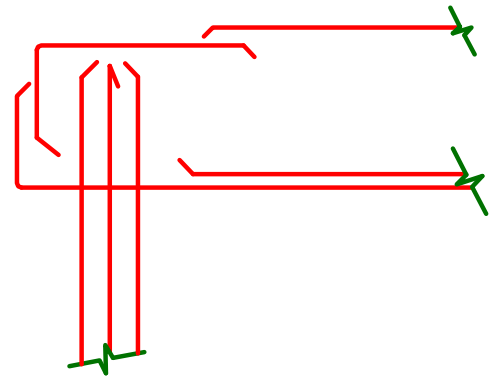
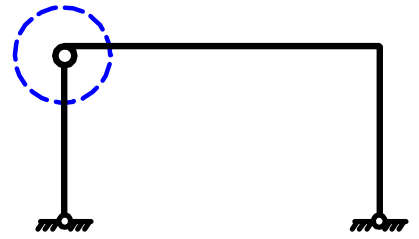


Stirrups الكانات

ترسم الكانات دائما عموديه على ال *C.L.*

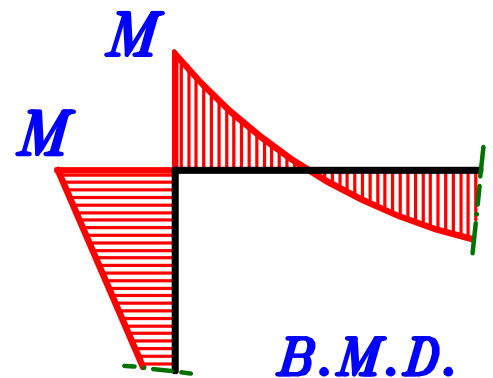
① Hinged Joints. (Joint between the beam & Link member)

joint لا تنقل عزوم

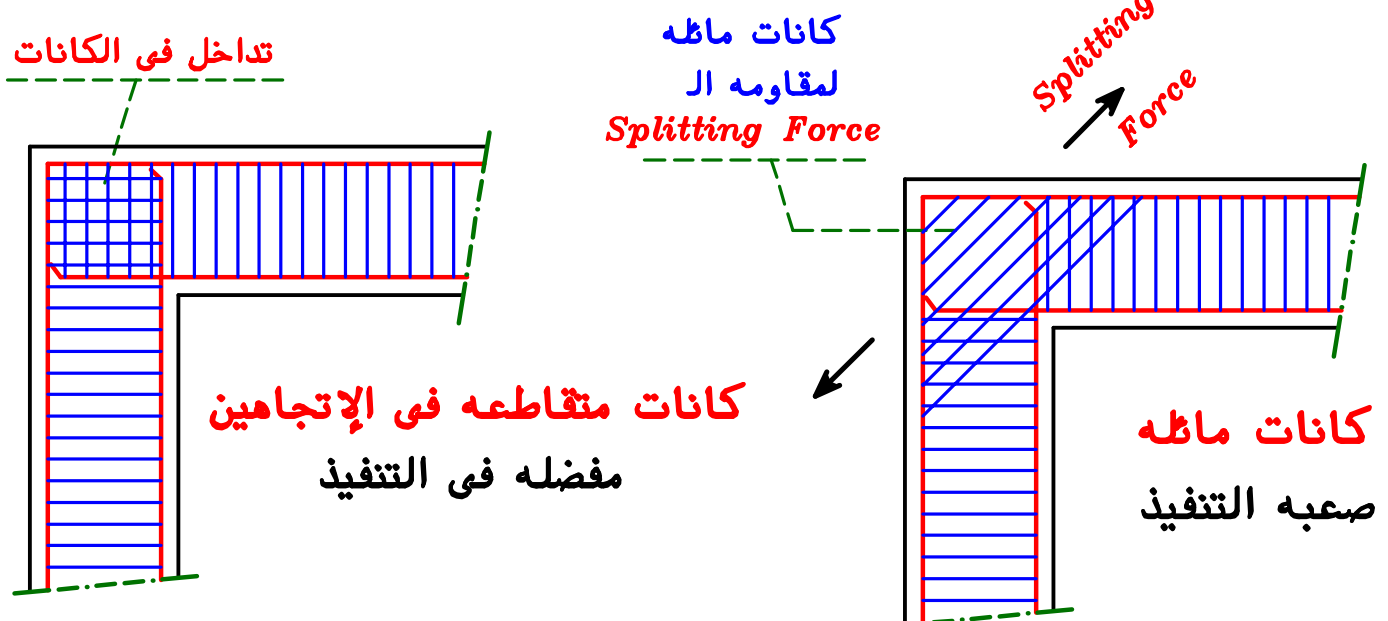


② **Rigid Joints.** **تثقل عزوم joints**

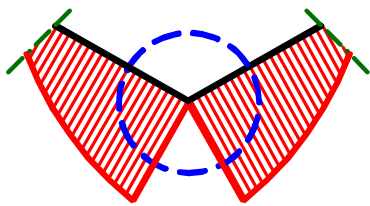
تقاطع أو تداخل



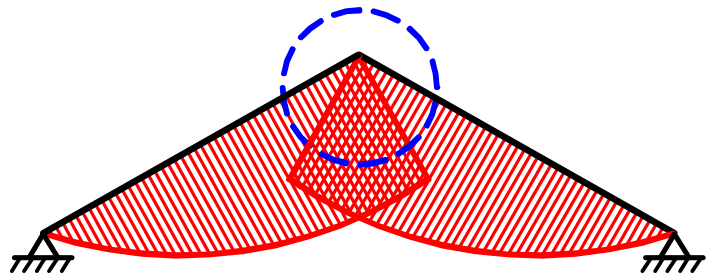
يجب أن تكمل الكانات فى الاتجاهين
أى يحدث تداخل فى الكانات .



Joints تنقل عزوم سواء تداخل أو تباعد .



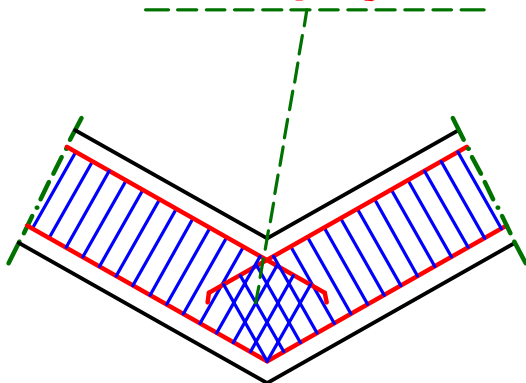
تباعد في ال $B.M.$



تداخل في ال $B.M.$

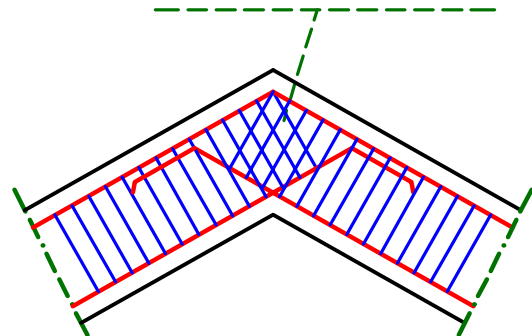
ترسم الكانات دائما عموديه على ال $C.L.$

تداخل في الكانات



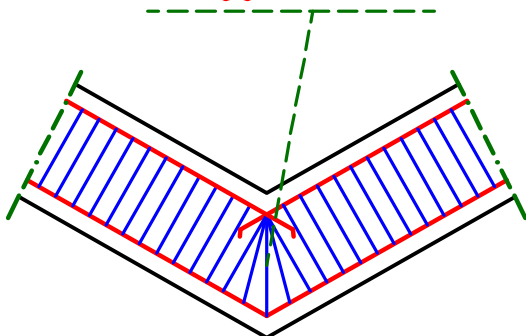
✓✓ كانات متقاطعه في الإتجاهين
مفضله في التنفيذ

تداخل في الكانات



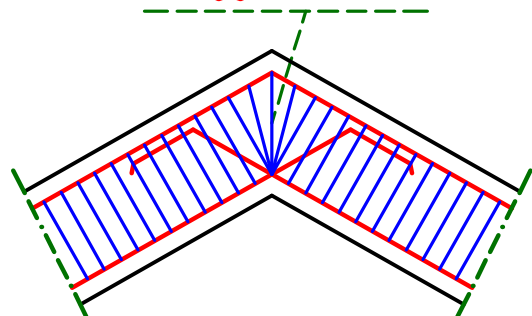
✓✓ كانات متقاطعه في الإتجاهين
مفضله في التنفيذ

كانات مروحه



كانات مروحه
صعبه التنفيذ

كانات مروحه



كانات مروحه
صعبه التنفيذ

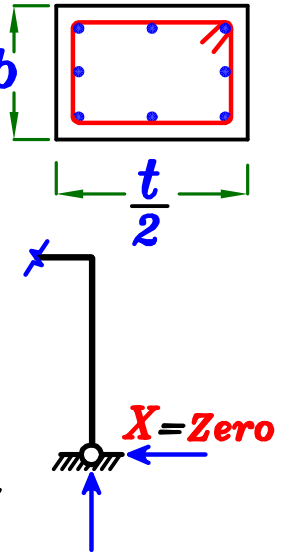
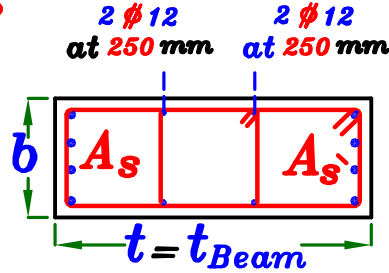
Cross Sections.

Ⓐ Axially Loaded Member.

① Link Member. (Compression OR Tension) $(b * \frac{t}{2})$

② فى بعض الاحيان يكون العمود معطى كما بالشكل
و لكن لا يكون عليه **B.M.**
فى هذه الحالة تؤخذ تخانته بنفس تخانه الكمره المحموله عليه

$$A_{smin.} = \frac{0.8}{100} * b * t \quad A_s = A_s' = \frac{A_{smin.}}{2}$$



Ⓑ Horizontal & Inclined members.

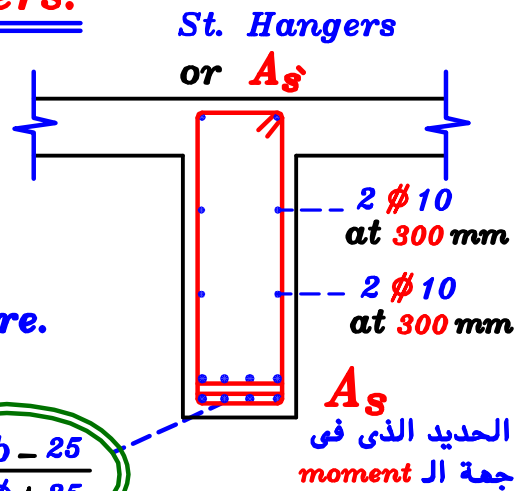
(مثل الكمرات) لا توجد كانات داخلية

الحديد الذى فى الجبهه المقابله لل
Stirrup Hangers IF Ten. Failure.

Compression Steel (A_s') IF Comp. Failure.

و غالبا فى الكمرات تكون $\frac{e}{t} > 0.5$

$$n = \frac{b - 25}{\phi + 25}$$



$$n = \frac{b - 25}{\phi + 25}$$

Ⓒ Vertical members. مثل الأعمده

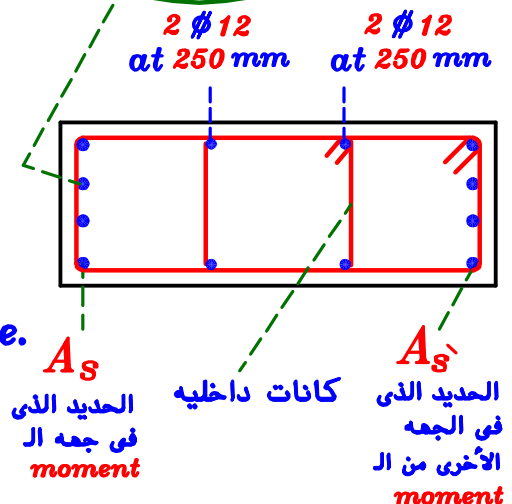
أكبر مسافه بين سيخين متتاليين = ٢٥٠ مم

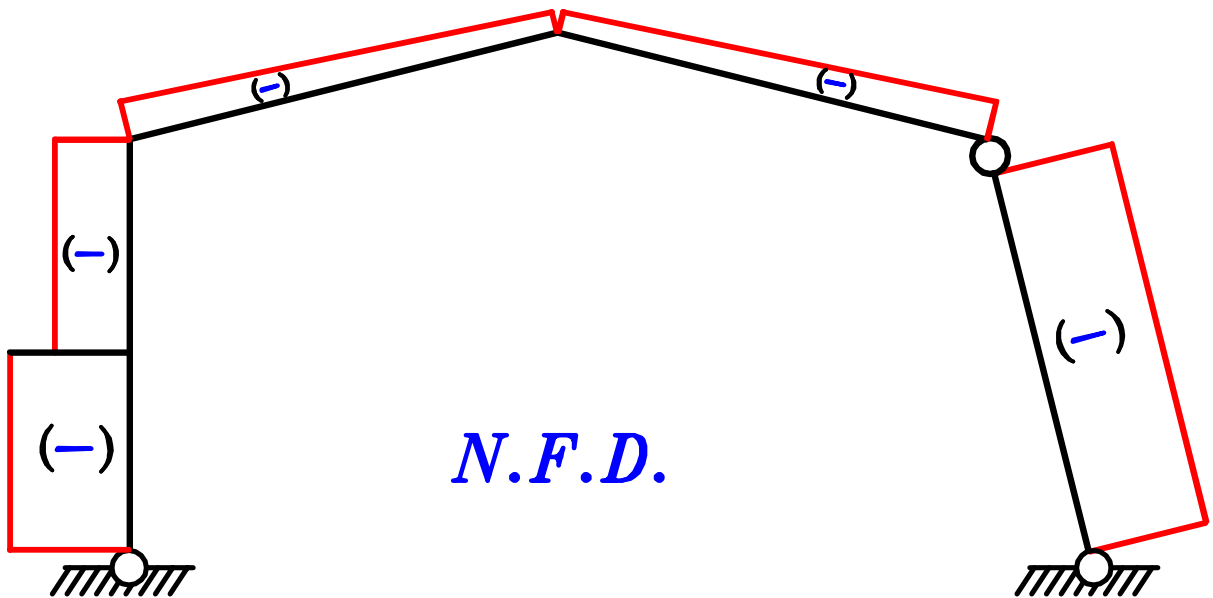
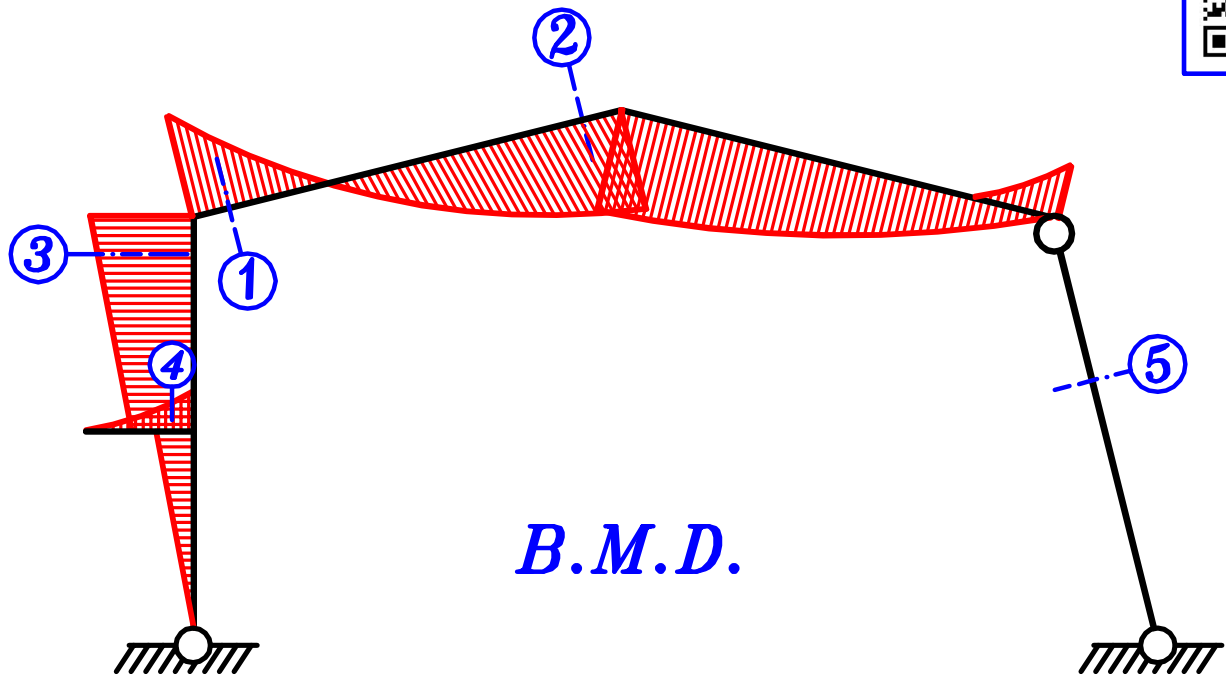
أكبر مسافه بين فرع كانه و الآخر = ٣٠٠ مم

الحديد الذى فى الجبهه الأخرى من ال **moment**

Take $A_s' = \text{Stirrup Hangers} \approx 0.4 A_s$ IF Ten. Failure.

Take $A_s' = A_s$ IF Comp. Failure.





بعد رسم ال *B.M.D.* & *N.F.D.* نحدد ال *Critical Sections* كما سبق .
ثم نصمم القطاعات بالترتيب كالاتى .

① نبدأ بتصميم القطاع الموجود على الكمره المؤثر عليه أكبر *moment* و ذلك لتحديد عمق القطاع «*t*»

take $C_1 = 3.5$, $J = 0.78$ The sec. as R-Sec.

Get $d_o = C_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}} \rightarrow d_o \rightarrow t_o = d_o + \text{cover}$

take $t_1 = (1.1 \rightarrow 1.3) t_o$

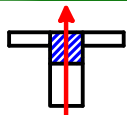
\therefore Check $\frac{P}{F_{cu} b t}$

② IF $\frac{P_{u.L.}}{F_{cu} b t} \leq 0.04 \rightarrow \text{neglect } N_{u.L.}$

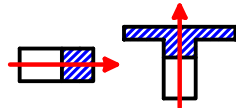
and Design the Sec. on B.M. only as Beams.

$\therefore d = d_1 = C_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}}$ take $C_1 = 3.5$, $J = 0.78$ (R-Sec.)
take $C_1 = 6.0$, $J = 0.826$ (T-Sec., L-Sec.)

ملحوظه هامه :



في بدايه التصميم نعمل تصميم على M , P على أن القطاع R-sec. ولكن اذا أهملنا ال P فنعمل تصميم على M فقط فيجب مراعاة



اذا كان القطاع R-sec. or T-sec.

③ IF $\frac{P}{F_{cu} b t} > 0.04 \rightarrow \text{Don't neglect } P_{u.L.}$

and the sec. designed as R-sec.

Get A_s From e_s IF Ten. Failure $\rightarrow A_s' = \text{Stirrup Hangers}$

Get A_s From I.D. IF Comp. Failure $\rightarrow A_s' = A_s$

④ نصمم باقى قطاعات الكمره على نفس ال depth ل ① Sec.

٣ ثم نصمم القطاع الموجود على العمود حيث يؤثر M & P كبيره

take $C_1 = 3.5$, $J = 0.78$

$$\text{Get } d_o = C_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}} \rightarrow d_o \rightarrow t_o = d_o + \text{cover}$$

$$\text{take } t_2 = (1.1 \rightarrow 1.3) t_o$$

Get A_s From e_s IF Ten. Failure $\rightarrow A_s' = \text{Stirrups Hangers} \approx 0.4 A_s$

Get A_s From I.D. IF Comp. Failure $\rightarrow A_s' = A_s$

ملحوظه هامه

IF $t_{(Column)} < 0.8 t_{(Beam)}$ Take $t_{(Column)} = t_{(Beam)}$

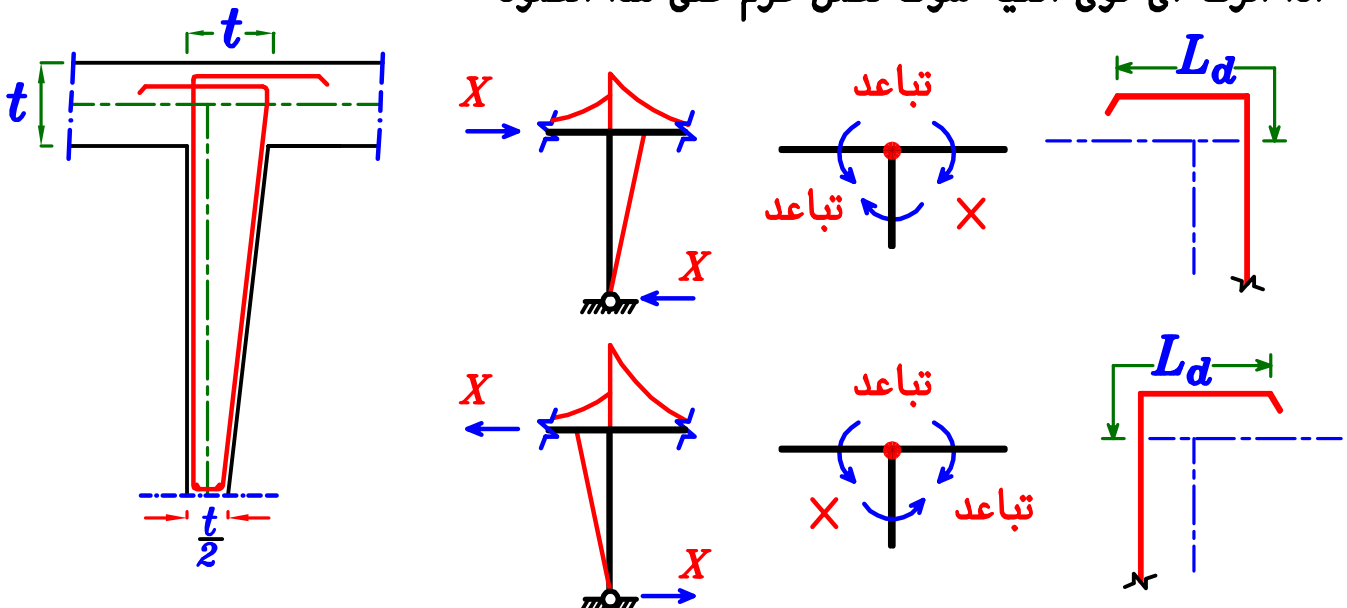
و هذا فى ال **Frames** فقط وليس فى ال **Girders**
أى ليس مع أعمده ال **Link members**

ملحوظه هامه

إذا كان العمود ليس **Link member** و لكن يوجد عليه **Normal** فقط
سنأخذ تخانته نفس تخانه الكمره و سنعمل على تصميم القطاع على **Normal** فقط
و سوف يكن التسليح أقل من ال **minimum** لذا سنأخذه يساوى ال **minimum**

$$A_{s_{total}} = A_{s_{min.}} = \frac{0.8}{100} * b * t \xrightarrow{\text{Take}} A_s = A_s' = \frac{A_{s_{min.}}}{2}$$

إذا أثرت أى قوى أفقيه سوف تعمل عزم على هذا العمود

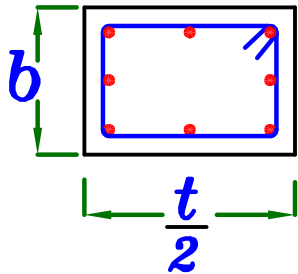
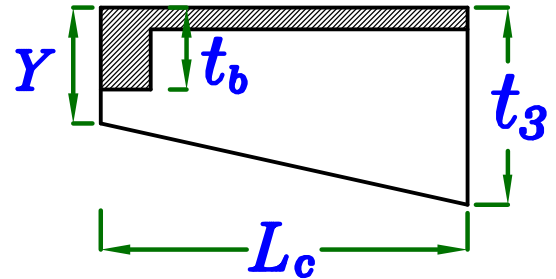


④ ثم نصمم قطاع ال *Cantilever* (Sec.④)

و يكون له عمق مختلف عن باقى ال *Frame*

$$d_3 = C_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \quad C_1 = 3.5, J = 0.78, \quad t_3 = d_3 + \text{Cover}$$

$$Y = \left\{ \begin{array}{l} \frac{t_3}{2} \\ t_b = \frac{\text{Spacing}}{12} \\ t_3 - \frac{L_c}{3} \end{array} \right\} \text{الأكبر}$$



⑤ ثم نصمم قطاع ال *Link member* (Sec.⑤)

و عادة تؤخذ أبعاد هذا القطاع $(b * \frac{t}{2})$

$$P_{U.L.} = 0.35 A_c F_{cu} + 0.67 A_s F_y \quad \text{و يصمم كأنه عمود}$$

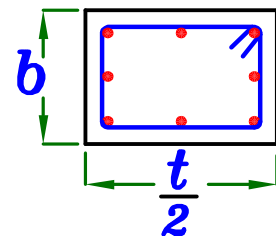
ملحوظه

إذا كان ال *Link member* عليه *Tension* و ليس *Compression*

تؤخذ أبعاد هذا القطاع $(b * \frac{t}{2})$

$$A_s = \frac{T_{U.L.}}{F_y / \delta_s}$$

و يصمم كأنه *Tie*

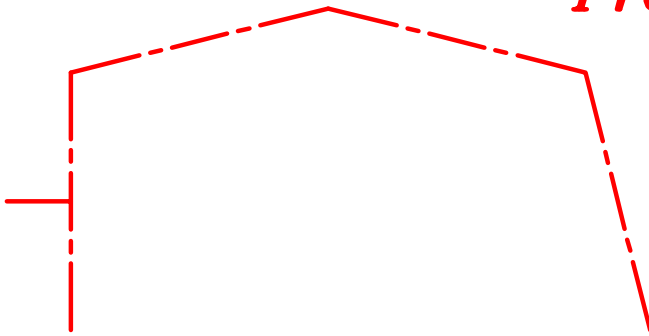


Steps to Draw Frame Concrete Dimensions.



① نبدأ برسم ال $C.L.$ لل $Frame$

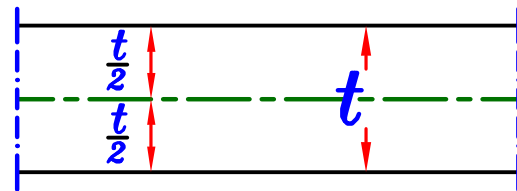
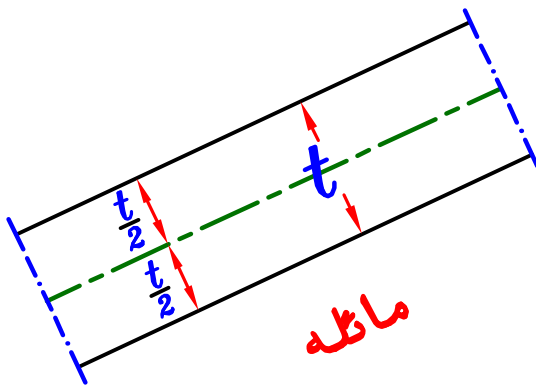
بمقياس الرسم المطلوب



② نرسم عمق ال $members$ المختلفه بنفس مقياس الرسم

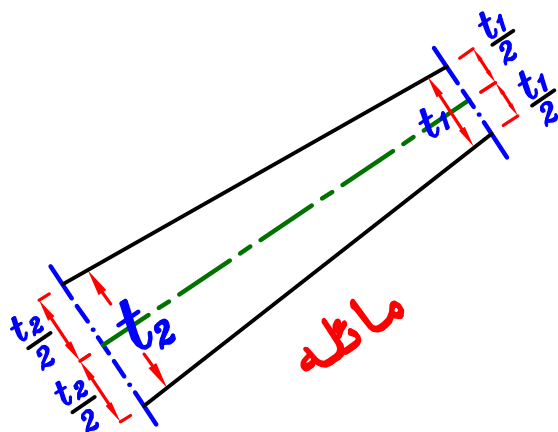
و ذلك حسب شكل كل $member$ مثل :

⌈ كمره لها عمق ثابت « t »

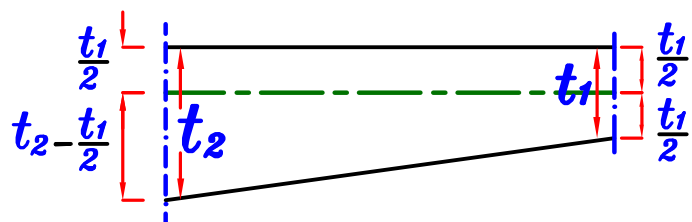


أفقيه

⌈ كمره لها عمقان مختلفان « t_1 » & « t_2 »

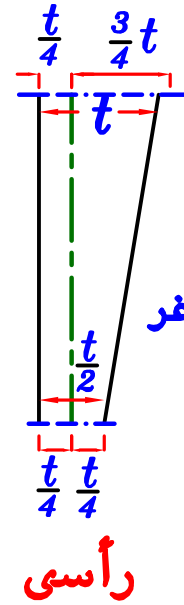
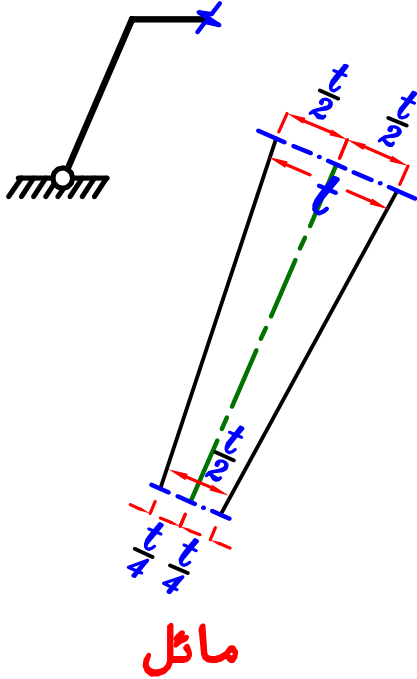


يكون ال $C.L.$ فى منتصف العمق الأصغر



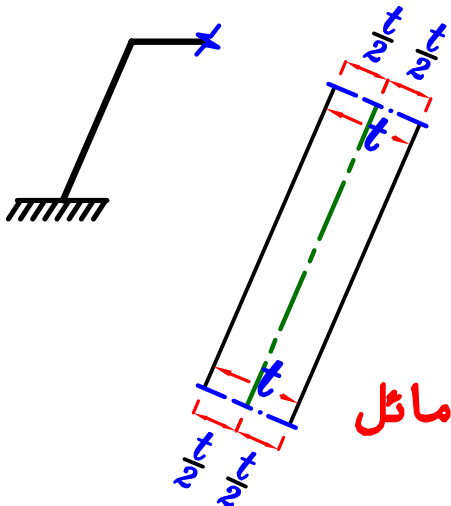
أفقيه

ج الأعمدة التي آخرها Hinged support

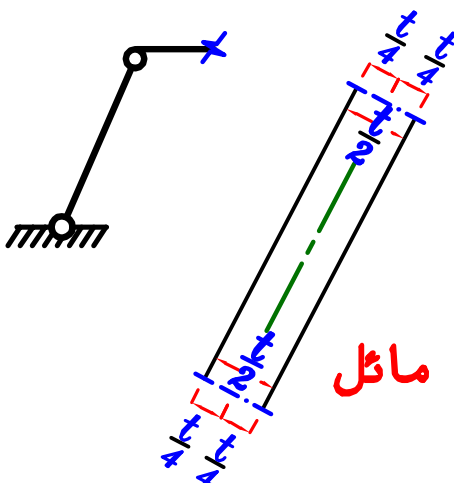


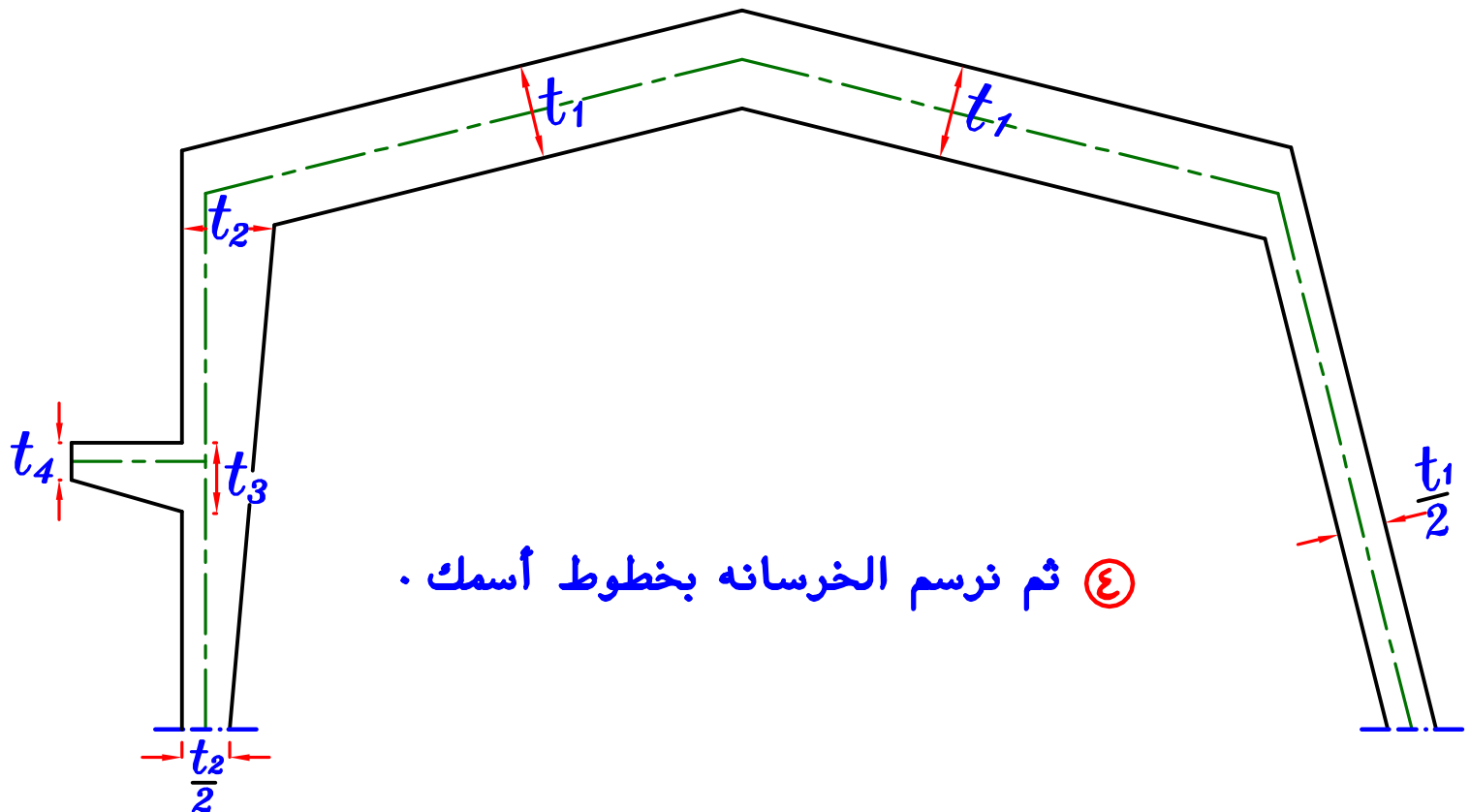
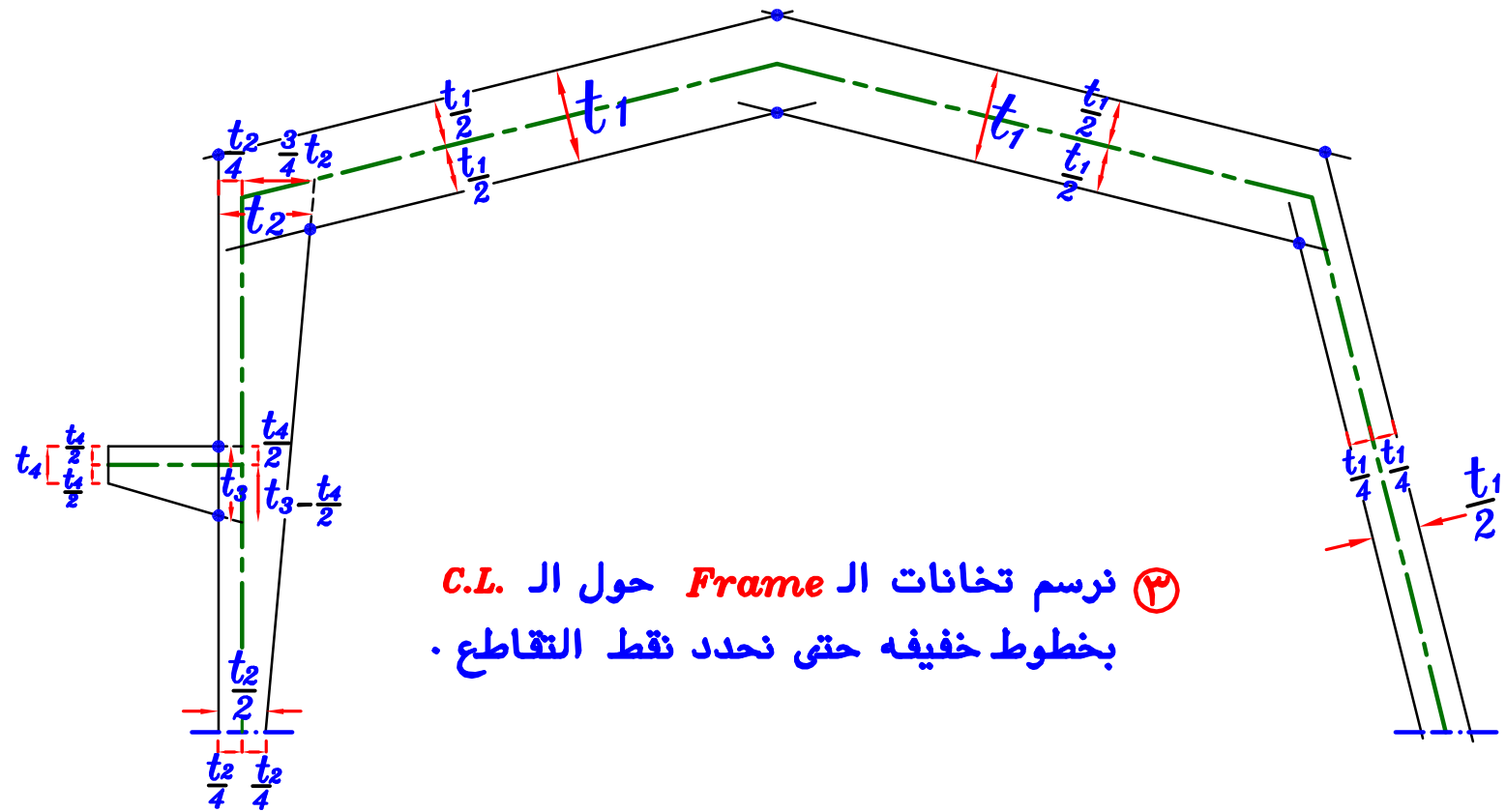
يكون ال C.L. في منتصف العمق الأصغر

د الأعمدة التي آخرها Fixed support



ه الأعمدة ال Link member.



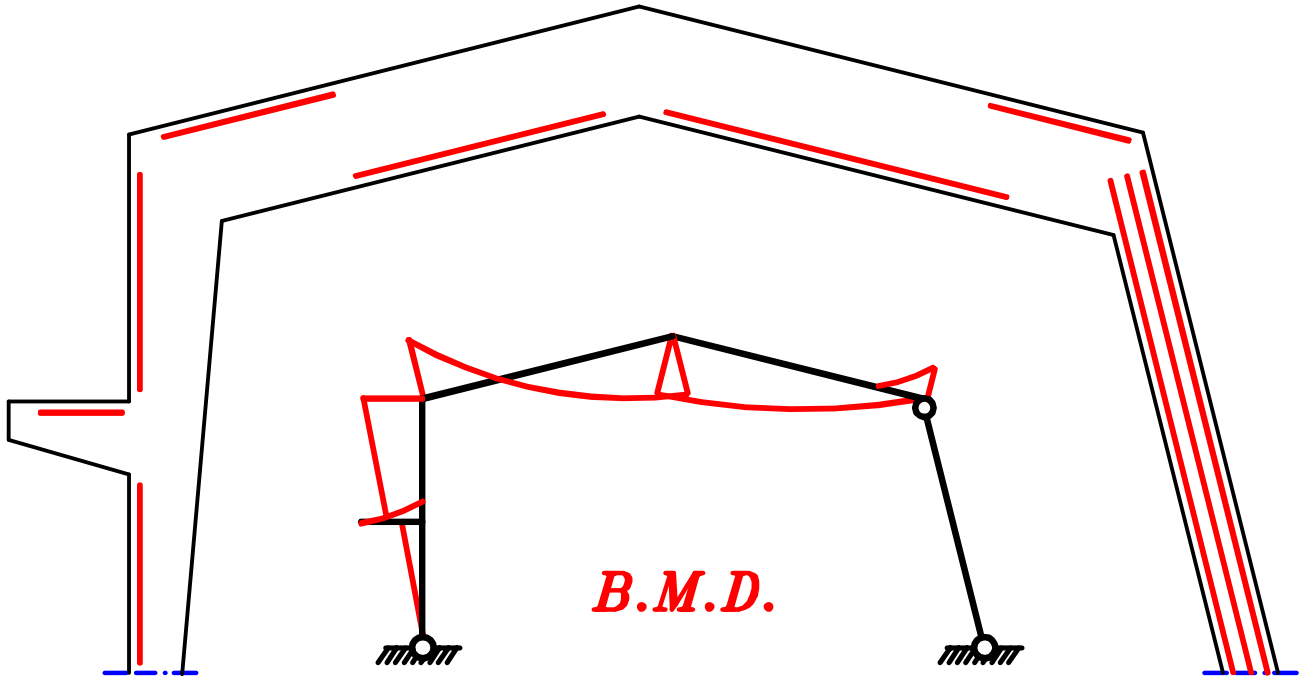


Steps to Draw Frame Reinforcement.

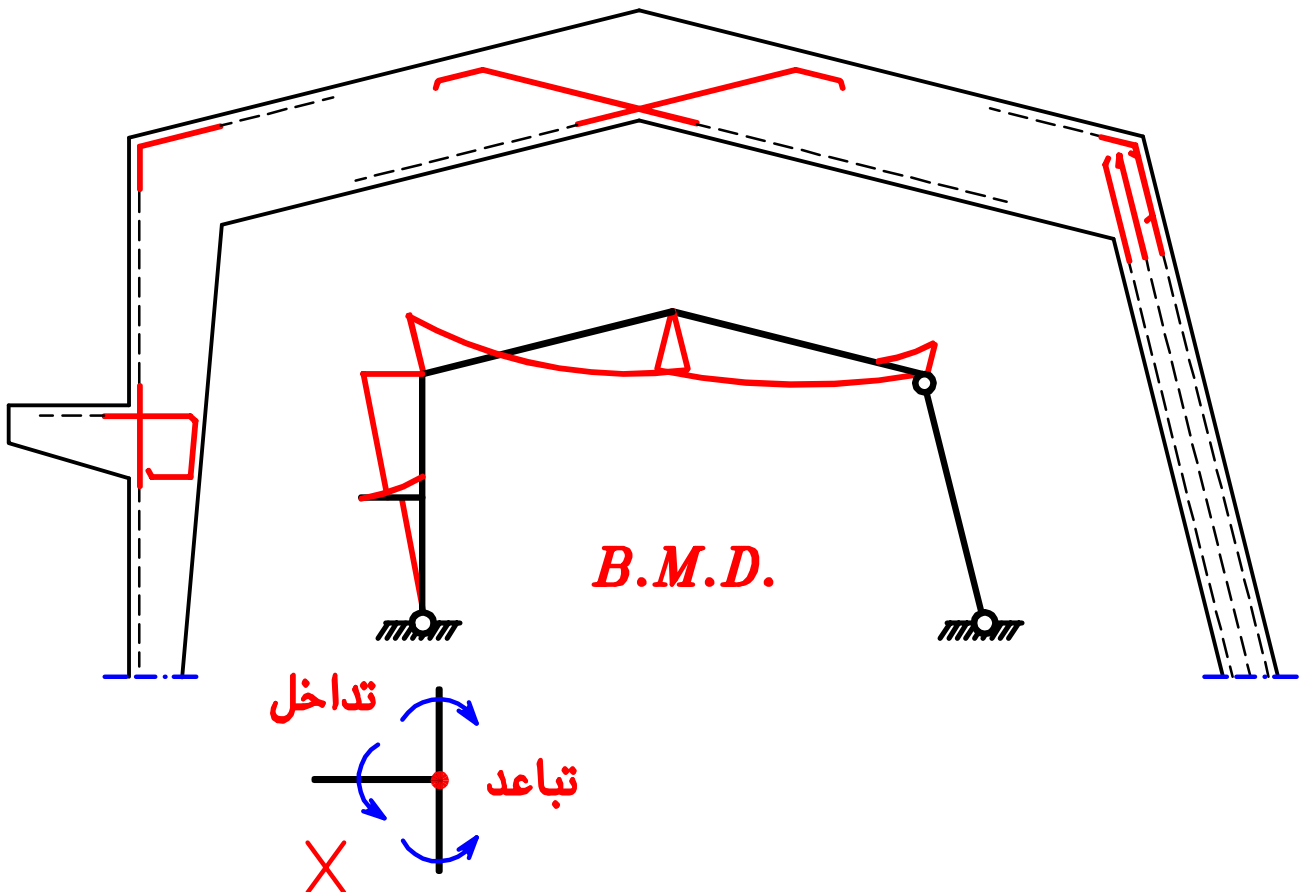


مراحل رسم التسليح للـ **Frame** مع مراعاة الترتيب

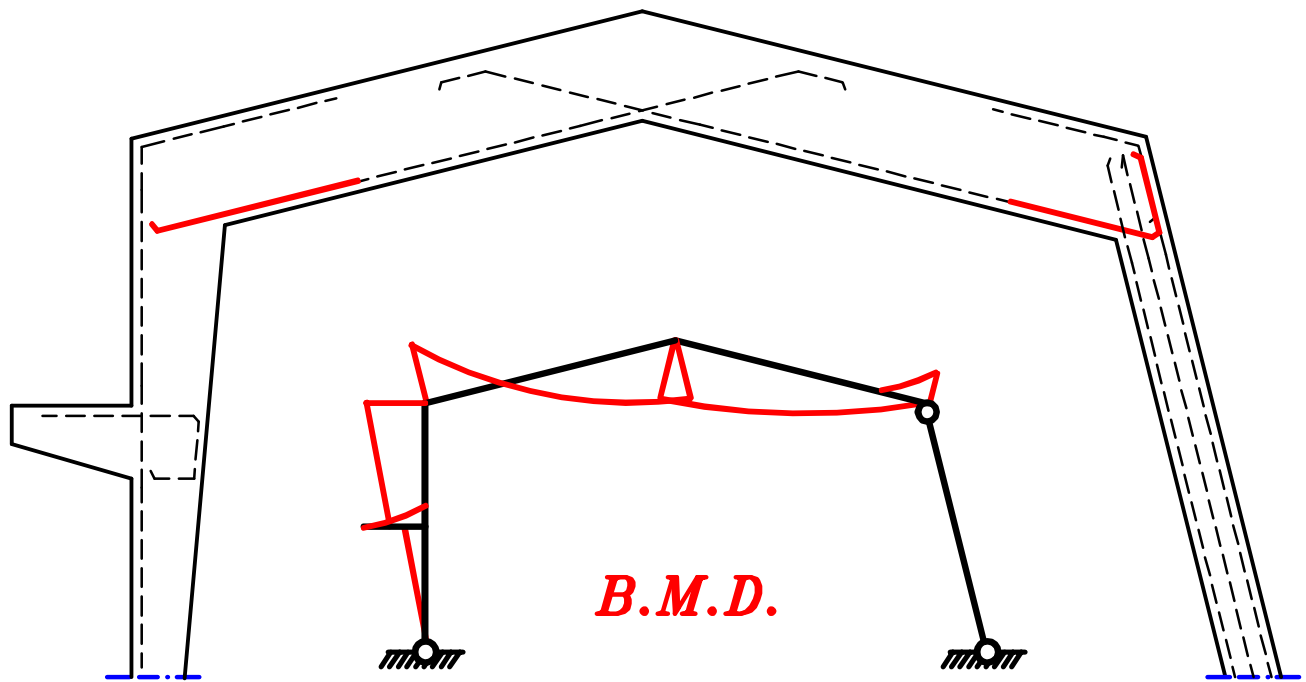
١- رسم مكان التسليح الرئيسى جهة الـ **moment**.



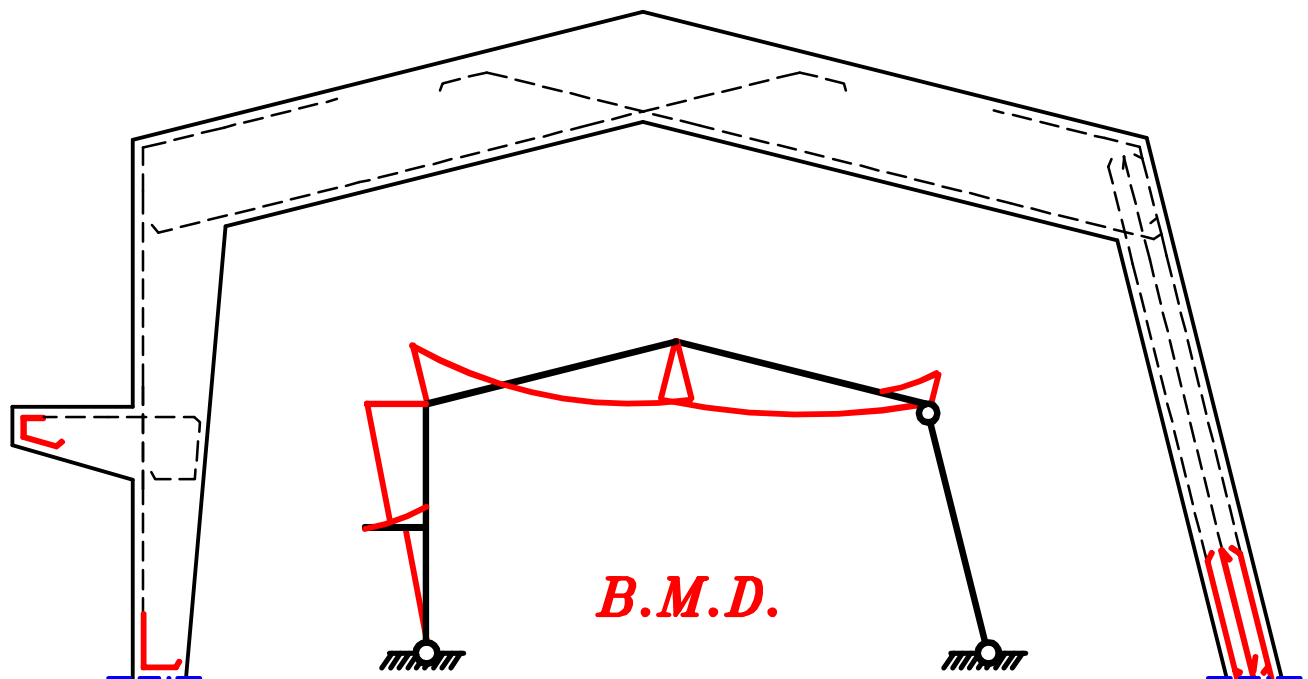
٢- تسليح الـ **Joints** (عمل التباعد و التداخل).



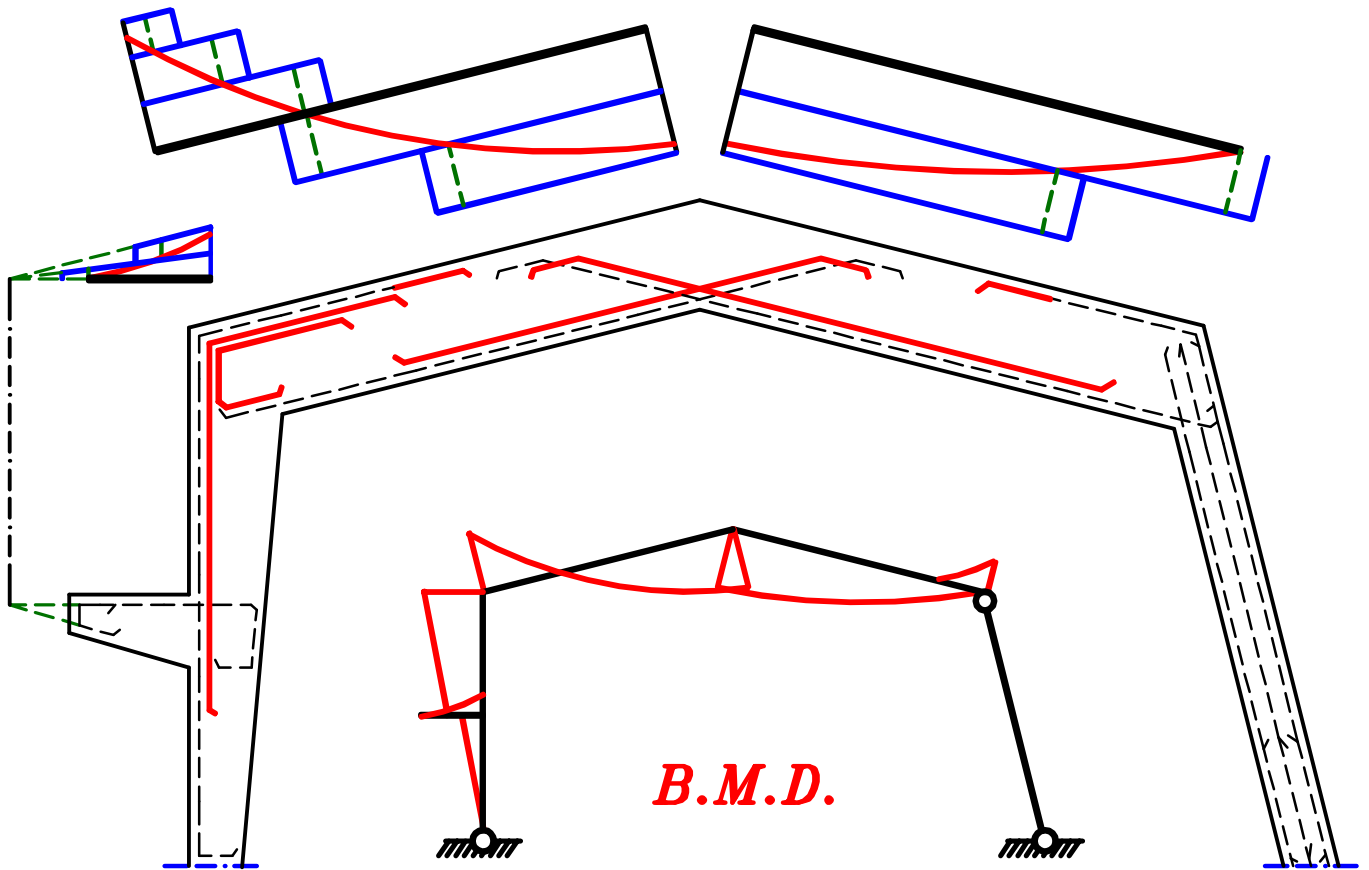
٣- الحديد السفلى يرسم من وش العمود الى وش العمود .



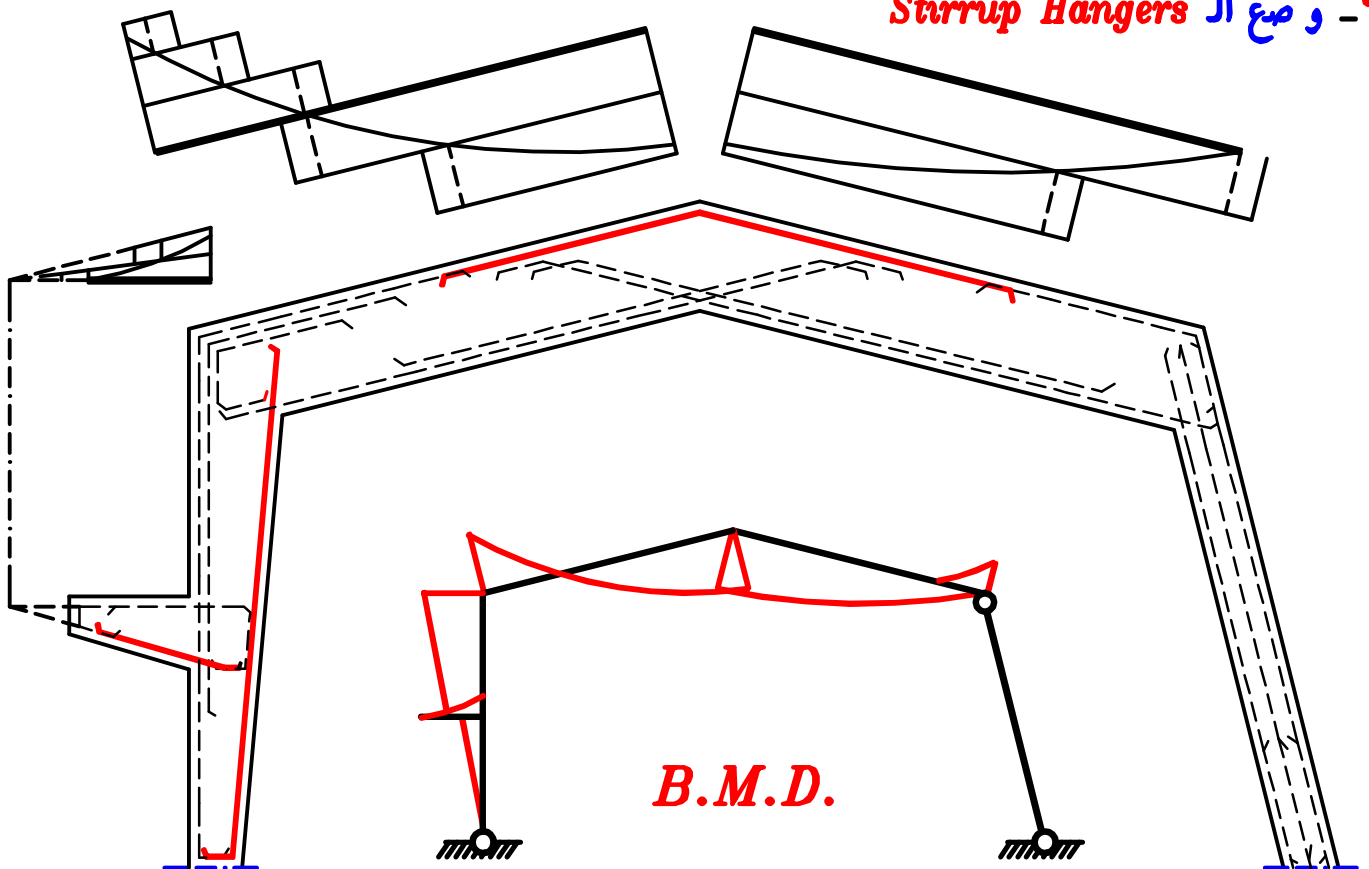
٤- رسم التسليح عند نهاية الاعمده (عمل أشاير أو لف الحديد فى العمود) و طرف ال *Cantilever* .



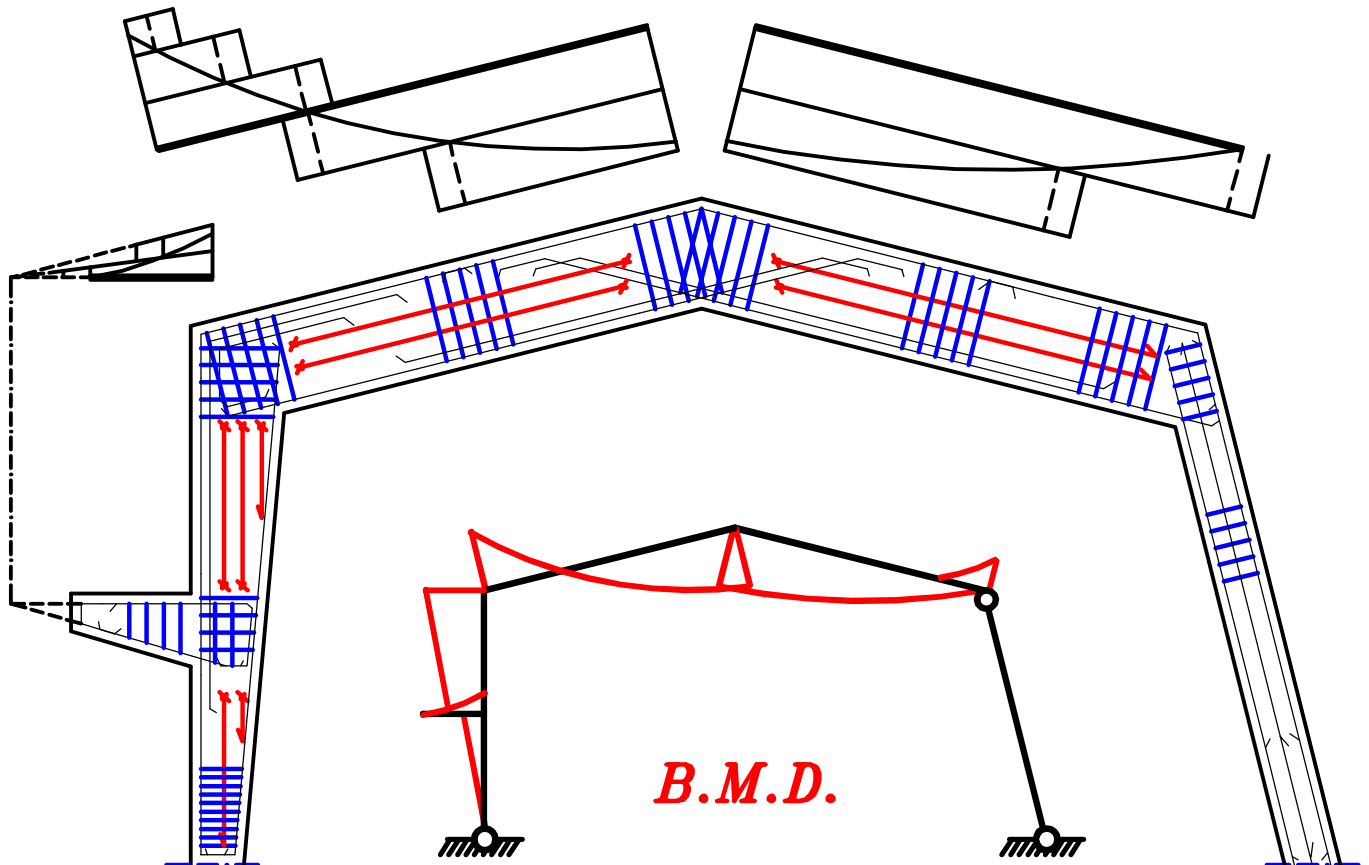
٥- رسم البلوكات مع مراعاة عدد الاسياخ و عدد الصفوف .



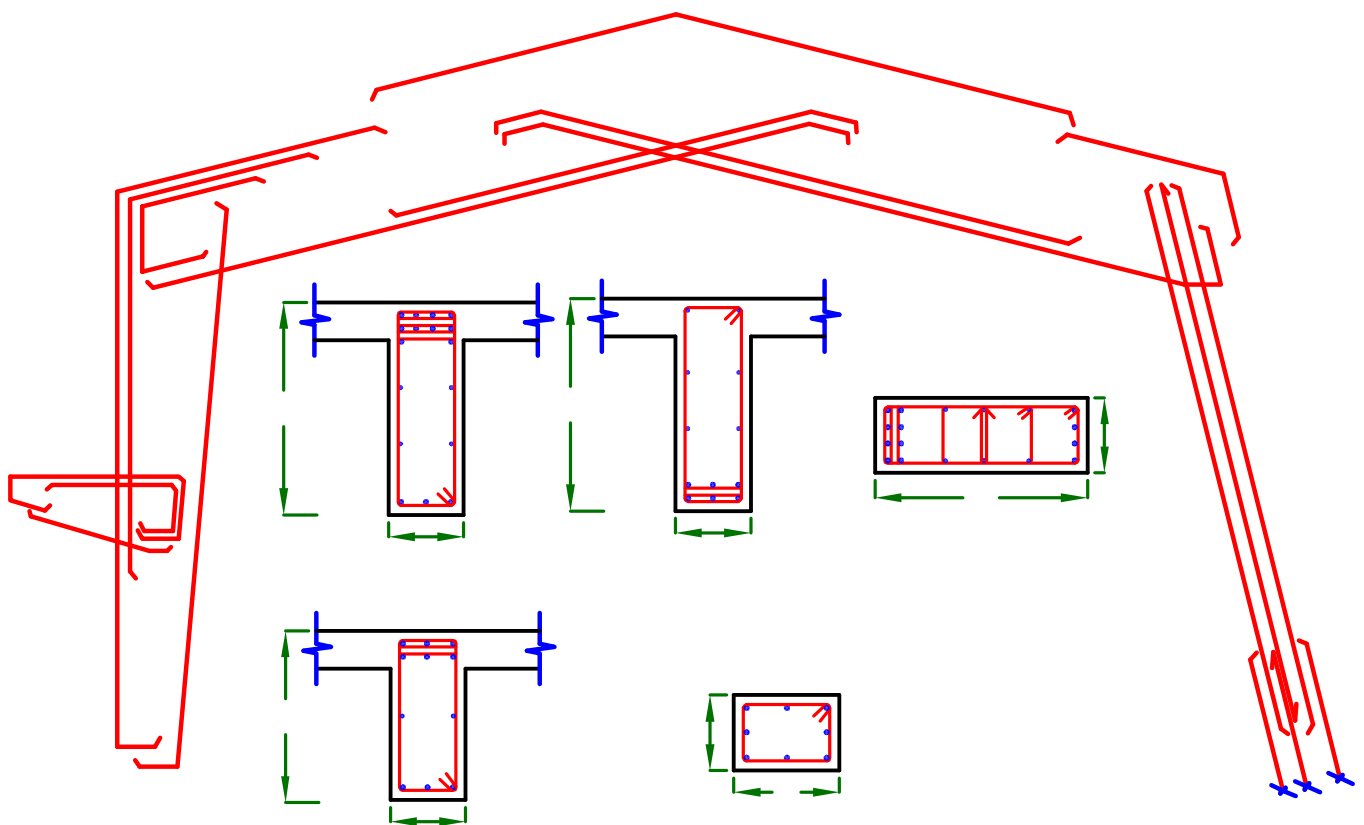
٦- وضع ال Stirrup Hangers

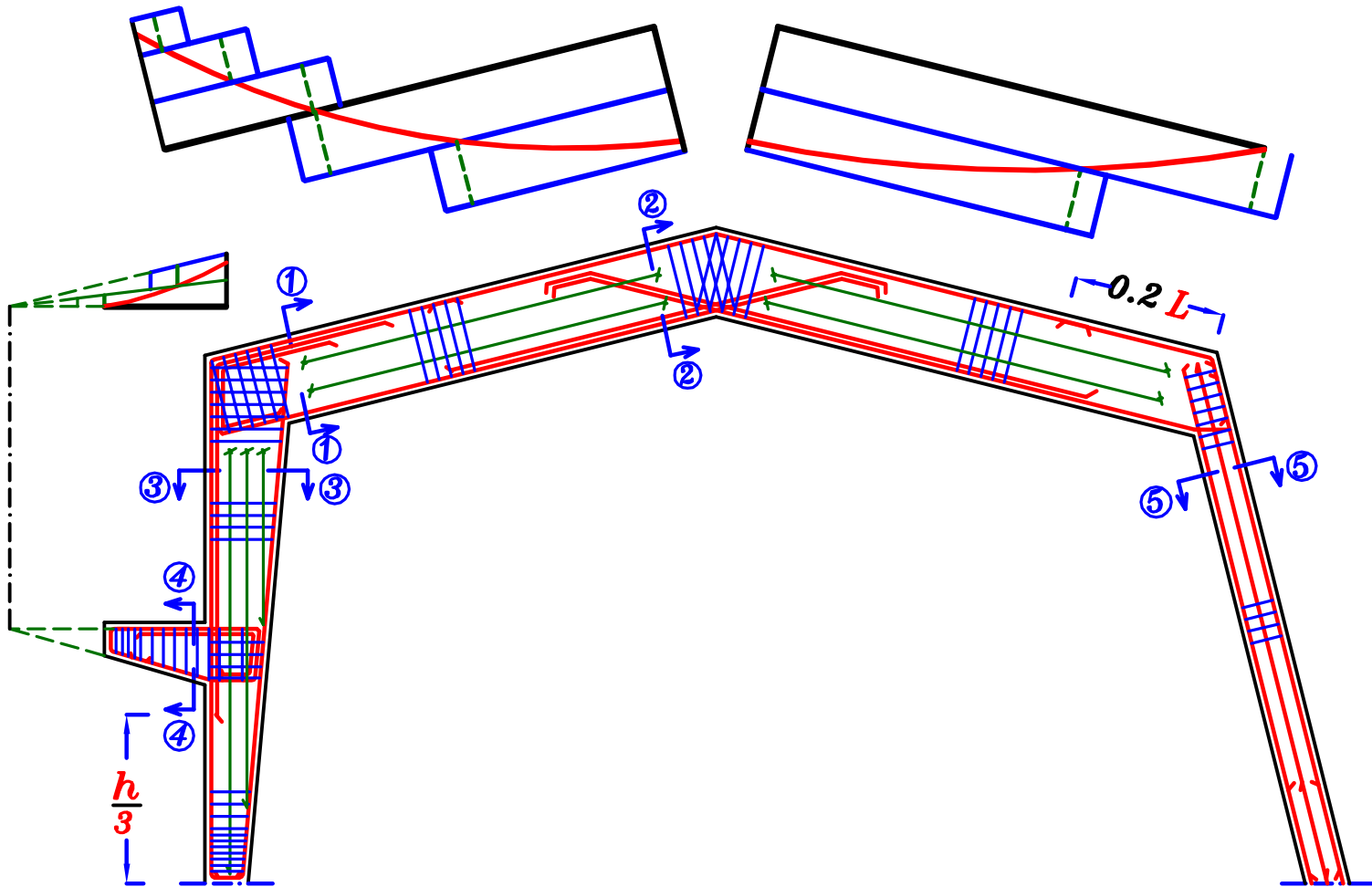


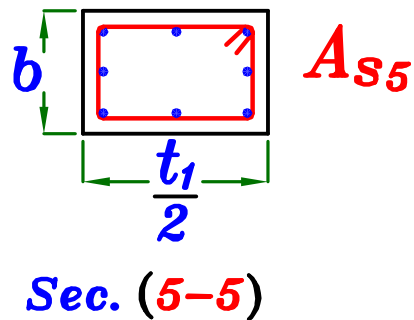
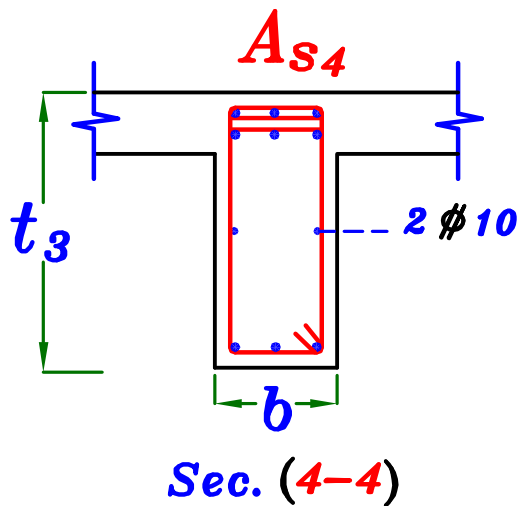
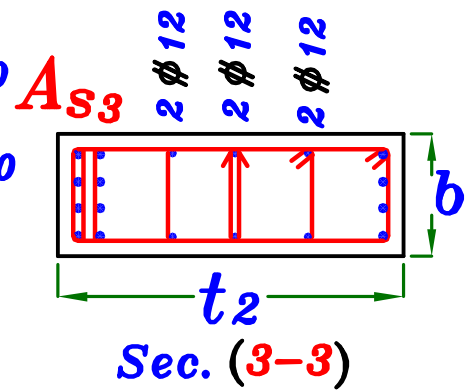
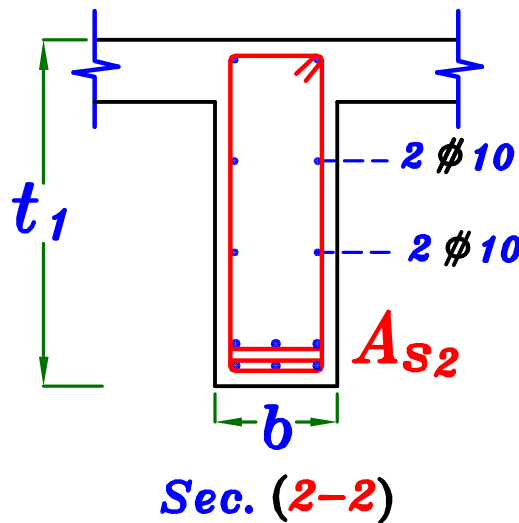
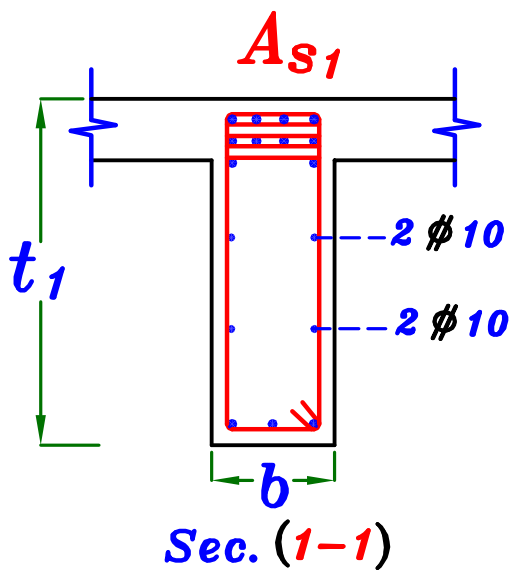
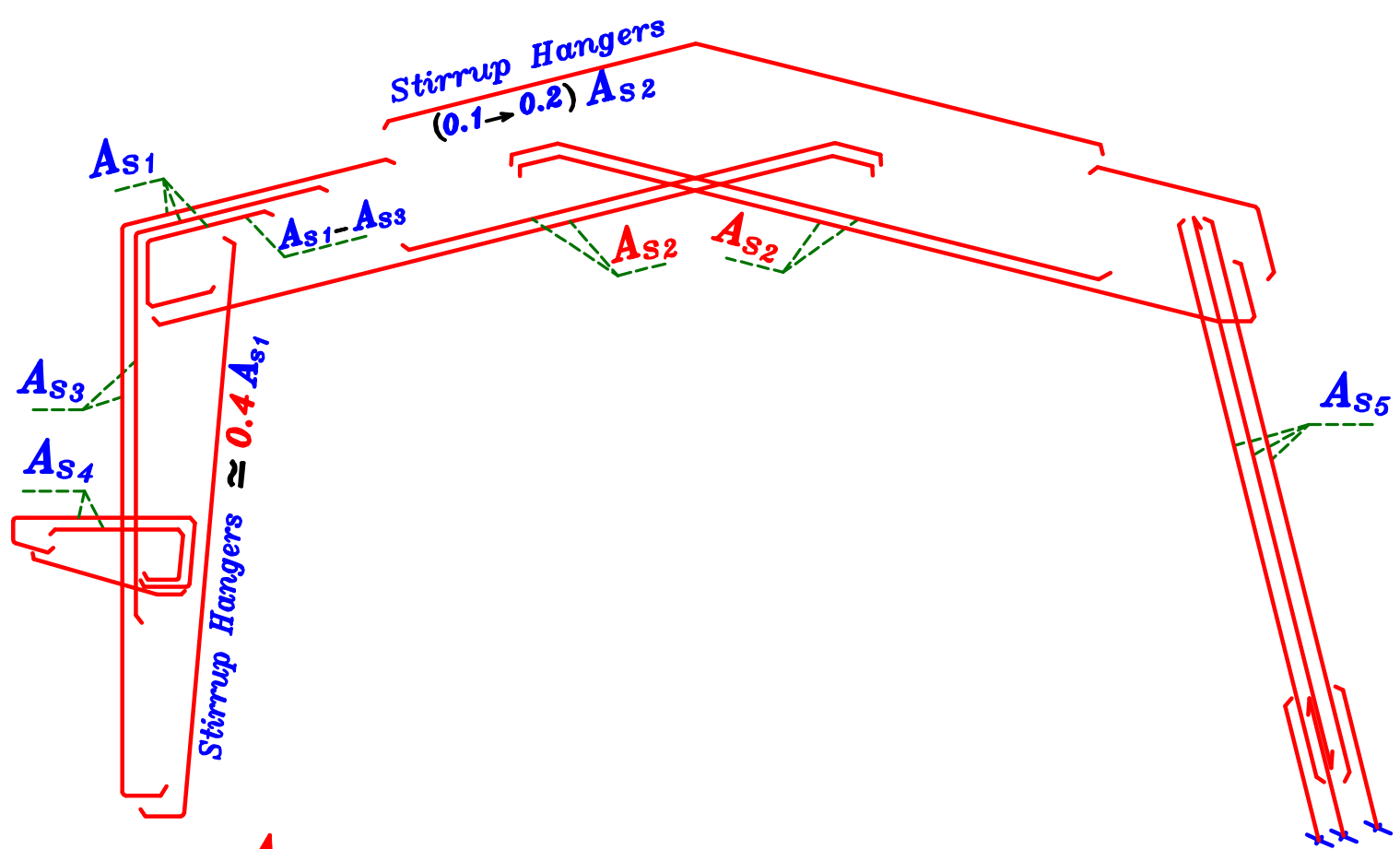
٧ - وضع الكانات و ال Shrinkage bars و ال Buckling bars



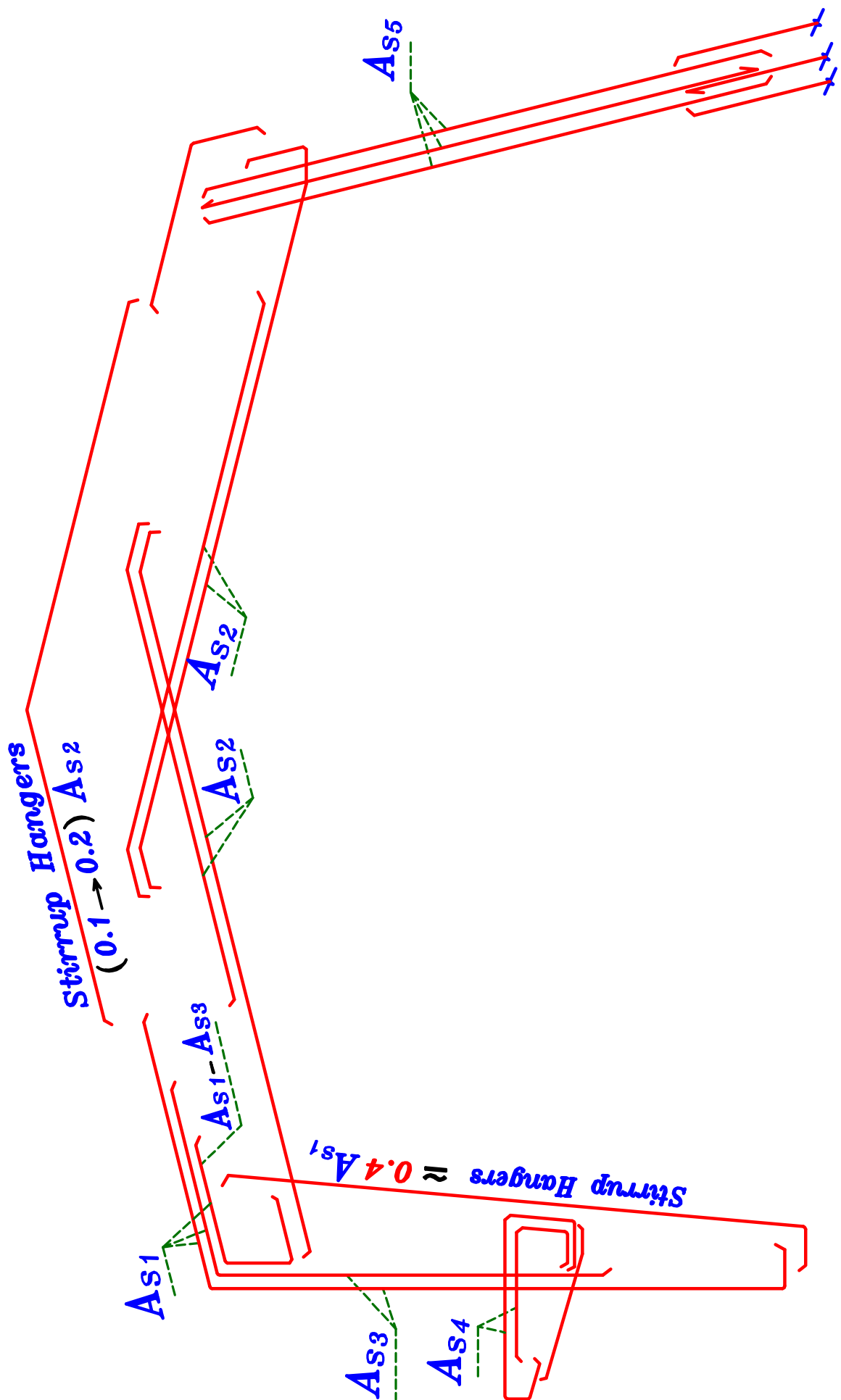
٨ - رسم التفريد و ال Sections











Examples on Frames.

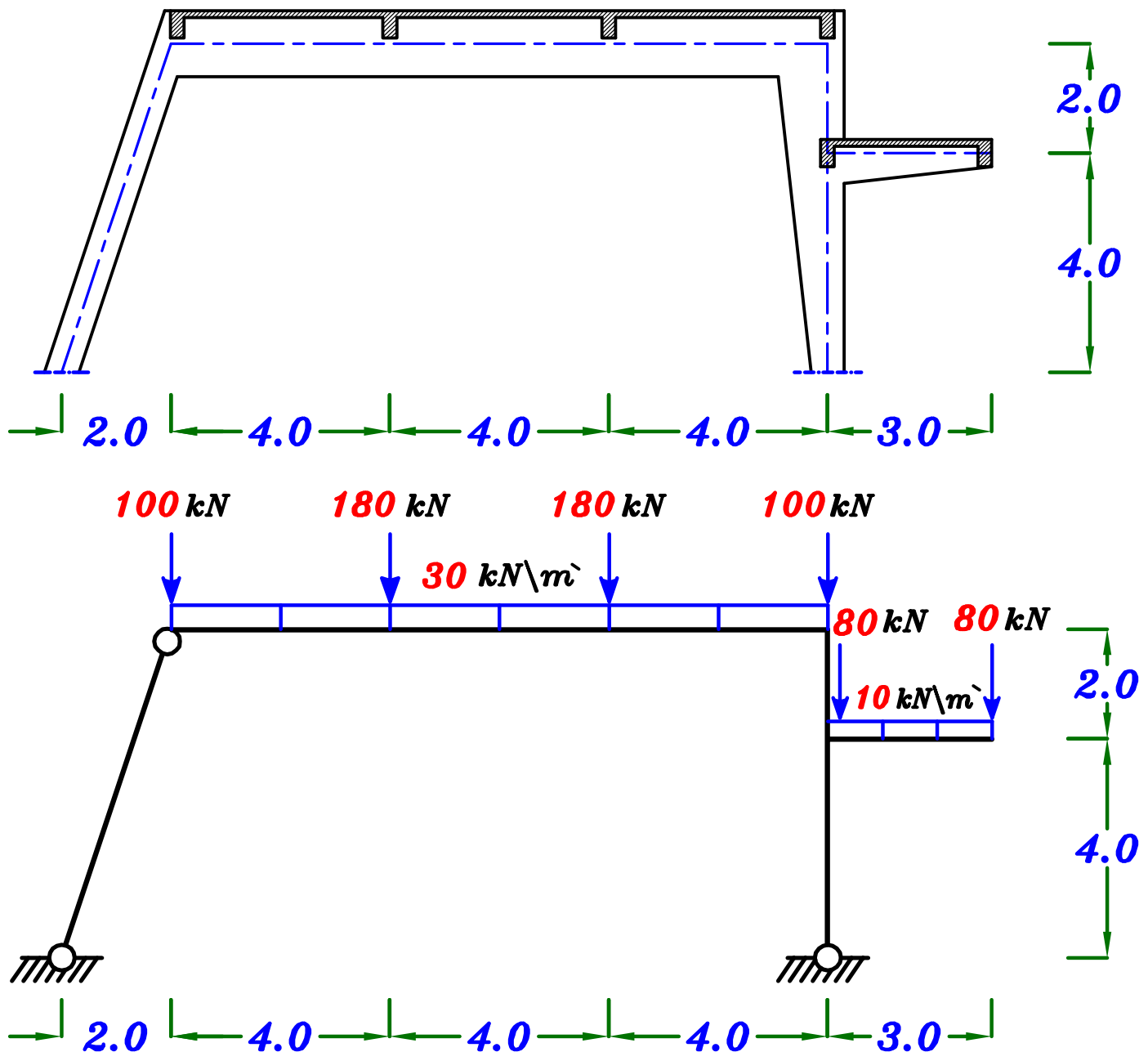
For the shown reinforcement concrete Frame of spacing **6.0 m** and subjected to the given working loads.

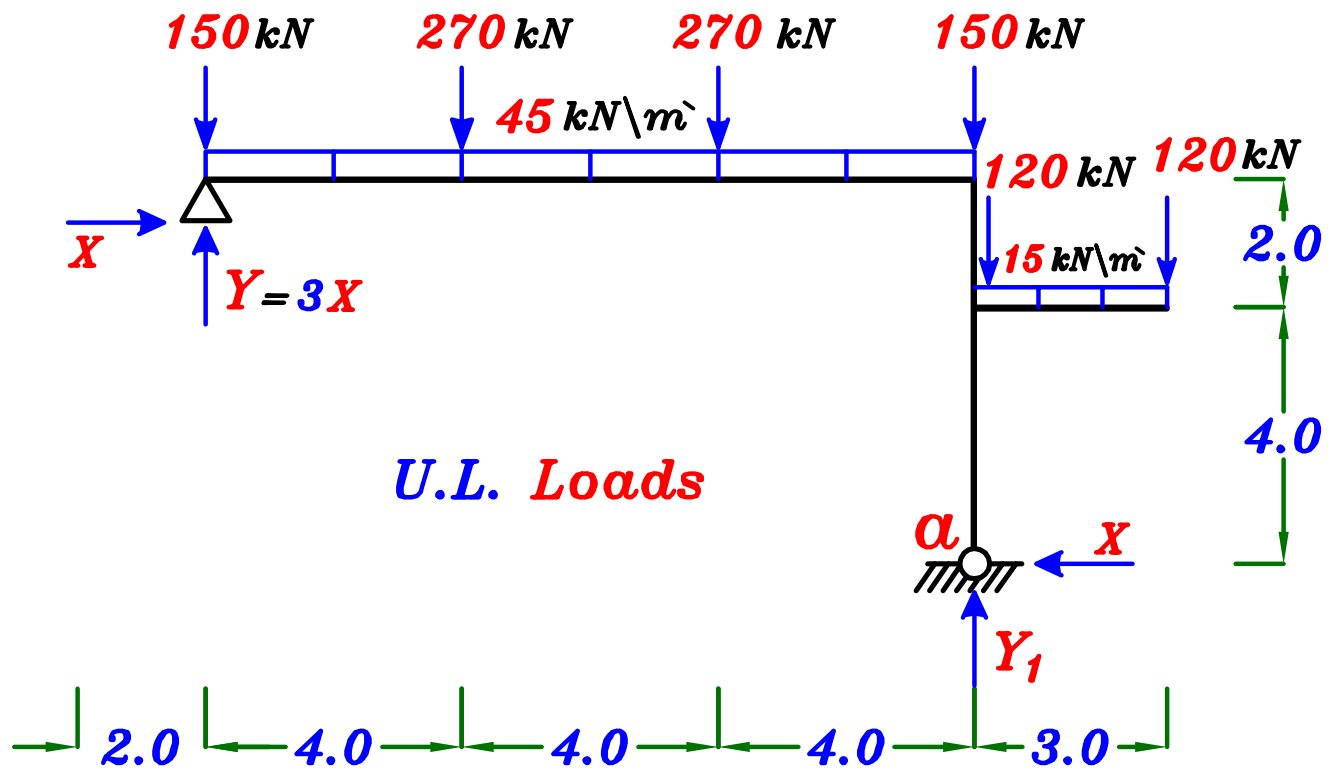
The Following is required :

- 1- Draw the internal Force diagrams (**B.M. , S.F. and N.F.**) For the Frame.
- 2- Design the critical sections of the Frame For Bending.
- 3- Draw details of reinforcement of the Frame using moment of resistance diagram.

$$F_{cu} = 25 \text{ N/mm}^2 , F_y = 360 \text{ N/mm}^2 , \text{Spacing} = 6.0 \text{ m}$$

$$b_{\text{(Beams)}} = 250 \text{ mm} , b_{\text{(Frame)}} = 350 \text{ mm} , t_s = 120 \text{ mm}$$

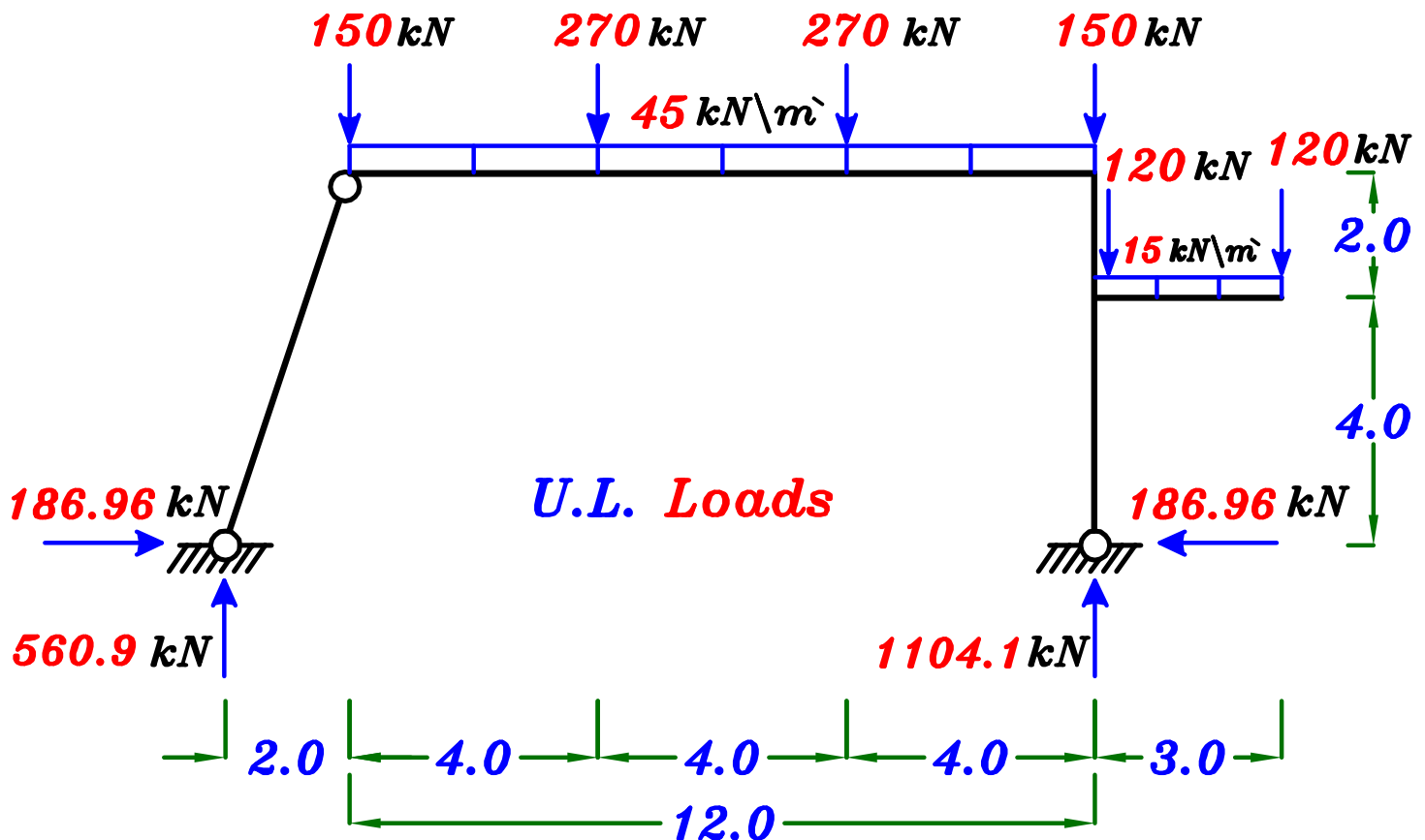


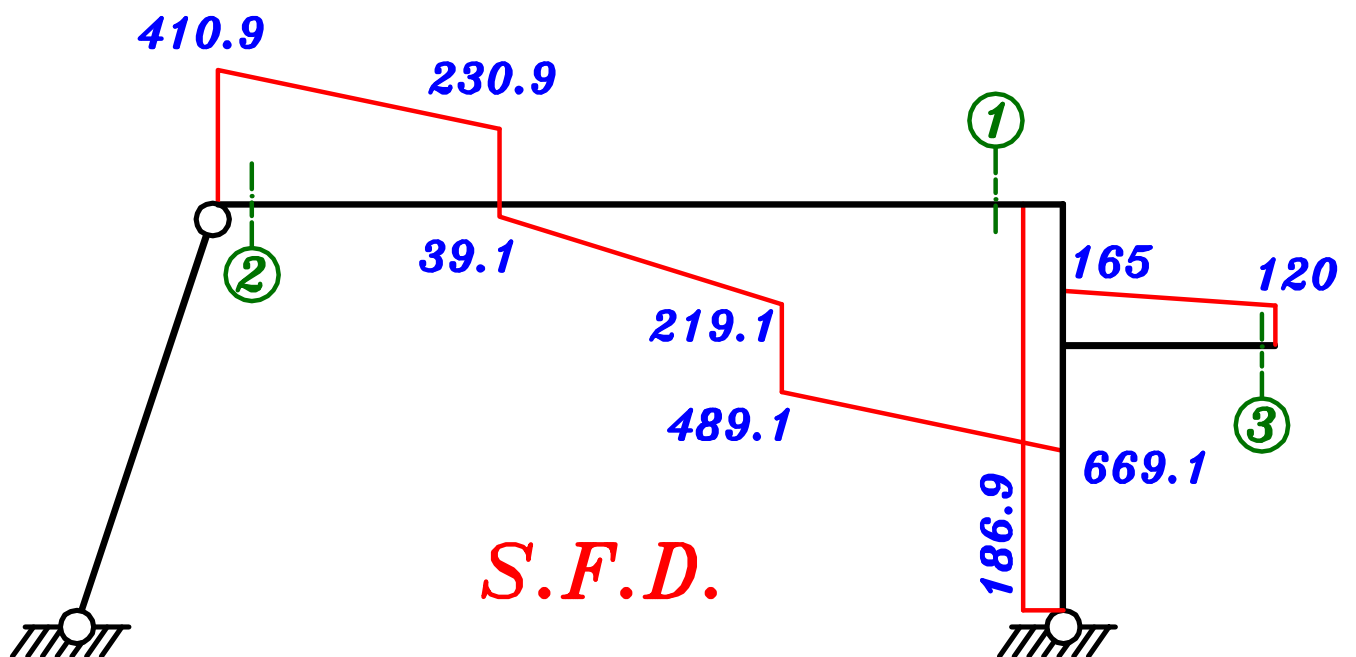
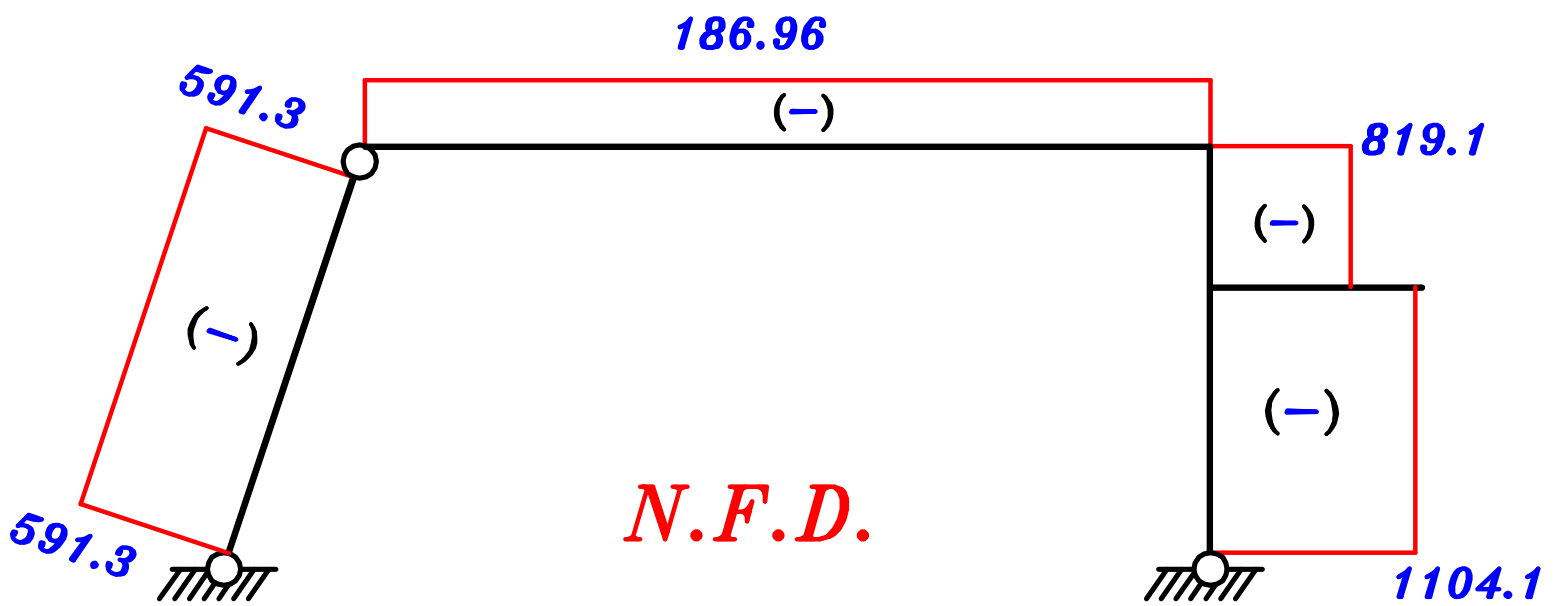
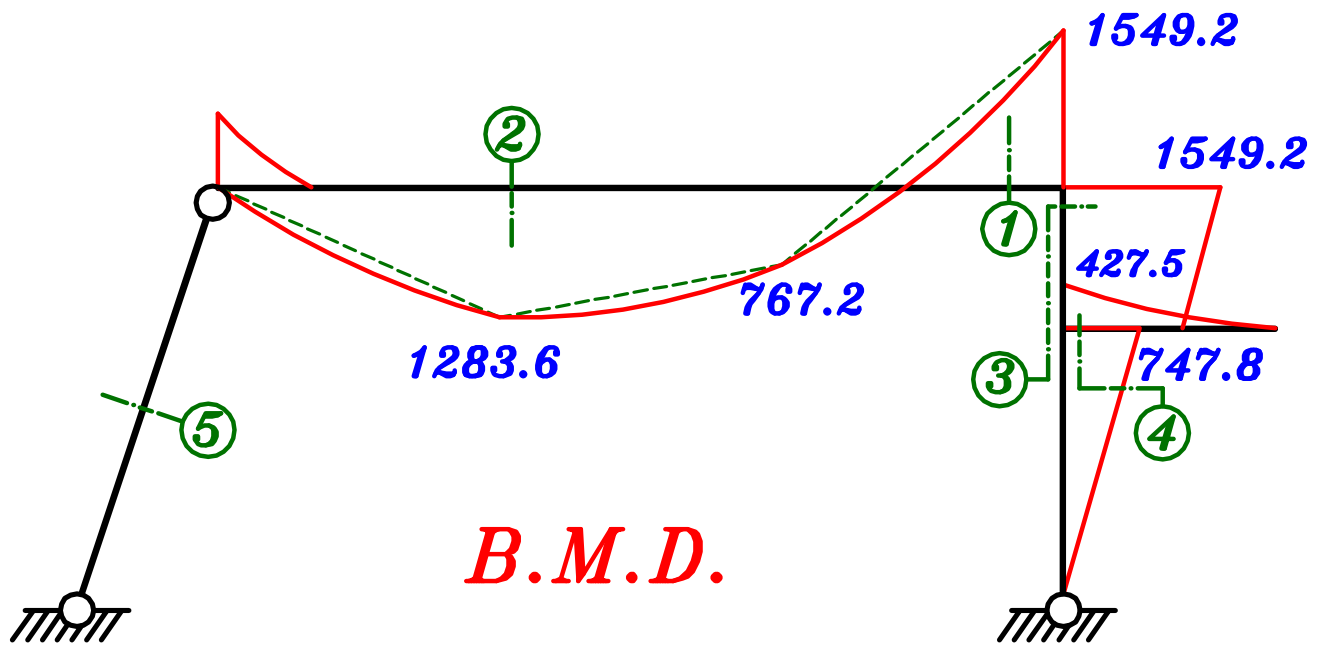


$$\therefore \sum M_{\alpha} = \text{Zero}$$

$$\therefore 3X(12) + X(6) - 45(12)(6) - 150(12) - 270(8) - 270(4) + 120(3) + 15(3)(1.5) = \text{Zero}$$

$$X = 186.96 \text{ kN} , Y = 3X = 560.9 \text{ kN} , Y_1 = 1104.1 \text{ kN}$$





Design of Sections.

Sec. ①

$$M = 1549.2 \text{ kN.m} , P = 186.96 \text{ kN} , b = 350 \text{ mm}$$

$$d_o = 3.5 \sqrt{\frac{1549.2 * 10^6}{25 * 350}} = 1472.7 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1472.7) = (1619 \rightarrow 1913) \text{ mm}$$

$$\text{Take } d = 1650 \text{ mm} , t = 1650 + 100 = 1750 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{186.96 * 10^3}{25 * 350 * 1750} = 0.012 < 0.04 \therefore (\text{neglect } P)$$

$$\therefore \text{The sec. still R-sec. } C_1 = 3.50 \longrightarrow J = 0.78$$

$$\therefore \text{Take } d = d_o = 1472.7 \text{ mm}$$

$$\therefore \text{Take } d = 1500 \text{ mm} , t = 1600 \text{ mm}$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1549.2 * 10^6}{0.780 * 360 * 1472.7} = 3746.2 \text{ mm}^2$$

$$\text{— Check } A_{s_{min.}} \quad A_{s_{req.}} = 3746.2 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1500 = 1640.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 3746.2 \text{ mm}^2 \quad (10 \phi 22)$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{22 + 25} = 6.91 = 6.0 \text{ bars}$$

Sec. ② $M = 1283.6 \text{ kN.m}$, $P = 186.96 \text{ kN}$, $b = 350 \text{ mm}$

$d = 1500 \text{ mm}$ (the same depth of sec. ①)

Check $\frac{P}{F_{cu} b t} = \frac{186.96 * 10^3}{25 * 350 * 1500} = 0.014 < 0.04 \therefore (\text{neglect } P)$

\therefore The sec. will be T-sec. \therefore use B

$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = \text{Spacing} = 6.0 \text{ m} = 6000 \text{ mm} \\ 16 t_s + b = 16 * 120 + 350 = 2270 \text{ mm} \\ K \frac{L}{5} + b = 0.8 * \frac{12000}{5} + 350 = 2270 \text{ mm} \end{array} \right\} \quad \begin{array}{l} K = 0.8 \\ \text{Diagram of a T-section with a parabolic top flange of width 12000 mm and depth 120 mm.} \\ \boxed{B = 2270 \text{ mm}} \end{array}$$

$$\therefore d = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} B}} \therefore 1500 = c_1 \sqrt{\frac{1283.6 * 10^6}{25 * 2270}} \rightarrow c_1 = 9.97 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{u.L.}}{J F_y d} = \frac{1283.6 * 10^6}{0.826 * 360 * 1500} = 2877.7 \text{ mm}^2$$

– Check $A_{s_{min.}}$ $A_{s_{req.}} = 2877.7 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1500 = 1640.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2877.7 \text{ mm}^2 \quad \boxed{8 \phi 22}$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 2877.7 \quad \boxed{4 \phi 12}$$

Sec. ③ R-Sec. $M = 1549.2 \text{ kN.m}$, $P = 819.1 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{1549.2 \cdot 10^6}{25 \cdot 350}} = 1472.7 \text{ mm (as R-Sec.)}$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1472.7) = (1619 \rightarrow 1913) \text{ mm}$$

Take $d = 1650 \text{ mm}$, $t = 1650 + 100 = 1750 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{819.1 \cdot 10^3}{25 \cdot 350 \cdot 1750} = 0.053 > 0.04$ (Don't neglect P)

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{1549.2}{819.1} = 1.89 \text{ m} \quad \therefore \frac{e}{t} = \frac{1.89}{1.75} = 1.08 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.89 + \frac{1.75}{2} - 0.10 = 2.665 \text{ m}$$

$$M_s = P \cdot e_s = 819.1 \cdot 2.665 = 2182.9 \text{ kN.m}$$

$$\therefore 1650 = C_1 \sqrt{\frac{2182.9 \cdot 10^6}{25 \cdot 350}} \rightarrow C_1 = 3.30 \rightarrow J = 0.767$$

$$A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \backslash \gamma_s)} = \frac{2182.9 \cdot 10^6}{0.767 \cdot 360 \cdot 1650} - \frac{819.1 \cdot 10^3}{(360 \backslash 1.15)} = 2174.7 \text{ mm}^2$$

– Check $A_{s_{min.}}$ $A_{s_{req.}} = 2174.7 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 350 \cdot 1650 = 1084.7 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 2174.7 \text{ mm}^2$ **6 ϕ 22**

Stirrup Hangers $\approx 0.4 A_s \approx 0.4 (2174.7) = 870 \text{ mm}^2$ **3 ϕ 22**

Sec. ④ $M = 427.5 \text{ kN.m}$, $b = 350 \text{ mm}$

\therefore The sec. is R-sec. $C_1 = 3.50 \rightarrow J = 0.78$

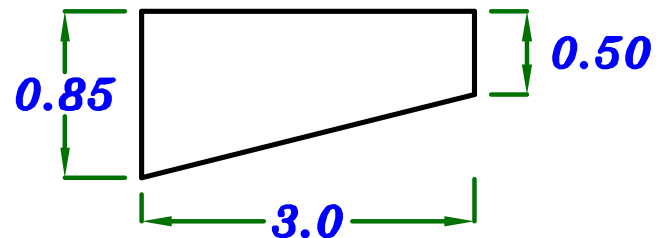
$$d = 3.5 \sqrt{\frac{427.5 * 10^6}{25 * 350}} = 773.6 \text{ mm (as R-Sec.)}$$

\therefore Take $d = 800 \text{ mm}$, $t = 850 \text{ mm}$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{427.5 * 10^6}{0.780 * 360 * 773.6} = 1968 \text{ mm}^2$$

$6 \phi 22$

$$Y = \left\{ \begin{array}{l} \frac{t}{2} = \frac{850}{2} = 425 \text{ mm} \\ t_b = \frac{\text{spacing}}{12} = \frac{6000}{12} = 500 \text{ mm} \\ t - \frac{L_c}{3} = 850 - \frac{3000}{3} = -150 \text{ mm} \end{array} \right\} Y = 500 \text{ mm}$$



Sec. ⑤

$(350 * 800)$ Axially Loaded Column. $P = 591.3 \text{ kN}$

$$\therefore P_{U.L.} = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

$$\therefore 591.3 * 10^3 = 0.35 (350 * 800) (25) + 0.67 A_s (360)$$

$$\therefore A_s = -7706 \text{ mm}^2 = (-Ve) \text{ Value}$$

$$\therefore A_s = A_{s_{min}} = \frac{0.8}{100} * 350 * 800 = 2240 \text{ mm}^2$$

$10 \phi 18$

Check Shear.

– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{25}{1.5}} = 2.85 \text{ N/mm}^2$$

Sec. ① $Q = 669.1 \text{ kN}$

$$q_u = \frac{Q}{b d} = \frac{669.1 * 10^3}{350 * 1500} = 1.27 \text{ N/mm}^2$$

$\therefore q_{cu} < q_u < q_{max.} \therefore$ We need Stirrups more Than $5 \phi 8 \text{ m}$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.27 - \frac{0.98}{2} = \frac{2 * 50.3 (240 \setminus 1.15)}{350 * S} \rightarrow S = 76.9 \text{ mm} < 100 \text{ mm}$$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

$$1.27 - \frac{0.98}{2} = \frac{2 * 78.5 (240 \setminus 1.15)}{350 * S} \rightarrow S = 120 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups m} = \frac{1000}{S} = \frac{1000}{120} = 8.33 = 9.0$$

\therefore Use Stirrups $9 \phi 10 \text{ m}$ 2 branches

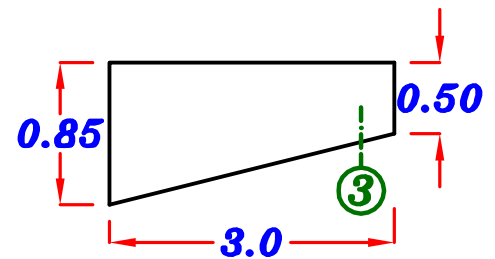
Sec. ② $Q = 410.9 \text{ kN}$

$$q_u = \frac{Q}{b d} = \frac{410.9 * 10^3}{350 * 1500} = 0.78 \text{ N/mm}^2$$

$\therefore q_u < q_{cu} \longrightarrow \text{Use min. stirrups } \boxed{5 \phi 8 \text{ / m}}$

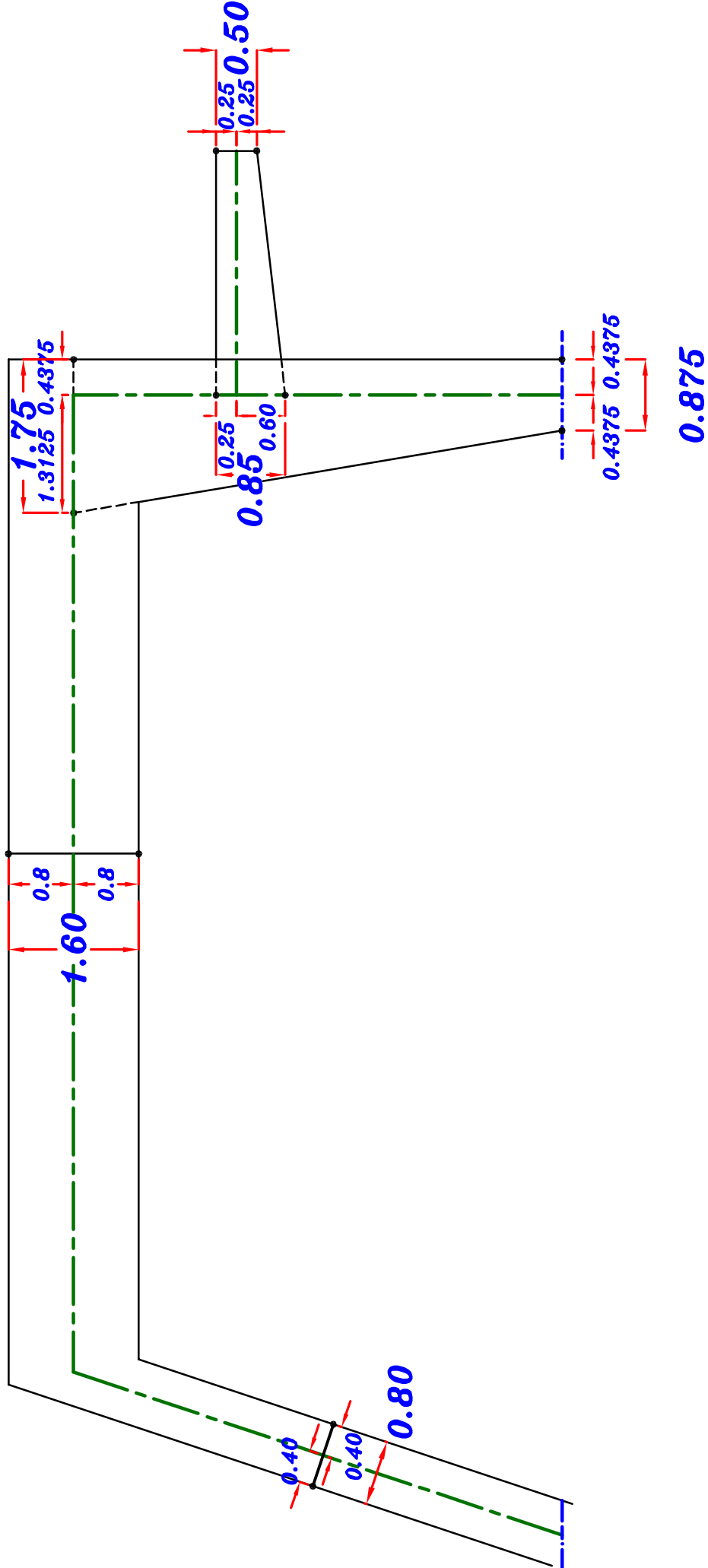
Sec. ③

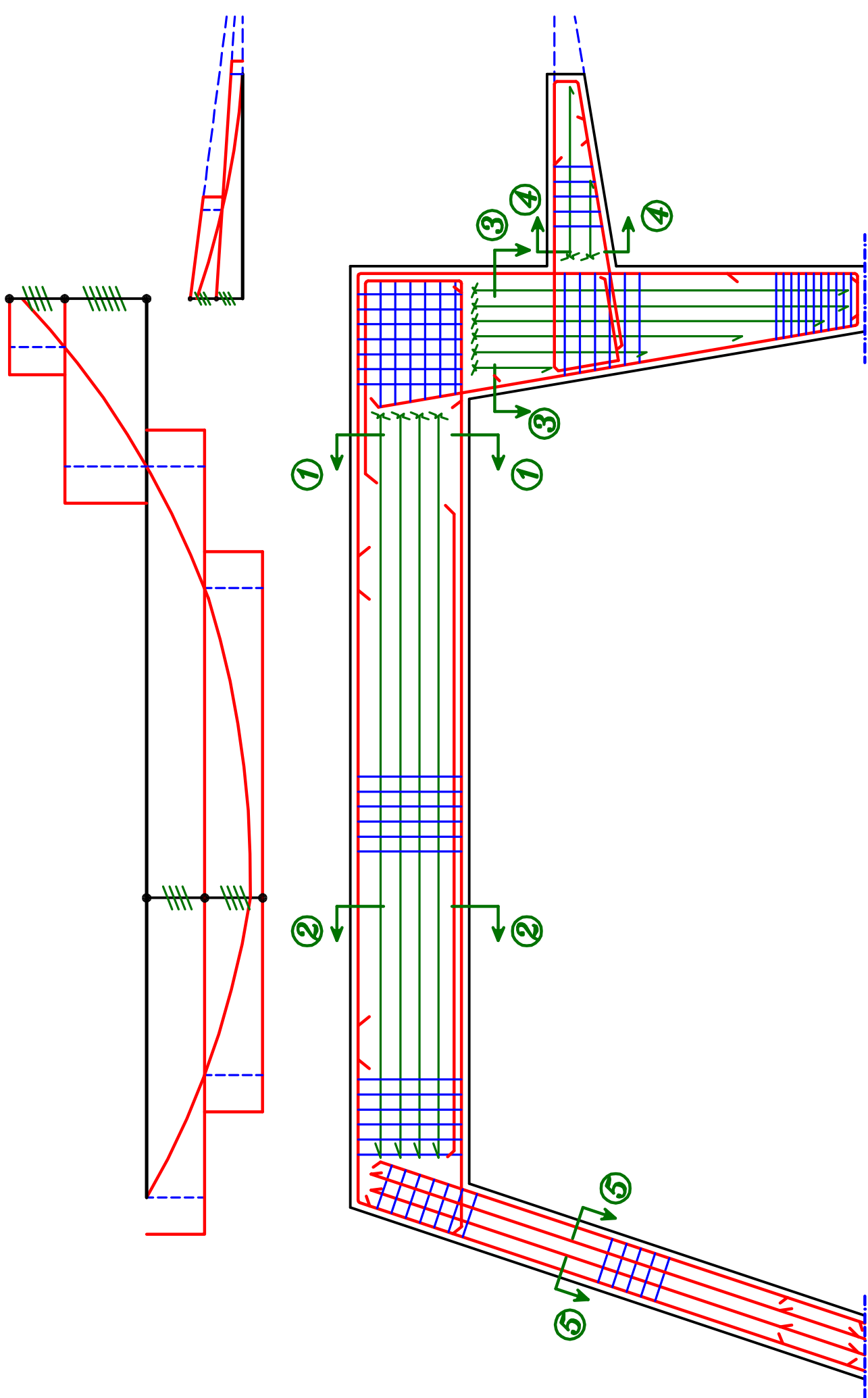
$Q = 120 \text{ kN} \quad \tan \beta = 0.116$

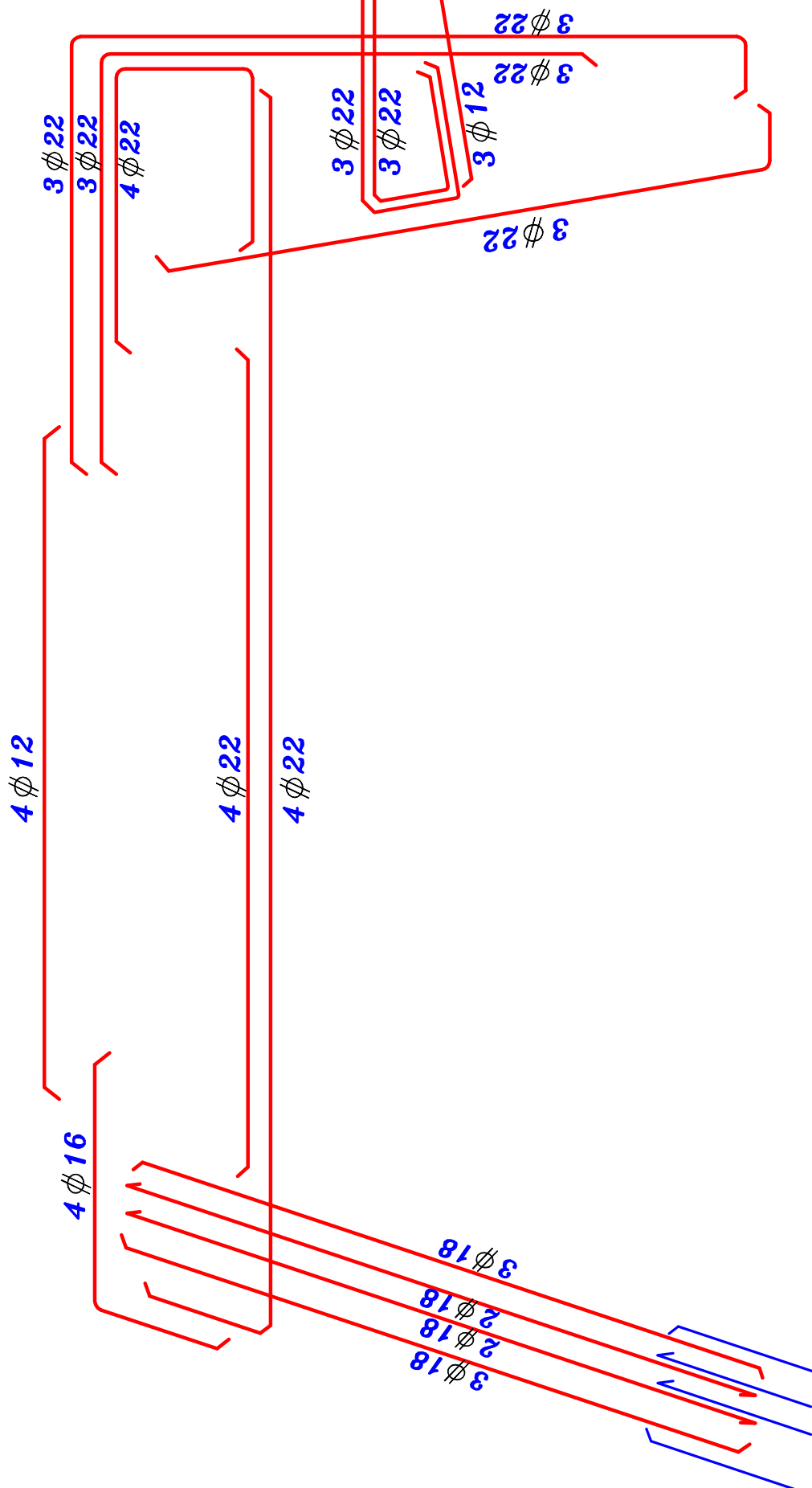


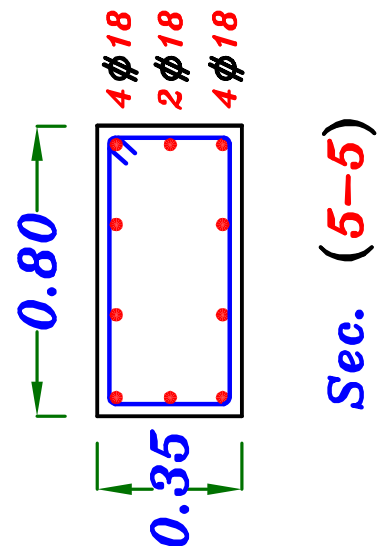
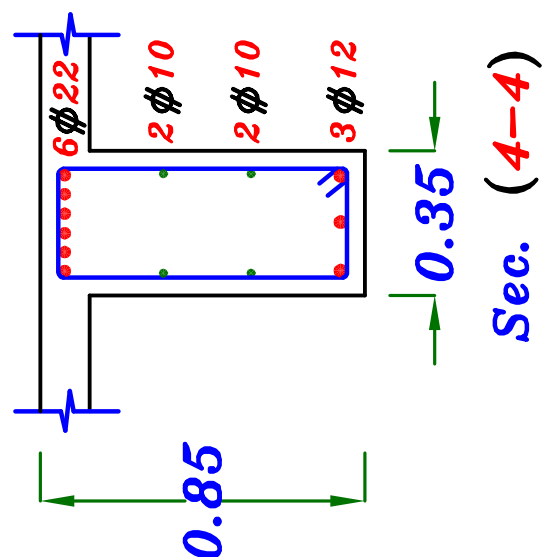
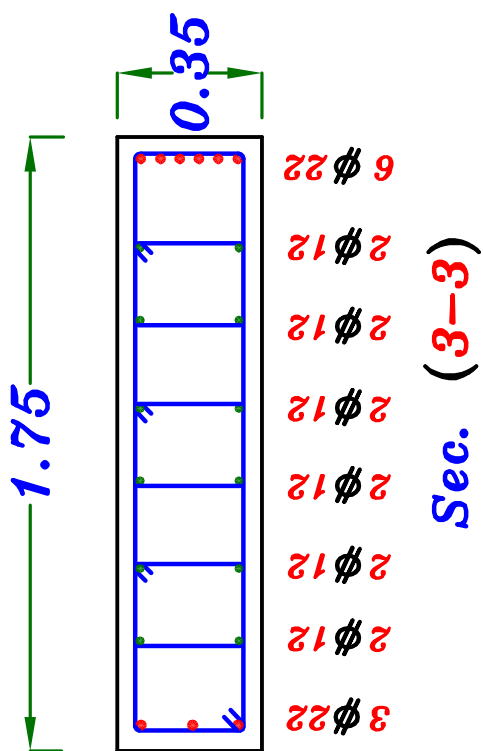
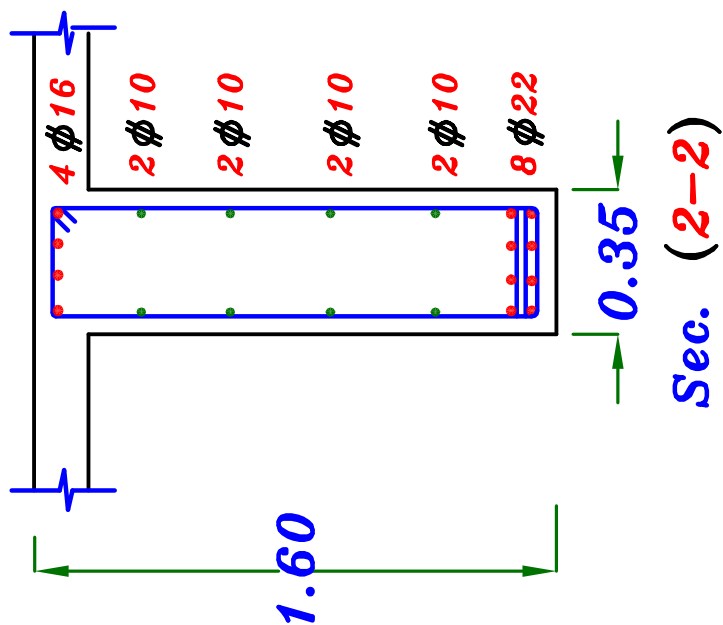
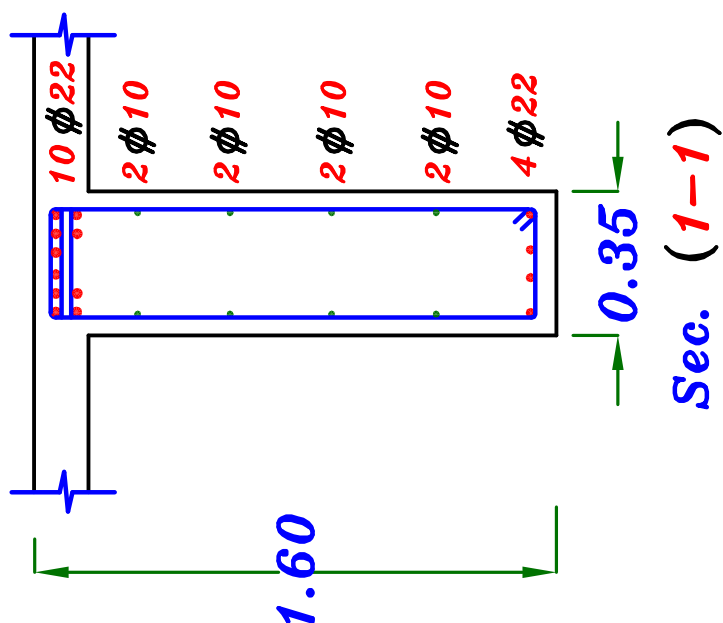
$$\begin{aligned} \therefore q_u &= \frac{Q}{b d} - \frac{M \tan \beta}{b d^2} \\ &= \frac{120 * 10^3}{350 * 450} - \text{ZERO} = 0.761 \text{ N/mm}^2 \end{aligned}$$

$\therefore q_u < q_{cu} \longrightarrow \text{Use min. stirrups } \boxed{5 \phi 8 \text{ / m}}$

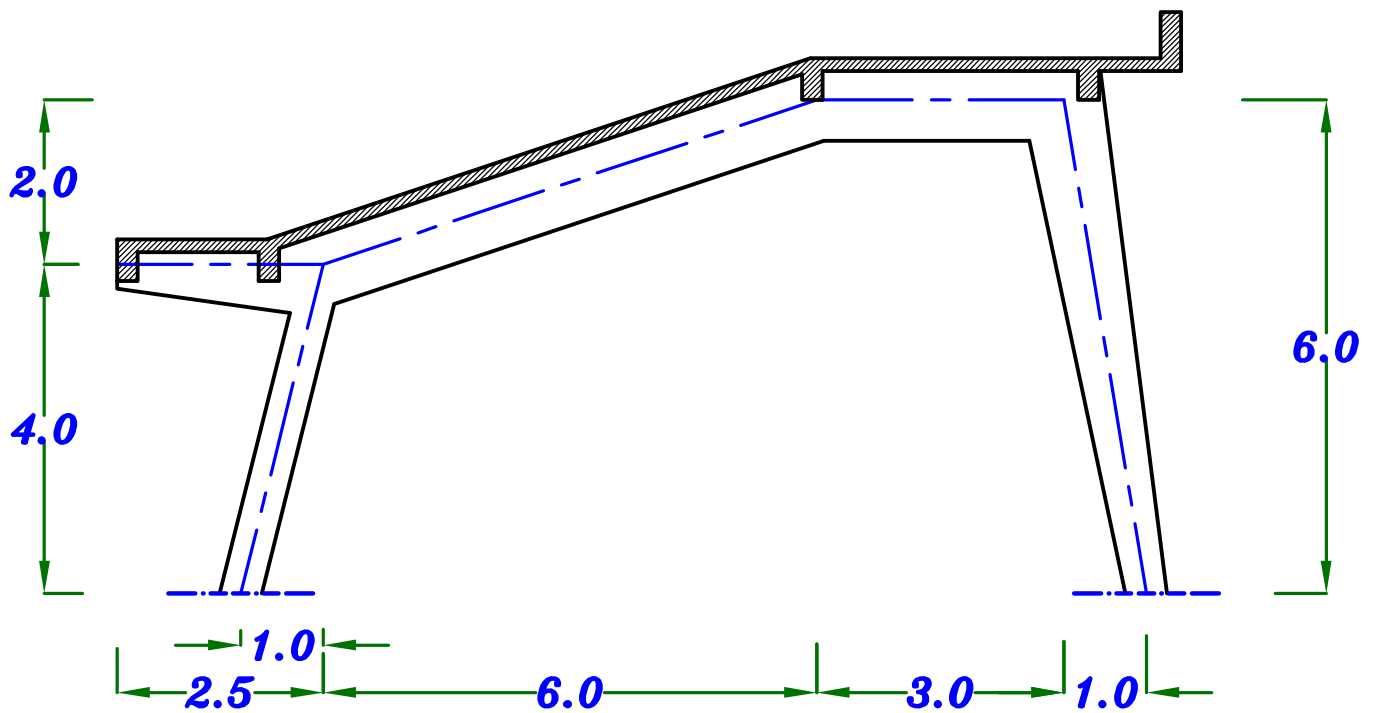








Example.



Data.

$$F_{cu} = 25 \text{ N/mm}^2$$

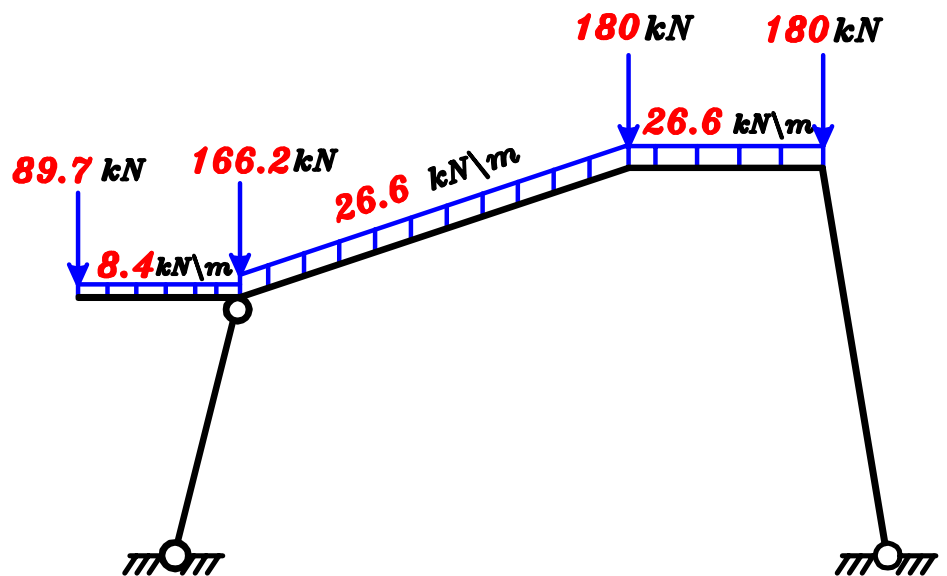
$$F_y = 360 \text{ N/mm}^2$$

$$b_{(Beams)} = 250 \text{ mm}$$

$$b_{(Frame)} = 350 \text{ mm}$$

$$t_s = 140 \text{ mm}$$

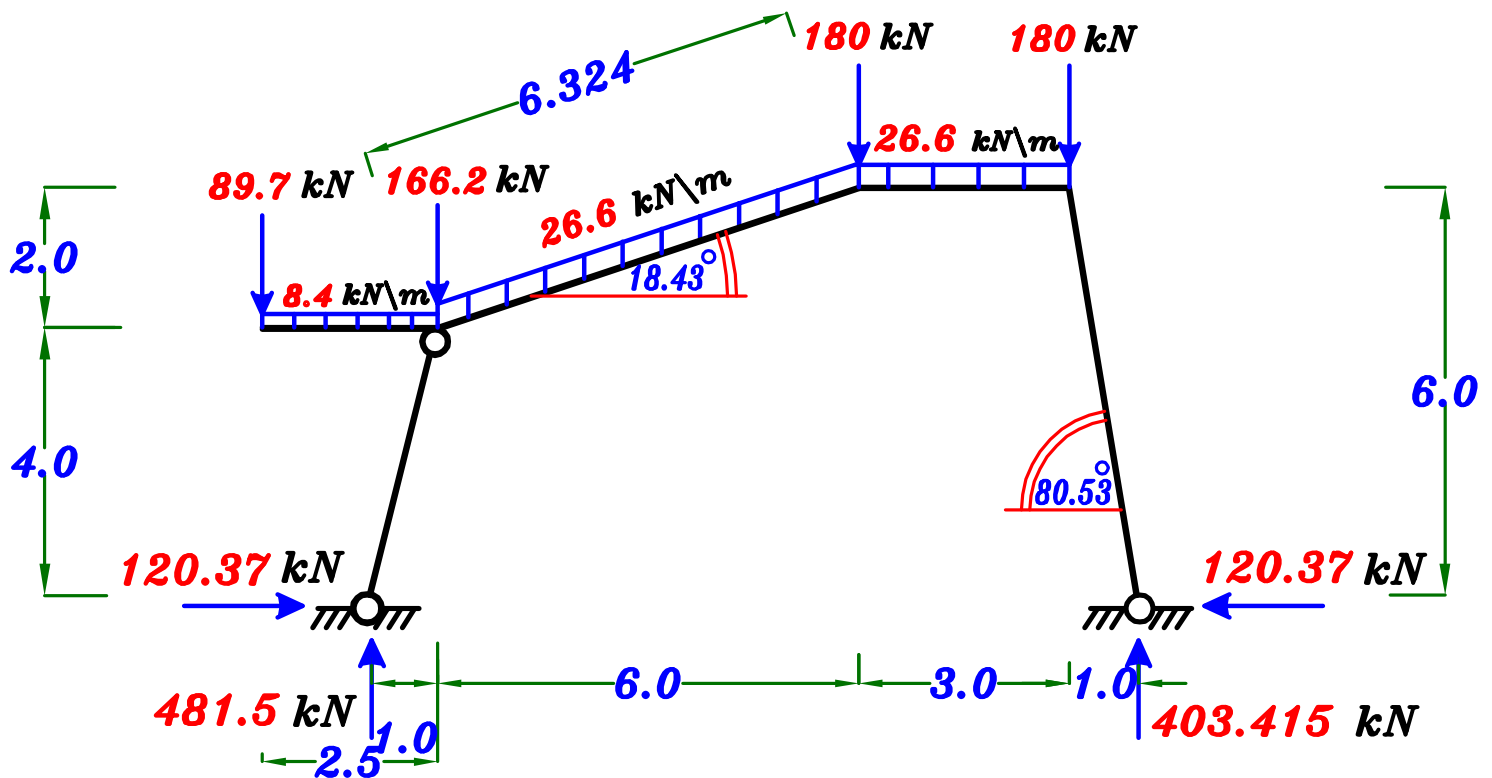
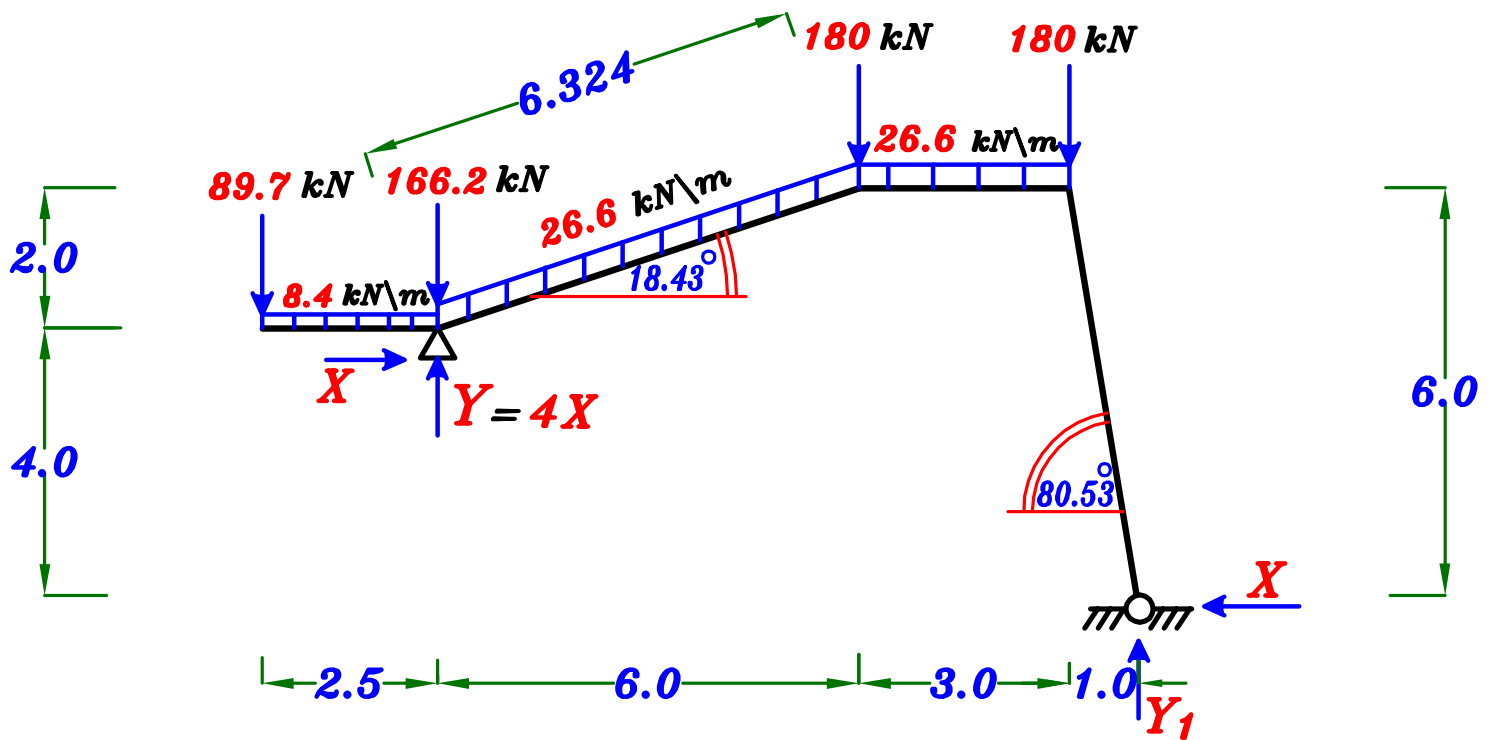
$$\text{Spacing} = 6.0 \text{ m}$$



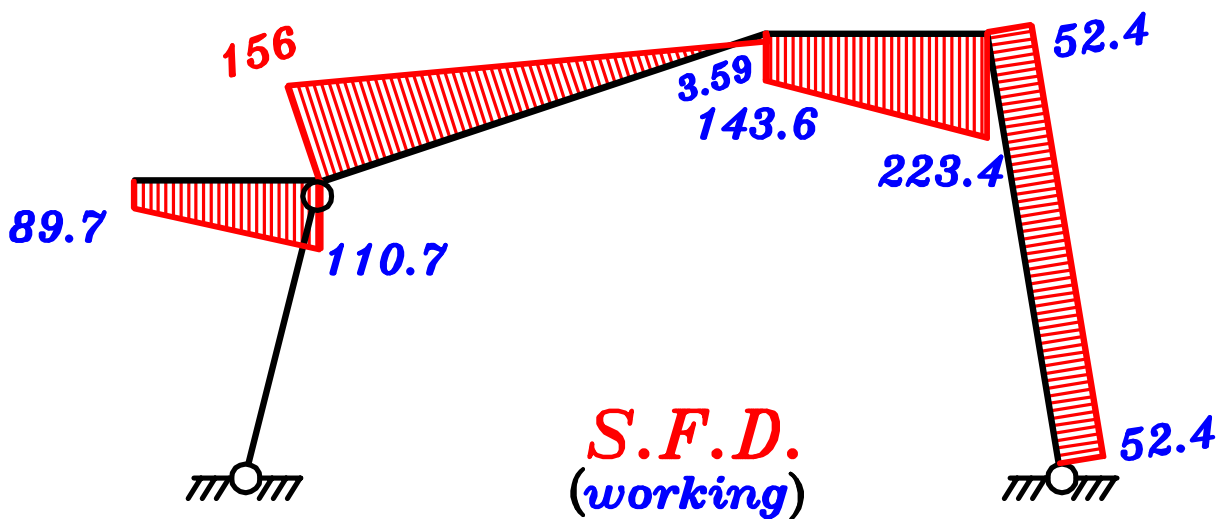
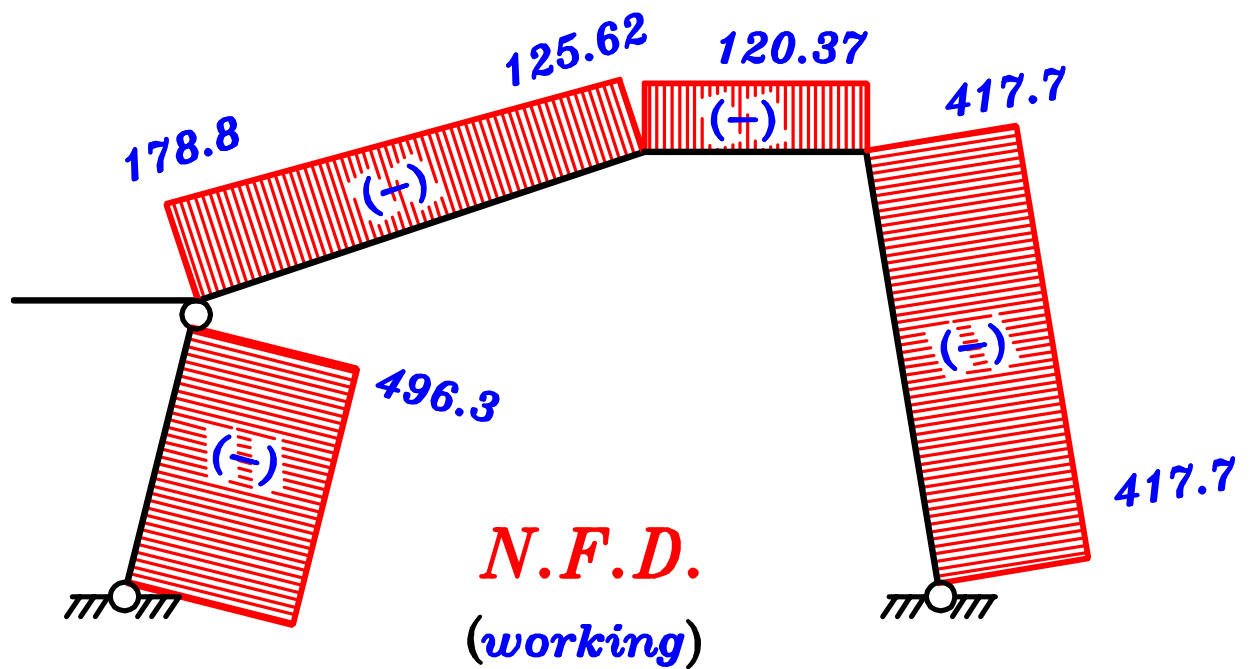
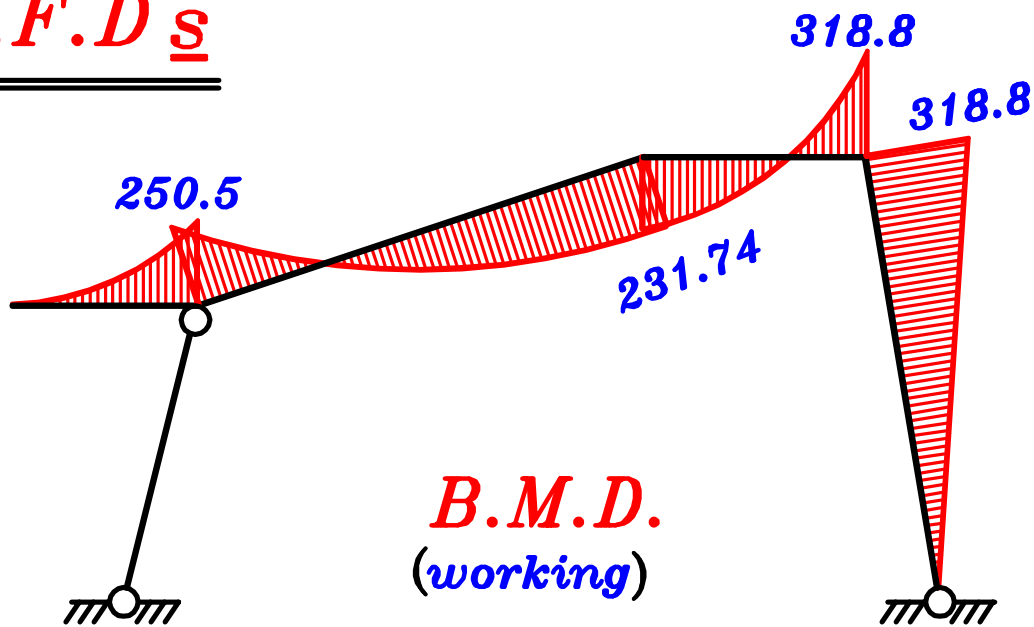
Req.

- ① Draw the Internal Forces Diagrams For the Frame due to the given working Loads. (**Case of total Load is only required**)
- ② Design the critical sections of the Frame.
using U.L. design method in bending and shear.
- ③ Draw Details of RFT. For Frame. **in elevation to scale 1:50**
and cross-section to scale 1:10
making curtailment of steel using Moment of Resistance Method.

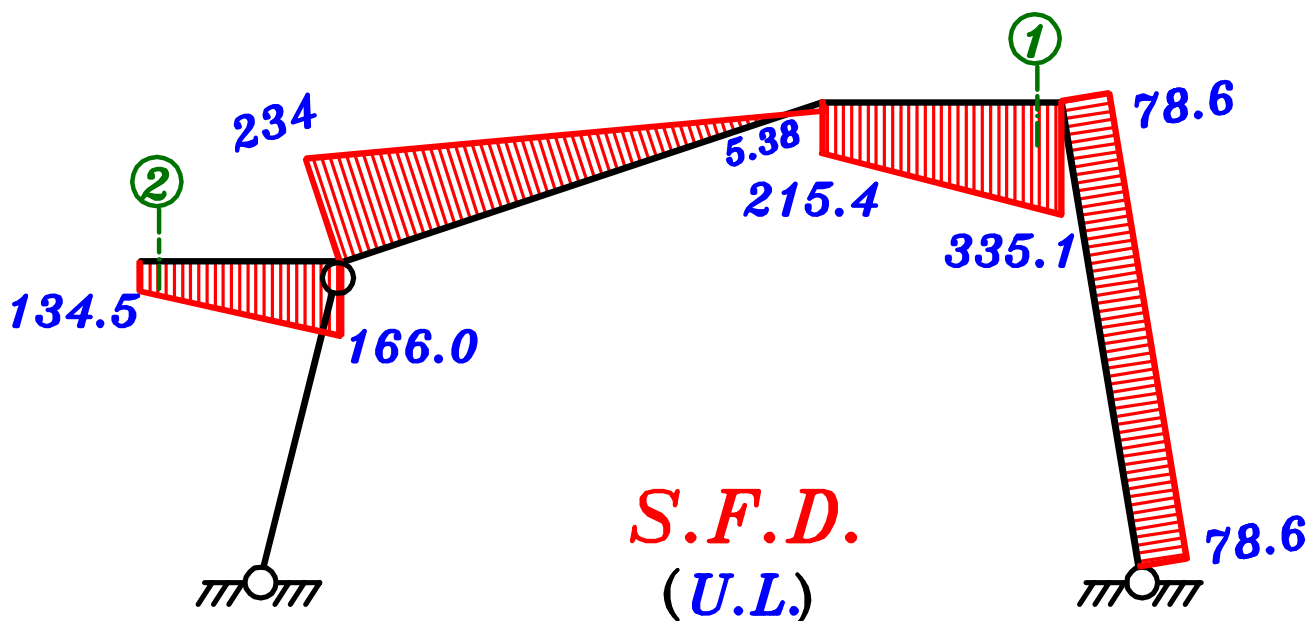
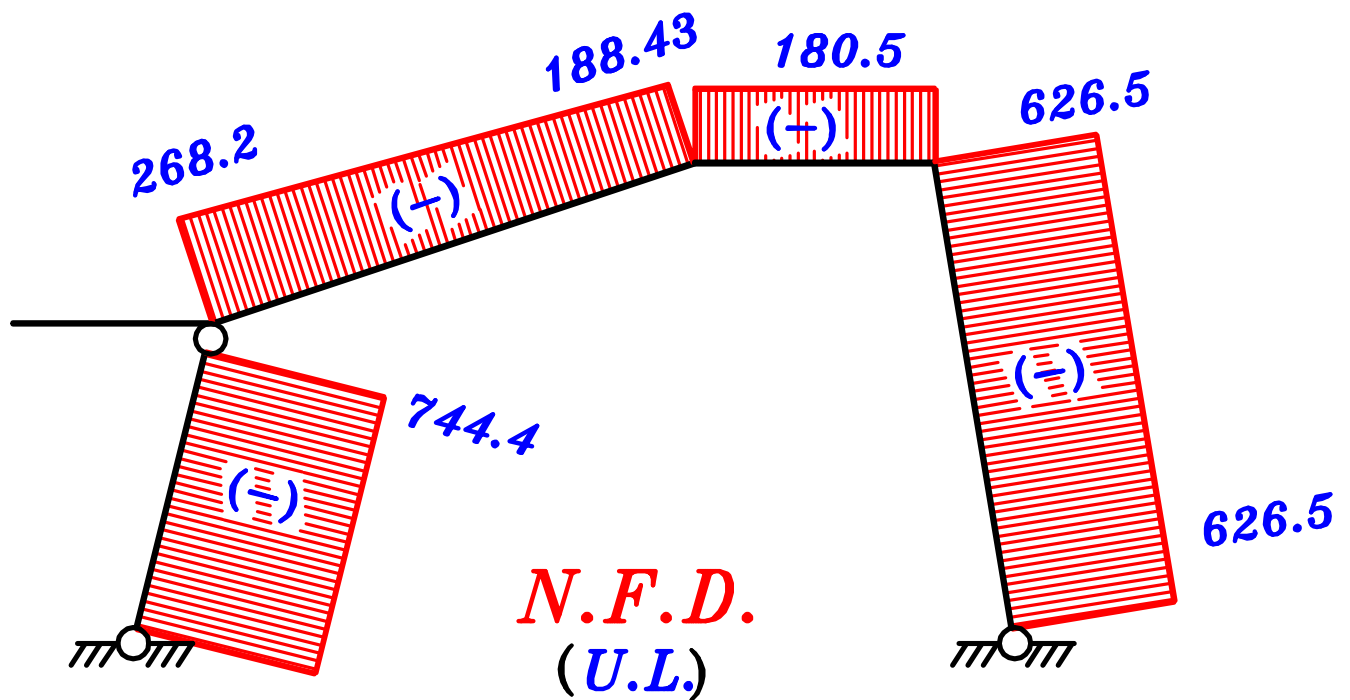
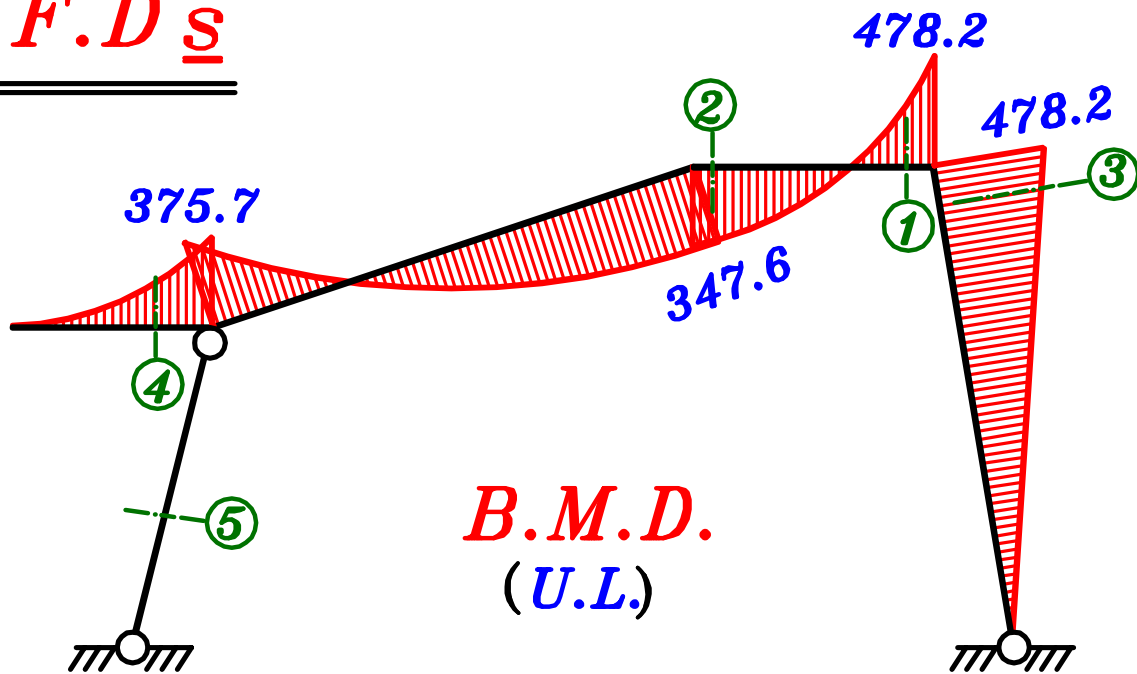
Loads on the Frame.



I.F.D



I.F.D. \underline{s}



Design of Sections.

Sec. ①

$$M = 478.2 \text{ kN.m} , P = 180.5 \text{ kN} , b = 350 \text{ mm}$$

$$d_o = 3.5 \sqrt{\frac{478.2 * 10^6}{25 * 350}} = 818.2 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (818.2) = (900 \rightarrow 1063) \text{ mm}$$

$$\text{Take } d = 950 \text{ mm} , t = 950 + 50 = 1000 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{180.5 * 10^3}{25 * 350 * 1000} = 0.020 < 0.04 \therefore (\text{neglect } P)$$

$$\therefore \text{Take } d = d_o = 818.2 \text{ mm}$$

$$\therefore \text{Take } \boxed{d = 850 \text{ mm}} , \boxed{t = 900 \text{ mm}}$$

$$\therefore \text{The sec. still R-sec. } C_1 = 3.50 \rightarrow J = 0.78$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{478.2 * 10^6}{0.780 * 360 * 818.2} = 2081.4 \text{ mm}^2$$

$$\text{— Check } A_{s_{min.}} \quad A_{s_{req.}} = 2081.4 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 850 = 929.7 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2081.4 \text{ mm}^2 \quad \boxed{11 \phi 16}$$

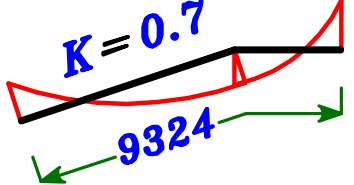
$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{16 + 25} = 7.92 = 7.0 \text{ bars}$$

Sec. ② $M = 347.6 \text{ kN.m}$, $P = 186.3 \text{ kN}$, $b = 350 \text{ mm}$

$d = 850 \text{ mm}$ (the same depth of Sec. ①)

Check $\frac{P}{F_{cu} b t} = \frac{186.3 * 10^3}{25 * 350 * 850} = 0.025 < 0.04 \therefore (\text{neglect } P)$

\therefore The sec. will be T-sec. \therefore use B

$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = \text{Spacing} = 6.0 \text{ m} = 6000 \text{ mm} \\ 16 t_s + b = 16 * 140 + 350 = 2590 \text{ mm} \\ K \frac{L}{5} + b = 0.7 * \frac{9324}{5} + 350 = 1655.3 \text{ mm} \end{array} \right\}$$


$B = 1655.3 \text{ mm}$

$$\therefore d = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} B}} \therefore 850 = c_1 \sqrt{\frac{347.6 * 10^6}{25 * 1655.3}} \rightarrow c_1 = 9.27 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{u.L.}}{J F_y d} = \frac{347.6 * 10^6}{0.826 * 360 * 850} = 1375.2 \text{ mm}^2$$

– Check $A_{s_{min.}}$ $A_{s_{req.}} = 1375.2 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 850 = 929.7 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1375.2 \text{ mm}^2 \quad (7 \phi 16)$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 1375.2 \quad (2 \phi 12)$$

Sec. ③ R-Sec. $M = 478.2 \text{ kN.m}$, $P = 626.5 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{478.2 * 10^6}{25 * 350}} = 818.2 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (818.2) = (900 \rightarrow 1063) \text{ mm}$$

Take $d = 950 \text{ mm}$, $t = 950 + 50 = 1000 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{626.5 * 10^3}{25 * 350 * 1000} = 0.071 > 0.04$ (Don't neglect P)

∴ Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{478.2}{626.5} = 0.763 \text{ m} \quad \therefore \frac{e}{t} = \frac{0.763}{1.0} = 0.763 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 0.763 + \frac{1.0}{2} - 0.05 = 1.213 \text{ m}$$

$$M_s = P * e_s = 626.5 * 1.213 = 759.9 \text{ kN.m}$$

$$\therefore 950 = C_1 \sqrt{\frac{759.9 * 10^6}{25 * 350}} \rightarrow C_1 = 3.22 \rightarrow J = 0.764$$

$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{u.l.}}{(F_y \setminus \delta_s)} = \frac{759.9 * 10^6}{0.764 * 360 * 950} - \frac{626.5 * 10^3}{(360 \setminus 1.15)} = 907 \text{ mm}^2$$

– Check $A_{s_{min.}}$ $A_{s_{req.}} = 907 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 950 = 1039 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$\left. \begin{aligned} A_{s_{min.}} &= \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 950 = 1039 \text{ mm}^2 \\ 1.3 A_{s_{req.}} &= 1.3 * 907 = 1179.1 \text{ mm}^2 \end{aligned} \right\} \text{الأقل} = 1039 \text{ mm}^2 \quad (6 \phi 16)$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{16 + 25} = 7.92 = 7.0$$

$$\text{Stirrup Hangers} \approx 0.4 A_s \approx 0.4 (1039) = 416 \text{ mm}^2 \quad (2 \phi 18)$$

Sec. ④ $M = 375.7 \text{ kN.m}$, $b = 350 \text{ mm}$

\therefore The sec. is **R-sec.** $C_1 = 3.50 \rightarrow J = 0.78$

$$d = 3.5 \sqrt{\frac{375.7 * 10^6}{25 * 350}} = 725.2 \text{ cm. (as R-Sec.)}$$

\therefore Take $d = 750 \text{ mm}$, $t = 800 \text{ mm}$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{375.7 * 10^6}{0.780 * 360 * 725.2} = 1844.9 \text{ mm}^2$$

– Check $A_{s_{min.}}$ $A_{s_{req.}} = 1844.9 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 750 = 820.3 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 1844.9 \text{ mm}^2$ **10 ϕ 16**

$$Y = \left\{ \begin{array}{l} \frac{t}{2} = \frac{800}{2} = 400 \text{ mm} \\ t_b = \frac{\text{spacing}}{12} = \frac{6000}{12} = 500 \text{ mm} \\ t - \frac{L_c}{3} = 800 - \frac{2500}{3} = -33.3 \text{ mm} \end{array} \right\} Y = 500 \text{ mm}$$

Sec. ⑤

($350 * 450$) Axially Loaded Column. $P = 744.4 \text{ kN}$

$$\therefore P_{U.L.} = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

$$\therefore 744.4 * 10^3 = 0.35 (350 * 450) (25) + 0.67 A_s (360)$$

$$\therefore A_s = -2627 \text{ mm}^2 = (-Ve) \text{ Value}$$

$$\therefore A_s = A_{s_{min.}} = \frac{0.8}{100} * 350 * 450 = 1260 \text{ mm}^2$$
 12 ϕ 12

Check Shear.

– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{25}{1.5}} = 2.85 \text{ N/mm}^2$$

Sec. ① $Q = 335.1 \text{ kN}$

$$\therefore \text{Actual shear stress.} = q_u = \frac{Q}{b d} = \frac{335.1 * 10^3}{350 * 850} = 1.126 \text{ N/mm}^2$$

$\therefore q_{cu} < q_u < q_{max.} \therefore$ We need Stirrups more Than $5 \phi 8 \setminus m$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \setminus \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.126 - \frac{0.98}{2} = \frac{2 * 50.3 (240 \setminus 1.15)}{350 * S} \rightarrow S = 94.32 \text{ mm} < 100 \text{ mm}$$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

$$1.126 - \frac{0.98}{2} = \frac{2 * 78.5 (240 \setminus 1.15)}{350 * S} \rightarrow S = 147.19 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups} \setminus m = \frac{1000}{S} = \frac{1000}{147.19} = 6.80 = 7.0$$

\therefore Use Stirrups $7 \phi 10 \setminus m$ 2 branches

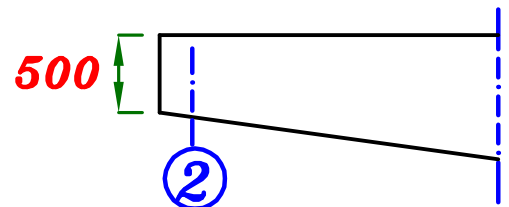
Sec. ② $Q = 134.5 \text{ kN}$

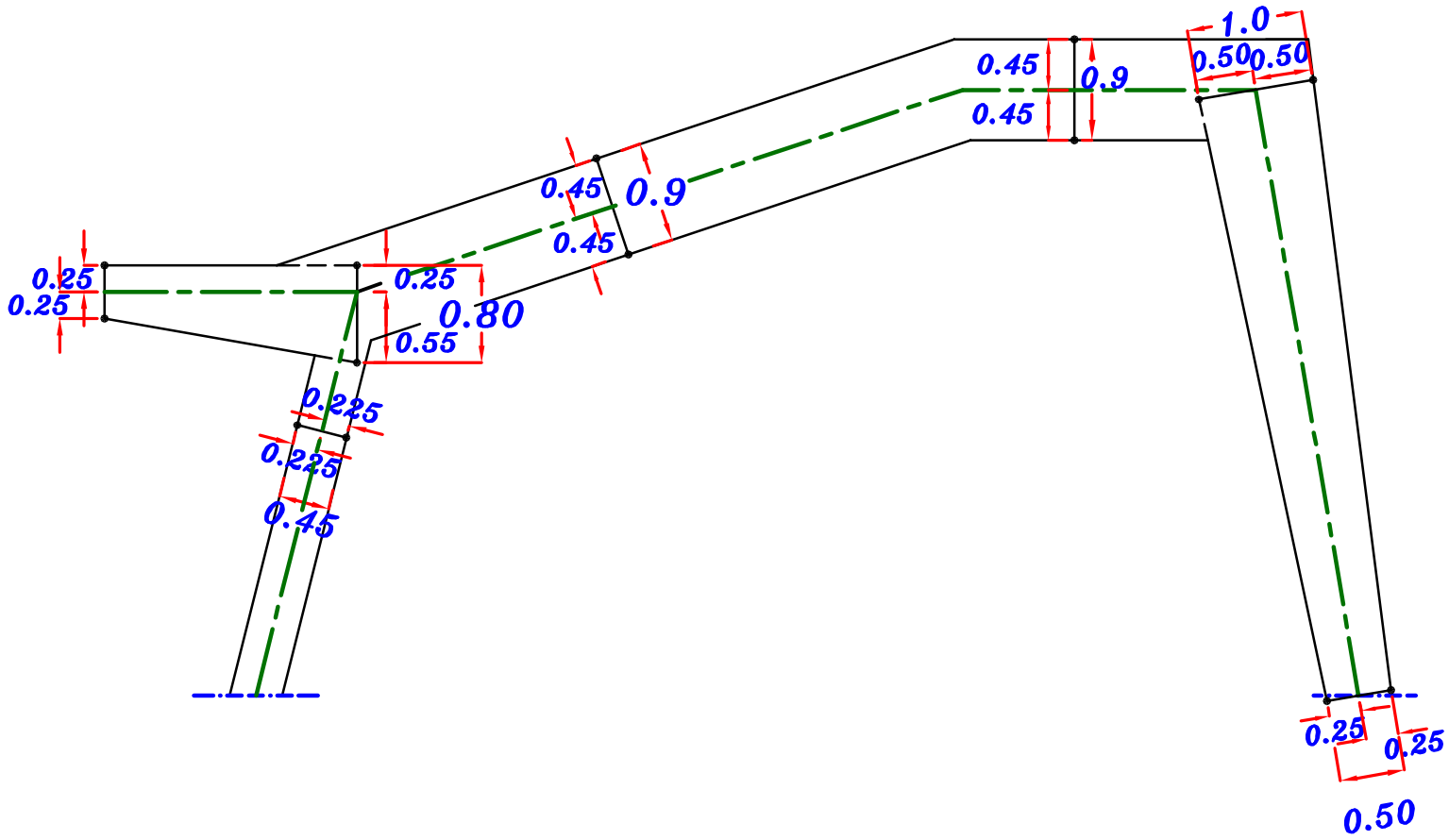
\therefore Actual shear stress. =

$$q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

$$= \frac{134.5 * 10^3}{350 * 450} - \text{ZERO} = 0.853 \text{ N/mm}^2$$

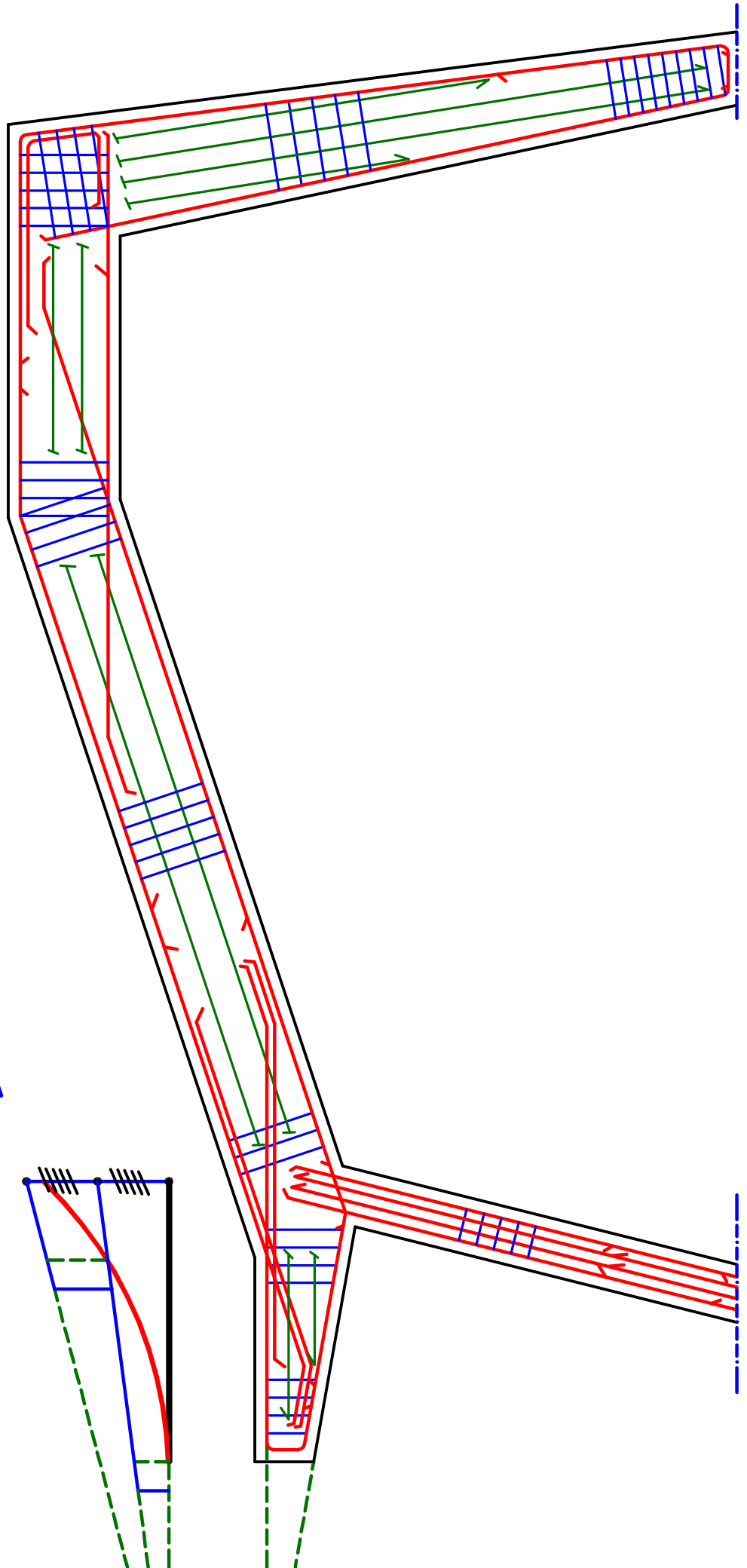
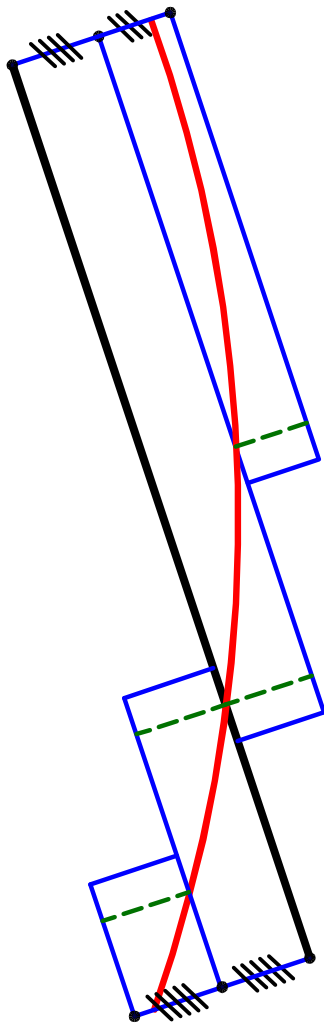
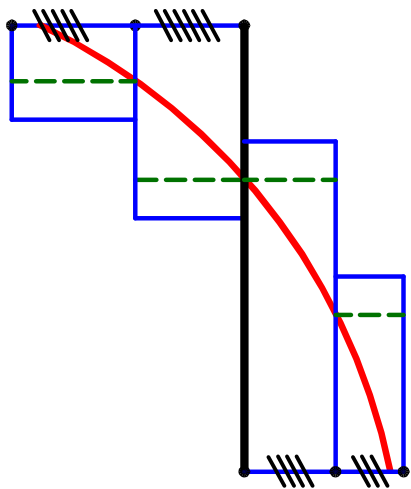
$\therefore q_u < q_{cu} \rightarrow$ Use min. stirrups $5 \phi 8 \setminus m$

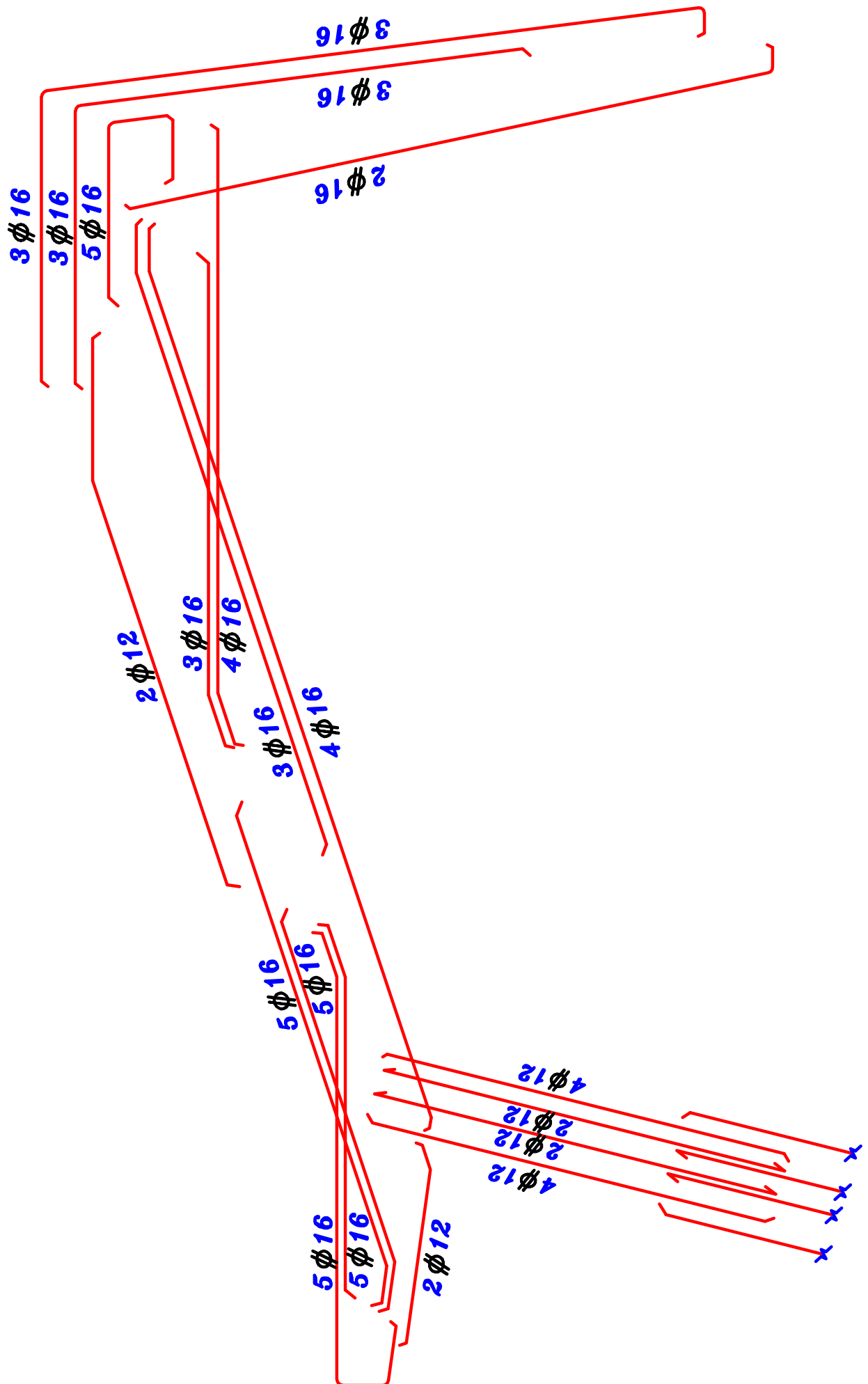


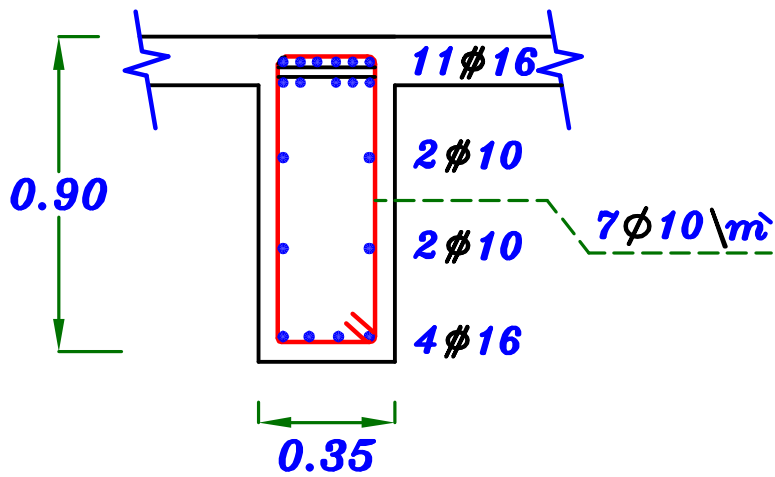


مراحل رسم التسليح لل *Frame* مع مراعاة الترتيب

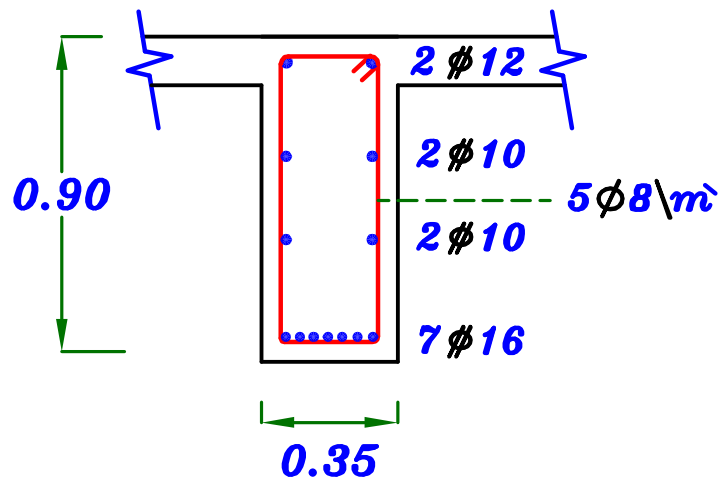
- ١- رسم مكان التسليح الرئيسى جهة ال *moment*
- ٢- تسليح ال *Joints* (عمل التباعد و التداخل)
- ٣- الحديد السفلى يرسم من وش العمود الى وش العمود
- ٤- رسم التسليح عند نهاية الاعمده (عمل أشاير أو لف الحديد فى العمود)
- ٥- رسم البلوكات مع مراعاة عدد الاسياخ و عدد الصفوف
- ٦- وضع ال *Stirrup Hangers*
- ٧- وضع الكانات و ال *Shrinkage bars* و ال *Buckling bars*
- ٨- رسم التفريد و ال *Sections*



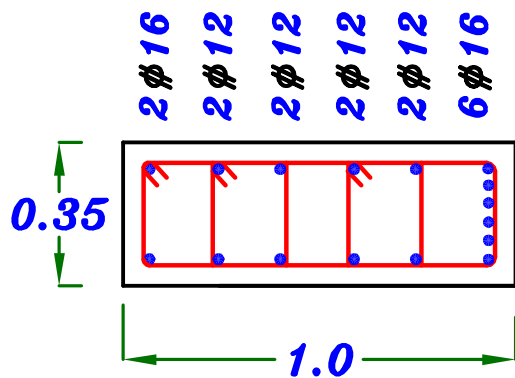




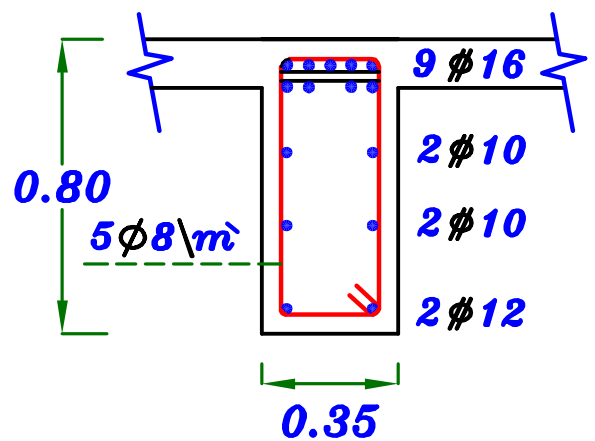
Sec. (1-1)



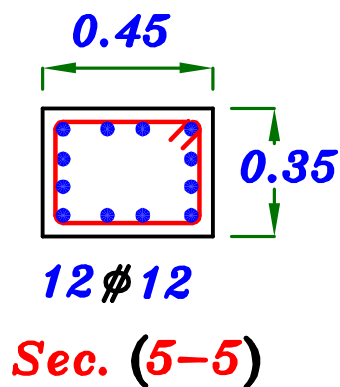
Sec. (2-2)



Sec. (3-3)



Sec. (4-4)



Sec. (5-5)

Example.

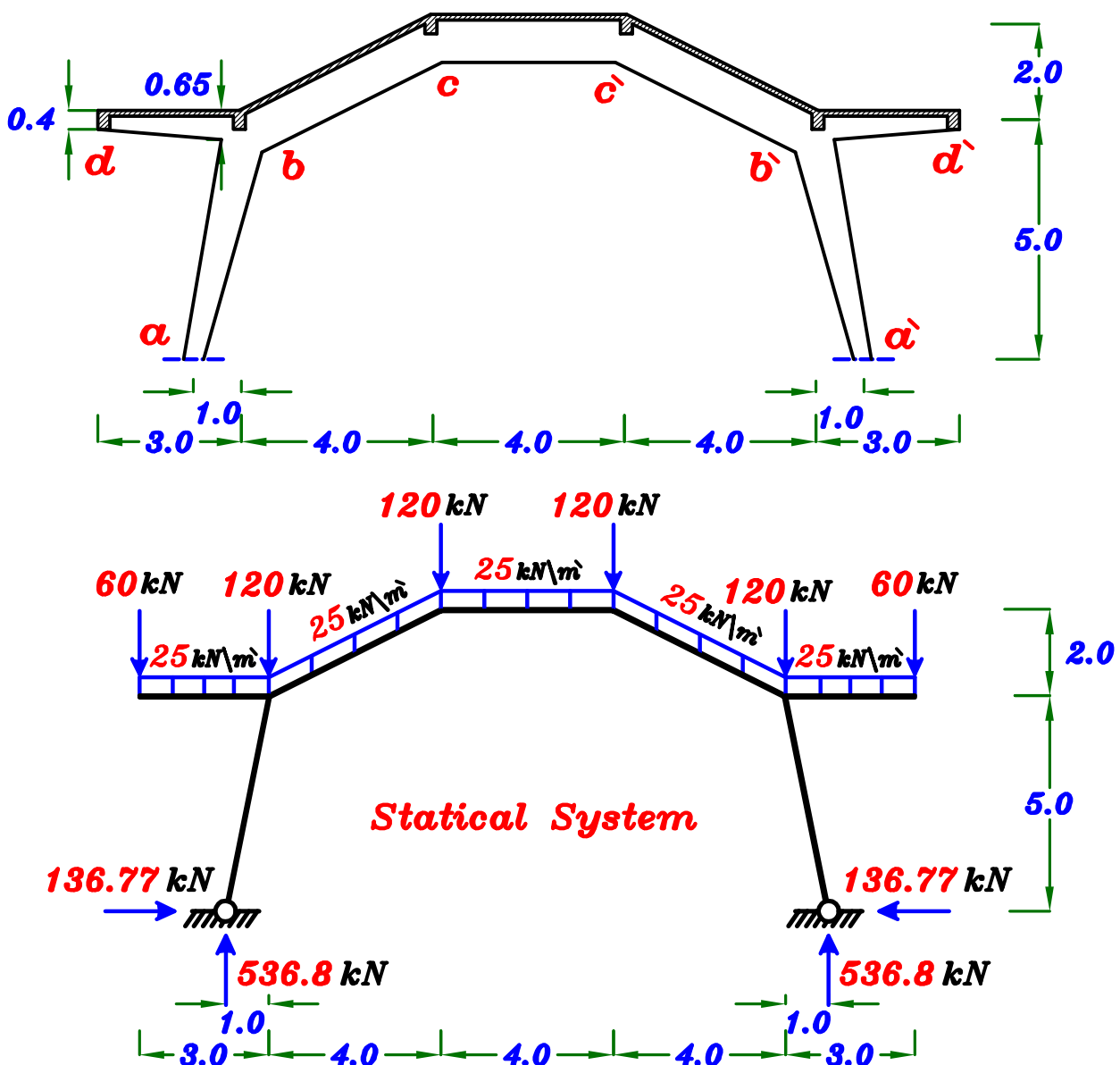
The Figure shows a sectional elevation of an intermediate two hinged Frame (a b c d d' c' b' a') of a shed. The shed is composed of a group of beams and Frames.

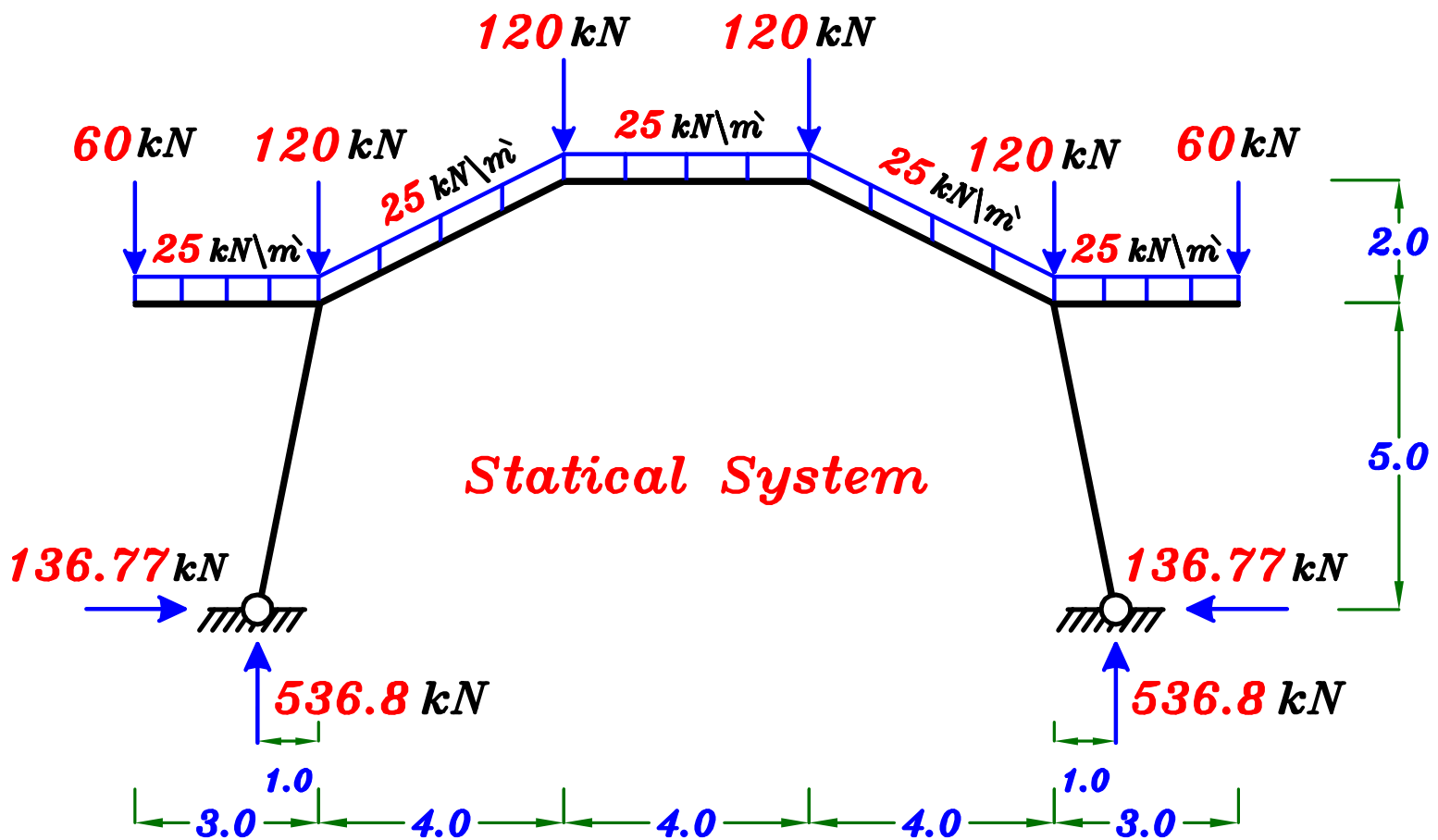
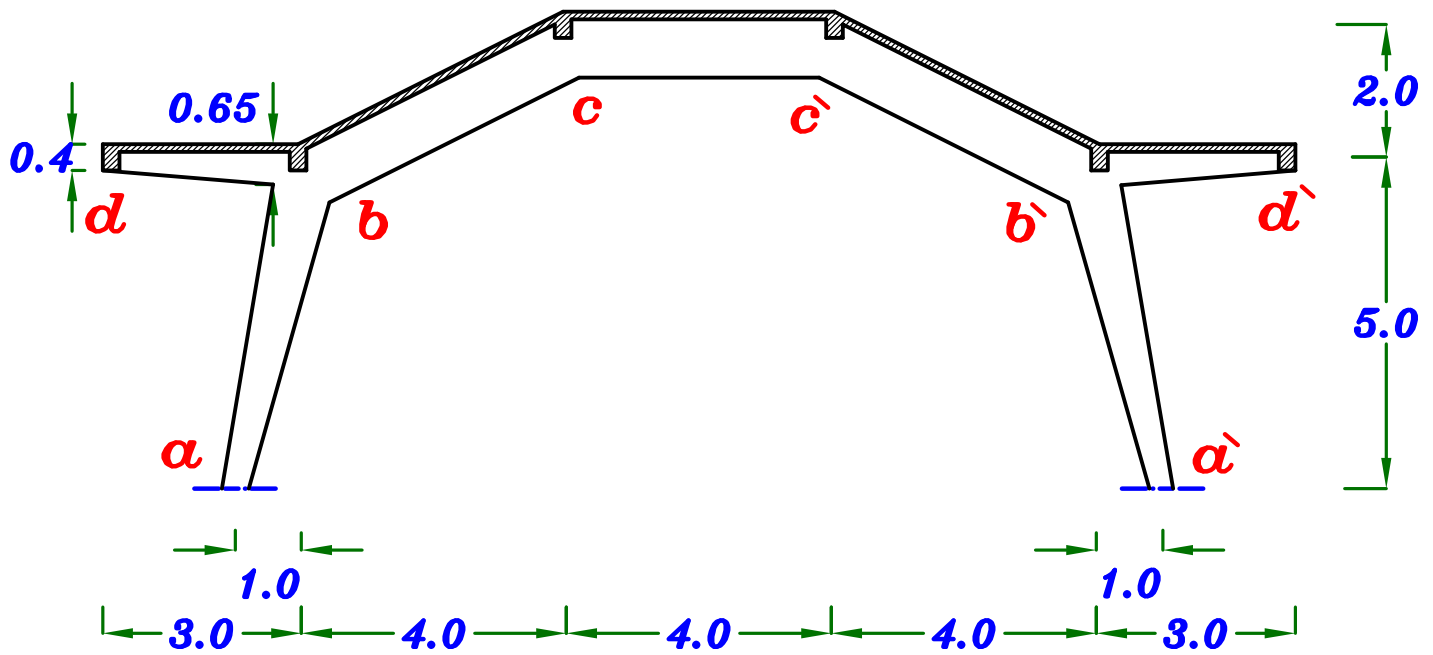
For the given working loads and reactions it is required to :

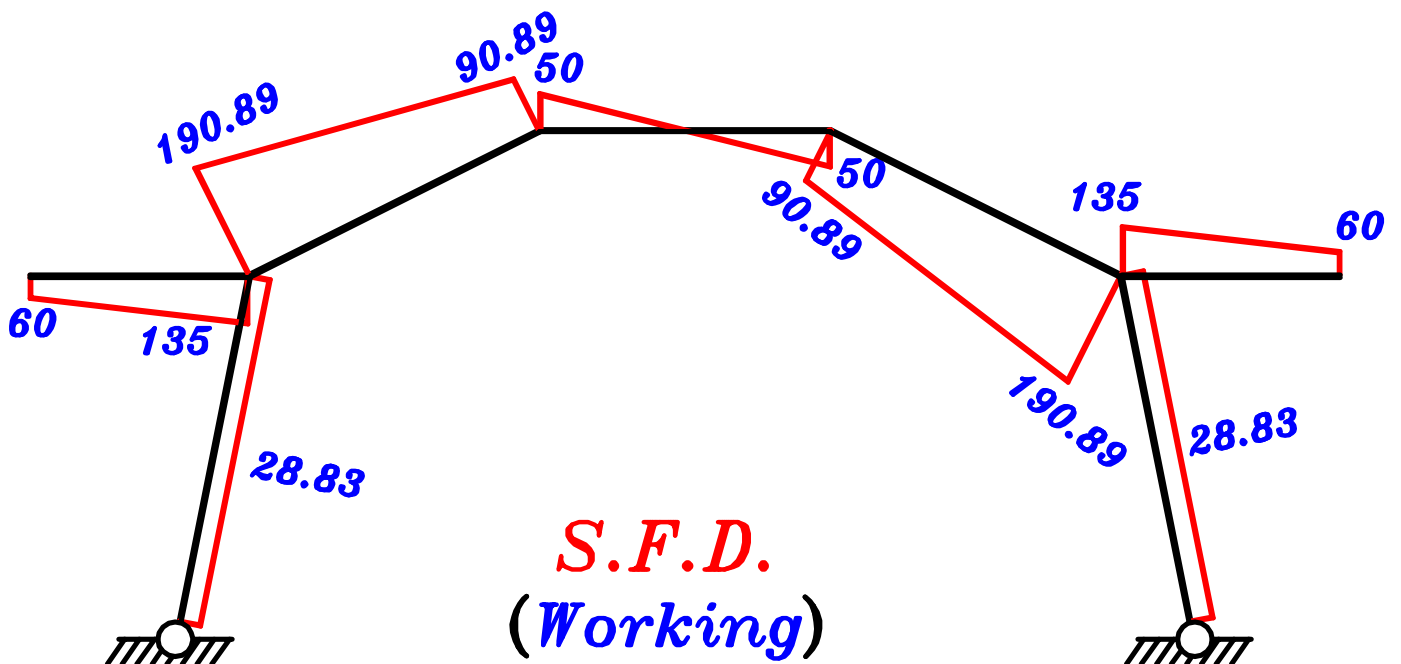
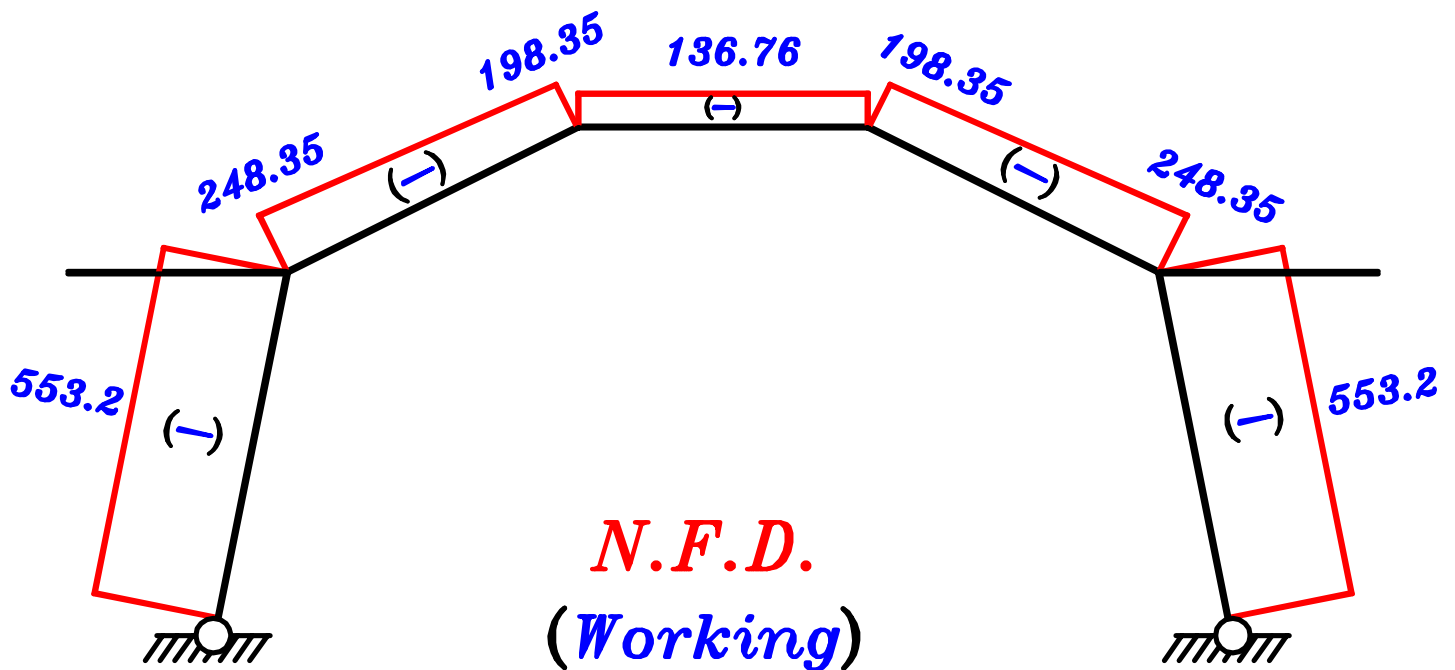
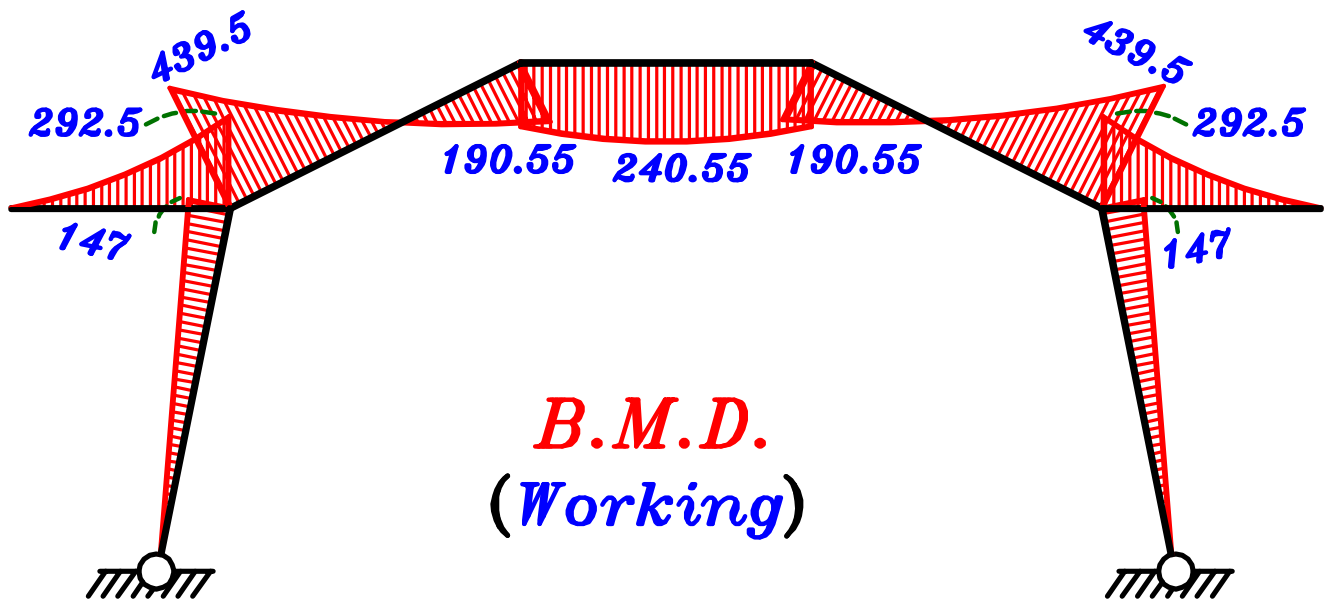
- 1) Draw the shearing, Normal Force and Bending Moment diagrams For the Frame.
- 2) Using the ultimate limit design method, design the critical sections For an intermediate Frame to satisfy the requirements of the internal Forces. using the dimensions given For the part (b d).
- 3) Complete detailed drawings (i.e. elevation and sections) showing all necessary reinforcement using moment of resistance diagram.

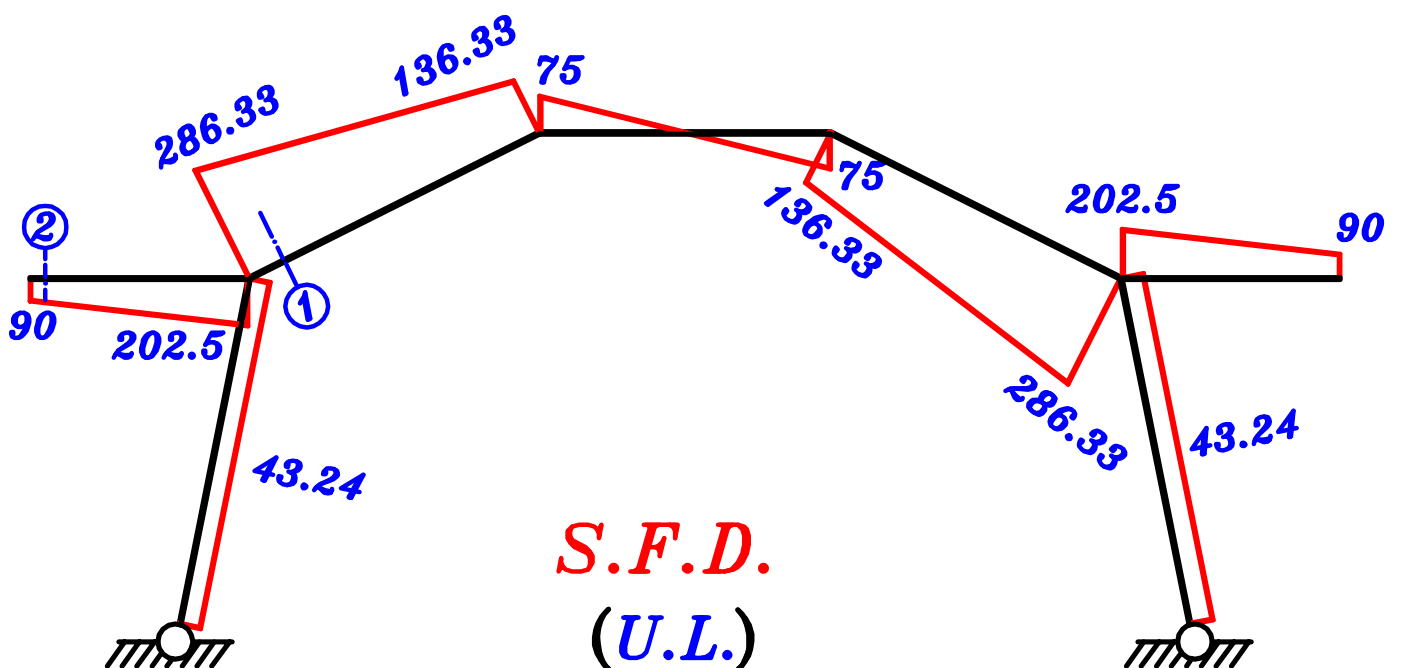
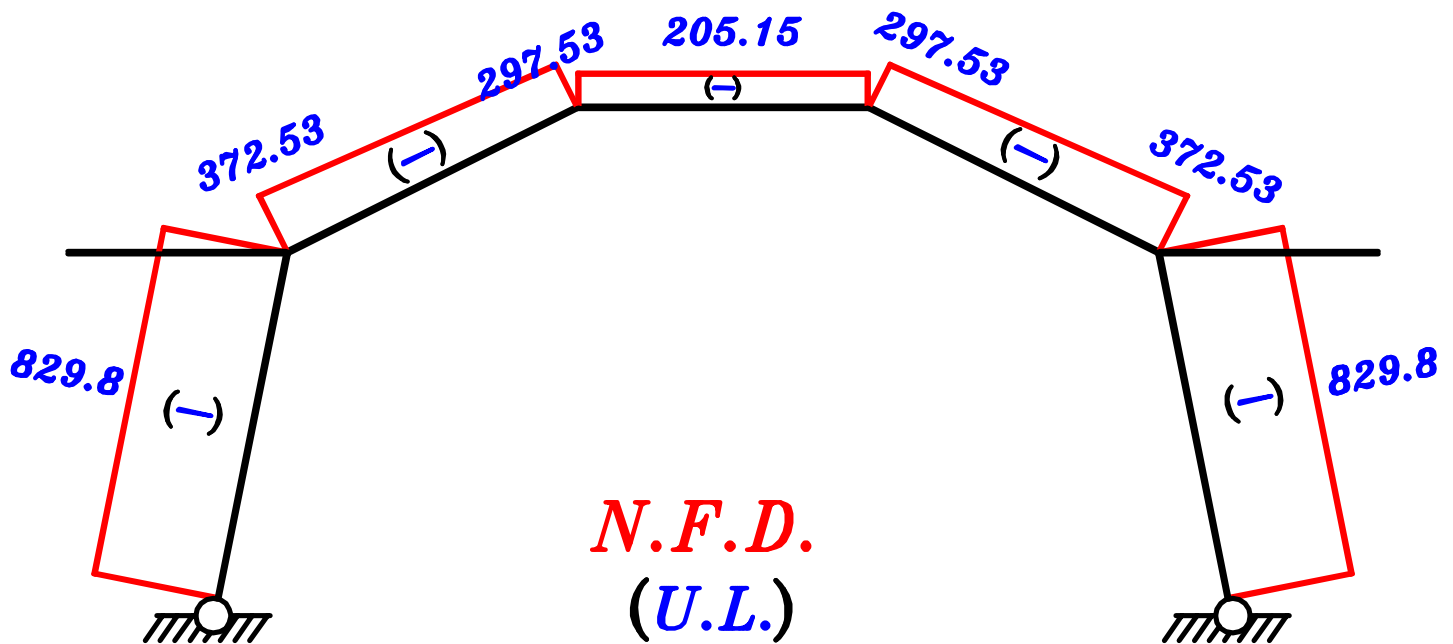
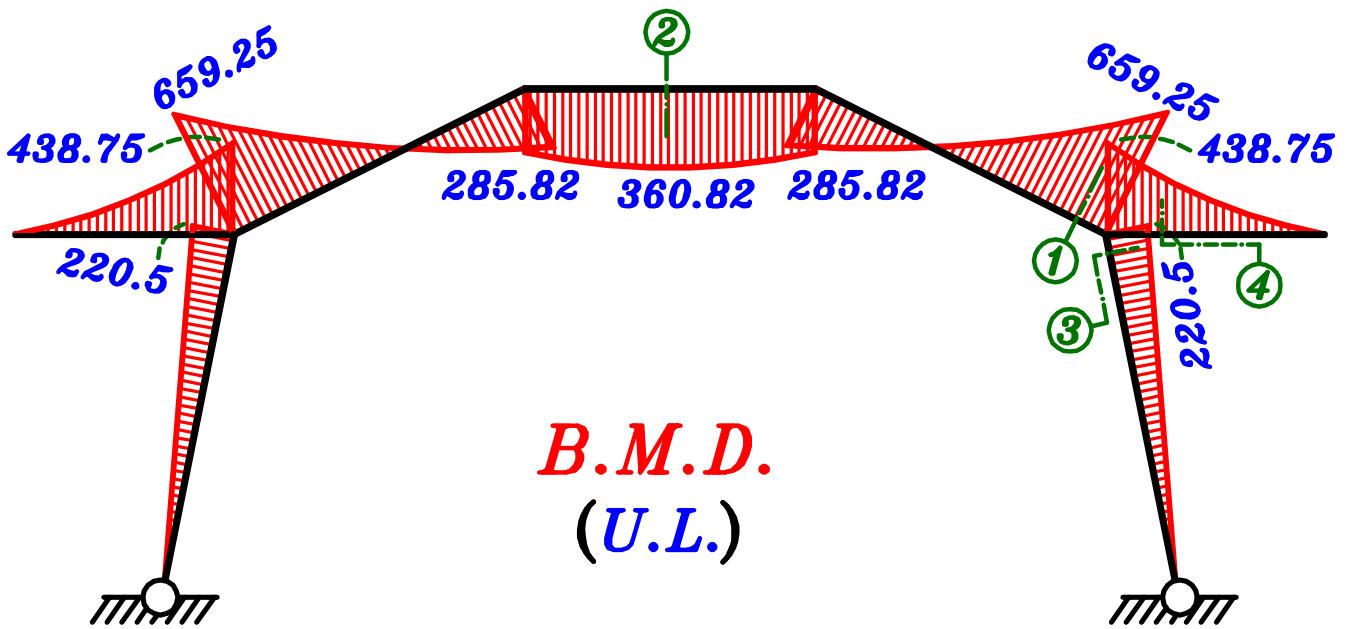
Data to be used:

- The spacing between Frames is 5.0 m center to center.
- Slab thickness $t_s = 120$ mm
- Breadth of all beams = 250 mm and Frames = 350 mm
- Concrete characteristic strength $F_{cu} = 25$ N/mm² and steel of grade 360/520









Design of Sections.

Sec. ① $M = 659.25 \text{ kN.m}$, $P = 372.53 \text{ kN}$, $b = 350 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{659.25 \cdot 10^6}{25 \cdot 350}} = 960.7 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (960.7) = (1056.77 \rightarrow 1248.9) \text{ mm}$$

Take $d = 1100 \text{ mm}$, $t = 1100 + 100 = 1200 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{372.53 \cdot 10^3}{25 \cdot 350 \cdot 1200} = 0.035 < 0.04 \therefore (\text{neglect } P)$

\therefore Take $d = d_o = 960.7 \text{ mm}$

\therefore Take $d = 1000 \text{ mm}$, $t = 1100 \text{ mm}$

$\therefore C_1 = 3.50 \rightarrow J = 0.78$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{659.25 \cdot 10^6}{0.780 \cdot 360 \cdot 1000} = 2347.75 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2347.75 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 350 \cdot 950 = 1039 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 2347.75 \text{ mm}^2$ **10 ϕ 18**

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{18 + 25} = 7.56 = 7.0 \text{ bars}$$

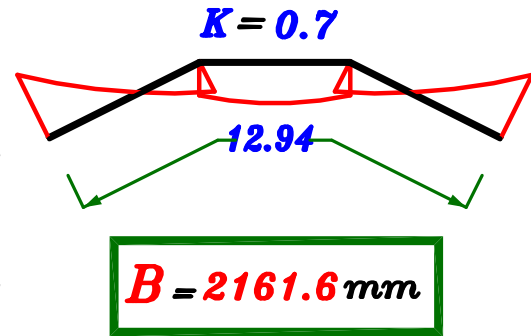
Sec. ② $M = 360.82 \text{ kN.m}$, $P = 205.15 \text{ kN}$, $b = 350 \text{ mm}$

$d = 950 \text{ mm}$ (the same depth of Sec. ①)

Check $\frac{P}{F_{cu} b t} = \frac{205.15 * 10^3}{25 * 350 * 1000} = 0.0213 < 0.04 \therefore (\text{neglect } P)$

\therefore The sec. will be T-Sec.

$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = \text{Spacing} = 5.0 \text{ m} = 5000 \text{ mm} \\ 16 t_s + b = 16 * 120 + 350 = 2270 \text{ mm} \\ K \frac{L}{5} + b = 0.7 * \frac{12940}{5} + 350 = 2161.6 \text{ mm} \end{array} \right\}$$



$$\therefore d = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} B}} \therefore 1000 = c_1 \sqrt{\frac{360.82 * 10^6}{25 * 2161.6}} \rightarrow c_1 = 12.24 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{u.L.}}{J F_y d} = \frac{360.82 * 10^6}{0.826 * 360 * 1000} = 1213.41 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1213.41 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1000 = 1039.75 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1213.41 \text{ mm}^2 \quad \boxed{5 \phi 18}$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 1371 \quad \boxed{2 \phi 12}$$

Sec. ③ R-Sec. $M = 220.5 \text{ kN.m}$, $P = 829.8 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{220.5 * 10^6}{25 * 350}} = 555.6 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (555.6) = (611.17 \rightarrow 722.3) \text{ mm}$$

$$\therefore \text{Take } d = 650 \text{ mm} , t = 700 \text{ mm}$$

$$\therefore t_{(Column)} < 0.8 t_{(Beam)} \xrightarrow{\text{Take}} t_{(Column)} = t_{(Beam)} = 1100 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{829.8 * 10^3}{25 * 350 * 1100} = 0.086 > 0.04 \quad (\text{Don't neglect } P)$$

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{220.5}{829.8} = 0.265 \text{ m} \therefore \frac{e}{t} = \frac{0.265}{1.1} = 0.24 < 0.5 \xrightarrow{\text{Use}} \text{I.D.}$$

\therefore Use Interaction Diagram

$$\zeta = \frac{1100 - 200}{1100} = 0.818 = 0.80 \xrightarrow{\text{use}} \text{ECCS Design Aids Page 4-24}$$

$$\left. \begin{aligned} \frac{P_U}{F_{cu} b t} &= \frac{829.8 * 10^3}{25 * 350 * 1100} = 0.086 \\ \frac{M_U}{F_{cu} b t^2} &= \frac{220.5 * 10^6}{25 * 350 * 1100^2} = 0.021 \end{aligned} \right\} p < 1.0 \xrightarrow{\text{Take}} p = 1.0$$

$$\mu = p * F_{cu} * 10^{-4} = 1.0 * 25 * 10^{-4} = 2.5 * 10^{-3}$$

$$A_s = A_{s'} = \mu * b * t = 2.5 * 10^{-3} * 350 * 1100 = 962.5 \text{ mm}^2$$

$$\text{— Check } A_{s_{min.}} = \frac{0.8}{100} * b * t = \frac{0.8}{100} * 350 * 1100 = 3080 \text{ mm}^2$$

$$A_{s_{Total}} = A_s + A_{s'} = 2 * 962.5 = 1925 \text{ mm}^2 \therefore A_{s_{Total}} < A_{s_{min.}}$$

$$\therefore \text{take } A_s = A_{s'} = \frac{A_{s_{min.}}}{2} = \frac{3080}{2} = 1540 \text{ mm}^2 \quad (7 \phi 18)$$

Sec. ④ $M_{u.L.} = 438.7 \text{ kN.m}$, R-Sec., $b = 350 \text{ mm}$

$d = 600 \text{ mm}$ (As given in Data.)

$$\therefore d = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}} \therefore 600 = c_1 \sqrt{\frac{438.7 \cdot 10^6}{25 \cdot 350}} \rightarrow c_1 = 2.68 < 2.78$$

\therefore We have to increase Dimensions
OR use A_s using First Principles.
OR use A_s using I.D.

Use A_s using First Principles.

$$\alpha_{max} = 0.8 \left(\frac{2}{3} \right) \left[\frac{600}{600 + (F_y \setminus \delta_s)} \right] \cdot d = 0.35 d = 0.35 \cdot 600 = 210 \text{ mm}$$

$$M_{u.L. max} = \frac{2}{3} \frac{F_{cu}}{\delta_c} \alpha_{max} b \left(d - \frac{\alpha_{max}}{2} \right) = \frac{2}{3} \left(\frac{25}{1.5} \right) (210)(350) \left(600 - \frac{210}{2} \right) = 404250000 = 404.25 \text{ kN.m}$$

– Get $\Delta M = M_{u.L.} - M_{u.L. max} = 438.7 - 404.25 = 34.45 \text{ kN.m}$

– Get A_s From $\Delta M = A_s \cdot \frac{F_y}{\delta_s} (d - d')$

$$\therefore 34.45 \cdot 10^6 = A_s \cdot \left(\frac{360}{1.15} \right) (600 - 50) \rightarrow A_s = 200 \text{ mm}^2$$

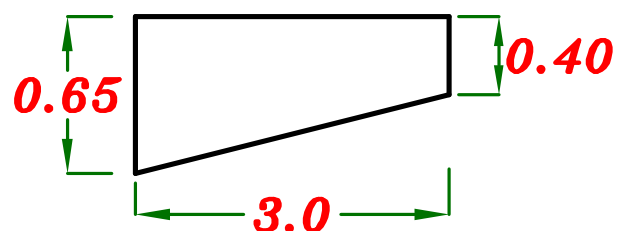
2 ϕ 12

$$\mu_{max} = 5 \cdot 10^{-4} F_{cu} = 5 \cdot 10^{-4} \cdot 25 = 0.0125 \text{ From old Tables Page (6)}$$

$$\therefore A_s = \mu_{max} b d + A_s = 0.0125 (350) (600) + 200 = 2825 \text{ mm}^2$$

– Check $\frac{A_s}{A_s} = \frac{200}{2825} = 0.07 < 0.40 \therefore \text{o.k.}$

12 ϕ 18



Check Shear.

– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{25}{1.5}} = 2.85 \text{ N/mm}^2$$

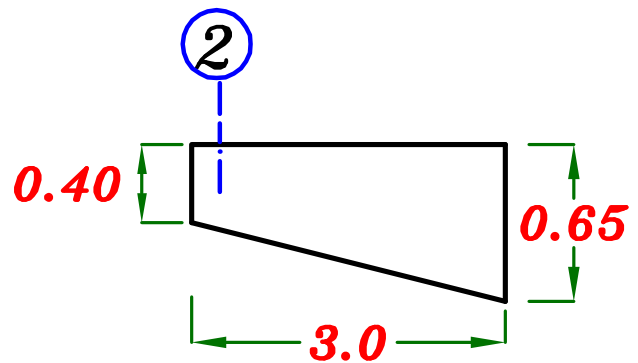
Sec. ① $Q = 286.33 \text{ kN}$

$$\therefore q_U = \frac{Q}{b d} = \frac{286.33 * 10^3}{350 * 1000} = 0.818 \text{ N/mm}^2$$

$q_U < q_{cu} \longrightarrow$ Use min. stirrups $5 \phi 8 \text{ m}$

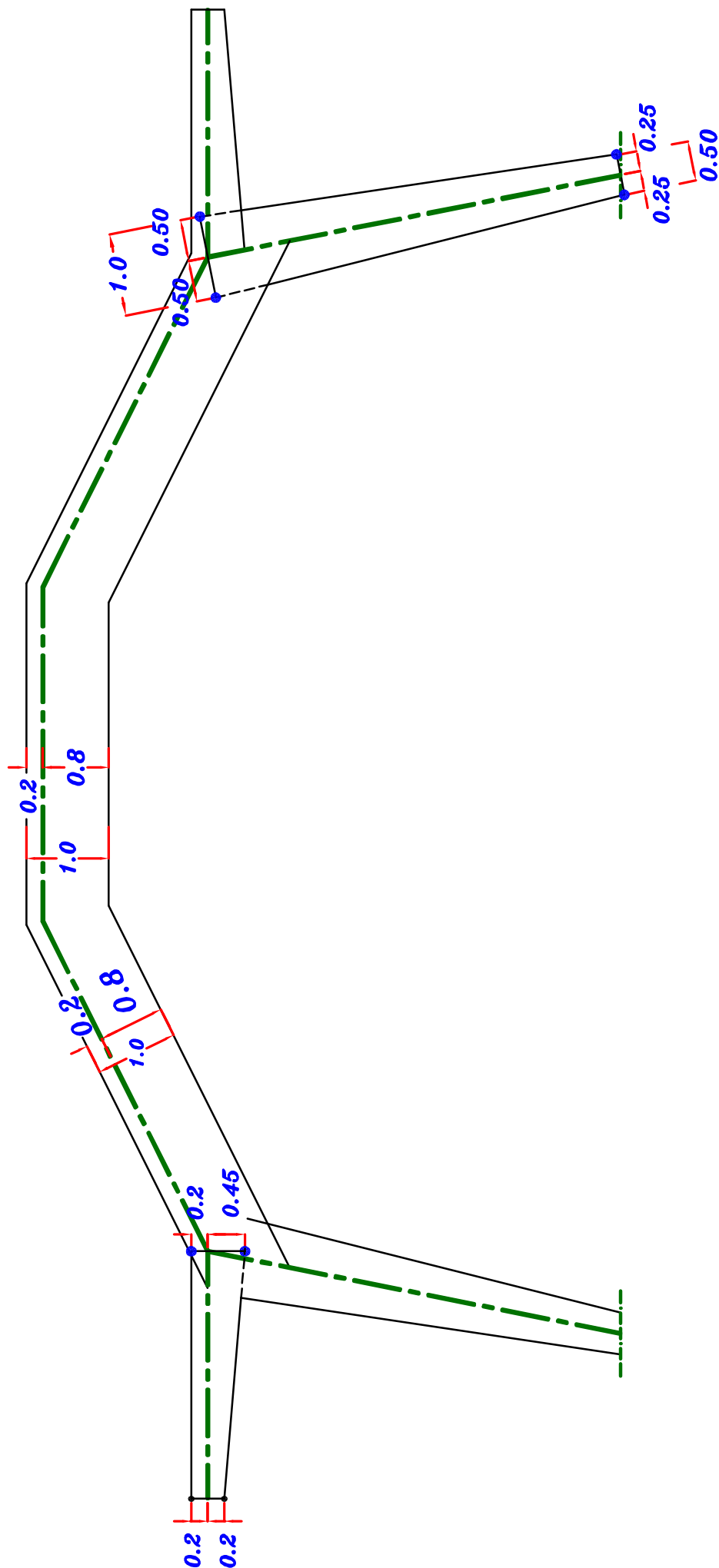
Sec. ② $Q = 90 \text{ kN}$

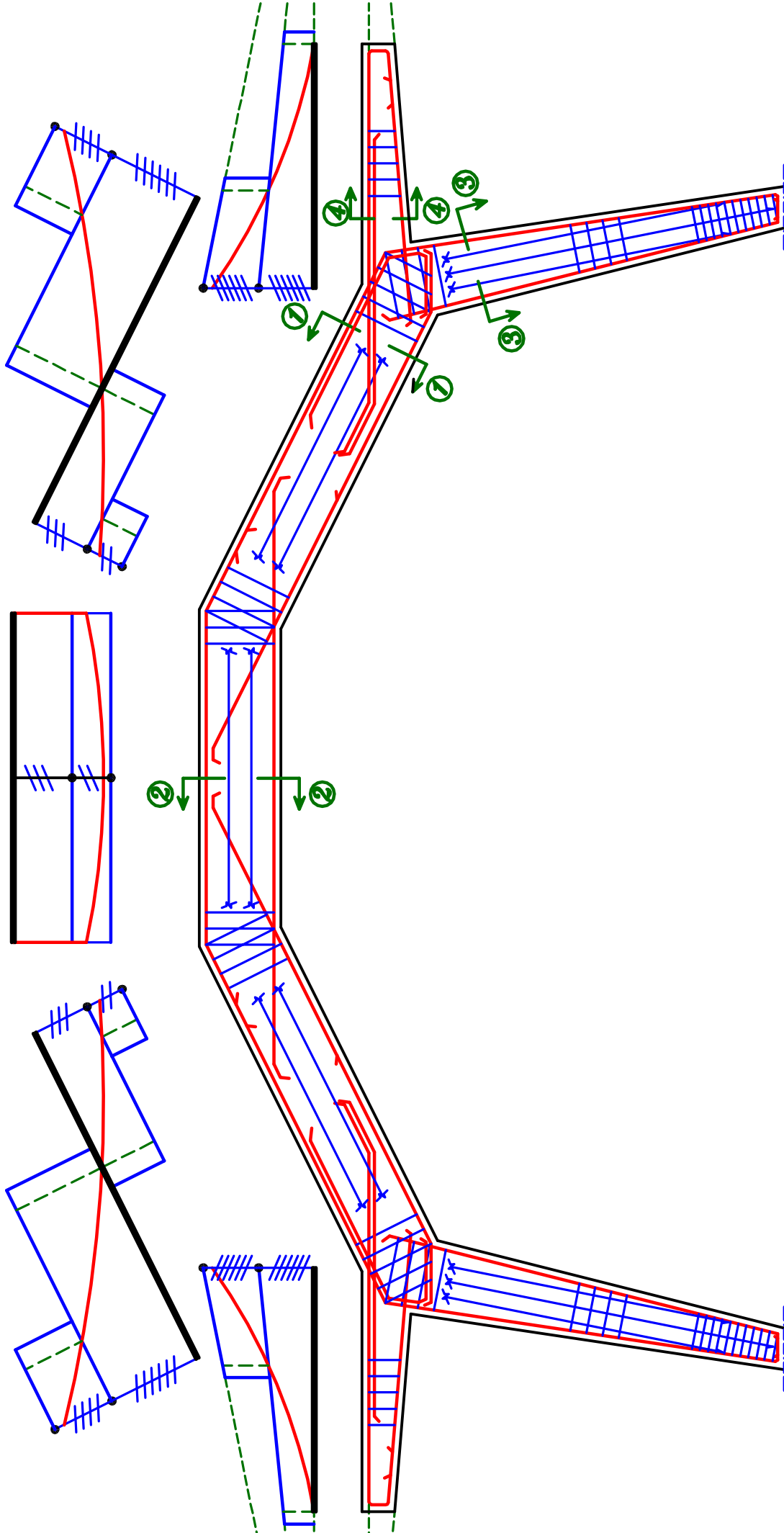
$\tan \beta = \text{Zero}$



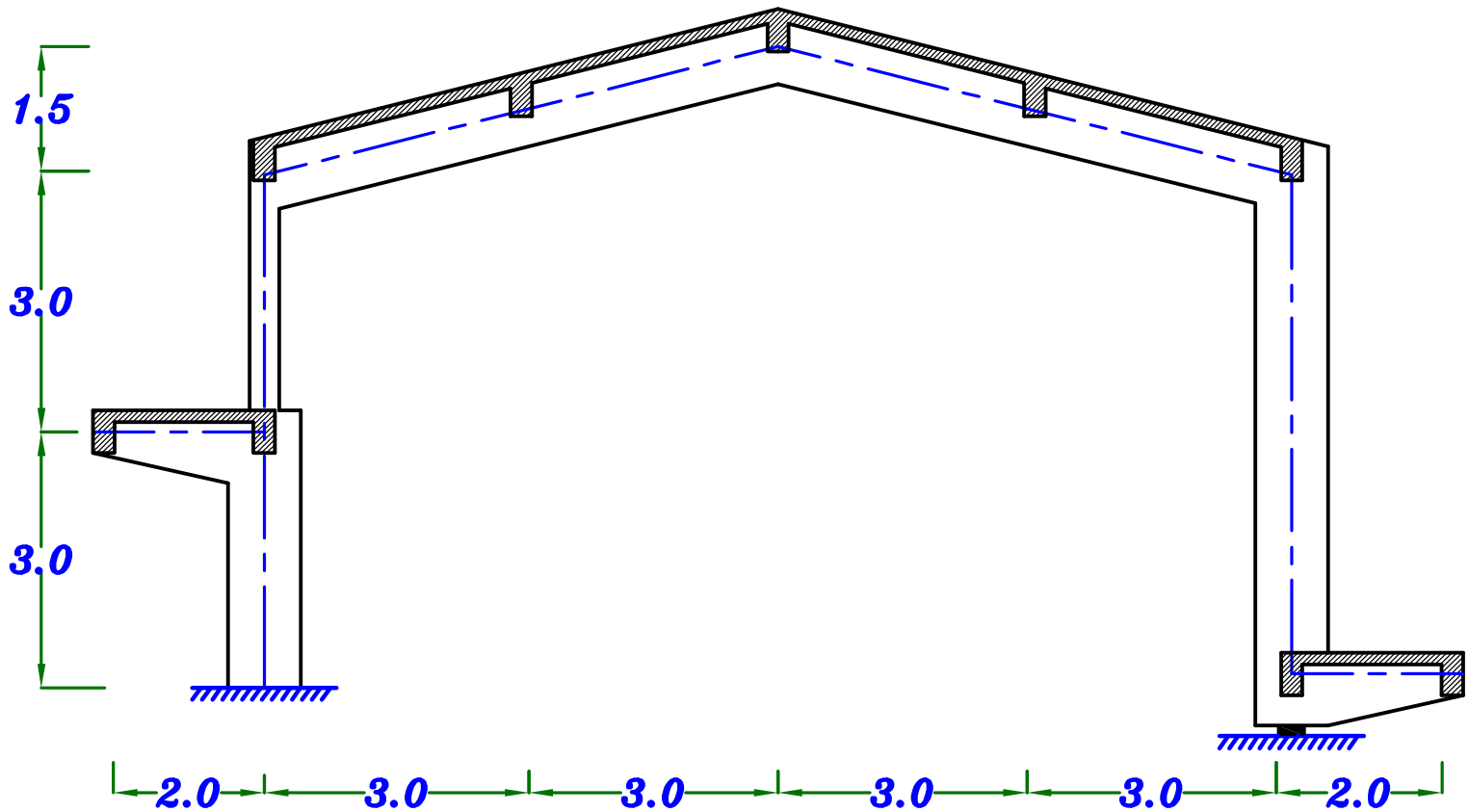
$$\begin{aligned} \therefore \text{Actual shear stress.} &= q_U = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2} \\ &= \frac{90 * 10^3}{350 * 350} - \text{ZERO} = 0.73 \text{ N/mm}^2 \end{aligned}$$

$q_U < q_{cu} \longrightarrow$ Use min. stirrups $5 \phi 8 \text{ m}$





Example.



Data.

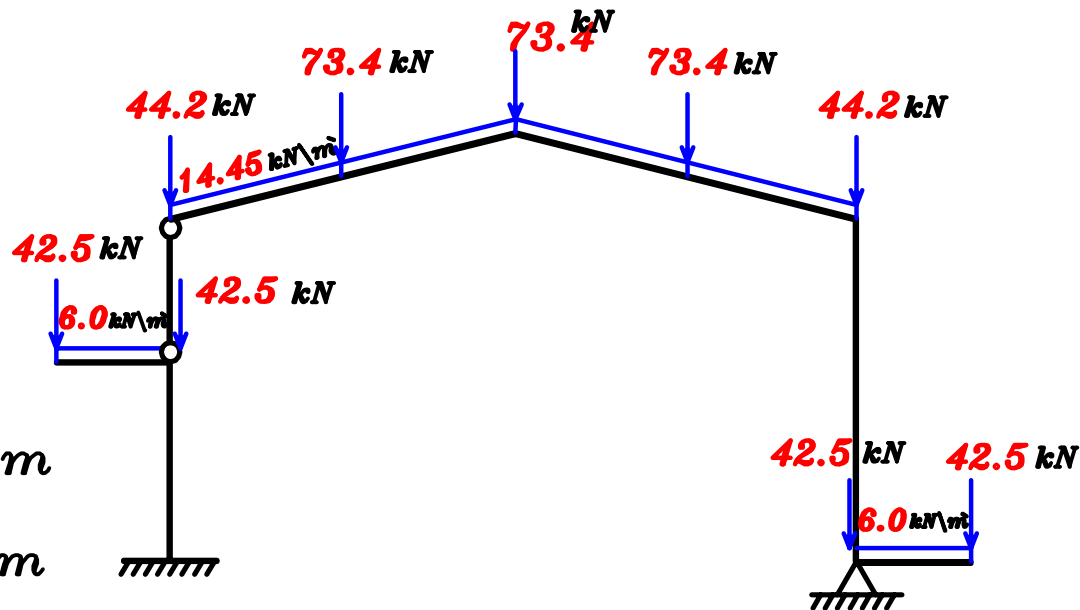
$$F_{cu}/F_y = 25/360$$

$$t_s = 140 \text{ mm}$$

$$\text{Spacing} = 6.0 \text{ m}$$

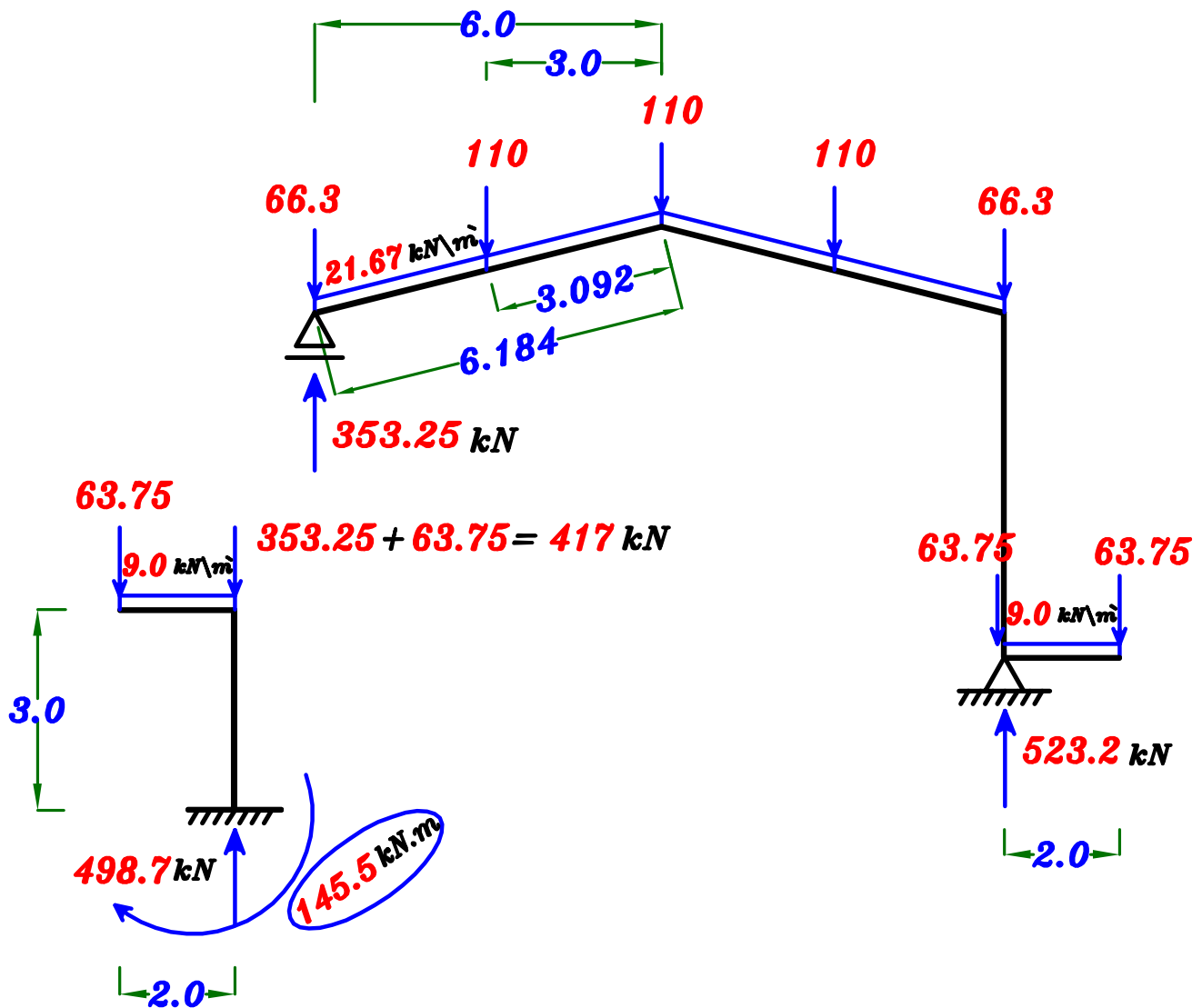
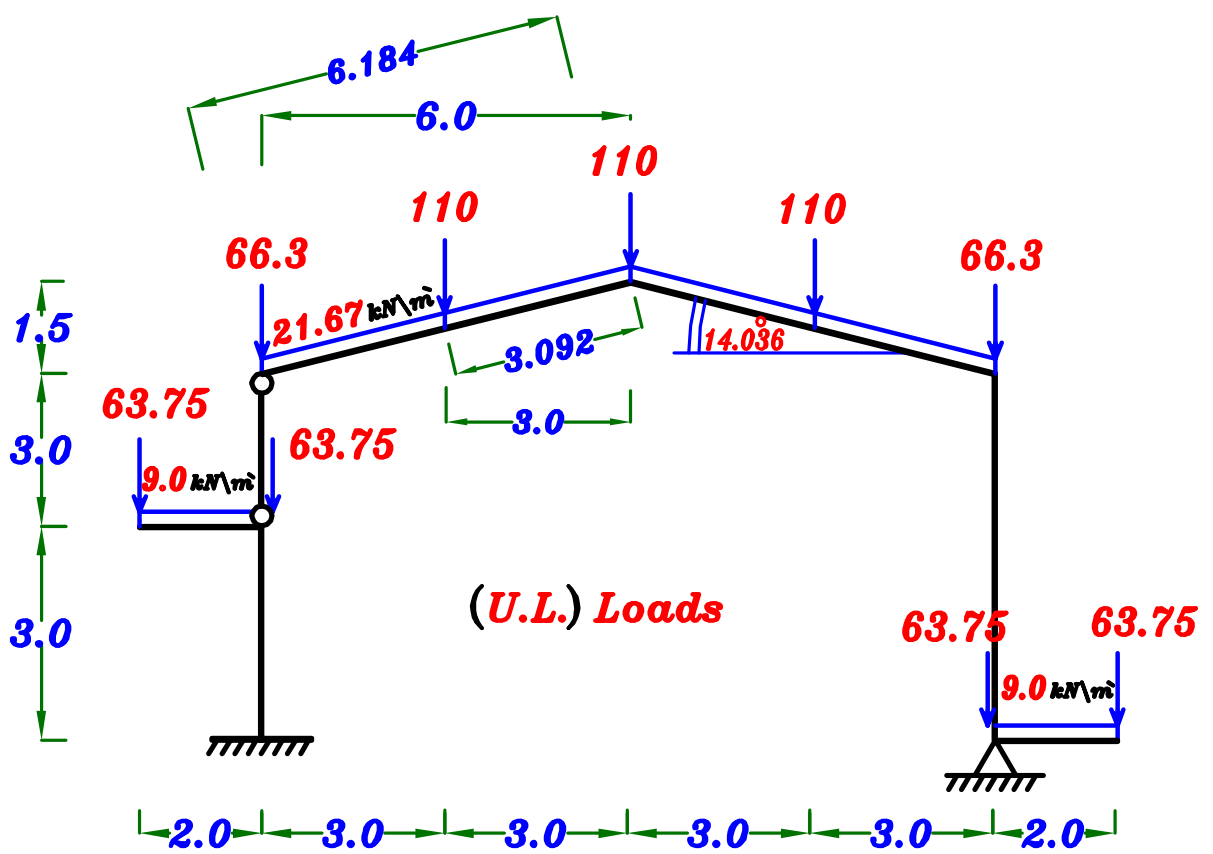
$$b_{(\text{Beams})} = 250 \text{ mm}$$

$$b_{(\text{Frames})} = 350 \text{ mm}$$



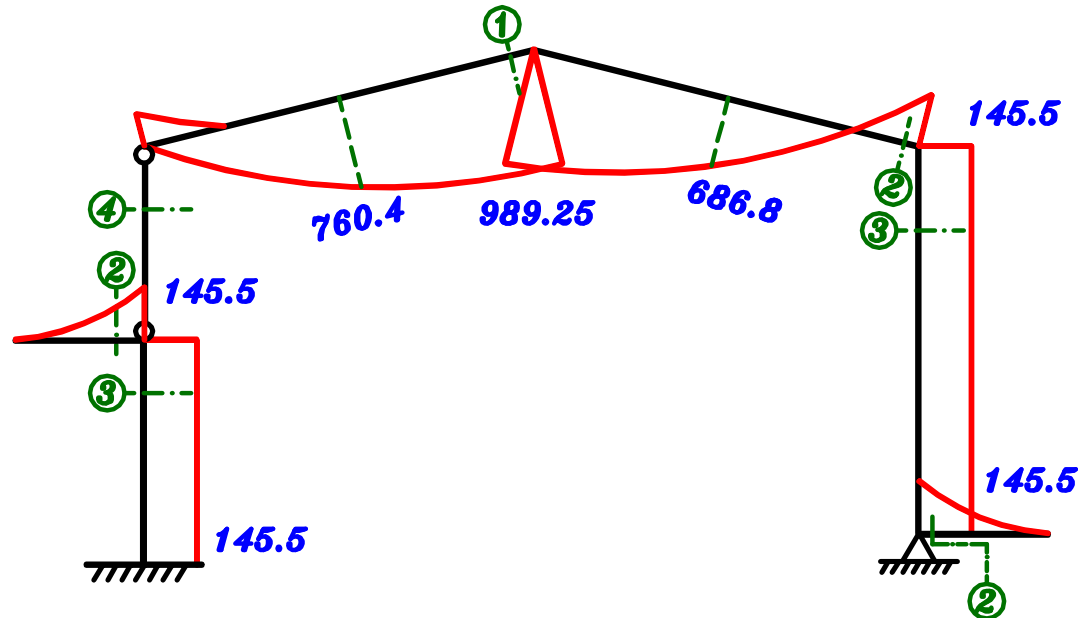
Req.

- ① Draw I.F.D. due to U.L. Loads.
- ② Design the critical sections of the Frame using U.L.D.M.
- ③ Draw details of RFT. to scale 1:50 in elevation & scale 1:20 cross-sec. making curtailment of steel using Moment of Resistance.

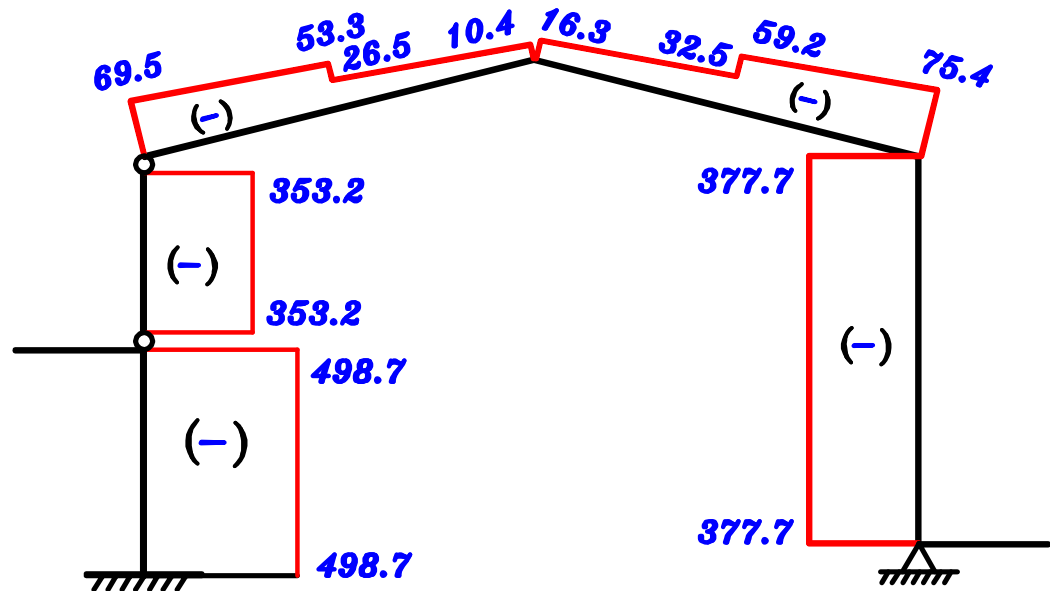


1 I.F.D. For the Frame.

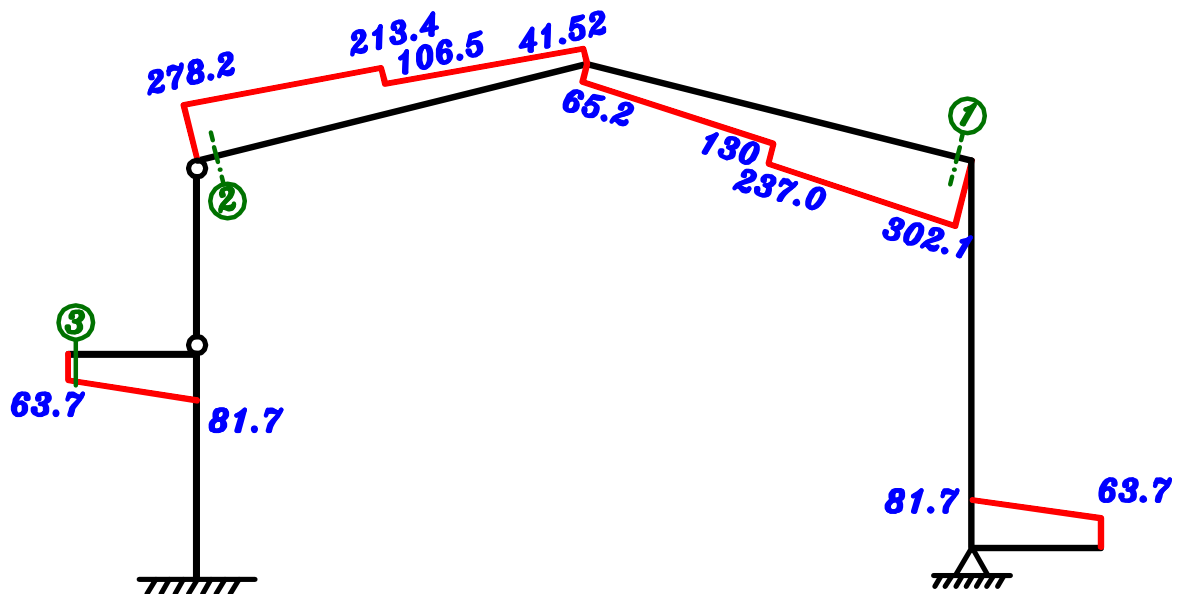
B.M.D.
(U.L.)



N.F.D.
(U.L.)



S.F.D.
(U.L.)



Design of Sections.

Sec. ①

$$M = 989.25 \text{ kN.m} , P = 10.4 \text{ kN} , b = 350 \text{ mm}$$

$$d_o = 3.5 \sqrt{\frac{989.25 * 10^6}{25 * 350}} = 1176.8 \text{ mm} \quad (\text{as R-Sec.})$$

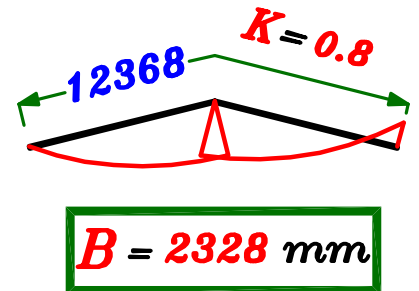
$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1176.8) = (1294.5 \rightarrow 1529) \text{ mm}$$

$$\text{Take } d = 1300 \text{ mm} , t = 1300 + 100 = 1400 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{10.4 * 10^3}{25 * 350 * 1400} = 0.00085 < 0.04 \therefore (\text{neglect } P)$$

The sec. will be T-sec.

$$B = \left\{ \begin{array}{l} \text{C.L. - C.L. = Spacing} = 6.0 \text{ m} = 6000 \text{ mm} \\ 16 t_s + b = 16 * 140 + 350 = 2590 \text{ mm} \\ K \frac{L}{5} + b = 0.8 * \frac{12368}{5} + 350 = 2328 \text{ mm} \end{array} \right\}$$



$$\text{Take } C_1 = 6.0 \rightarrow J = 0.826$$

$$\therefore d = 6.0 \sqrt{\frac{989.25 * 10^6}{25 * 2328}} = 782.2 \text{ mm}$$

$$\therefore \text{Take } d = 800 \text{ mm} , t = 850 \text{ mm}$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{989.25 * 10^6}{0.826 * 360 * 782.2} = 4253 \text{ mm}^2$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 4253 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 800 = 875 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 4253 \text{ mm}^2 \quad (12 \phi 22)$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{22 + 25} = 6.91 = 6.0 \text{ bars}$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 4253 \quad (4 \phi 12)$$

Sec. ② $M = 145.5 \text{ kN.m}$, $P = 75.4 \text{ kN}$, $b = 350 \text{ mm}$

$d = 800 \text{ mm}$ (the same depth of Sec. ①)

Check $\frac{P}{F_{cu} b t} = \frac{75.4 * 10^3}{25 * 350 * 850} = 0.010 < 0.04 \therefore (\text{neglect } P)$

$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \therefore 800 = c_1 \sqrt{\frac{145.5 * 10^6}{25 * 350}} \rightarrow c_1 = 6.20 \rightarrow J = 0.826$

$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{145.5 * 10^6}{0.826 * 360 * 800} = 611 \text{ mm}^2$

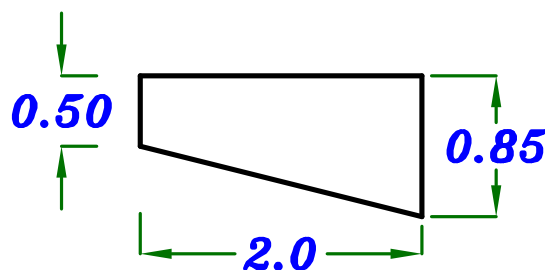
Check $A_{s_{min.}}$ $A_{s_{req.}} = 611 \text{ mm}^2$

$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 800 = 875 \text{ mm}^2$

$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$

$A_{s_{min.}} = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 800 = 875 \text{ mm}^2$ } الأقل
 $1.3 A_{s_{req.}} = 1.3 * 611 = 794.3 \text{ mm}^2$ } = 794.3 mm² (3 ϕ 22)

$Y = \left\{ \begin{array}{l} \frac{t}{2} = \frac{850}{2} = 425 = 450 \text{ mm} \\ t_b = \frac{\text{spacing}}{12} = \frac{6000}{12} = 500 \text{ mm} \\ t - \frac{L_c}{3} = 850 - \frac{2000}{3} = 183 \text{ mm} \end{array} \right\} Y = 500 \text{ mm}$



Sec. ③ R-Sec. $M = 145.5 \text{ kN.m}$, $P = 377.7 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{145.5 * 10^6}{25 * 350}} = 451.3 \text{ mm (as R-Sec.)}$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (451.3) = (496.4 \rightarrow 586.7) \text{ mm}$$

$$\therefore \text{Take } d = 500 \text{ mm} , t = 550 \text{ mm}$$

$$\therefore t_{(Column)} < 0.8 t_{(Beam)} \xrightarrow{\text{Take}} t_{(Column)} = t_{(Beam)} = 850 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{377.7 * 10^3}{25 * 350 * 850} = 0.0507 > 0.04 \text{ (Don't neglect } P \text{)}$$

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{145.5}{377.7} = 0.385 \text{ m} \therefore \frac{e}{t} = \frac{0.385}{0.85} = 0.45 < 0.5 \xrightarrow{\text{Use}} \text{I.D.}$$

\therefore Use Interaction Diagram

$$\zeta = \frac{850 - 100}{850} = 0.88 = 0.80 \xrightarrow{\text{use}} \text{ECSS Design Aids Page 4-24}$$

$$\left. \begin{aligned} \frac{P_U}{F_{cu} b t} &= \frac{377.7 * 10^3}{25 * 350 * 850} = 0.0507 \\ \frac{M_U}{F_{cu} b t^2} &= \frac{145.5 * 10^6}{25 * 350 * 850^2} = 0.023 \end{aligned} \right\} \rho < 1.0 \xrightarrow{\text{Take}} \rho = 1.0$$

$$\mu = \rho * F_{cu} * 10^{-4} = 1.0 * 25 * 10^{-4} = 2.5 * 10^{-3}$$

$$A_s = A_{s'} = \mu * b * t = 2.5 * 10^{-3} * 350 * 850 = 743 \text{ mm}^2$$

$$\text{— Check } A_{s_{min.}} = \frac{0.8}{100} * b * t = \frac{0.8}{100} * 350 * 850 = 2380 \text{ mm}^2$$

$$A_{s_{Total}} = A_s + A_{s'} = 2 * 743 = 1486 \text{ mm}^2 \therefore A_{s_{Total}} < A_{s_{min.}}$$

$$\therefore \text{take } A_s = A_{s'} = \frac{A_{s_{min.}}}{2} = \frac{2380}{2} = 1190 \text{ mm}^2 \quad \textcircled{4 \phi 22}$$

Sec. ④ (350*400)

Axially Loaded Column. $P = 353.2 \text{ kN}$

$$\therefore P_{U.L.} = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

$$\therefore 353.2 * 10^3 = 0.35 (350 * 400) (25) + 0.67 A_s (360)$$

$$\therefore A_s = - 3614 \text{ mm}^2 = (-Ve) \text{ Value}$$

$$\therefore A_s = A_{s_{min.}} = \frac{0.8}{100} * 350 * 400 = 1120 \text{ mm}^2 \quad \textcircled{10 \phi 12}$$

Check Shear.

– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\gamma_g}} = 0.7 \sqrt{\frac{25}{1.5}} = 2.85 \text{ N/mm}^2$$

$$\text{Sec. ①} \quad Q = 302.1 \text{ kN}$$

$$q_u = \frac{Q}{b d} = \frac{302.1 * 10^3}{350 * 800} = 1.07 \text{ N/mm}^2$$

$$\therefore q_{cu} < q_u < q_{max.} \therefore \text{We need Stirrups more Than } 5 \phi 8 \text{ \textbackslash m}$$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \backslash \delta_s)}{b S}$$

$$* \text{Take } n = 2, \phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$$

$$1.07 - \frac{0.98}{2} = \frac{2 * 50.3 (240 \backslash 1.15)}{350 * S} \rightarrow S = 103.4 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups \textbackslash m} = \frac{1000}{S} = \frac{1000}{103.4} = 9.67 = 10$$

$$\therefore \text{Use Stirrups } \boxed{10 \phi 8 \text{ \textbackslash m}} \text{ 2 branches}$$

Sec. ② $Q = 278.2 \text{ kN}$

$$q_u = \frac{Q}{b d} = \frac{278.2 * 10^3}{350 * 800} = 0.993 \text{ N/mm}^2$$

$\therefore q_{cu} < q_u < q_{max.}$ \therefore We need Stirrups more Than $5 \phi 8 \setminus m$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \setminus \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

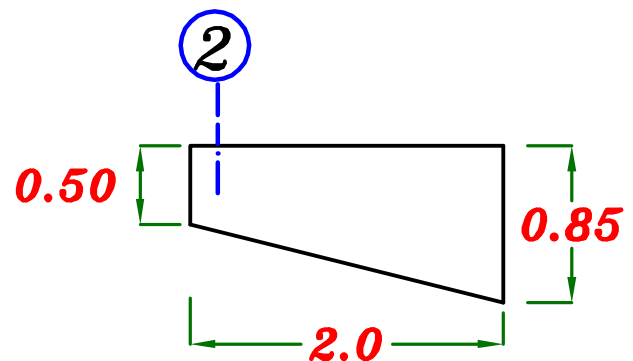
$$0.993 - \frac{0.98}{2} = \frac{2 * 50.3 (240 \setminus 1.15)}{350 * S} \rightarrow S = 119.2 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups} \setminus m = \frac{1000}{S} = \frac{1000}{119.2} = 8.39 = 9.0$$

\therefore Use Stirrups $9 \phi 8 \setminus m$ 2 branches

Sec. ③ $Q = 63.7 \text{ kN}$

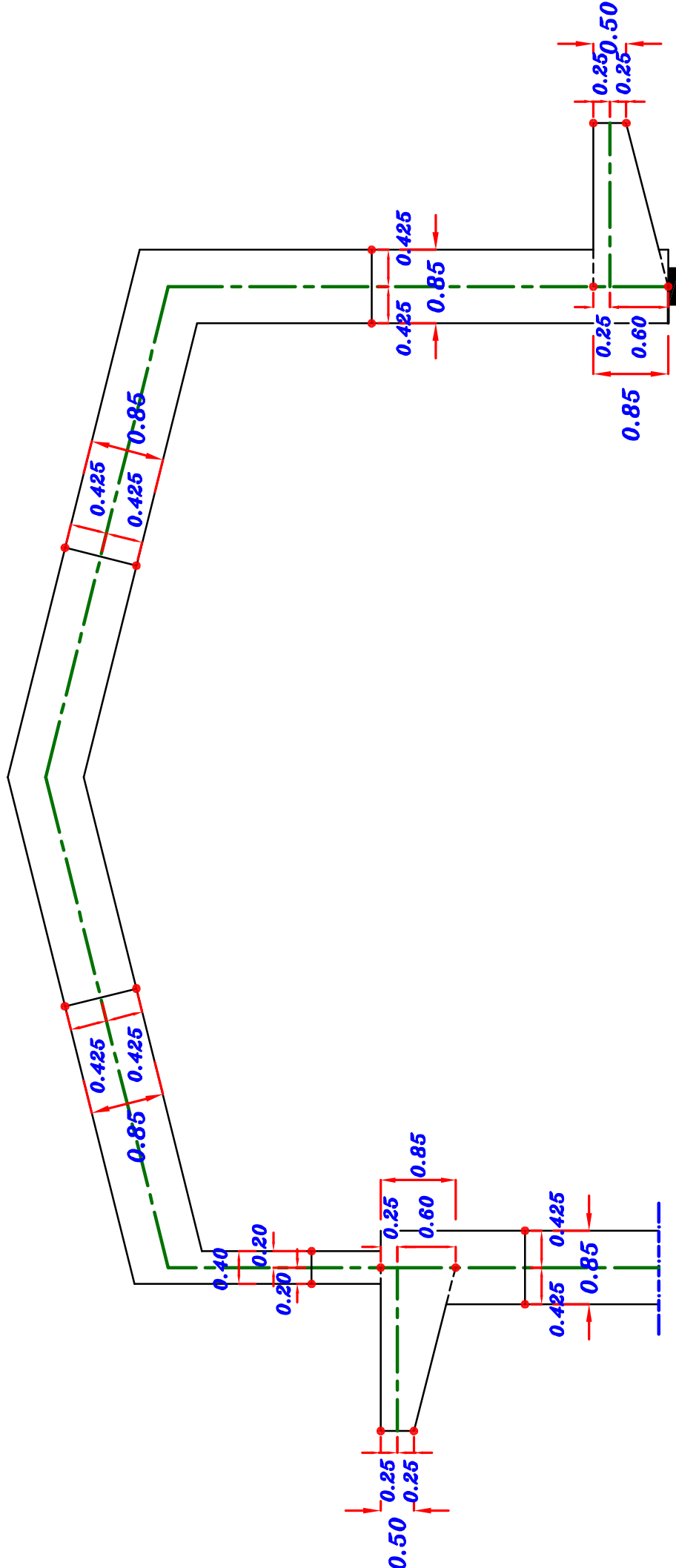
$\tan \beta = \text{Zero}$

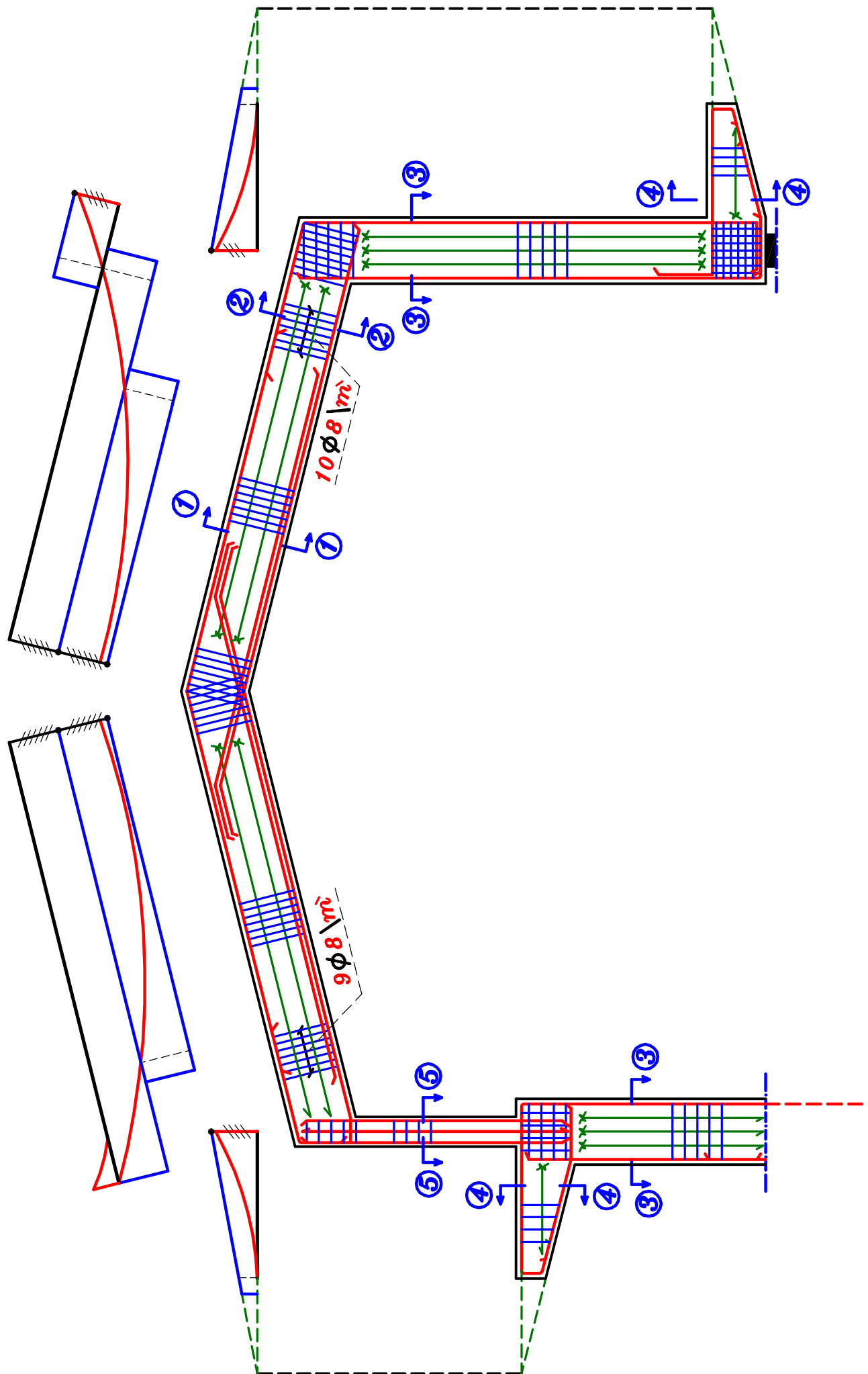


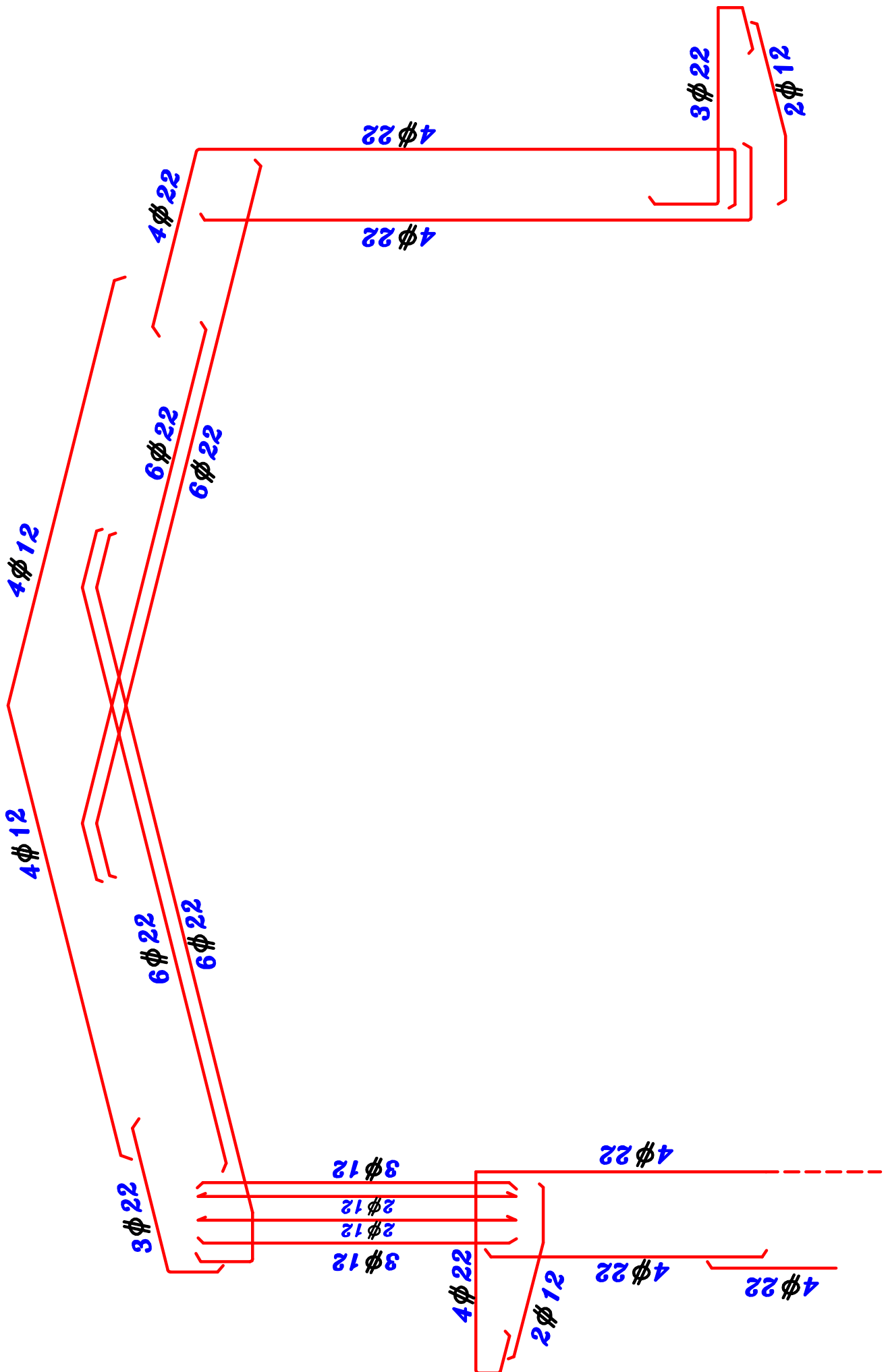
$$\therefore \text{Actual shear stress.} = q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

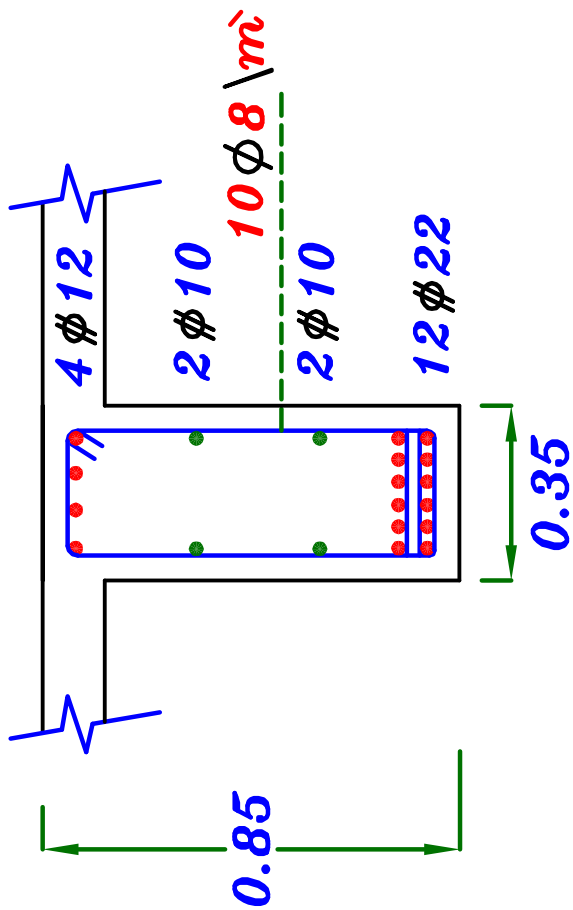
$$= \frac{63.7 * 10^3}{350 * 450} - \text{ZERO} = 0.404 \text{ N/mm}^2$$

$\therefore q_u < q_{cu} \rightarrow$ Use min. stirrups $5 \phi 8 \setminus m$

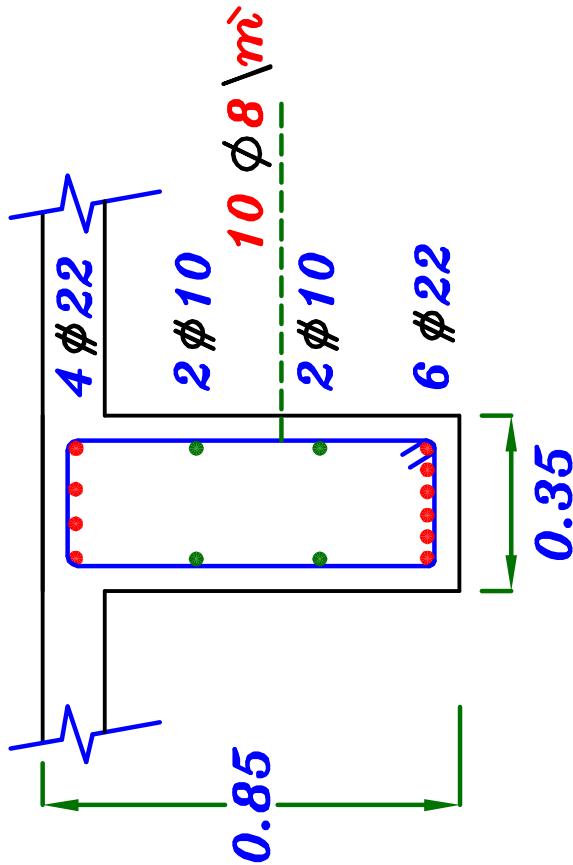




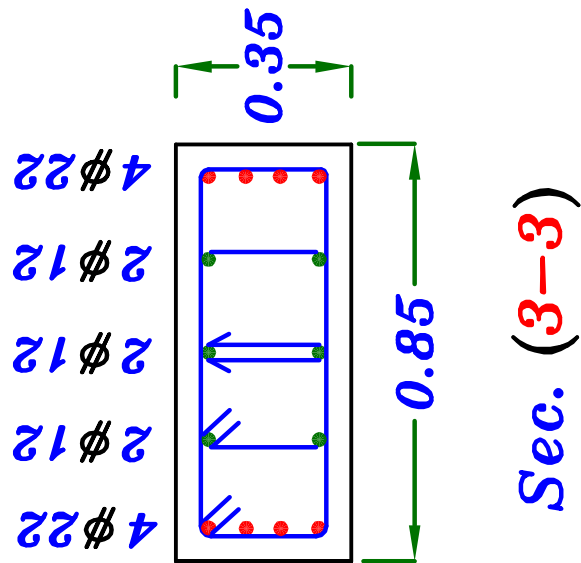




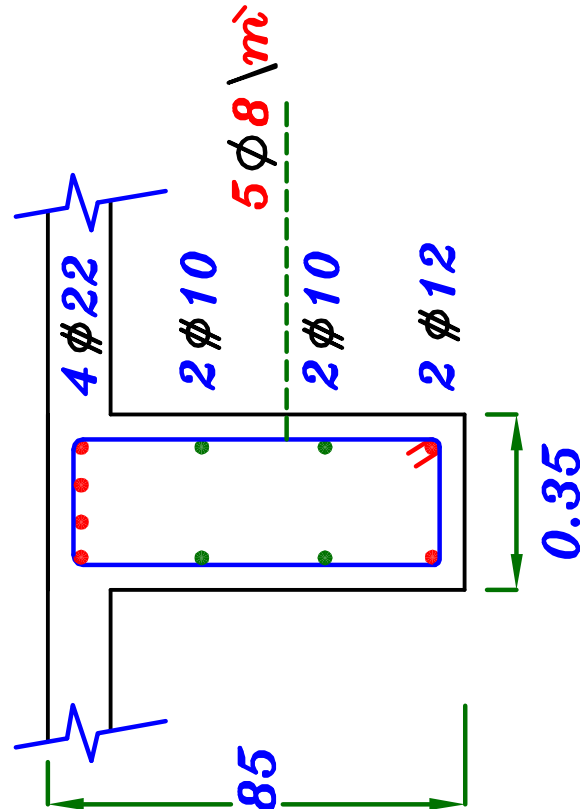
Sec. (1-1)



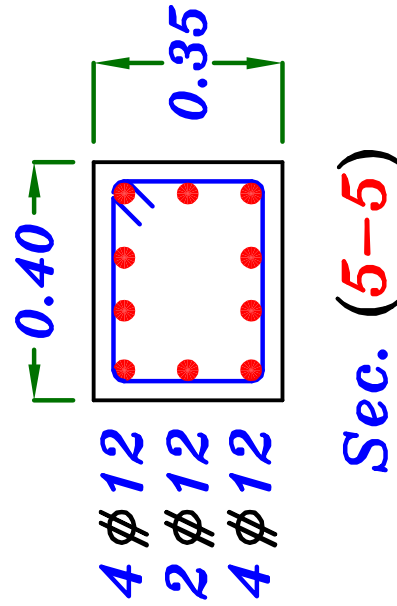
Sec. (2-2)



Sec. (3-3)

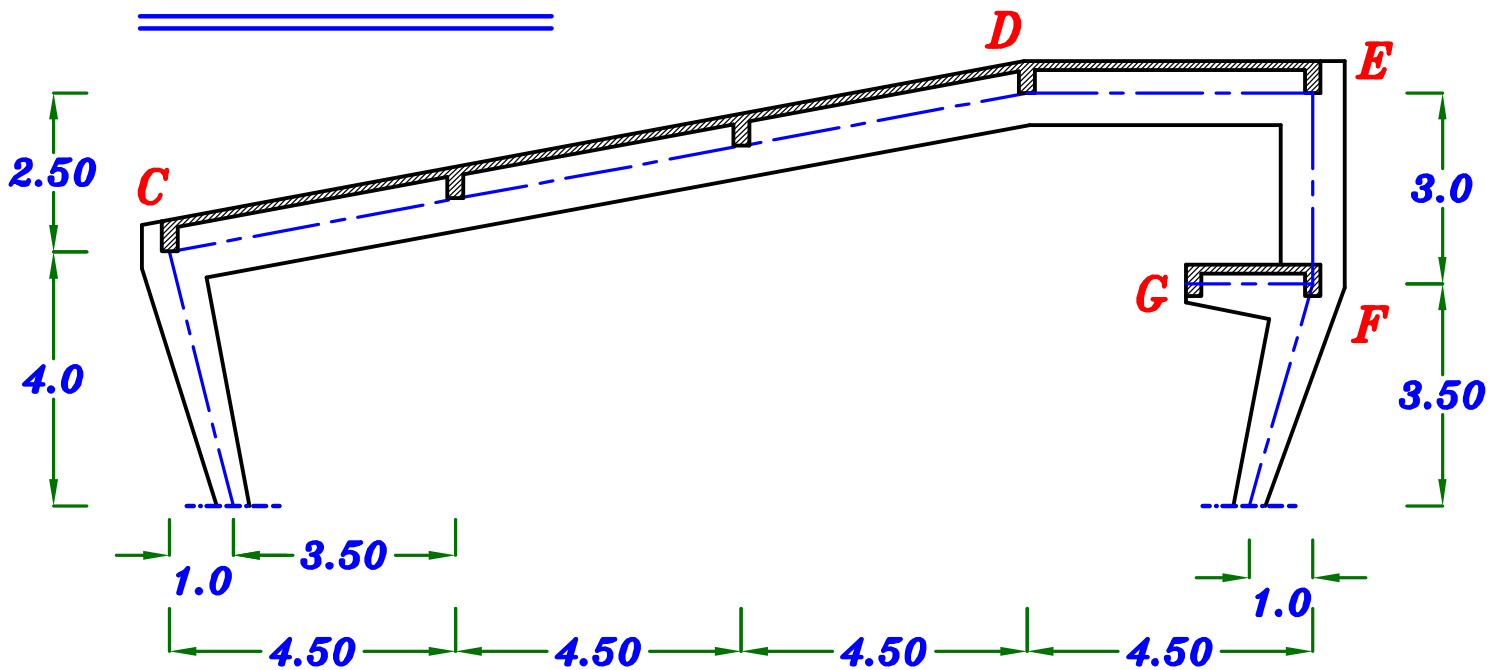


Sec. (4-4)



Sec. (5-5)

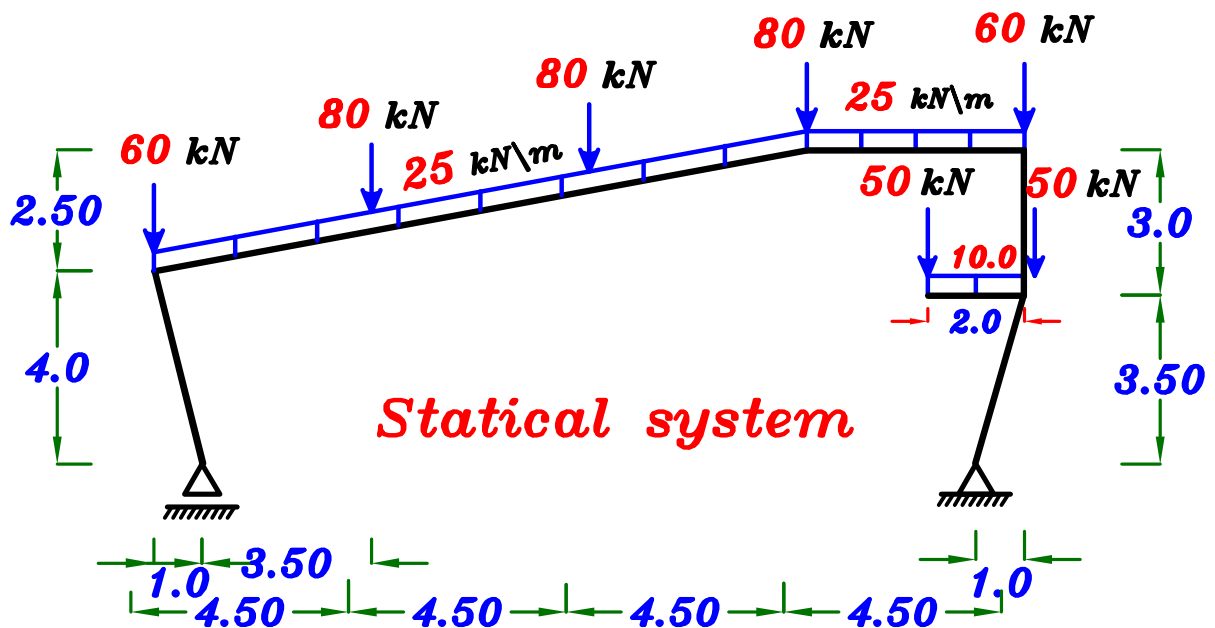
Example.



Data.

$$F_{cu} = 30 \text{ N/mm}^2 \quad F_y = 360 \text{ N/mm}^2$$

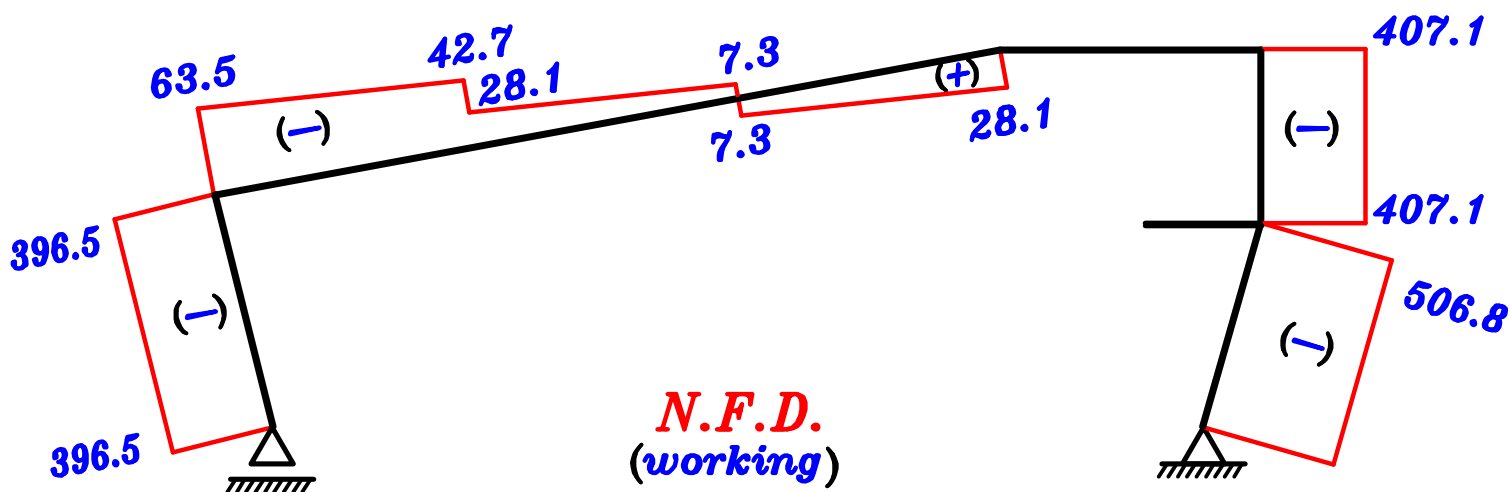
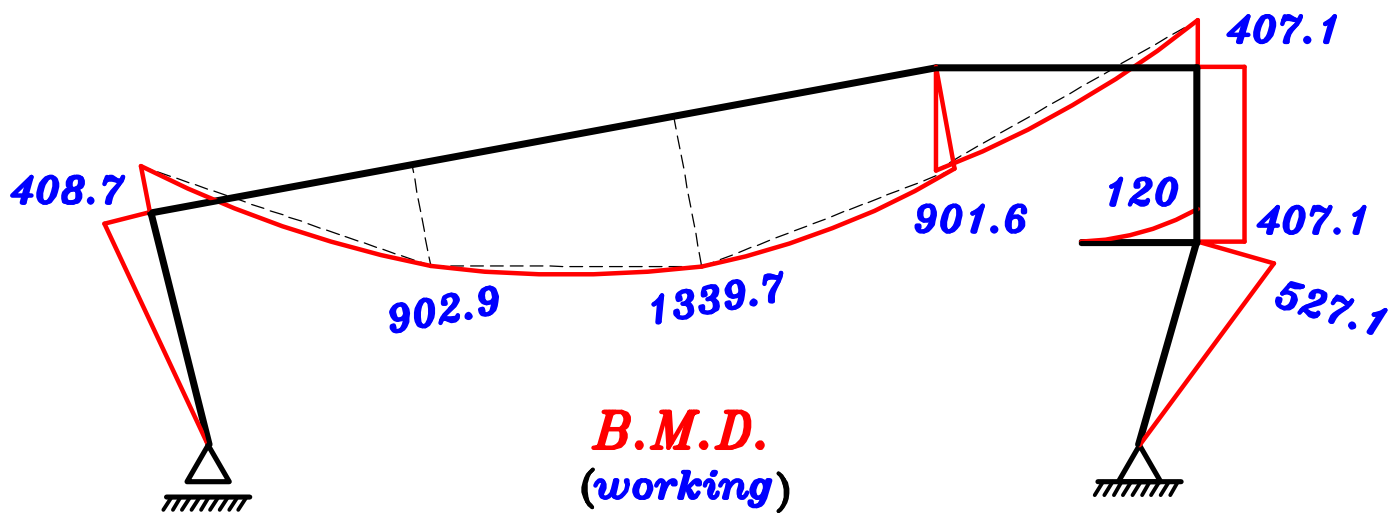
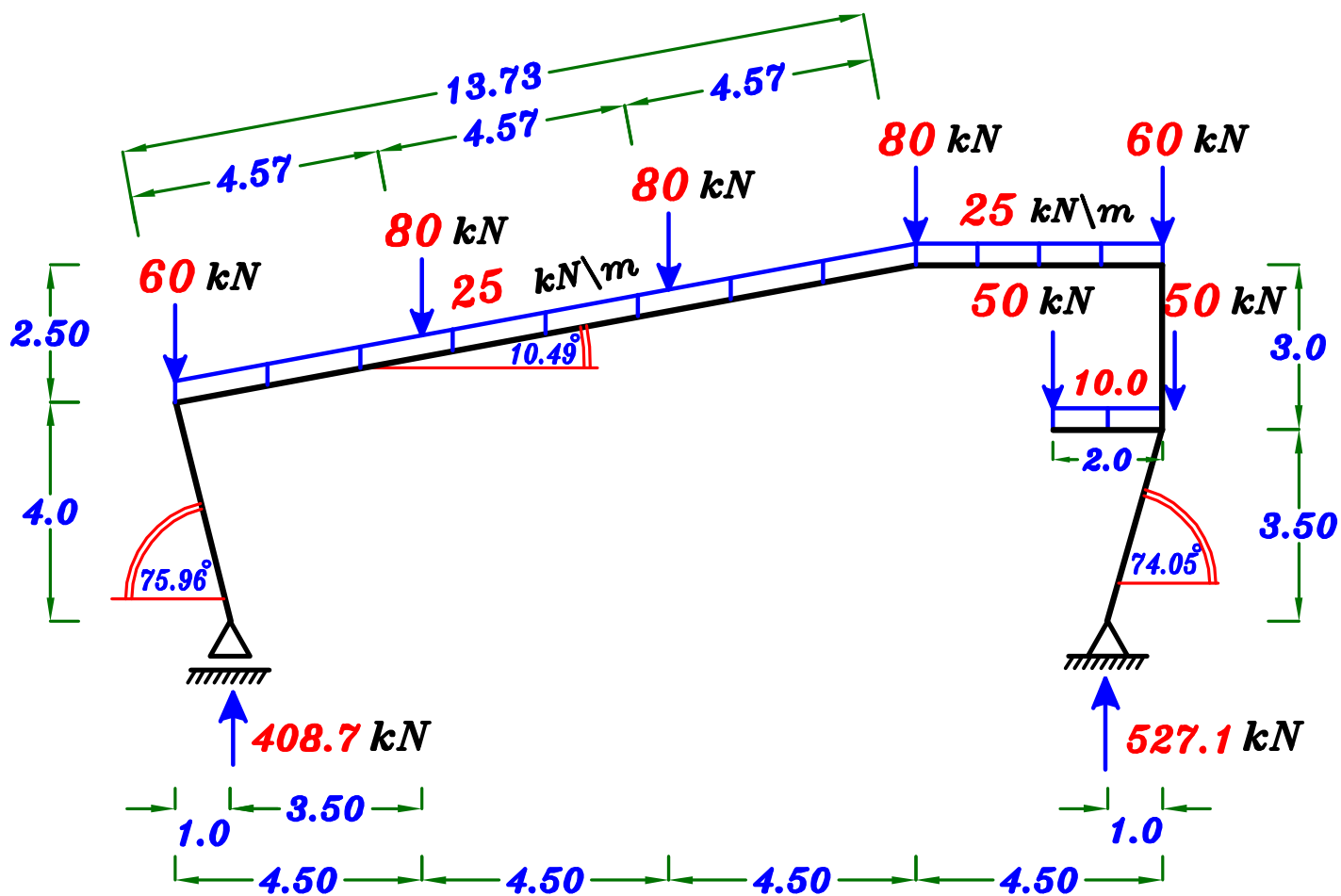
$$t_s = 120 \text{ mm} \quad \text{Spacing} = 6.0 \text{ m}$$

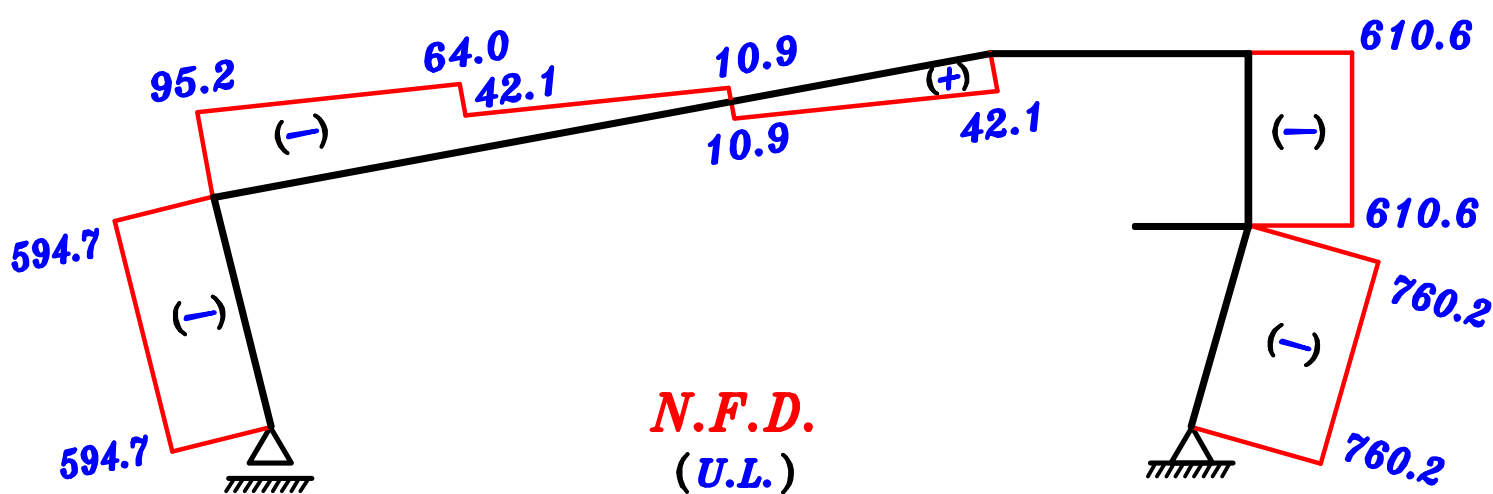
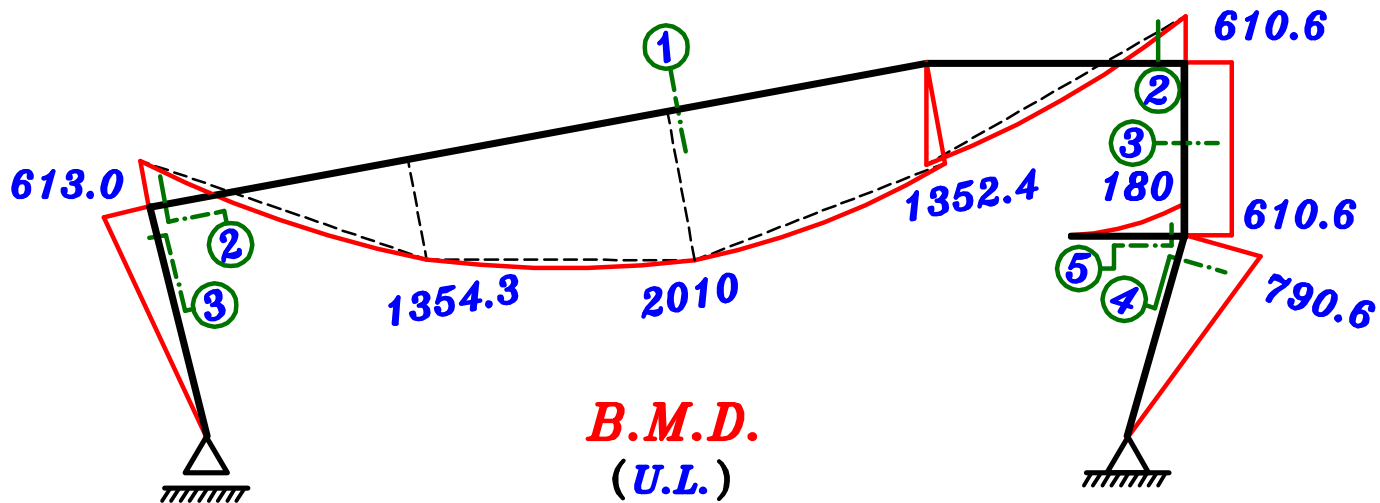


Static system

Req.

- 1- For the given working loads, draw the bending moment Shear Force, Normal Force diagrams of the Frame.
- 2- Using Ultimate Limit Design Method, design the critical sections of the Frame.
- 3- Check shear stresses For part (F G) of the Frame and Find the required shear reinforcement if necessary.
- 4- Draw moment of resistance diagram For part (C D E) only.
- 5- Draw to scale 1:50 an elevation of the Frame showing clearly the arrangement of the reinforcement. Draw to scale 1:25 cross-sections For the designed critical sections.





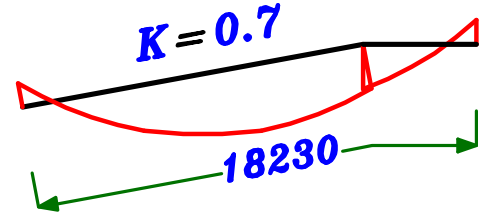
Design of Sections.

Take $b_{(Frame)} = 400 \text{ mm}$

Sec. ① $M = 2010 \text{ kN.m}$, $T = 10.9 \text{ kN}$ (Can be neglected)

The sec. will be T-sec.

$$B = \left\{ \begin{array}{l} \text{C.L. - C.L.} = \text{spacing} = 6.0 \text{ m} = 6000 \text{ mm} \\ 16t_s + b = 16 * 120 + 400 = 2320 \text{ mm} \\ K \frac{L}{5} + b = 0.7 * \frac{18230}{5} + 400 = 2952 \text{ mm} \end{array} \right\}$$



$$B = 2320 \text{ mm}$$

Take $C_1 = 6.0 \rightarrow J = 0.826$

$$\therefore d = 6.0 \sqrt{\frac{2010 * 10^6}{30 * 2320}} = 1019 \simeq 1000 \text{ mm}$$

\therefore Take $d = 1000 \text{ mm}$, $t = 1100 \text{ mm}$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{2010 * 10^6}{0.826 * 360 * 1000} = 6759 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 6759 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1000 = 1369.3 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 6759 \text{ mm}^2 \quad \text{14 } \phi 25$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 6759 \quad \text{6 } \phi 12$$

Sec. ② $M = 613.0 \text{ kN.m}$, $P = 95.2 \text{ kN}$, $b = 400 \text{ mm}$

$d = 1000 \text{ mm}$ (the same depth of Sec. ①)

Check $\frac{P}{F_{cu} b t} = \frac{95.2 * 10^3}{30 * 400 * 1100} = 0.0072 < 0.04 \therefore (\text{neglect } P)$

$\therefore d = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}} \therefore 1000 = c_1 \sqrt{\frac{613.0 * 10^6}{30 * 400}} \rightarrow c_1 = 4.42 \rightarrow J = 0.816$

$\therefore A_s = \frac{M_{u.L.}}{J F_y d} = \frac{613.0 * 10^6}{0.816 * 360 * 1000} = 2086 \text{ mm}^2$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2086 \text{ mm}^2$

$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1000 = 1369.3 \text{ mm}^2$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2086 \text{ mm}^2$ $5 \phi 25$

Sec. ③ R-Sec. $M = 613.0 \text{ kN.m}$, $P = 594.7 \text{ kN}$

$d_o = 3.5 \sqrt{\frac{613.0 * 10^6}{30 * 400}} = 791 \text{ mm}$ (as R-Sec.)

$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (791) = (870 \rightarrow 1028) \text{ mm}$

$\therefore \text{Take } d = 1000 \text{ mm} , t = 1100 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{594.7 * 10^3}{30 * 400 * 1100} = 0.045 > 0.04$ (Don't neglect P)

\therefore Design the Sec. on both N.F. & B.M.

$e = \frac{M}{P} = \frac{613.0}{594.7} = 1.03 \text{ m} \therefore \frac{e}{t} = \frac{1.03}{1.10} = 0.93 > 0.5 \xrightarrow{\text{Use}} e_s$

$e_s = e + \frac{t}{2} - C = 1.03 + \frac{1.10}{2} - 0.10 = 1.48 \text{ m}$

$$M_s = P * e_s = 594.7 * 1.48 = 880.1 \text{ kN.m}$$

$$\therefore 1000 = C_1 \sqrt{\frac{880.1 * 10^6}{30 * 400}} \rightarrow C_1 = 3.69 \rightarrow J = 0.79$$

$$A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \delta_s)}$$

$$= \frac{880.1 * 10^6}{0.79 * 360 * 1000} - \frac{594.7 * 10^3}{(360 \setminus 1.15)} = 1195 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1195 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1000 = 1369.3 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$A_{s_{min.}} = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1000 = 1369.3 \text{ mm}^2$$

$$1.3 A_{s_{req.}} = 1.3 * 1195 = 1553.5 \text{ mm}^2$$

الأقل } = 1369.3 \text{ mm}^2

3 ϕ 25

Sec. ④ R-Sec. $M = 790.6 \text{ kN.m}$, $P = 760.2 \text{ kN}$

$d = 1000 \text{ mm}$ (the same depth of Sec. ③)

Check $\frac{P}{F_{cu} b t} = \frac{760.2 * 10^3}{30 * 400 * 1100} = 0.057 > 0.04$ (Don't neglect P)

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{790.6}{760.2} = 1.04 \text{ m} \quad \therefore \frac{e}{t} = \frac{1.04}{1.10} = 0.94 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.04 + \frac{1.10}{2} - 0.10 = 1.49 \text{ m}$$

$$M_s = P * e_s = 760.2 * 1.49 = 1132.7 \text{ kN.m}$$

$$\therefore 1000 = C_1 \sqrt{\frac{1132.7 * 10^6}{30 * 400}} \rightarrow C_1 = 3.25 \rightarrow J = 0.765$$

$$A_s = \frac{M_s}{J F_y d} - \frac{P_{u.l.}}{(F_y \setminus \delta_s)} = \frac{1132.7 * 10^6}{0.765 * 360 * 1000} - \frac{760.2 * 10^3}{(360 \setminus 1.15)} = 1685 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1685 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1000 = 1369.3 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1685 \text{ mm}^2 \quad (4 \phi 25)$$

Sec. ⑤ $M = 180 \text{ kN.m}$, $b = 400 \text{ mm}$

$$d = 3.5 \sqrt{\frac{180 * 10^6}{30 * 400}} = 428.6 \text{ mm (as R-Sec.)}$$


$$\therefore \text{Take } d = 450 \text{ mm} , t = 500 \text{ mm}$$

$$\therefore A_s = \frac{M_{u.l.}}{J F_y d} = \frac{180 * 10^6}{0.78 * 360 * 428.6} = 1495 \text{ mm}^2$$

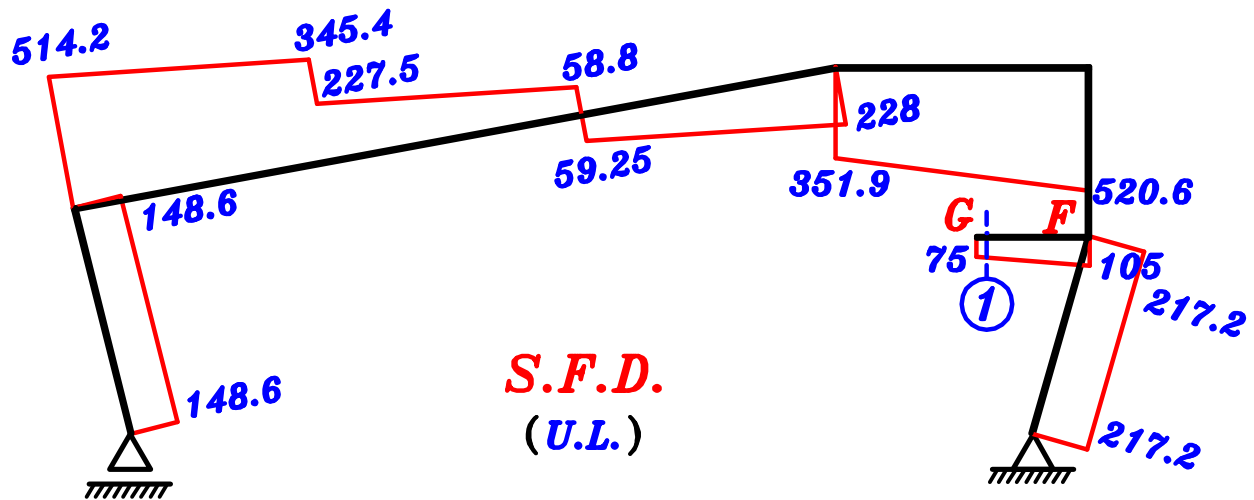
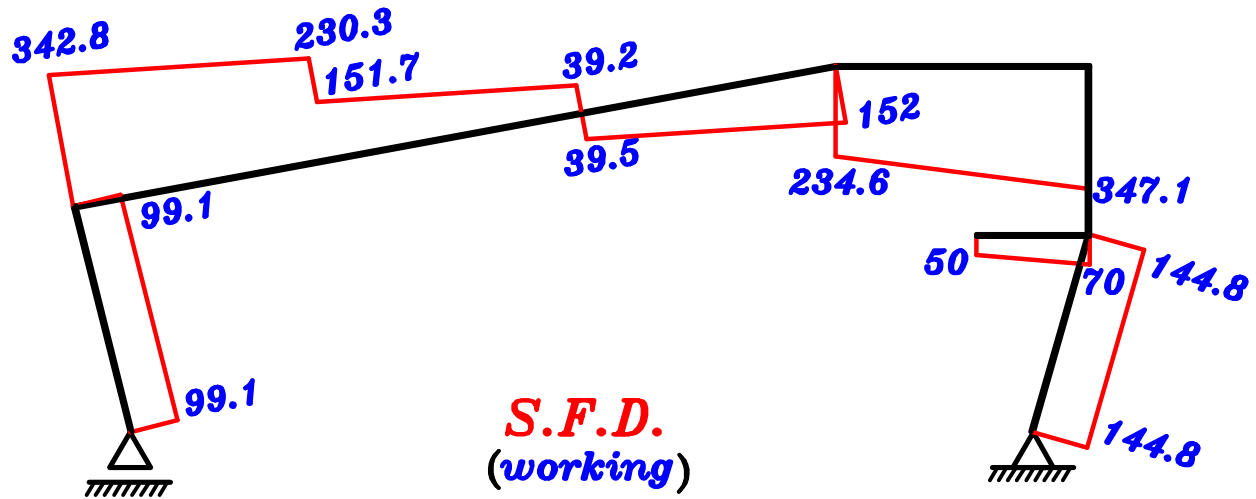
Check $A_{s_{min.}}$ $A_{s_{req.}} = 1495 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1000 = 1369.3 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1495 \text{ mm}^2 \quad (4 \phi 25)$$

Take $Y = 0.40 \text{ m}$ 

Check Shear. For part ((F G))



- Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_o}} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

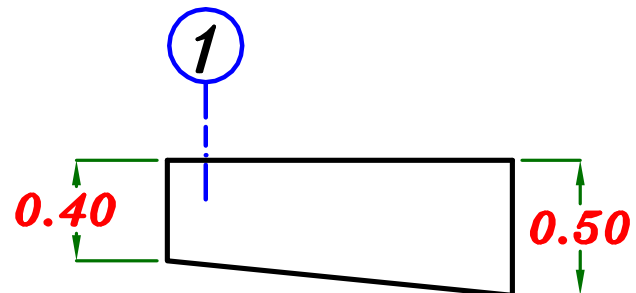
$$- q_{max.} = 0.70 \sqrt{\frac{F_{cu}}{\delta_o}} = 0.70 \sqrt{\frac{30}{1.5}} = 3.13 \text{ N/mm}^2$$

Sec. ① $Q = 75.0 \text{ kN}$

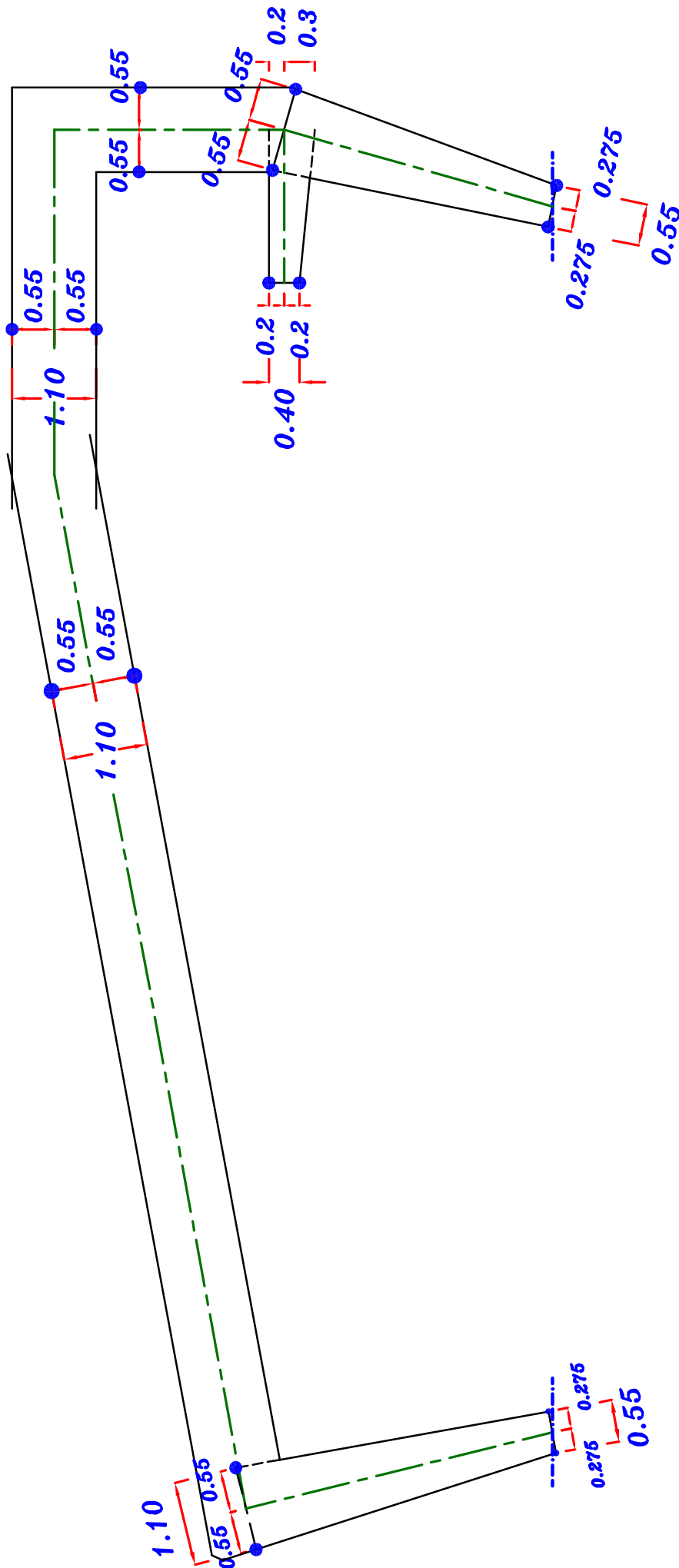
∴ Actual shear stress. =

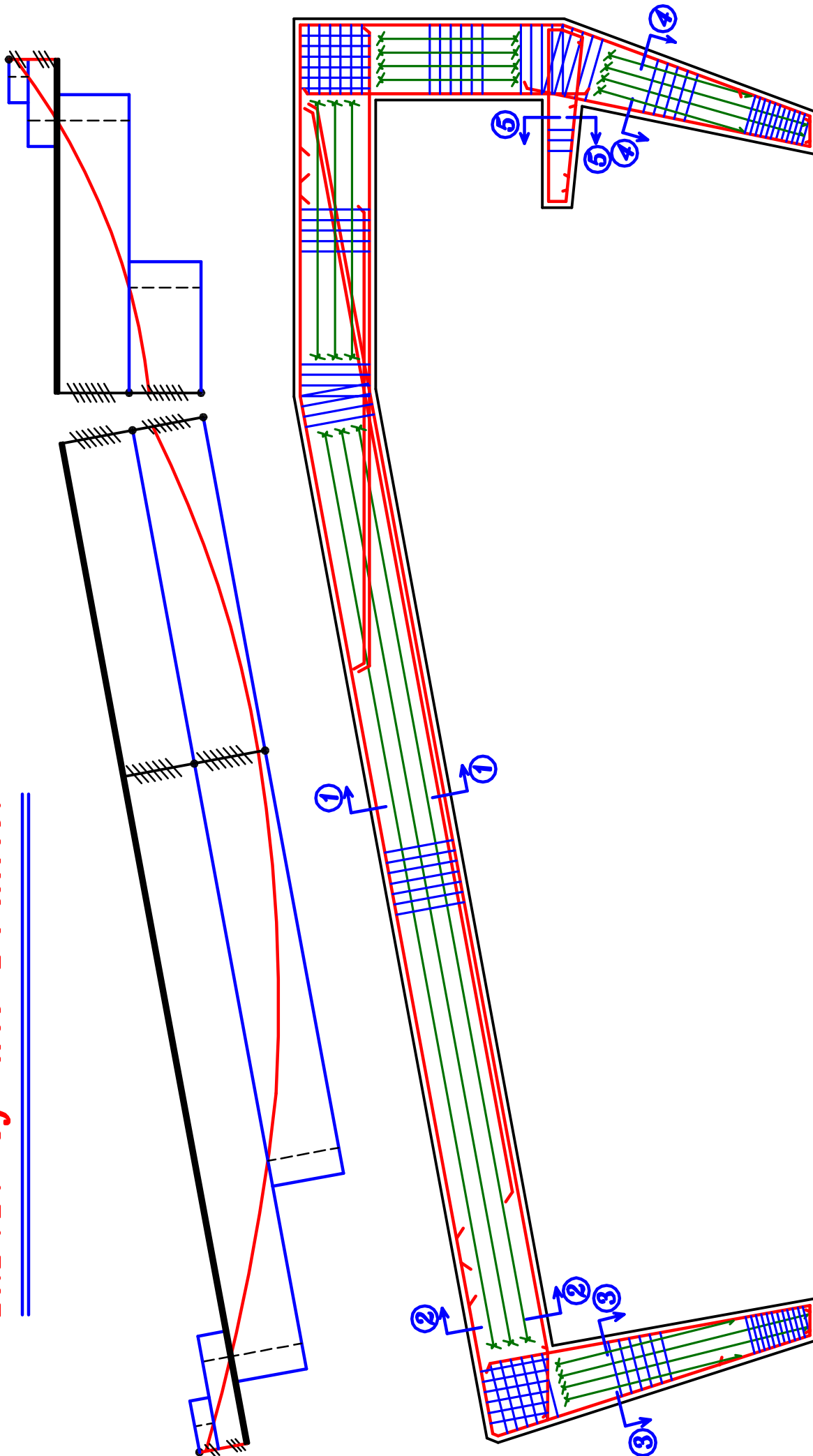
$$q_U = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

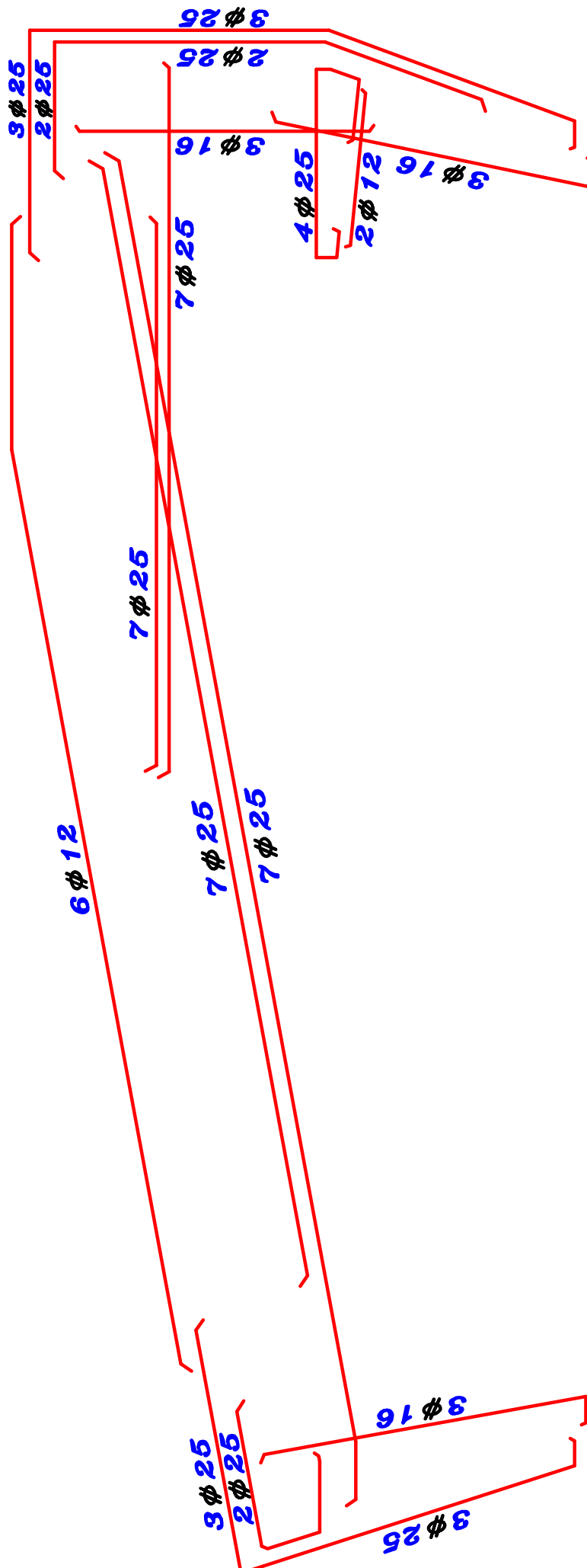
$$= \frac{75.0 * 10^3}{400 * 350} - \text{ZERO} = 0.535 \text{ N/mm}^2$$

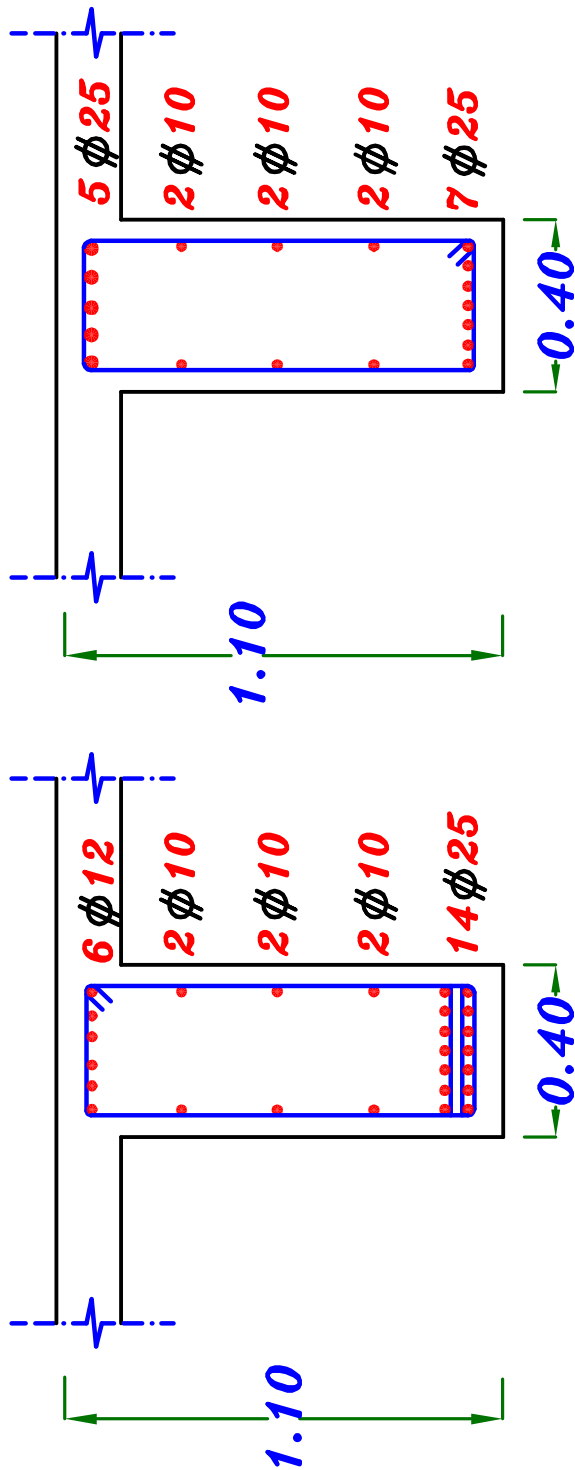


∴ $q_U < q_{cu} \longrightarrow$ Use min. stirrups **5 ϕ 8 \ m**



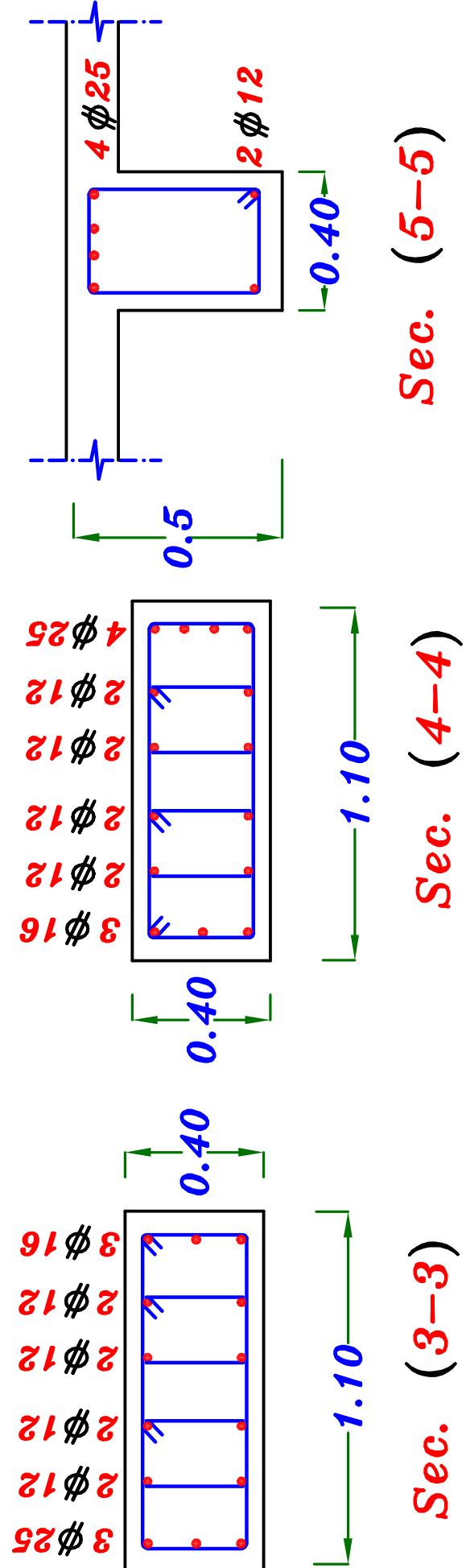






Sec. (2-2)

Sec. (1-1)



Sec. (3-3)

Sec. (4-4)

Sec. (5-5)

Example.

Figure (1) shows a sectional elevation of a reinforced concrete structure, The structure consists of reinforced concrete slabs supported by a system of secondary beams and Frame (**F**), spaced at 5.0 m It is required to :

- 1- Calculate the equivalent working loads For shear and moment For Beam (**B**).
- 2- Using the limit state design method (L.S.D.M.), design the critical sections For the Beam (**B**) to satisfy the internal Forces requirements and then draw its details of reinforcement in elevation to scale **1:50** and cross sections to scale **1:25** Imperical curtailment of bars is required.
- 3- Draw the N.F.D. , S.F.D. & B.M.D. For the intermediate Frame (**F**).
Using the given working loads.
- 4- Design the critical sections of Frame (**F**) to satisfy the internal Forces requirments using (**L.S.D.M**)
- 5- Draw details of reinforcement For Frame (**F**) in elevation to scale **1:50** and cross sections to scale **1:25**
Curtailment of bars using the moment of resistance diagram is required.

Data:

- Concrete characteristic strength $F_{cu} = 25 \text{ N/mm}^2$
- Steel used is St. 360/520
- Slab thickness $t_s = 150 \text{ mm}$
- Floor cover $F.C. = 2.0 \text{ kN/m}^2$
- Live Load on slabs $L.L. = 5 \text{ kN/m}^2/\text{HL. projection}$
- Own weight of beams $= 3.5 \text{ kN/m}$
- Own weight of Frames $= 7.0 \text{ kN/m}$
- $\gamma_{brick} = 16.0 \text{ kN/m}^3$

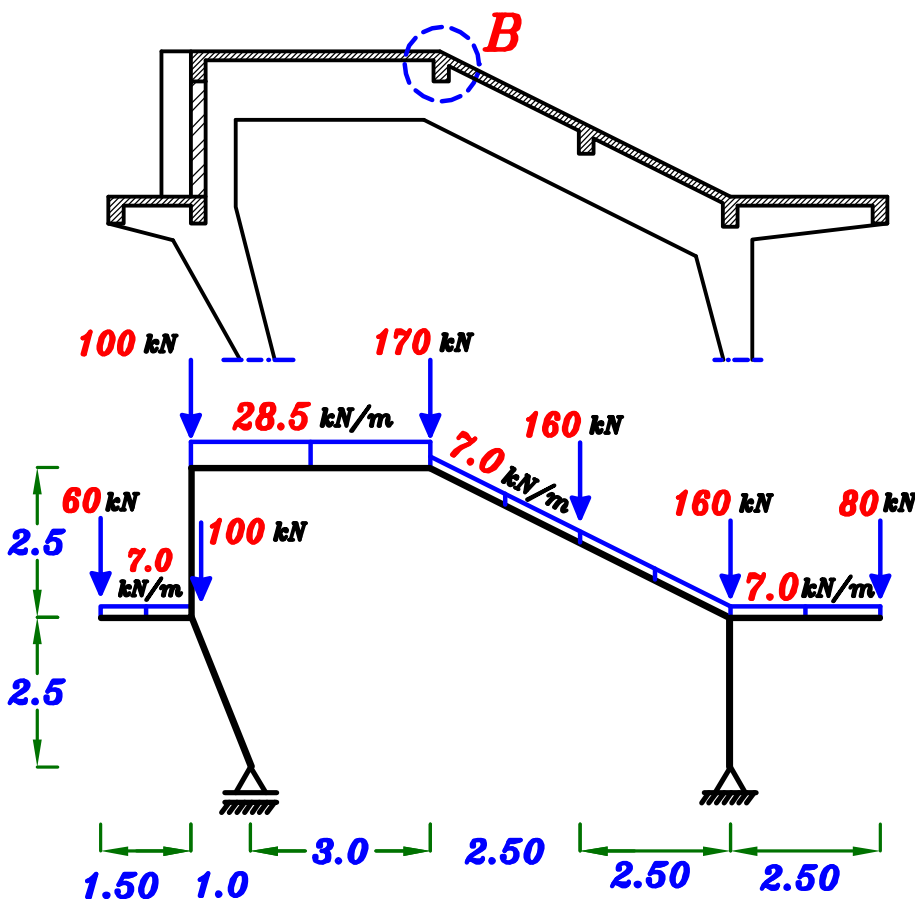
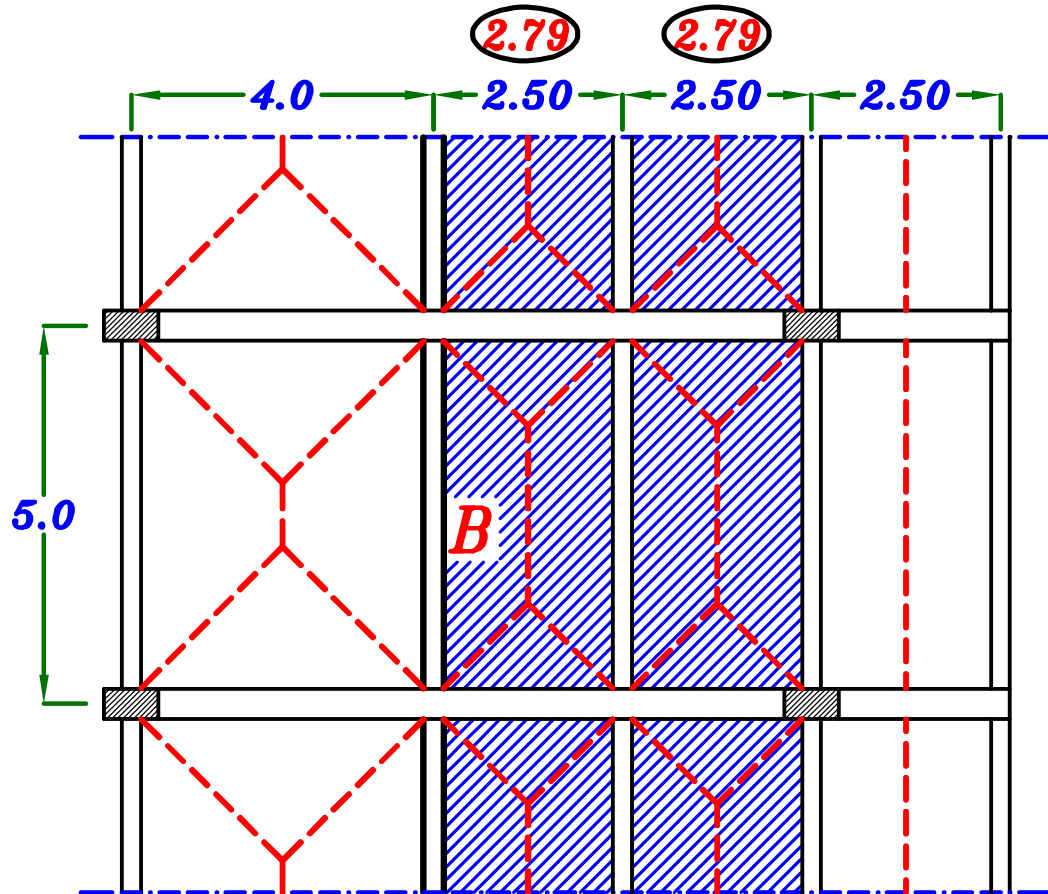


Figure (1)

1- Calculate the equivalent working loads For shear and moment For Beam (B).

$$\theta = 26.56^\circ$$



* For Horizontal Slab.

$$w_{sh} = o.w. + F.C. + L.L. = 0.15 * 25 + 2.0 + 5.0$$

$$w_{sh} = 10.75 \text{ kN/m}^2$$

$$C_a = 1 - \frac{1}{2} \left(\frac{4.0}{5.0} \right) = 0.60 \quad C_e = 1 - \frac{1}{3} \left(\frac{4.0}{5.0} \right)^2 = 0.78$$

* For Inclined Slab.

$$w_{si} = o.w. + F.C. + L.L. * \cos \theta$$

$$= 0.15 * 25 + 2.0 + 5.0 * \cos 26.56^\circ = 10.22 \text{ kN/m}^2$$

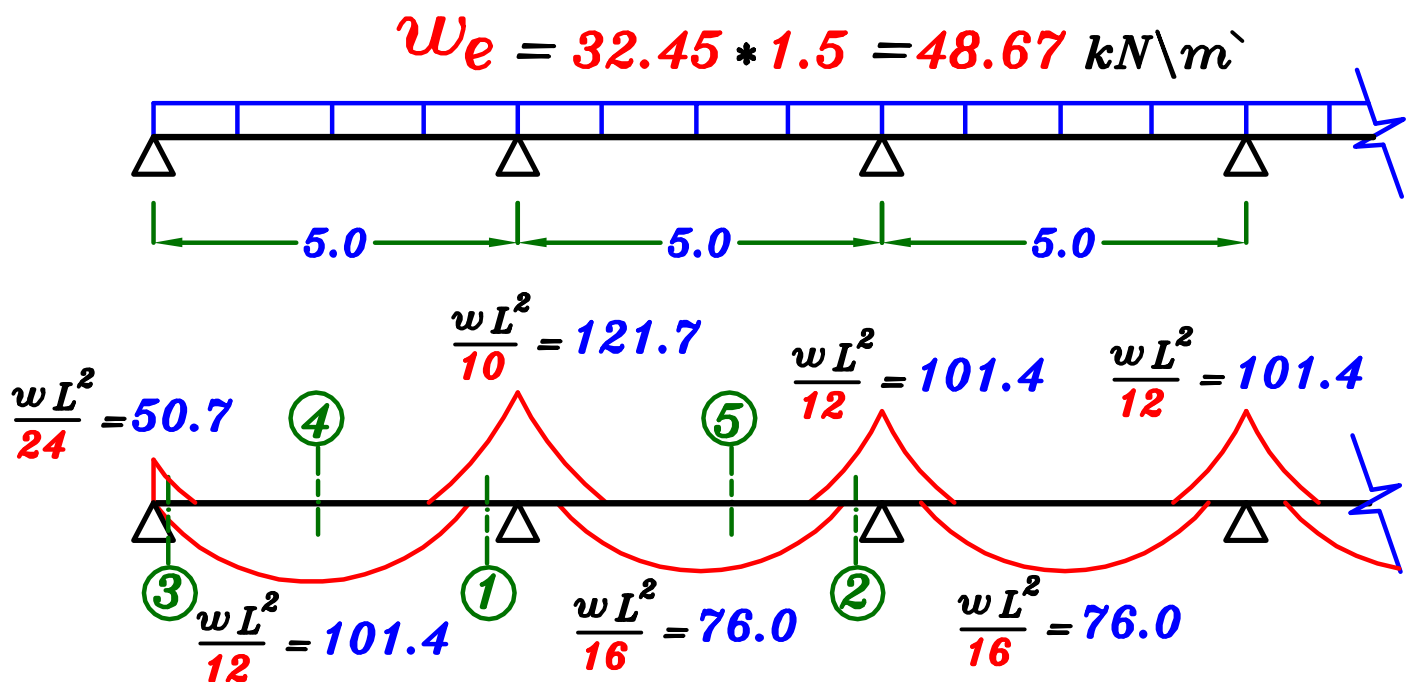
$$w_{si} = 10.22 \text{ kN/m}^2$$

$$C_a = 1 - \frac{1}{2} \left(\frac{2.79}{5.0} \right) = 0.72 \quad C_e = 1 - \frac{1}{3} \left(\frac{2.79}{5.0} \right)^2 = 0.89$$

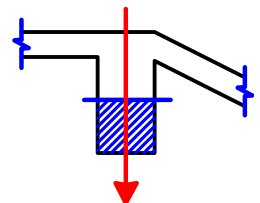
$$\begin{aligned}
 W_a &= 0.W. + C_a w_{sh} \frac{L_s}{2} + C_a w_{si} \frac{L_s}{2} \\
 &= 3.0 + (0.60)(10.75)\left(\frac{4.0}{2}\right) + (0.72)(10.22)\left(\frac{2.79}{2}\right) \\
 &= 26.16 \text{ kN/m}
 \end{aligned}$$

$$\begin{aligned}
 W_e &= 0.W. + C_e w_{sh} \frac{L_s}{2} + C_e w_{si} \frac{L_s}{2} \\
 &= 3.0 + (0.78)(10.75)\left(\frac{4.0}{2}\right) + (0.89)(10.22)\left(\frac{2.79}{2}\right) \\
 &= 32.45 \text{ kN/m}
 \end{aligned}$$

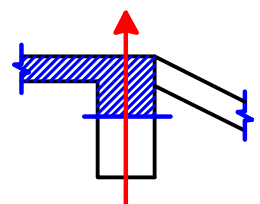
2- Using the limit state design method (L.S.D.M.), design the critical sections For the Beam (B) to satisfy the internal Forces requirements and then draw its details of reinforcement in elevation to scale 1:50 and cross sections to scale 1:25 Imperical curtailment of bars is required.



Sec. ① $M_{U.L.} = 121.7 \text{ kN.m}$ R-Sec.



Sec. ④ $M_{U.L.} = 101.4 \text{ kN.m}$ L-Sec.

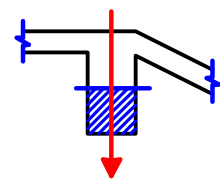


$\therefore M_L < 2 M_R \therefore$ Design R-Sec. First.

Sec. ①

$$M_{U.L.} = 121.7 \text{ kN.m}$$

R-Sec.



- Take C_1 between (3.0 → 4.0) $C_1 = 3.50$

- From charts $C_1 = 3.50 \rightarrow J = 0.78$

$$\text{- Get } d = C_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} = 3.50 \sqrt{\frac{121.7 * 10^6}{25 * 250}} = 488.4 \text{ mm}$$

- Take $d = 500 \text{ mm}$, $t = 550 \text{ mm}$

$$A_s = \frac{M_{U.L.}}{J F_y d} = \frac{121.7 * 10^6}{0.78 * 360 * 488.4} = 887.4 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 887.4 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 500 = 390.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 887.4 \text{ mm}^2$$

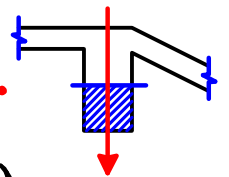
5 ϕ 16

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{250 - 25}{16 + 25} = 5.48 = 5.0 \text{ bars}$$

Sec. ②

$$M_{U.L.} = 101.4 \text{ kN.m}$$

R-Sec.



Take $d = 0.50 \text{ m}$ (The same d of Sec. ①)

$$\therefore d = C_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \therefore 350 = C_1 \sqrt{\frac{101.4 * 10^6}{25 * 250}} \rightarrow C_1 = 3.92 \rightarrow J = 0.801$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{101.4 * 10^6}{0.801 * 360 * 500} = 703.3 \text{ mm}^2$$

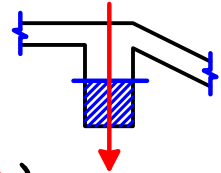
Check $A_{s_{min.}}$ $A_{s_{req.}} = 703.3 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 500 = 390.6 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 703.3 \text{ mm}^2$ $4 \phi 16$

Sec. ③ $M_{U.L.} = 50.7 \text{ kN.m}$

R-Sec.



Take $d = 0.50 \text{ m}$ (The same d of Sec. ①)

$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \therefore 350 = c_1 \sqrt{\frac{50.7 * 10^6}{25 * 250}} \rightarrow c_1 = 5.55 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{50.7 * 10^6}{0.826 * 360 * 500} = 341.0 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 341.0 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 500 = 390.6 \text{ mm}^2$$

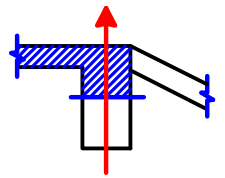
$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$

$$\left. \begin{aligned} A_{s_{min.}} &= \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 500 = 390.6 \text{ mm}^2 \\ 1.3 A_{s_{req.}} &= 1.3 * 341.0 = 443.3 \text{ mm}^2 \end{aligned} \right\} \begin{array}{l} \text{الأقل} \\ = 390.6 \text{ mm}^2 \end{array} \quad \text{2 } \phi 16$$

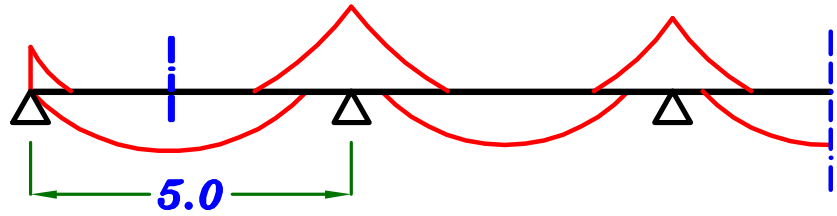
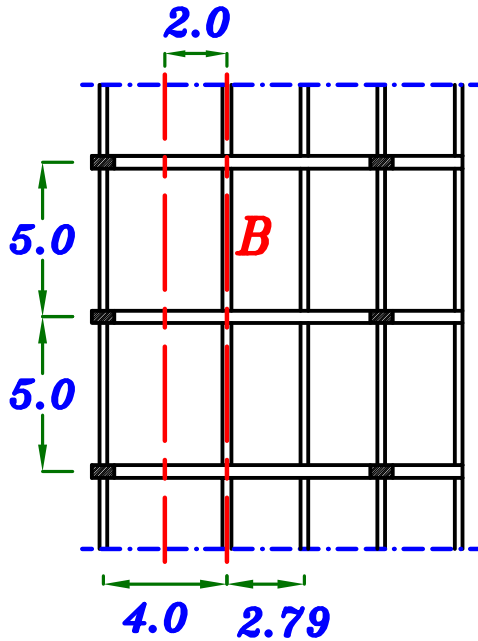
Sec. ④

$$M_{U.L.} = 101.4 \text{ kN.m}$$

L-Sec.



Take $d = 0.50 \text{ m}$ (The same d of Sec. ①)



$$B = \left\{ \begin{array}{l} C.L. - C.L. = 2.0 \text{ m} = 2000 \text{ mm} \\ 6 t_s + b = 6 * 150 + 250 = 1150 \text{ mm} \\ K \frac{L}{10} + b = 0.8 * \frac{5000}{10} + 250 = 650 \text{ mm} \end{array} \right\} \quad \boxed{B = 650 \text{ mm}}$$

$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} B}} \therefore 500 = c_1 \sqrt{\frac{101.4 * 10^6}{25 * 650}} \rightarrow c_1 = 6.33 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{101.4 * 10^6}{0.826 * 360 * 500} = 682 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 682 \text{ mm}^2$

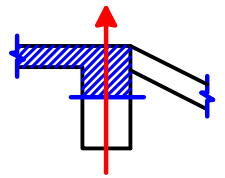
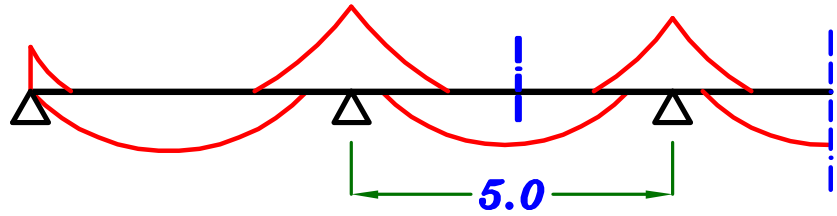
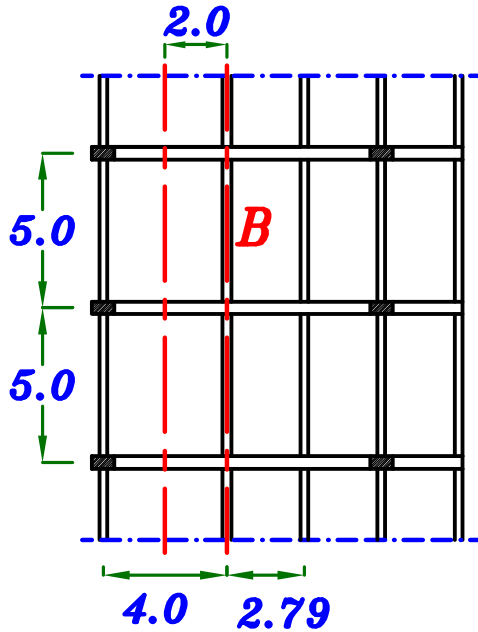
$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 500 = 390.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 682 \text{ mm}^2$$

4 ϕ 16

Sec. ⑤

$$M_{U.L.} = 76.0 \text{ kN.m}$$

L-Sec.Take $d = 0.50 \text{ m}$ (The same d of Sec. ①)

$$B = \left\{ \begin{array}{l} C.L. - C.L. = 2.0 \text{ m} = 2000 \text{ mm} \\ 6 t_s + b = 6 * 150 + 250 = 1150 \text{ mm} \\ K \frac{L}{10} + b = 0.7 * \frac{5000}{10} + 250 = 600 \text{ mm} \end{array} \right\} \quad \boxed{B = 600 \text{ mm}}$$

$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} B}} \therefore 500 = c_1 \sqrt{\frac{76.0 * 10^6}{25 * 600}} \rightarrow c_1 = 7.02 \rightarrow J = 0.826$$

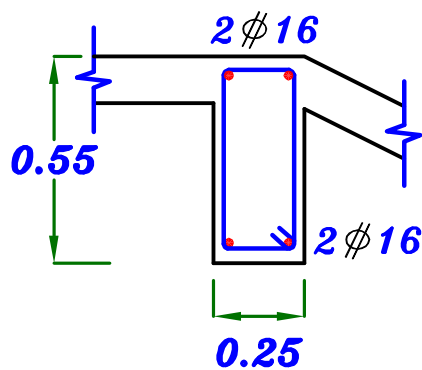
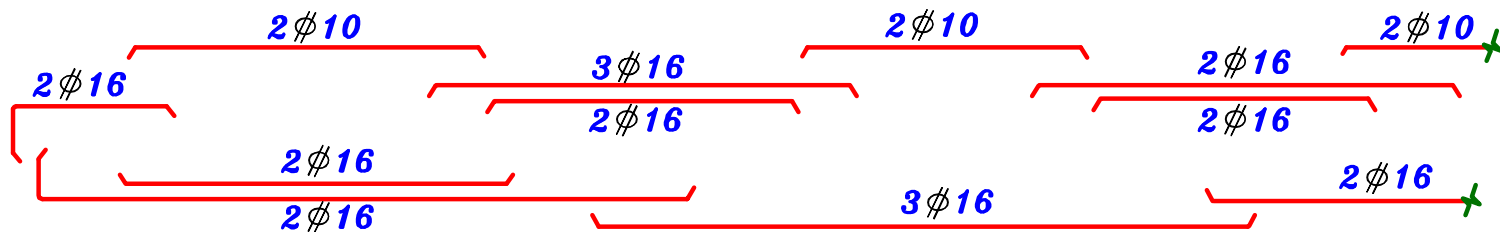
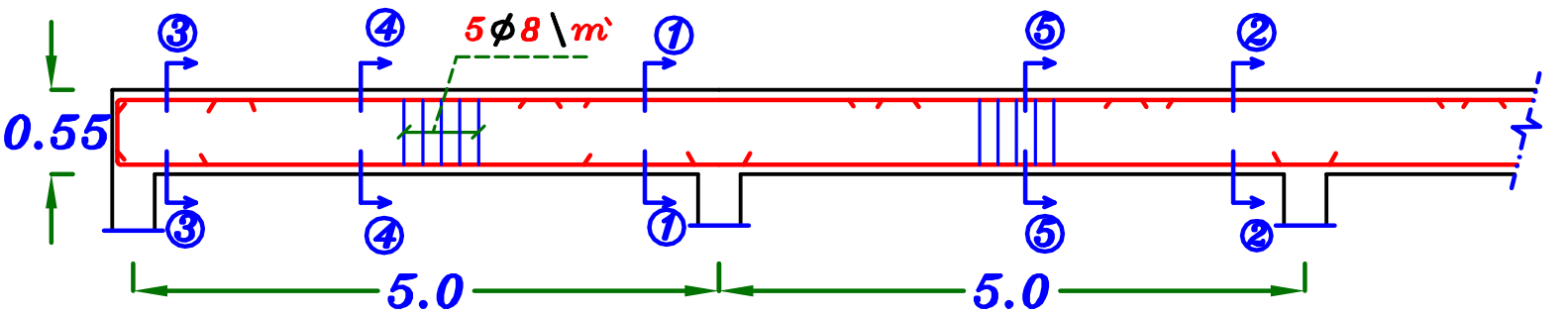
$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{76.0 * 10^6}{0.826 * 360 * 500} = 511.1 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 511.1 \text{ mm}^2$

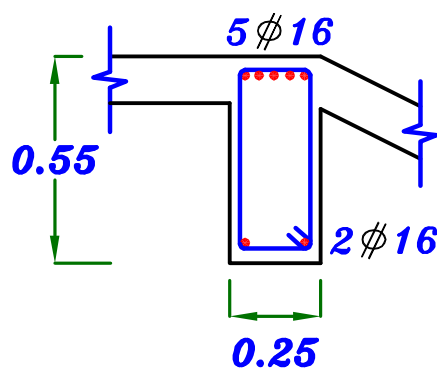
$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 500 = 390.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 511.1 \text{ mm}^2 \quad \boxed{\boxed{3 \phi 16}}$$

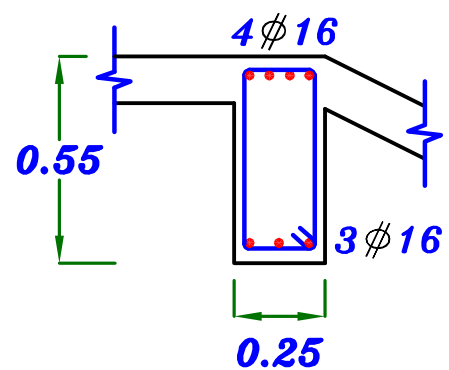
RFT. of Beam B



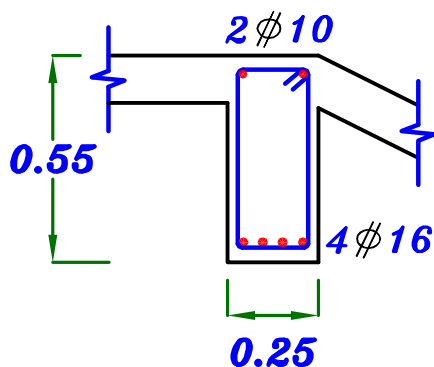
Sec. (3-3)



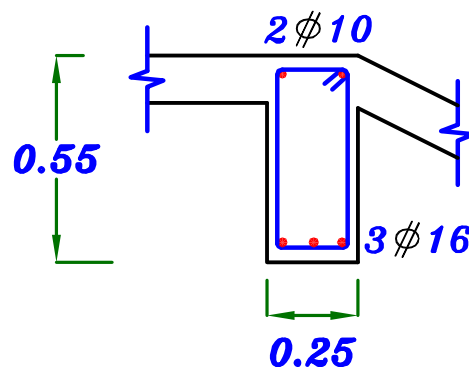
Sec. (1-1)



Sec. (2-2)

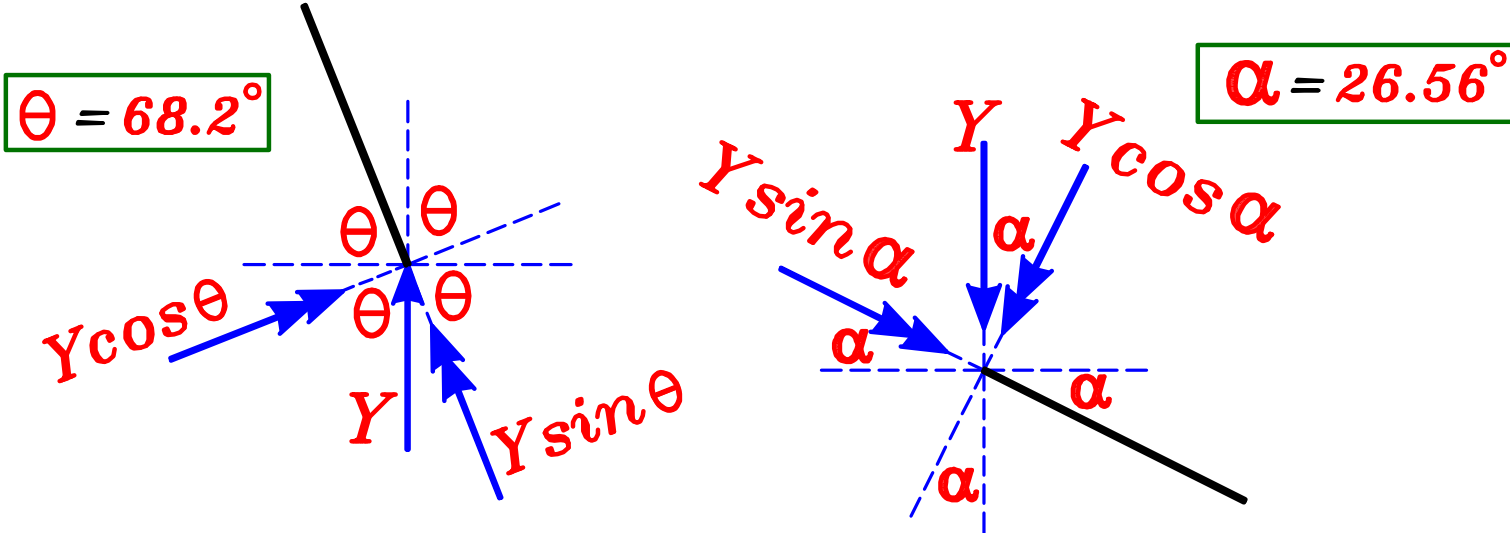
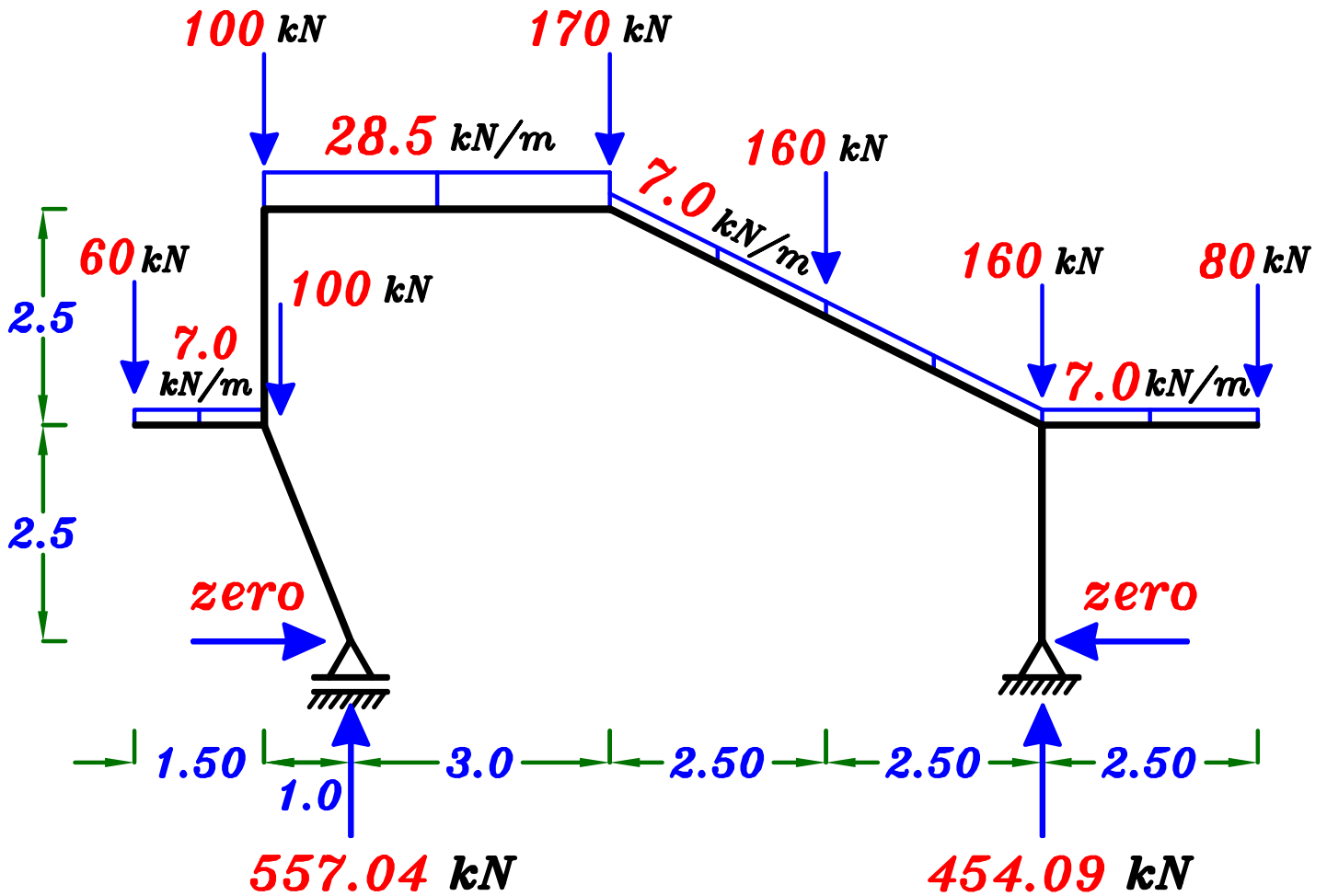


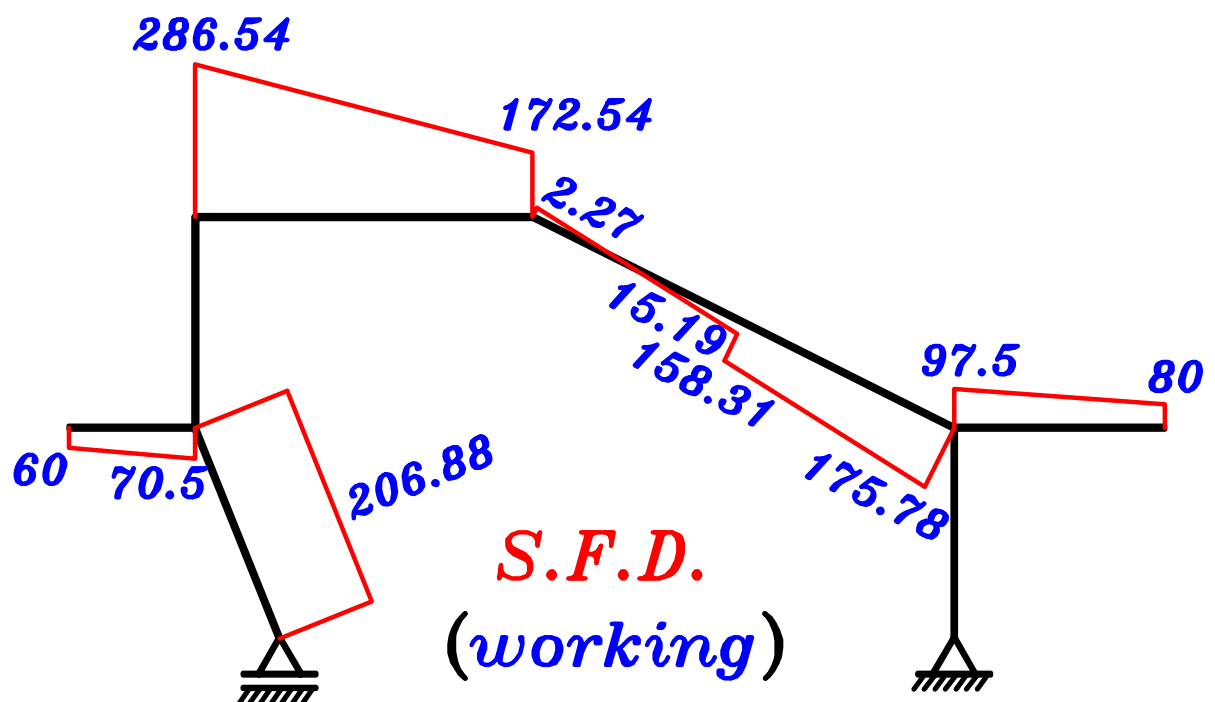
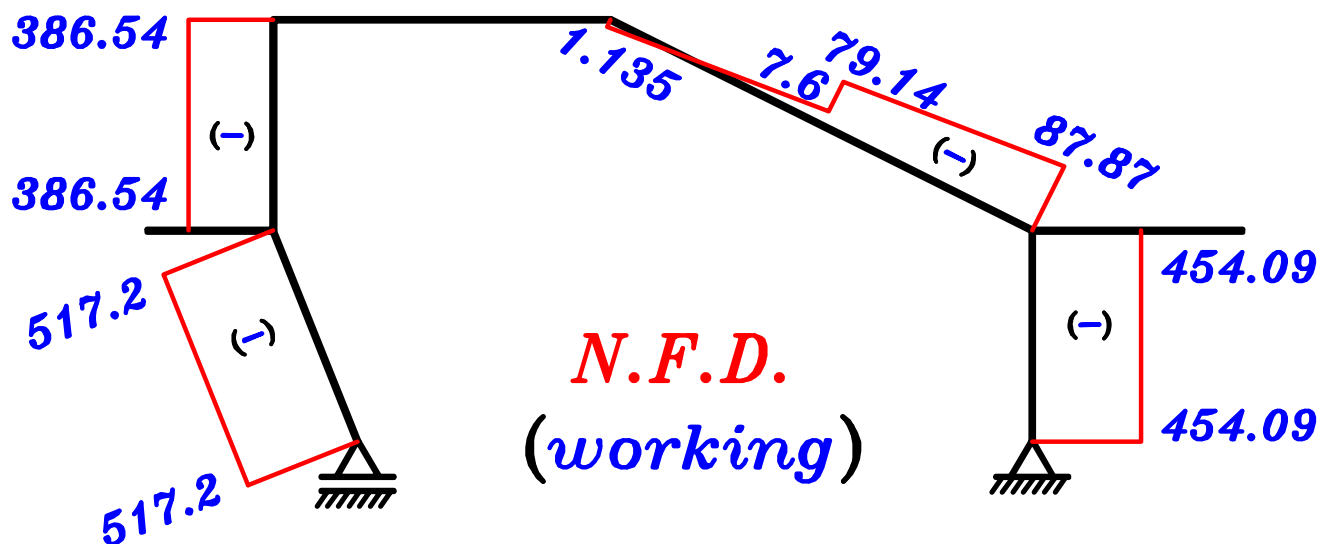
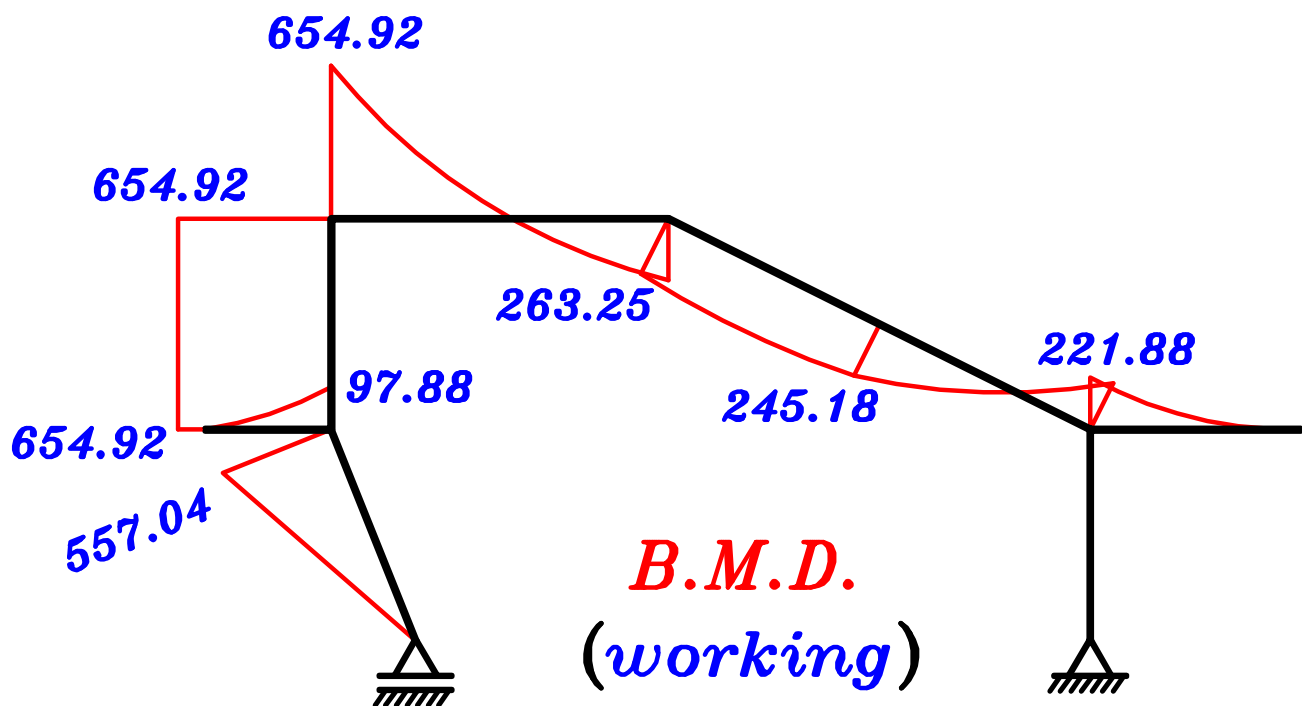
Sec. (4-4)

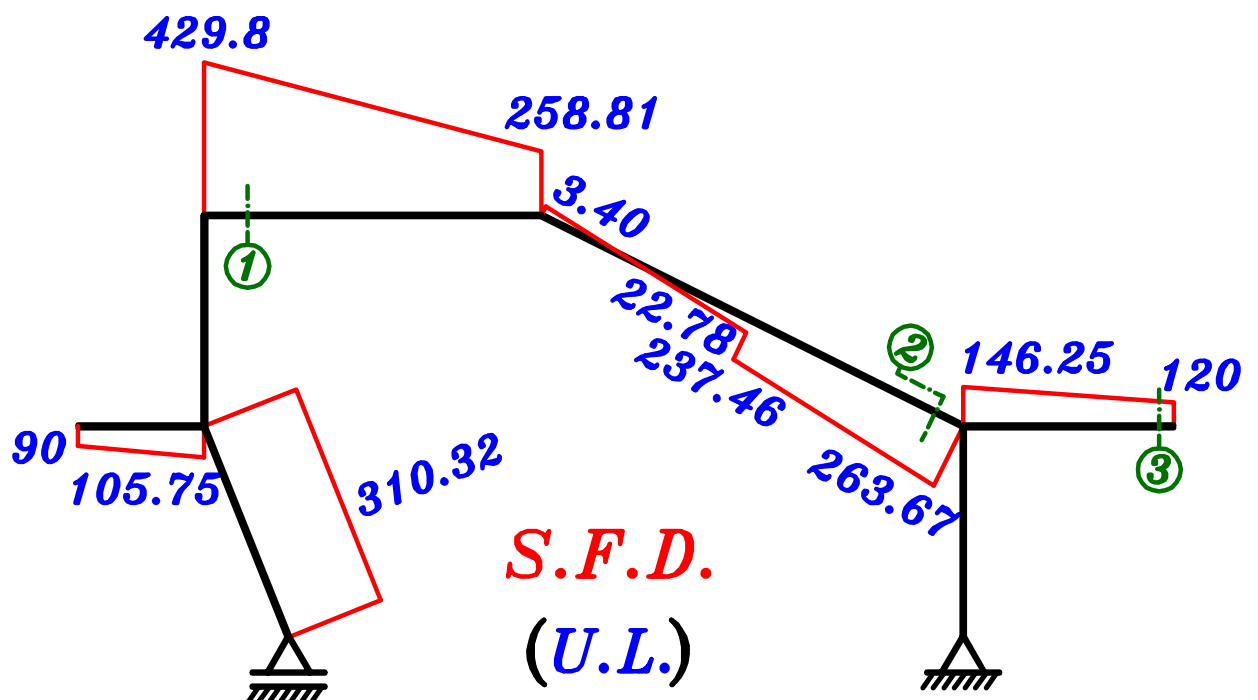
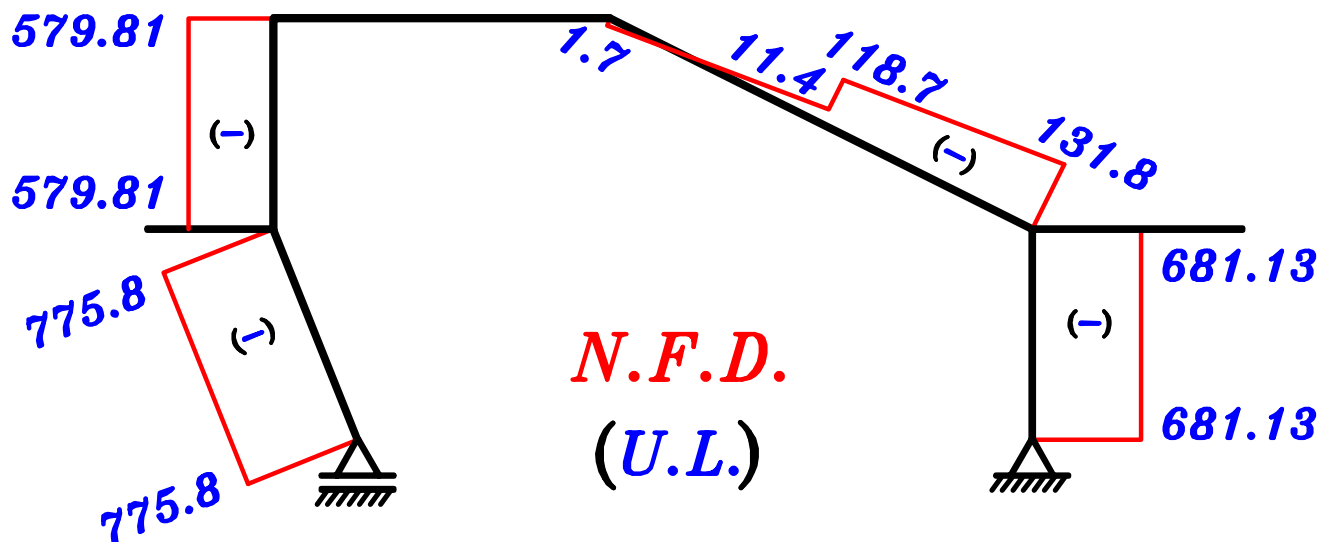
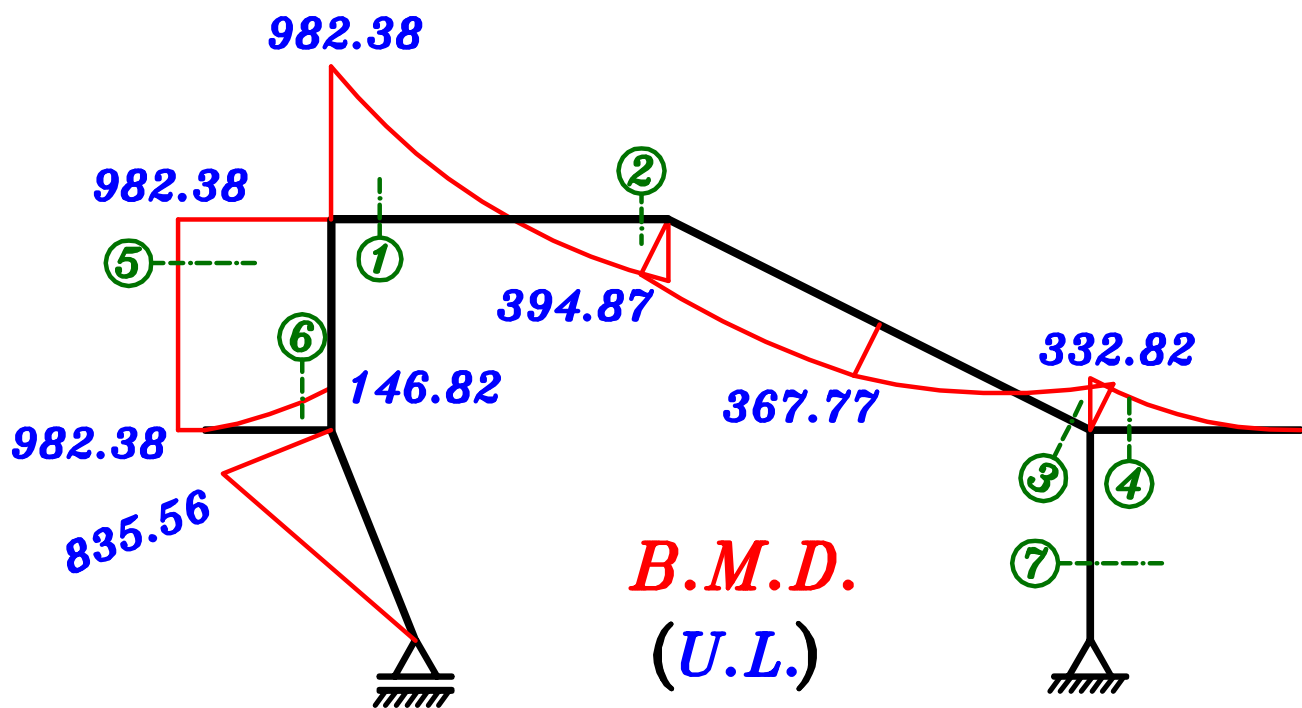


Sec. (5-5)

3- Draw the N.F.D. , S.F.D. & B.M.D. For the intermediate Frame (F) .
Using the given working loads.





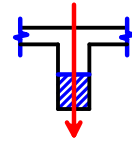


4- Design the critical sections of Frame (F)

to satisfy the internal Forces requirements using (L.S.D.M.)

Take $b = 350$ mm

Sec. ① $M = 982.38$ kN.m , R-Sec.



Take $C_1 = 3.50 \rightarrow J = 0.78$

$$d = 3.5 \sqrt{\frac{982.38 * 10^6}{25 * 350}} = 1172.7 \text{ mm}$$

Take $d = 1200$ mm , $t = 1300$ mm

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{982.38 * 10^6}{0.780 * 360 * 1172.7} = 2983.2 \text{ mm}^2$$

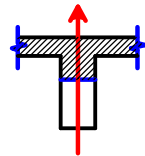
Check $A_{s_{min.}}$ $A_{s_{req.}} = 2983.2 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1200 = 1312.5 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2983.2 \text{ mm}^2 \quad (8 \phi 22)$$

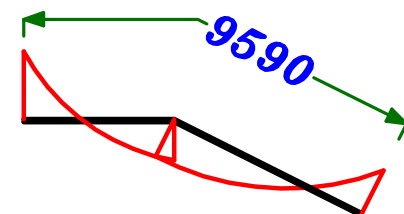
$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{22 + 25} = 6.91 = 6.0 \text{ bars}$$

Sec. ② $M = 394.87$ kN.m , T-Sec.



$d = 1200$ mm (the same depth of sec. ①)

$$B = \left\{ \begin{array}{l} C.L. - C.L. = 5.0 \text{ m} = 5000 \text{ mm} \\ 16 t_s + b = 16 * 150 + 350 = 2750 \text{ mm} \\ K \frac{L}{5} + b = 0.7 * \frac{9590}{5} + 350 = 1692.6 \text{ mm} \end{array} \right\}$$



$$B = 1692.6 \text{ mm}$$

$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} B}} \therefore 1200 = c_1 \sqrt{\frac{394.87 \cdot 10^6}{25 \cdot 1692.6}} \rightarrow c_1 = 12.42 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{394.87 \cdot 10^6}{0.826 \cdot 360 \cdot 1200} = 1106.6 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1106.6 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 350 \cdot 1200 = 1312.5 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$A_{s_{min.}} = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 350 \cdot 1200 = 1312.5 \text{ mm}^2 \quad \left. \begin{array}{l} \text{الأقل} \\ 1.3 A_{s_{req.}} = 1.3 \cdot 1106.6 = 1438.6 \text{ mm}^2 \end{array} \right\} = 363.3 \text{ mm}^2 \quad (4 \phi 22)$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 1283.3 \quad (2 \phi 12)$$

Sec. ③ $M = 332.82 \text{ kN.m}$, $P = 131.8 \text{ kN}$, $b = 350 \text{ mm}$

$$d = 1200 \text{ mm} \quad (\text{the same depth of Sec. ①})$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{131.8 \cdot 10^3}{25 \cdot 350 \cdot 1300} = 0.011 < 0.04 \quad (\text{Neglect } P)$$

The sec. will be R-sec. 

$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \therefore 1200 = c_1 \sqrt{\frac{332.82 \cdot 10^6}{25 \cdot 350}} \rightarrow c_1 = 6.15 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{332.82 \cdot 10^6}{0.826 \cdot 360 \cdot 1200} = 932.7 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 932.7 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1200 = 1312.5 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$\left. \begin{aligned} A_{s_{min.}} &= \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1200 = 1312.5 \text{ mm}^2 \\ 1.3 A_{s_{req.}} &= 1.3 * 932.7 = 1212.5 \text{ mm}^2 \end{aligned} \right\} \text{الأقل} = 1212.5 \text{ mm}^2 \quad (4 \phi 22)$$

Sec. ④ $M = 332.82 \text{ kN.m}$, $b = 350 \text{ mm}$

Take $C_1 = 3.50 \rightarrow J = 0.78$

$$d = 3.5 \sqrt{\frac{332.82 * 10^6}{25 * 350}} = 682.6 \text{ mm}$$

$d = 700 \text{ mm}$, $t = 750 \text{ mm}$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{332.82 * 10^6}{0.780 * 360 * 682.6} = 1736.4 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1736.4 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1200 = 1312.5 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1736.4 \text{ mm}^2 \quad (5 \phi 22)$$

$$Y = \left\{ \begin{aligned} \frac{t}{2} &= \frac{750}{2} = 375 \text{ mm} \\ t_b &= \frac{\text{spacing}}{12} = \frac{5000}{12} = 416.6 \text{ mm} \\ t - \frac{L_c}{3} &= 750 - \frac{2500}{3} = -83.3 \text{ mm} \end{aligned} \right\}$$

$Y = 450 \text{ mm}$

تم تصميم القطاع Sec. ④ غير Sec. ③ لان له عمق مختلف .

Sec. ⑤ R-Sec. $M = 982.38 \text{ kN.m}$, $P = 579.81 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{982.38 * 10^6}{25 * 350}} = 1172.7 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1172.7) = (1290 \rightarrow 1524) \text{ mm}$$

$$\therefore \text{Take } \boxed{d = 1300 \text{ mm}} , \boxed{t = 1400 \text{ mm}}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{579.81 * 10^3}{25 * 350 * 1400} = 0.047 > 0.04 \quad (\text{Don't neglect } P)$$

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{982.38}{579.81} = 1.69 \text{ m} \quad \therefore \quad \frac{e}{t} = \frac{1.69}{1.40} = 1.20 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.69 + \frac{1.40}{2} - 0.10 = 2.29 \text{ m}$$

$$M_s = P * e_s = 579.81 * 2.29 = 1327.76 \text{ kN.m}$$

$$\therefore 1300 = C_1 \sqrt{\frac{1327.76 * 10^6}{25 * 350}} \rightarrow C_1 = 3.33 \rightarrow J = 0.77$$

$$A_s = \frac{M_s}{J F_y d} - \frac{P_{u.l.}}{(F_y \setminus \delta_s)}$$

$$= \frac{1327.76 * 10^6}{0.77 * 360 * 1300} - \frac{579.81 * 10^3}{(360 \setminus 1.15)} = 1832.3 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1832.3 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1200 = 1312.5 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1832.3 \text{ mm}^2 \quad \textcircled{5 \phi 22}$$

Sec. ⑥ $M = 146.82 \text{ kN.m}$, $b = 350 \text{ mm}$ $R\text{-sec.}$

Take $C_1 = 3.50 \rightarrow J = 0.78$

$$d = 3.5 \sqrt{\frac{146.82 * 10^6}{25 * 350}} = 453.37 \text{ mm}$$

$$d = 500 \text{ mm} , t = 550 \text{ mm}$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{146.82 * 10^6}{0.780 * 360 * 453.37} = 1153.2 \text{ mm}^2$$

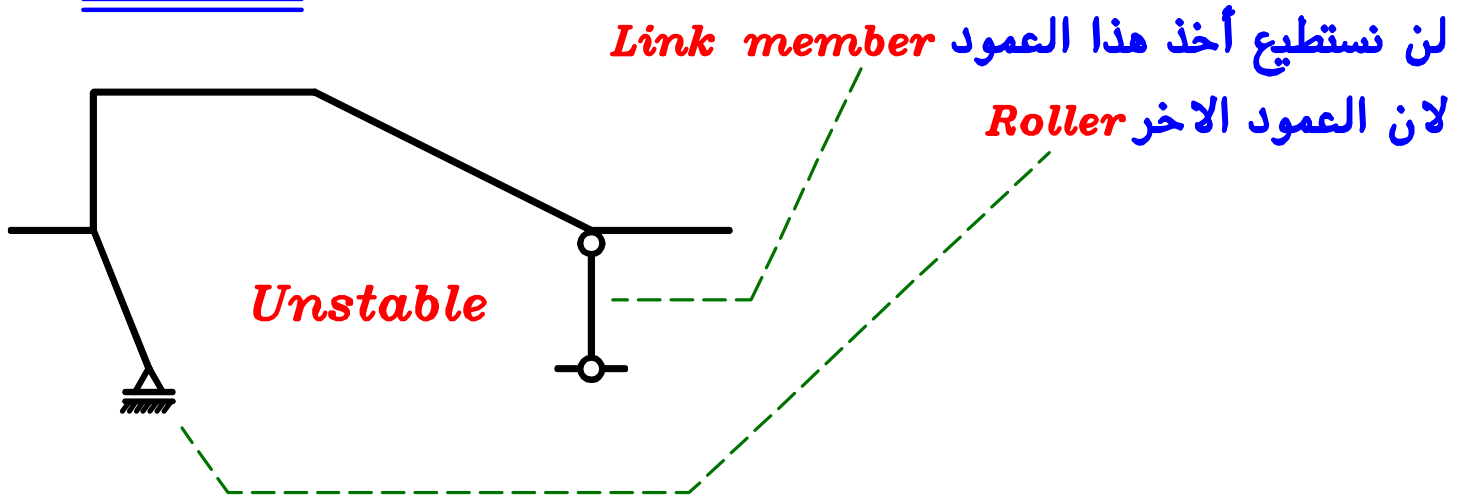
Check $A_{s_{min.}}$ $A_{s_{req.}} = 1153.2 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 1200 = 1312.5 \text{ mm}^2$$

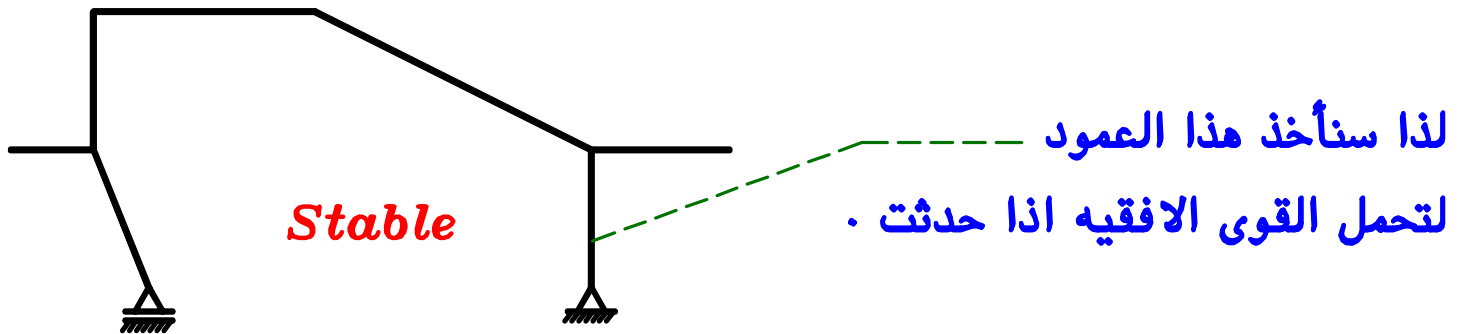
$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1153.2 \text{ mm}^2 \quad (4 \phi 22)$$

$$Y = \left\{ \begin{array}{l} \frac{t}{2} = \frac{550}{2} = 275 \text{ mm} \\ t_b = \frac{\text{spacing}}{12} = \frac{5000}{12} = 416.6 \text{ mm} \\ t - \frac{L_c}{3} = 550 - \frac{1500}{3} = 50 \text{ mm} \end{array} \right\} \quad Y = 450 \text{ mm}$$

Sec. ⑦



لانه في هذه الحالة اذا وجدت أى **HL. Load**
لن يوجد أى عمود يستطيع مقاومتها أى يكون **Unstable Frame**



$$P = 681.13 \text{ kN} , \quad b = 350 \text{ mm}$$

$$t = 1300 \text{ mm} \text{ (the same depth of the beam)}$$

$$\therefore P_{U.L.} = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

$$\therefore 681.13 * 10^3 = 0.35 (350 * 1300) (25) + 0.67 A_s (360)$$

$$\therefore A_s = - 13682 \text{ mm}^2 = - (Ve) \text{ Value}$$

$$\therefore A_{s_{total}} = A_{s_{min}} = \frac{0.8}{100} * 350 * 1300 = 3640 \text{ mm}^2$$

$$\therefore A_s = A_s' = \frac{A_{s_{min}}}{2} = \frac{3640}{2} = 1820 \text{ mm}^2$$

5#22

Check Shear.

- Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{25}{1.5}} = 2.85 \text{ N/mm}^2$$

Sec. ① $Q = 429.8 \text{ kN}$

$$\therefore \text{Actual shear stress.} = q_U = \frac{Q}{b d} = \frac{429.8 * 10^3}{350 * 1200} = 1.02 \text{ N/mm}^2$$

$\therefore q_{cu} < q_U < q_{max.}$ \therefore We need Stirrups more Than $5 \phi 8 \text{ m}$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y / \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.02 - \frac{0.98}{2} = \frac{2 * 50.3 (240 / 1.15)}{350 * S} \rightarrow S = 113.1 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups/m} = \frac{1000}{S} = \frac{1000}{113.1} = 8.84 = 9.0$$

\therefore Use Stirrups $9 \phi 8 \text{ m}$ 2 branches

Sec. ② $Q = 263.67 \text{ kN}$

$$\therefore \text{Actual shear stress.} = q_U = \frac{Q}{b d} = \frac{263.67 * 10^3}{350 * 1200} = 0.627 \text{ N/mm}^2$$

$\therefore q_U < q_{cu} \rightarrow$ Use min. stirrups $5 \phi 8 \text{ m}$ 2 branches

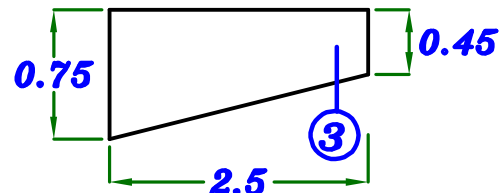
Sec. ③ $Q = 120 \text{ kN}$

\therefore Actual shear stress. =

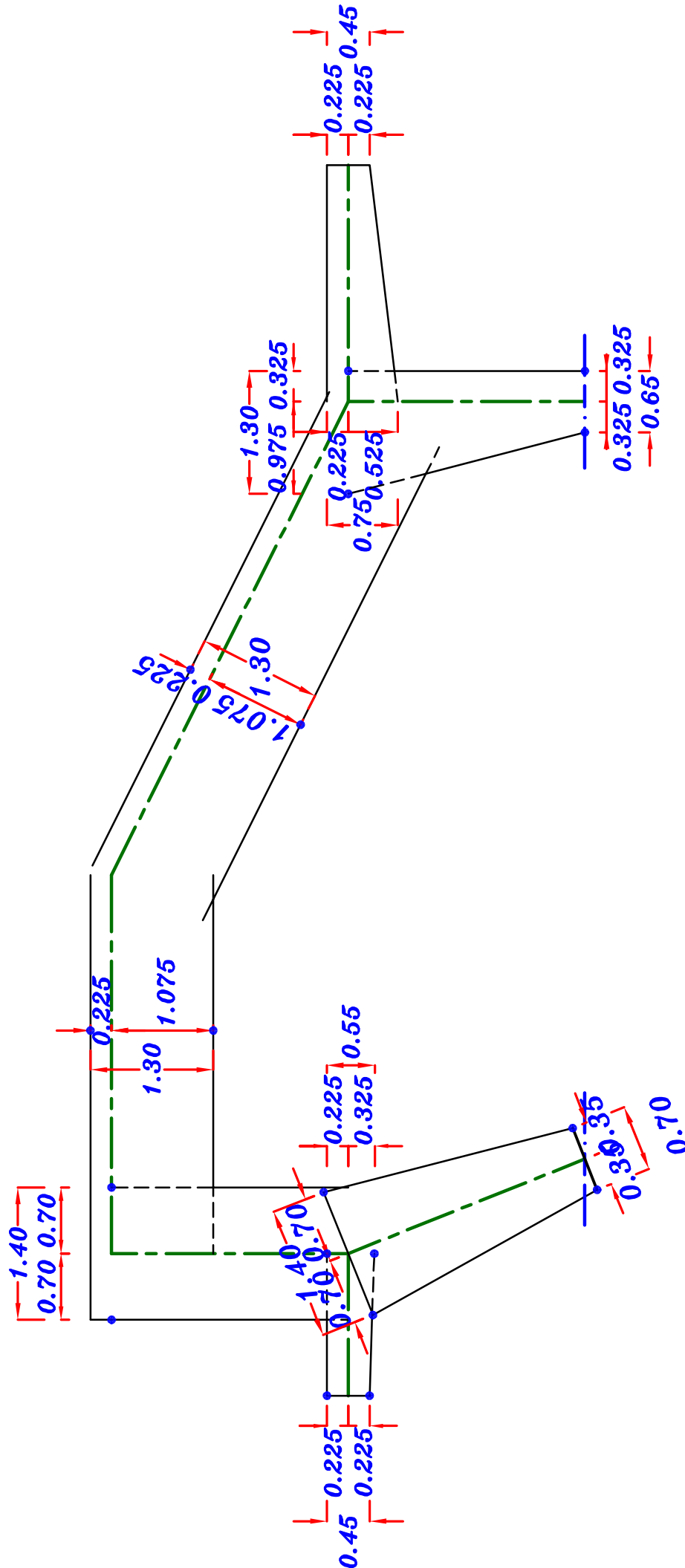
$$q_U = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

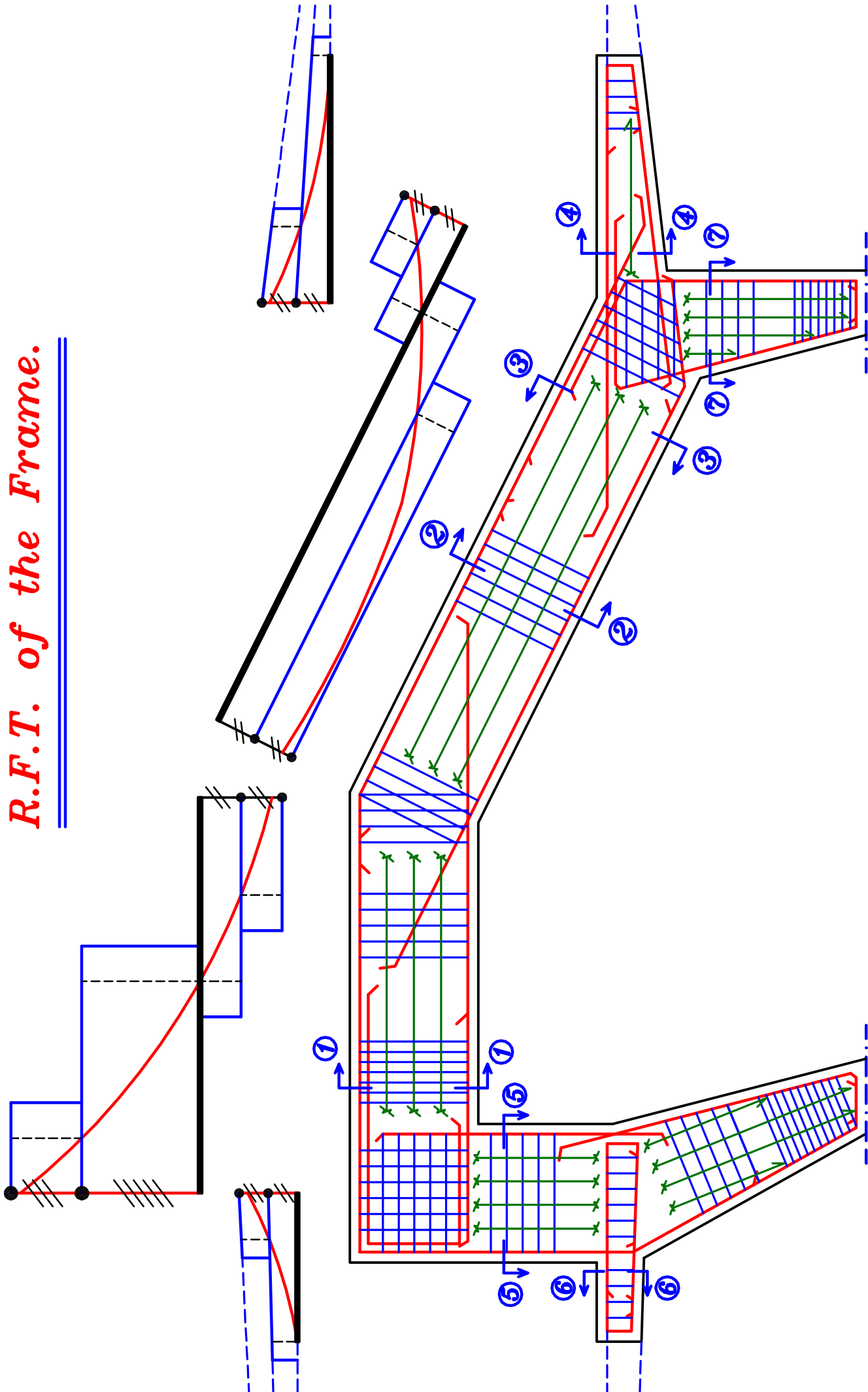
$$= \frac{120.0 * 10^3}{350 * 400} - \text{ZERO} = 0.857 \text{ N/mm}^2$$

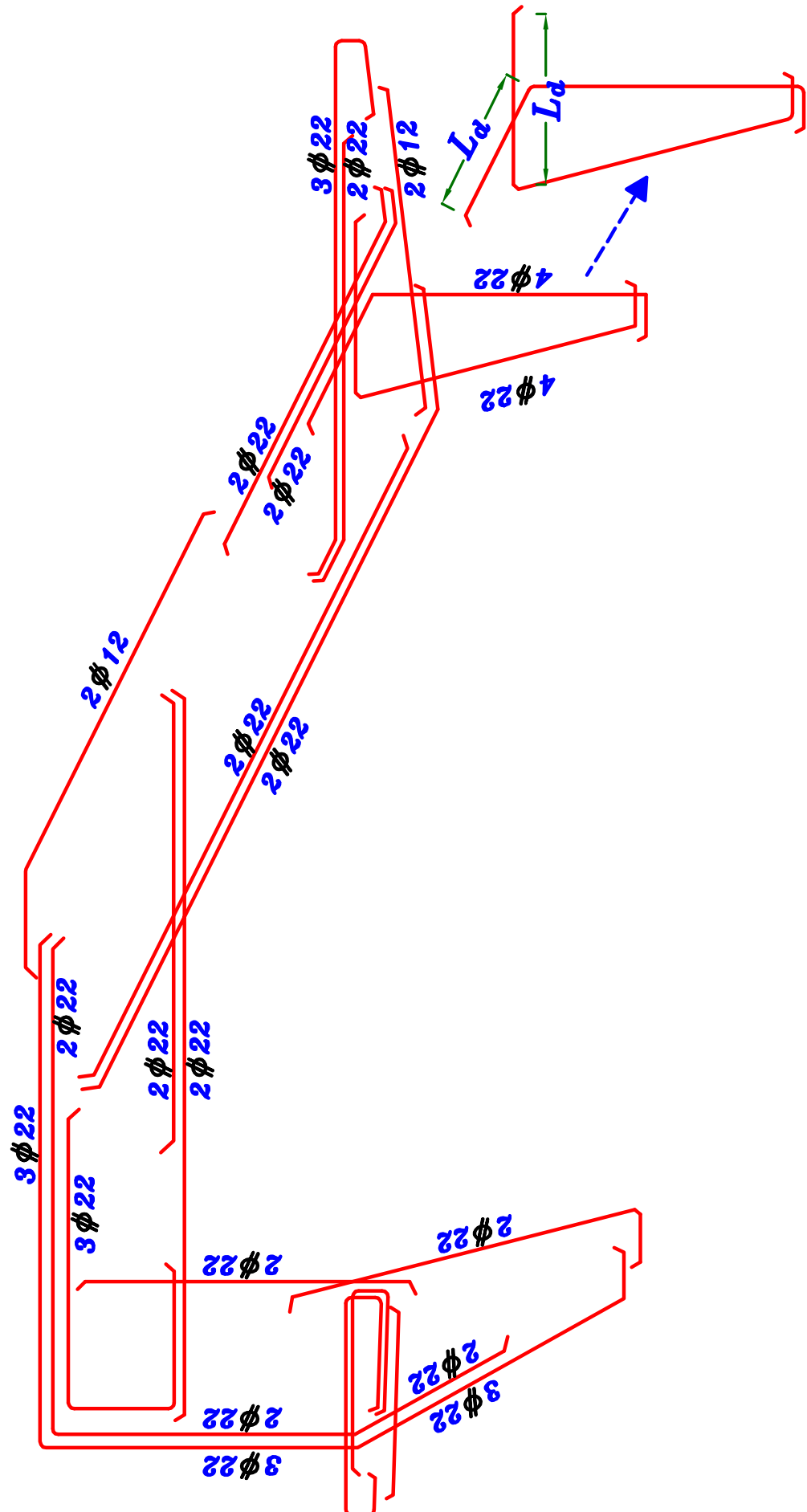
$\therefore q_U < q_{cu} \rightarrow$ Use min. stirrups $5 \phi 8 \text{ m}$

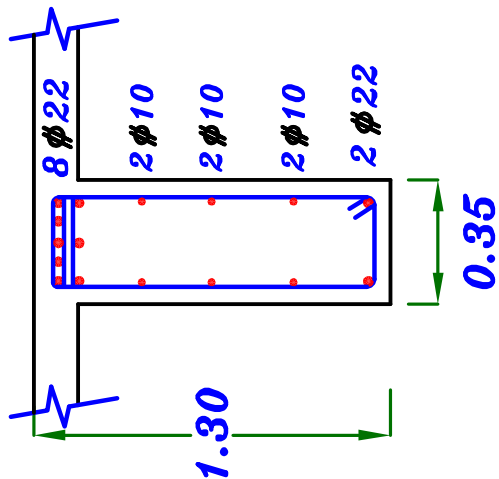


5- Draw details of reinforcement For Frame (F) in elevation to scale 1:50 and cross sections to scale 1:25

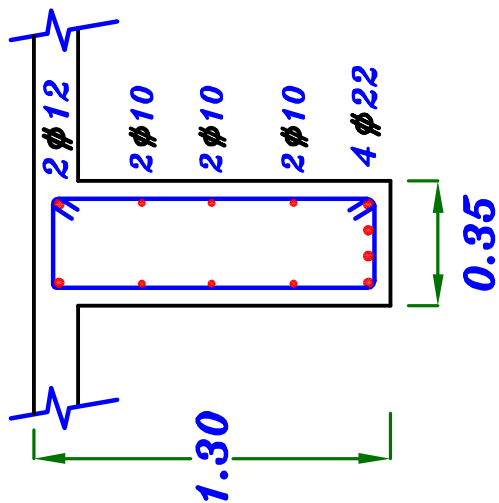




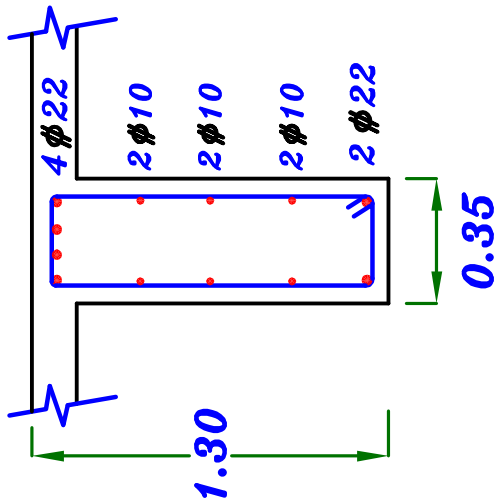




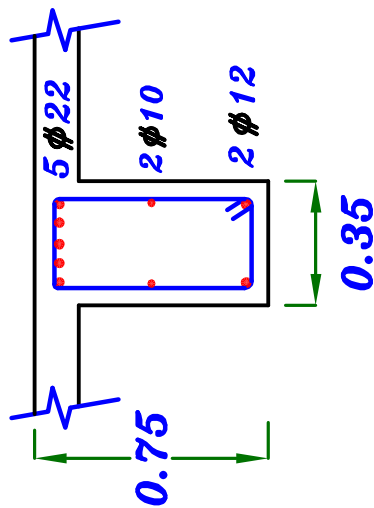
Sec. (1-1)



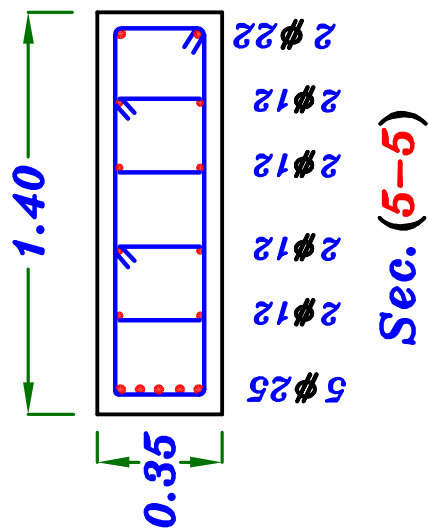
Sec. (2-2)



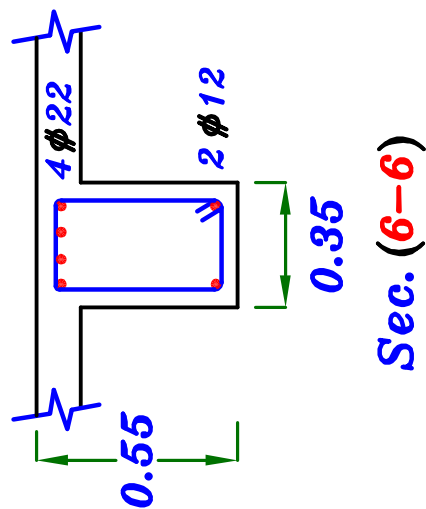
Sec. (3-3)



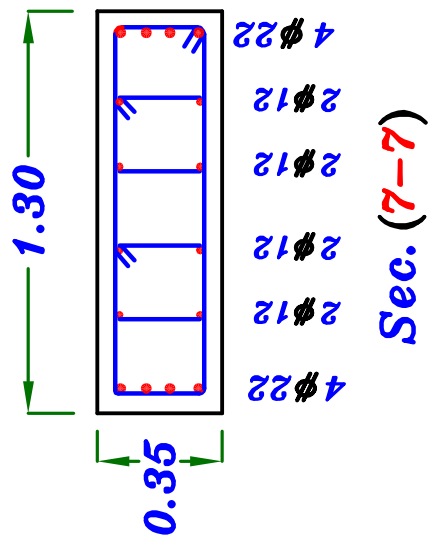
Sec. (4-4)



Sec. (5-5)



Sec. (6-6)



Sec. (7-7)

Example.

The reinforced concrete hall, Whose cross-section is shown in Fig. (1), Consists of a system of solid slabs and secondary beams supported on successive Frame (F) spaced at 6.0 m. It is required to:

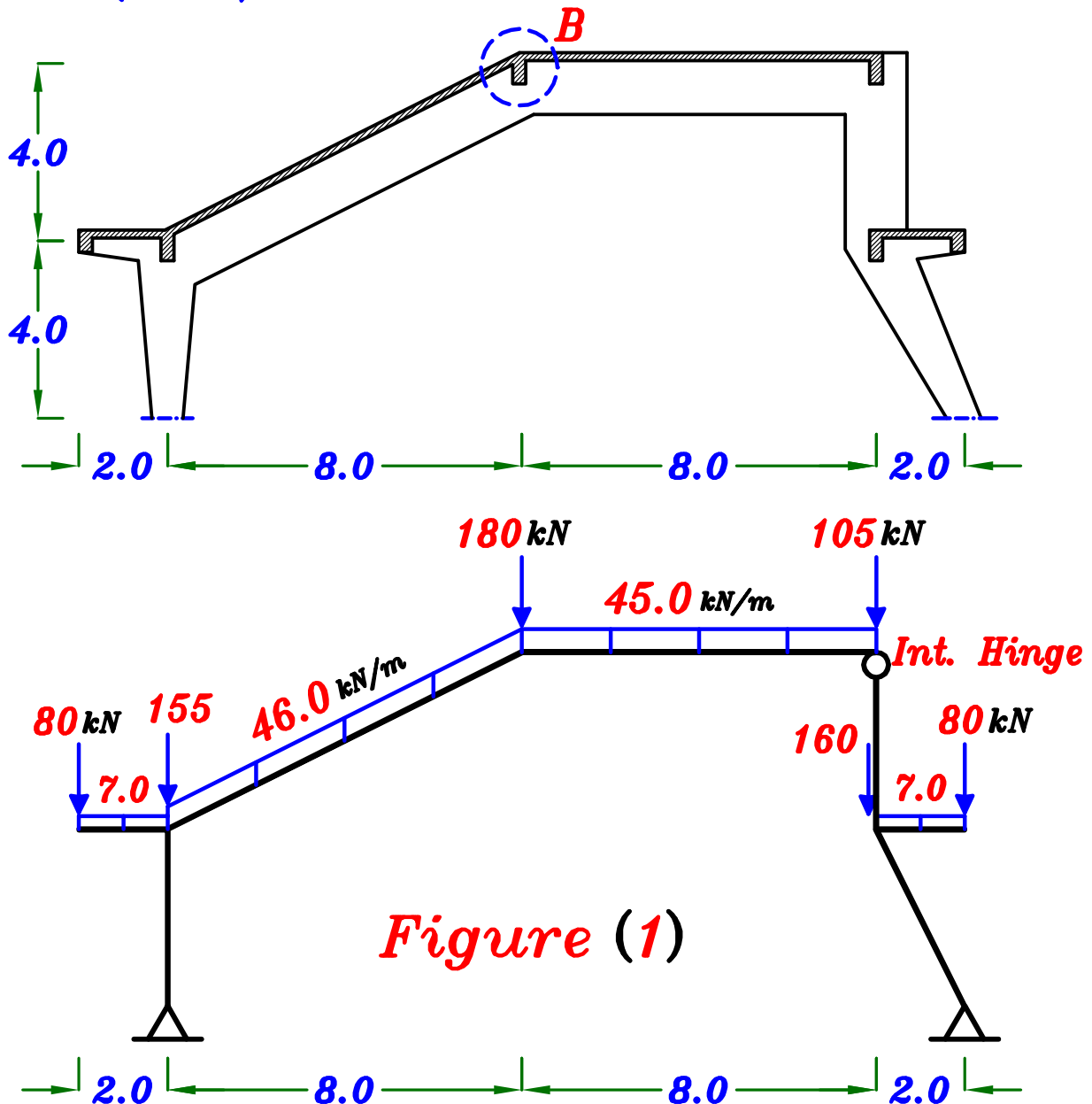
a - Draw the N.F.D , S.F.D & B.M.D For the intermediate Frame (F) using the given working total loads.

b - Design the critical sections of Frame (F) to satisfy the internal Forces requirements, using the limit state design method (LSDM)

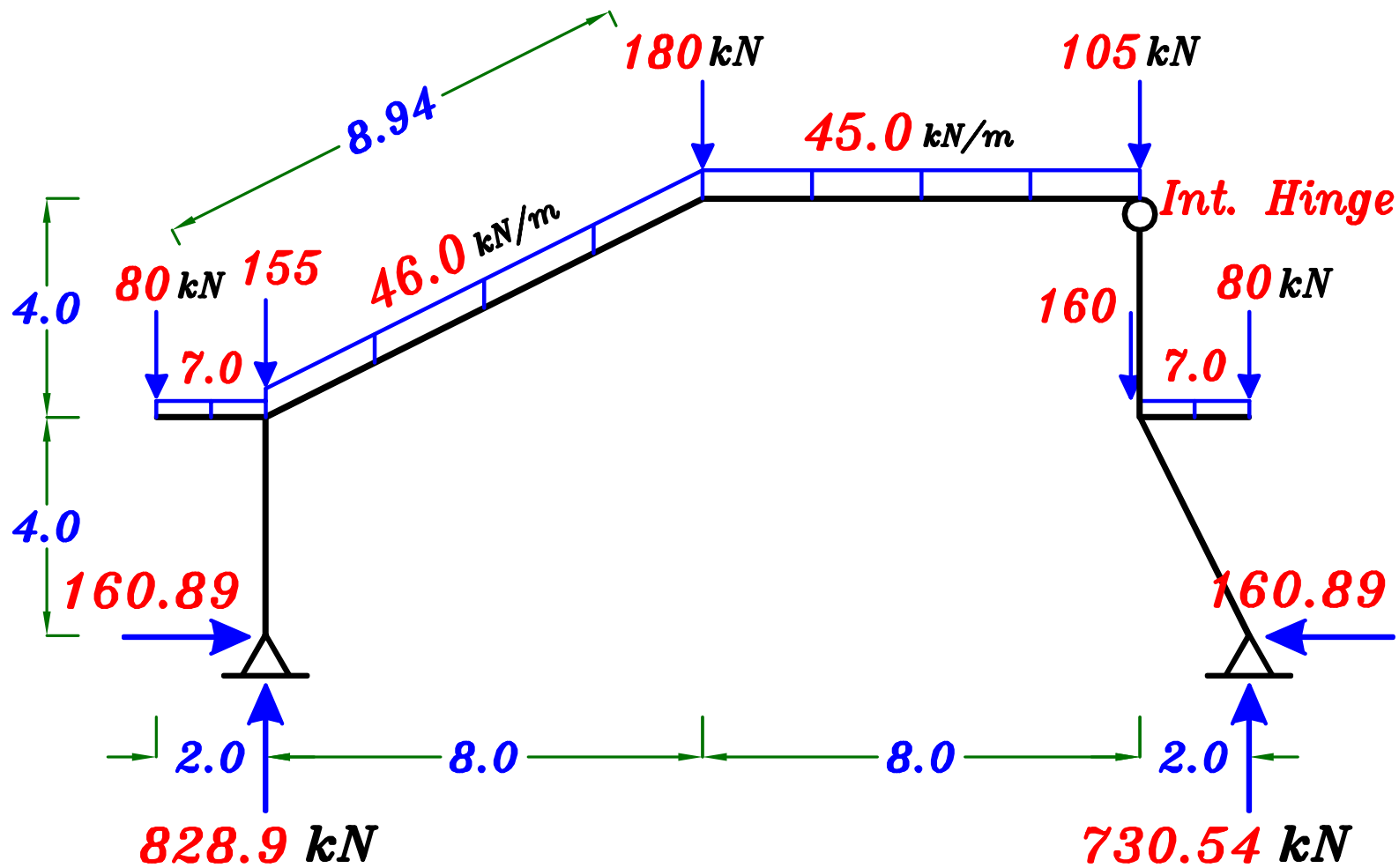
c - Draw the details of reinforcement For intermediate Frame (F) in elevation to scale 1:50 and cross sections to scale 1:25 . Curtailment of bars using the moment of resistance diagram is required.

Data:

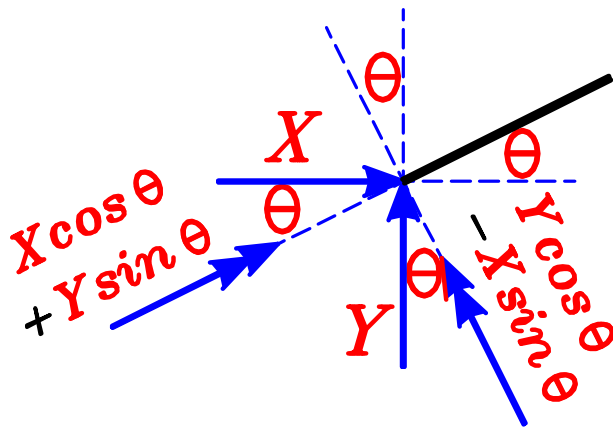
- Concrete characteristic strength $F_{cu} = 30 \text{ N/mm}^2$
- Steel used is St. 400/600
- $b = 400 \text{ mm}$ (Frame)



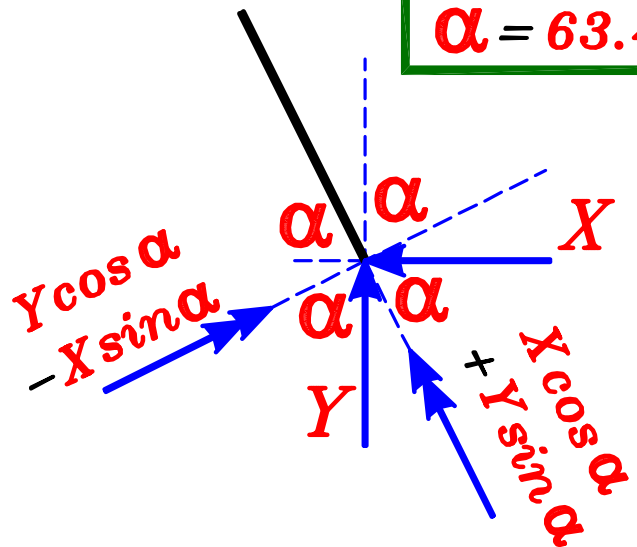
α – Draw the N.F.D , S.F.D & B.M.D For the intermediate Frame (**F**) using the given working total loads.

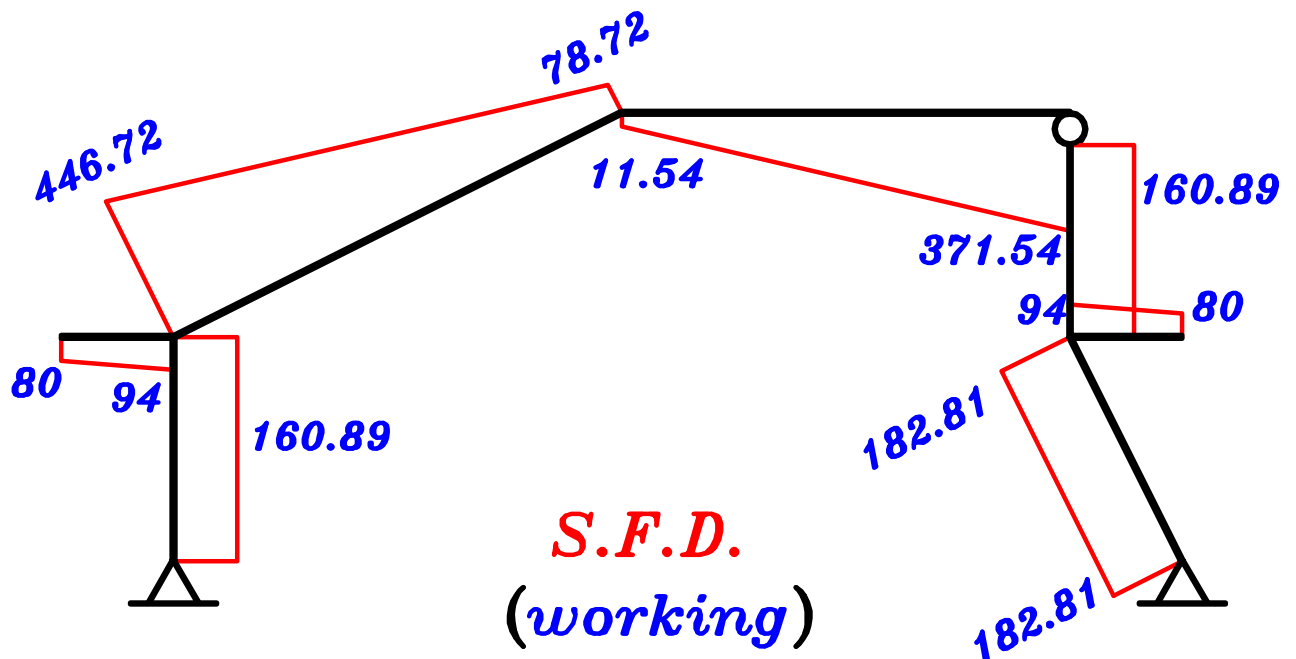
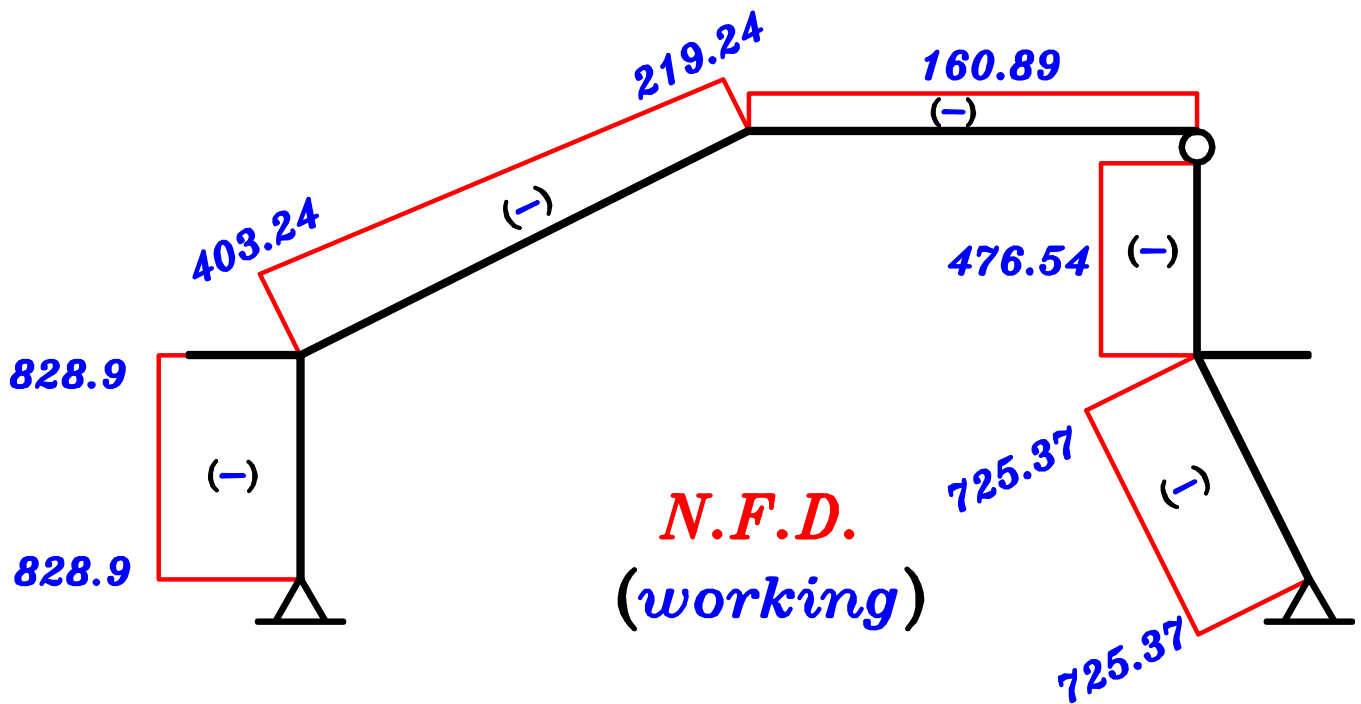
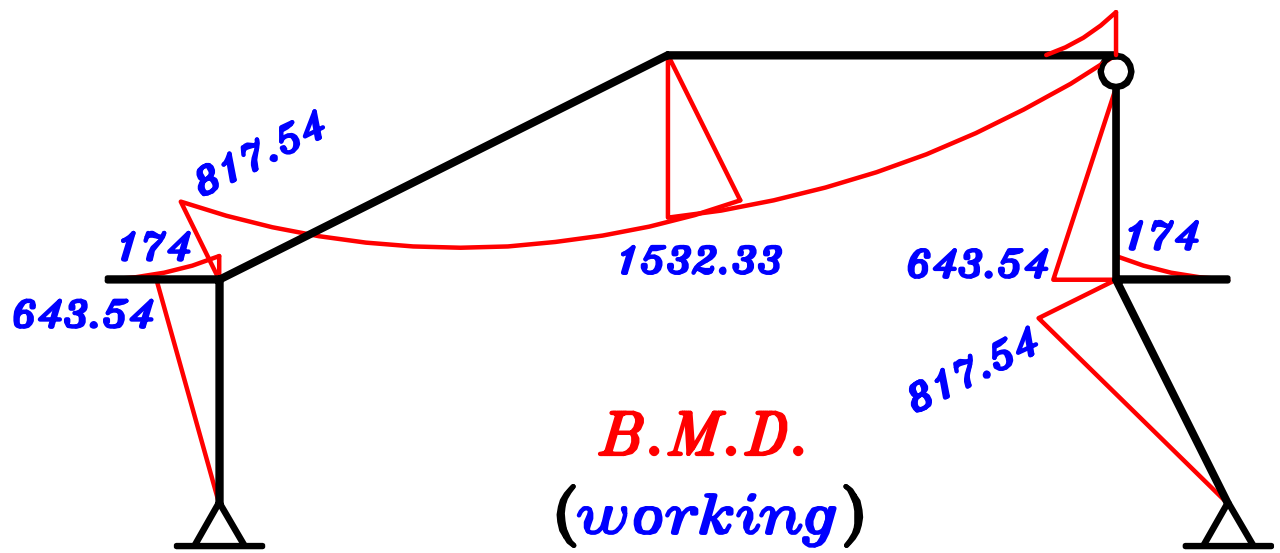


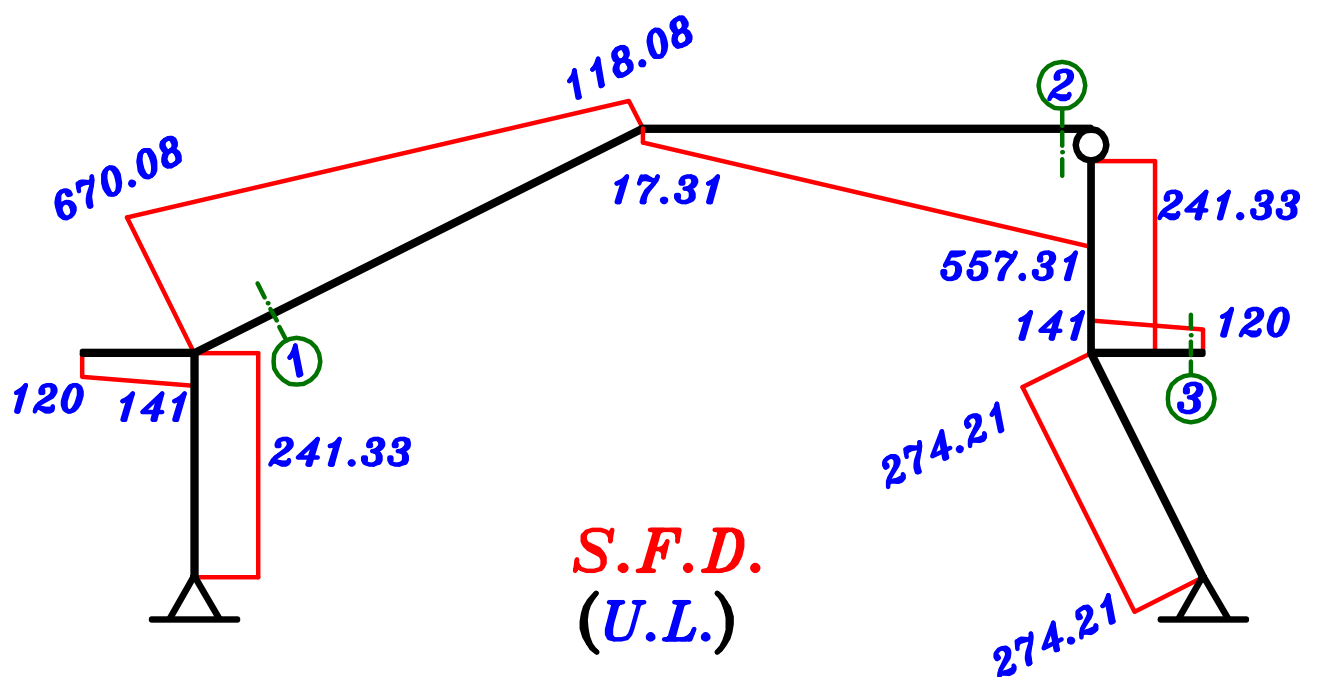
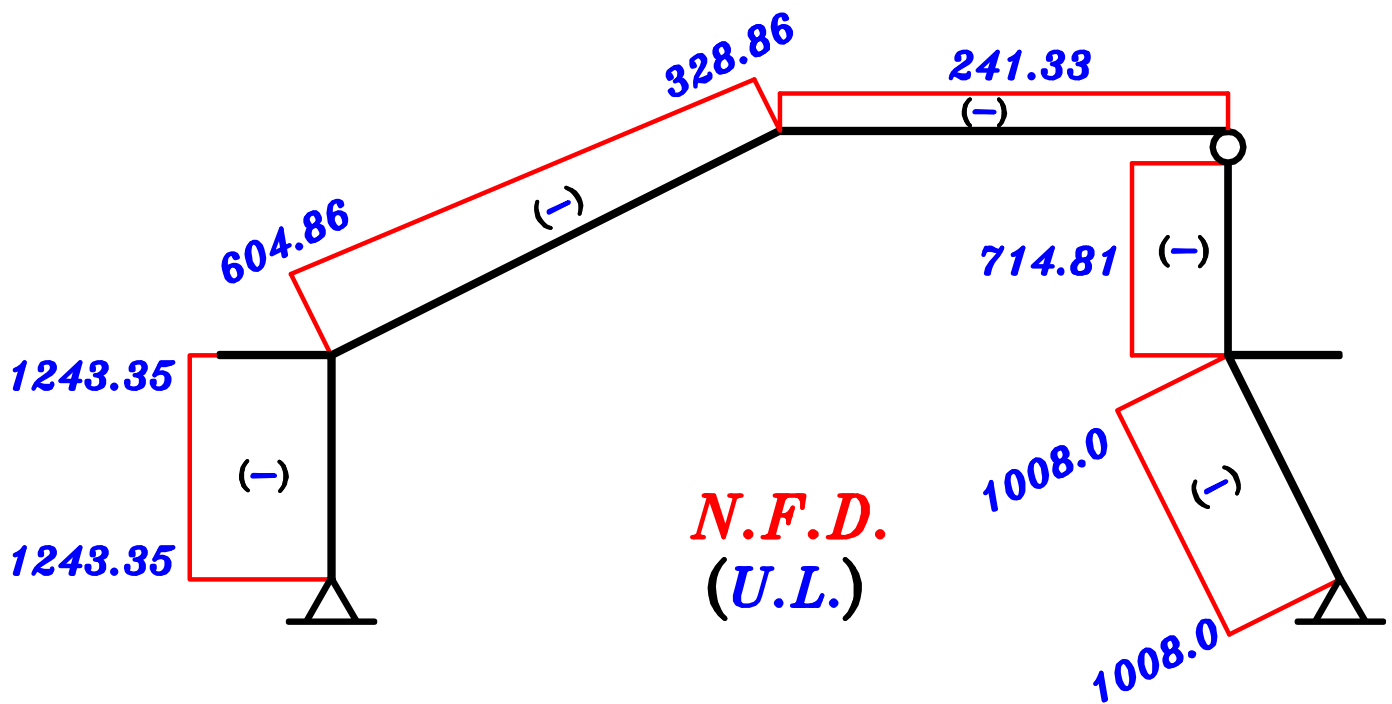
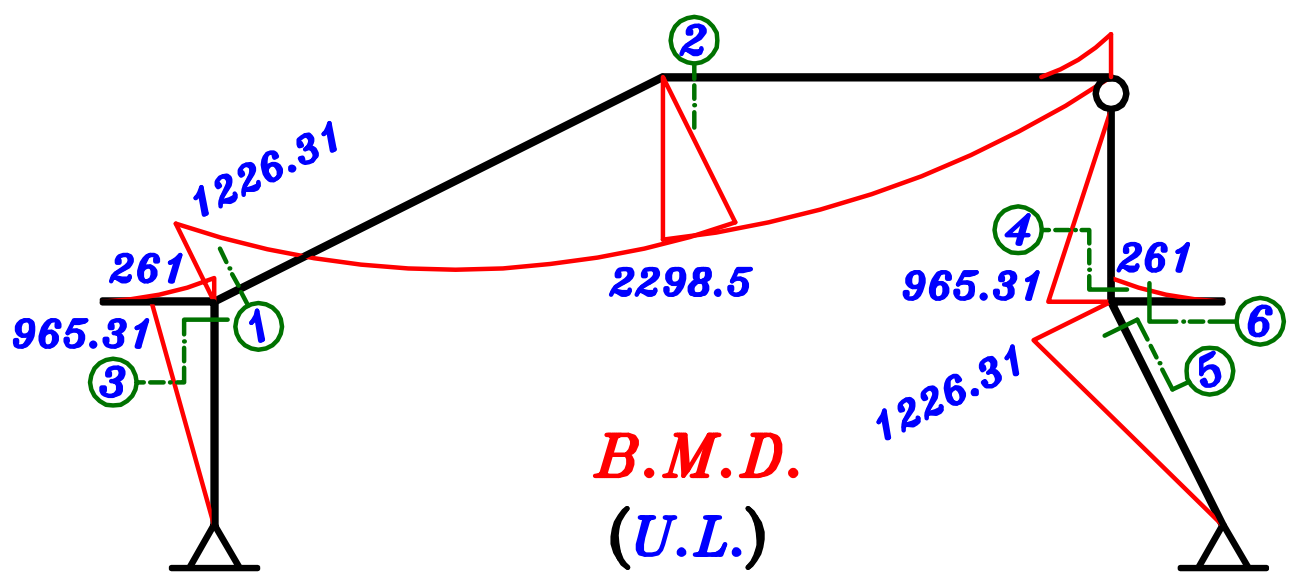
$$\theta = 26.56^\circ$$



$$\alpha = 63.44^\circ$$



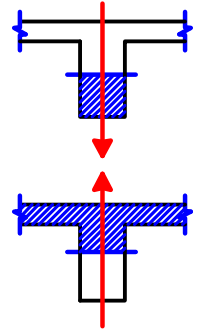




b – Design the critical sections of Frame (**F**) to satisfy the internal Forces requirements, using the limit state design method (**LSDM**)

Sec. ① $M_{U.L.} = 1226.31 \text{ kN.m}$ R-Sec.

Sec. ② $M_{U.L.} = 2298.5 \text{ kN.m}$ T-Sec.



$\therefore M_T < 2 M_R \therefore$ Design R-Sec. First.

Sec. ① $M = 1226.31 \text{ kN.m}$, $P = 604.86 \text{ kN}$, $b = 400 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{1226.31 \cdot 10^6}{30 \cdot 400}} = 1118.86 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1118.86) = (1230.74 \rightarrow 1454.5) \text{ mm}$$

$$\text{Take } d = 1300 \text{ mm} , \quad t = 1300 + 100 = 1400 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{604.86 \cdot 10^3}{30 \cdot 400 \cdot 1400} = 0.036 < 0.04 \therefore (\text{neglect } P)$$

$$\therefore \text{Take } d = d_o = 1118.86 \text{ mm} \therefore \text{Take } \boxed{d = 1200 \text{ mm}} , \quad \boxed{t = 1300 \text{ mm}}$$

$$\therefore C_1 = 3.50 \longrightarrow J = 0.78$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1226.31 \cdot 10^6}{0.780 \cdot 400 \cdot 1118.86} = 3512.9 \text{ mm}^2$$

$$\text{Check } \underline{A_{s_{min.}}} \quad A_{s_{req.}} = 3512.9 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{30}}{400} \right) 400 \cdot 1200 = 1478 \text{ mm}^2$$

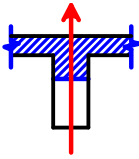
$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 3512.9 \text{ mm}^2 \quad \boxed{\boxed{8 \phi 25}}$$

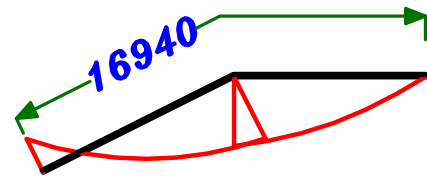
$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$

Sec. ② $M = 2298.5 \text{ kN.m}$, $P = 241.33 \text{ kN}$, $b = 400 \text{ mm}$

Take $d = 1.20 \text{ m}$ (The same d of Sec. ①)

Check $\frac{P}{F_{cu} b t} = \frac{241.33 * 10^3}{30 * 400 * 1300} = 0.0154 < 0.04 \therefore (\text{neglect } P)$

Designed as T-Sec. 



$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = \text{Spacing} = 6.0 \text{ m} = 6000 \text{ mm} \\ 16 t_s + b = 16 * 180 + 400 = 3280 \text{ mm} \\ K \frac{L}{5} + b = 0.8 * \frac{16940}{5} + 400 = 3110 \text{ mm} \end{array} \right\} \quad B = 3110 \text{ mm}$$

$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} B}} \therefore 1200 = c_1 \sqrt{\frac{2298.5 * 10^6}{30 * 3110}} \rightarrow c_1 = 7.64 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{2298.5 * 10^6}{0.826 * 400 * 1200} = 5797.2 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 5797.2 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{400} \right) 400 * 1200 = 1478 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 5797.2 \text{ mm}^2 \quad (12 \phi 25)$$

Sec. ③ R-Sec. $M = 965.31 \text{ kN.m}$, $P = 1243.35 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{965.31 * 10^6}{30 * 400}} = 992.7 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (992.7) = (1092 \rightarrow 1290.5) \text{ mm}$$

$$\therefore \text{Take } d = 1100 \text{ mm} , t = 1200 \text{ mm}$$

Check $\frac{P}{F_{cu} b t} = \frac{1243.35 \cdot 10^3}{30 \cdot 400 \cdot 1200} = 0.086 > 0.04$ (Don't neglect P)

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{965.31}{1243.35} = 0.77 \text{ m} \quad \therefore \frac{e}{t} = \frac{0.77}{1.20} = 0.64 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 0.77 + \frac{1.20}{2} - 0.10 = 1.27 \text{ m}$$

$$M_s = P \cdot e_s = 1243.35 \cdot 1.27 = 1579.0 \text{ kN.m}$$

$$\therefore 1100 = C_1 \sqrt{\frac{1579.0 \cdot 10^6}{30 \cdot 400}} \rightarrow C_1 = 3.03 \rightarrow J = 0.747$$

$$\begin{aligned} \therefore A_s &= \frac{M_s}{J F_y d} - \frac{P_{u.l.}}{(F_y \setminus \delta_s)} \\ &= \frac{1579.0 \cdot 10^6}{0.747 \cdot 400 \cdot 1100} - \frac{1243.35 \cdot 10^3}{(400 \setminus 1.15)} = 1229 \text{ mm}^2 \end{aligned}$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1229 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{30}}{400} \right) 400 \cdot 1100 = 1355.6 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$\left. \begin{aligned} A_{s_{min.}} &= \left(0.225 \cdot \frac{\sqrt{30}}{400} \right) 400 \cdot 1100 = 1355.6 \text{ mm}^2 \\ 1.3 A_{s_{req.}} &= 1.3 \cdot 1229 = 1597.7 \text{ mm}^2 \end{aligned} \right\} \text{الأقل} = 1355.6 \text{ mm}^2$$

3 ϕ 25

Sec. ④ R-Sec. $M = 965.31 \text{ kN.m}$, $P = 714.81 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{965.31 * 10^6}{30 * 400}} = 992.7 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (992.7) = (1092 \rightarrow 1290.5) \text{ mm}$$

$$\therefore \text{Take } \boxed{d = 1100 \text{ mm}} , \boxed{t = 1200 \text{ mm}}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{714.81 * 10^3}{30 * 400 * 1200} = 0.049 > 0.04 \quad (\text{Don't neglect } P)$$

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{965.31}{714.81} = 1.35 \text{ m} \therefore \frac{e}{t} = \frac{1.35}{1.20} = 1.12 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.35 + \frac{1.20}{2} - 0.10 = 1.85 \text{ m}$$

$$M_s = P * e_s = 714.81 * 1.85 = 1322.4 \text{ kN.m}$$

$$\therefore 1100 = C_1 \sqrt{\frac{1322.4 * 10^6}{30 * 400}} \rightarrow C_1 = 3.31 \rightarrow J = 0.769$$

$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{u.l.}}{(F_y \setminus \gamma_s)}$$

$$= \frac{1322.4 * 10^6}{0.769 * 400 * 1100} - \frac{714.81 * 10^3}{(400 \setminus 1.15)} = 1853.2 \text{ mm}^2$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 1853.2 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{400} \right) 400 * 1100 = 1355.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1853.2 \text{ mm}^2 \quad \boxed{4 \phi 25}$$

$$\text{Stirrup Hangers} \approx 0.4 A_s \approx 0.4 * 1853.2 = 741 \text{ mm}^2 \quad \boxed{2 \phi 22}$$

Sec. ⑤ R-Sec. $M = 1226.31 \text{ kN.m}$, $P = 1008.0 \text{ kN}$

Take $d = 1.10 \text{ m}$ (The same d of Sec. ④)

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{1008.0 * 10^3}{30 * 400 * 1200} = 0.070 > 0.04 \text{ (Don't neglect } P \text{)}$$

∴ Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{1226.31}{1008.0} = 1.21 \text{ m} \quad \therefore \frac{e}{t} = \frac{1.21}{1.20} = 1.0 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.21 + \frac{1.20}{2} - 0.10 = 1.71 \text{ m}$$

$$M_s = P * e_s = 1008.0 * 1.71 = 1723.7 \text{ kN.m}$$

$$\therefore 1100 = C_1 \sqrt{\frac{1723.7 * 10^6}{30 * 400}} \rightarrow C_1 = 2.90 \rightarrow J = 0.734$$

$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{u.l.}}{(F_y \setminus \delta_s)}$$

$$= \frac{1723.7 * 10^6}{0.734 * 400 * 1100} - \frac{1008.0 * 10^3}{(400 \setminus 1.15)} = 2439.2 \text{ mm}^2$$

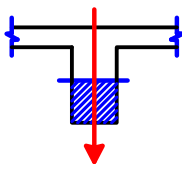
Check $A_{s_{min.}}$ $A_{s_{req.}} = 2439.2 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{400} \right) 400 * 1100 = 1355.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2439.2 \text{ mm}^2 \quad \textcircled{5 \phi 25}$$

$$\text{Stirrup Hangers} \approx 0.4 A_s \approx 0.4 * 2439.2 = 975.68 \text{ mm}^2 \quad \textcircled{2 \phi 25}$$

Sec. ⑥ $M = 261 \text{ kN.m}$, $b = 400 \text{ mm}$ *R-Sec.*



$$d = 3.5 \sqrt{\frac{261 * 10^6}{30 * 400}} = 516.1 \text{ mm}$$

\therefore Take $d = 550 \text{ mm}$, $t = 600 \text{ mm}$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{261 * 10^6}{0.78 * 400 * 516.1} = 1621 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1621 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{400} \right) 400 * 550 = 677.8 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 1621 \text{ mm}^2$ $4 \phi 25$

Take $Y = 0.40 \text{ m}$



Check Shear.

– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{30}{1.5}} = 3.13 \text{ N/mm}^2$$

Sec. ① $Q = 670.08 \text{ kN}$

$$\therefore \text{Actual shear stress.} = q_u = \frac{Q}{b d} = \frac{670.08 * 10^3}{400 * 1200} = 1.39 \text{ N/mm}^2$$

$\therefore q_{cu} < q_u < q_{max.}$ \therefore We need Stirrups more Than $5 \phi 8 \setminus m$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \setminus \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.39 - \frac{1.07}{2} = \frac{2 * 50.3 (240 \setminus 1.15)}{400 * S} \rightarrow S = 61.3 \text{ mm} < 100 \text{ mm}$$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

$$1.39 - \frac{1.07}{2} = \frac{2 * 78.5 (240 \setminus 1.15)}{400 * S} \rightarrow S = 95.8 \text{ mm} < 100 \text{ mm}$$

* Take $n = 4$, $\phi 8 \rightarrow A_s = 78.5 \text{ mm}^2$

$$1.39 - \frac{1.07}{2} = \frac{4 * 50.3 (240 \setminus 1.15)}{400 * S} \rightarrow S = 122.8 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups} \setminus m = \frac{1000}{S} = \frac{1000}{122.8} = 8.14 = 9.0$$

\therefore Use Stirrups $9 \phi 8 \setminus m$ 4 branches

Sec. ② $Q = 557.31 \text{ kN}$

$$\therefore \text{Actual shear stress.} = q_u = \frac{Q}{b d} = \frac{557.31 * 10^3}{400 * 1200} = 1.16 \text{ N} \setminus \text{mm}^2$$

$\therefore q_{cu} < q_u < q_{max.}$ \therefore We need Stirrups more Than $5 \phi 8 \setminus m$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \setminus \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.16 - \frac{1.07}{2} = \frac{2 * 50.3 (240 \setminus 1.15)}{400 * S} \rightarrow S = 83.97 \text{ mm} < 100 \text{ mm}$$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

$$1.39 - \frac{1.07}{2} = \frac{2 * 78.5 (240 \setminus 1.15)}{400 * S} \rightarrow S = 131.0 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups \setminus m} = \frac{1000}{S} = \frac{1000}{131.0} = 7.63 = 8.0$$

\therefore Use Stirrups $8 \phi 10 \setminus \text{m}$ 2 branches

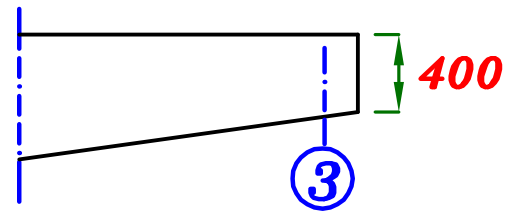
Sec. ③ $Q = 120.0 \text{ kN}$

\therefore Actual shear stress. =

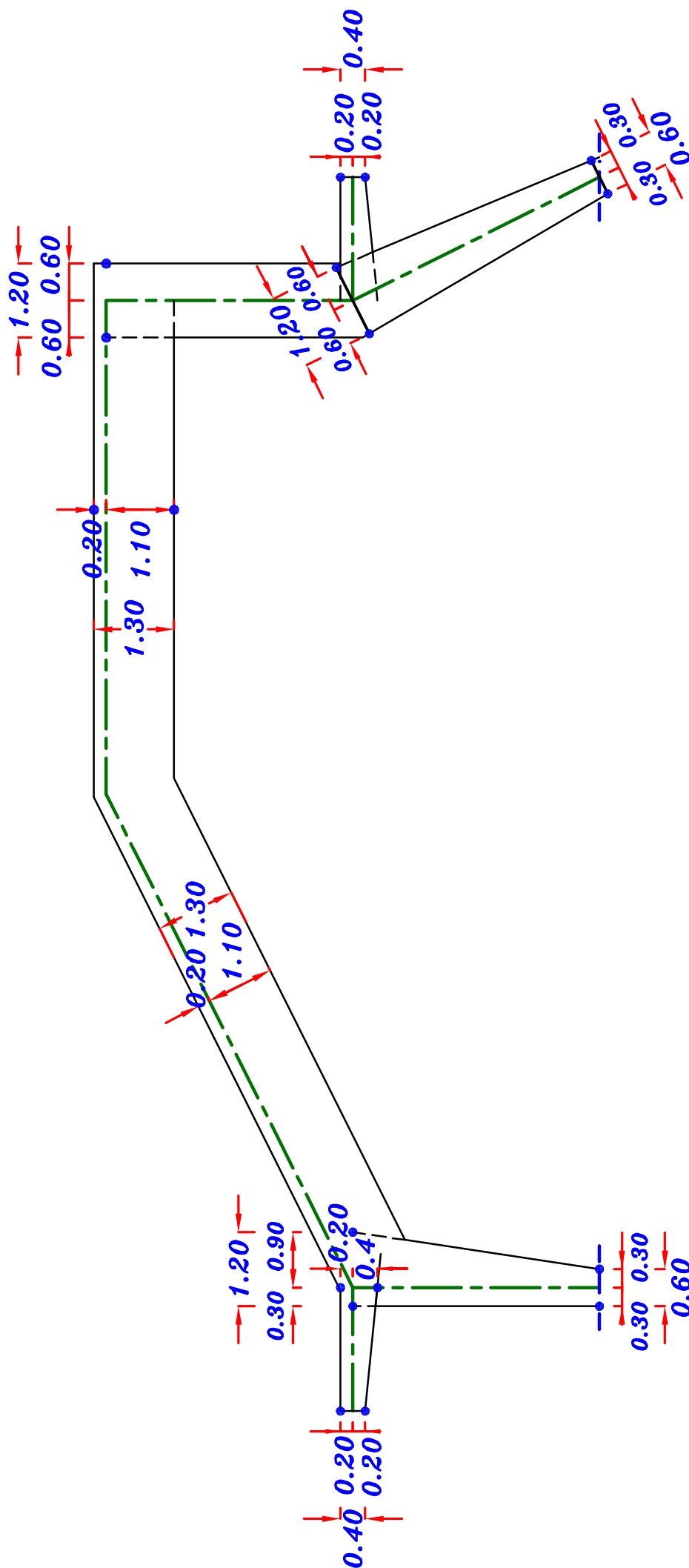
$$q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

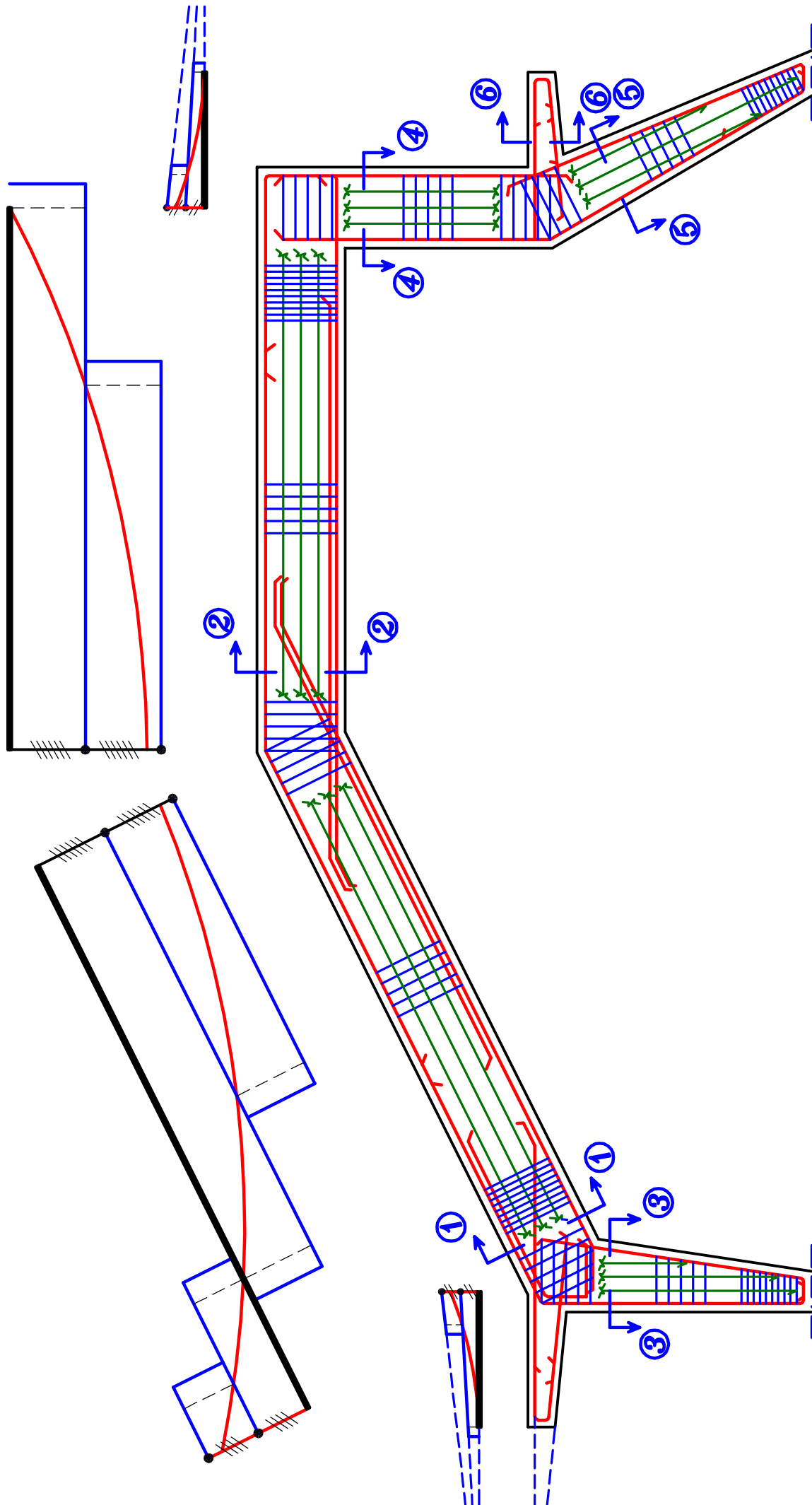
$$= \frac{120.0 * 10^3}{400 * 350} - \text{ZERO} = 0.857 \text{ N \setminus mm}^2$$

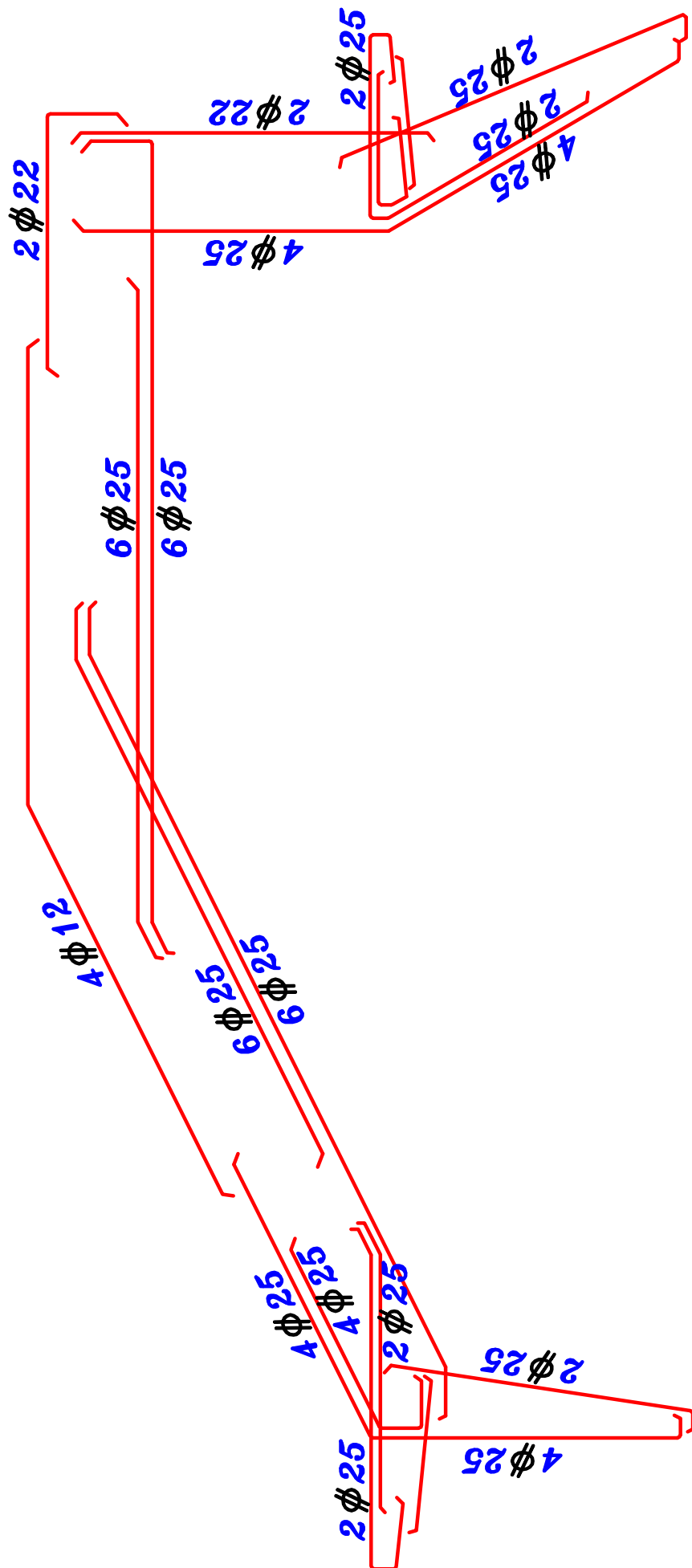
$\therefore q_u < q_{cu} \rightarrow$ Use min. stirrups $5 \phi 8 \setminus \text{m}$

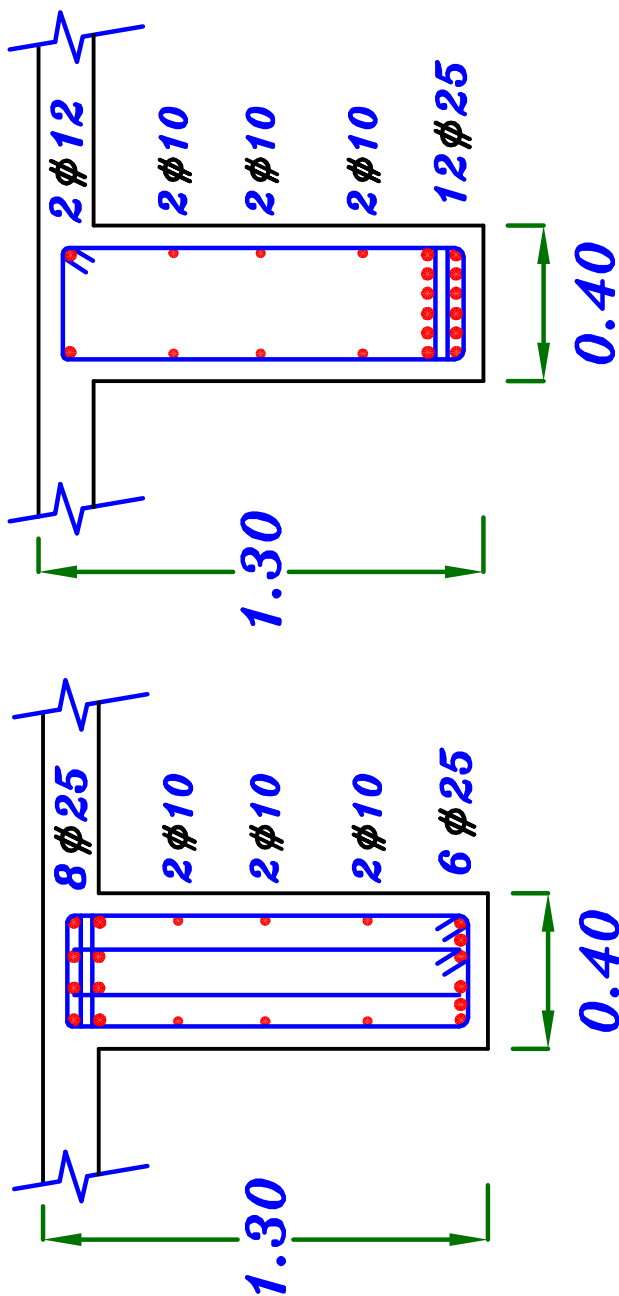


C – Draw the details of reinforcement For intermediate Frame (F) in elevation to scale **1:50** and cross sections to scale **1:25** . Curtailment of bars using the moment diagram is required.

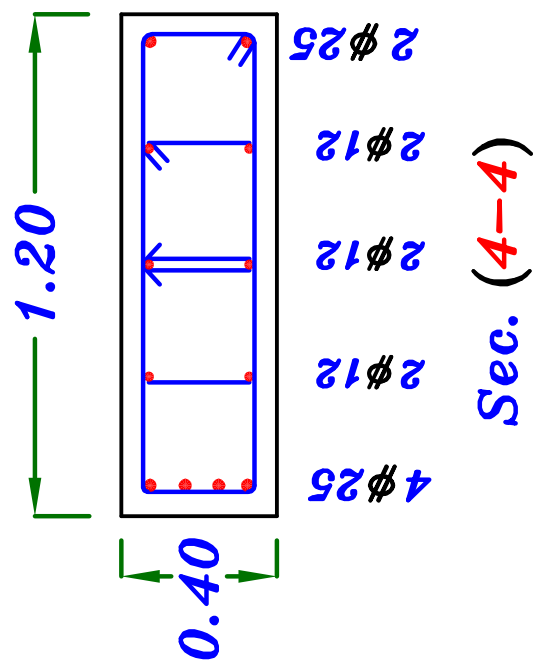




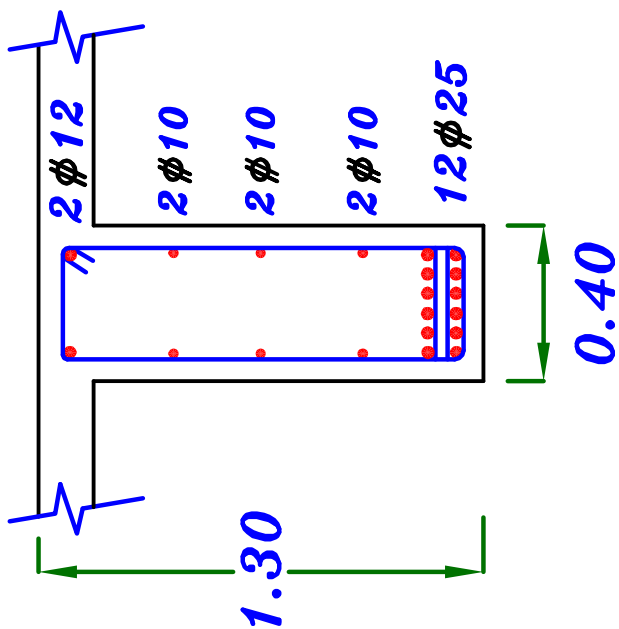




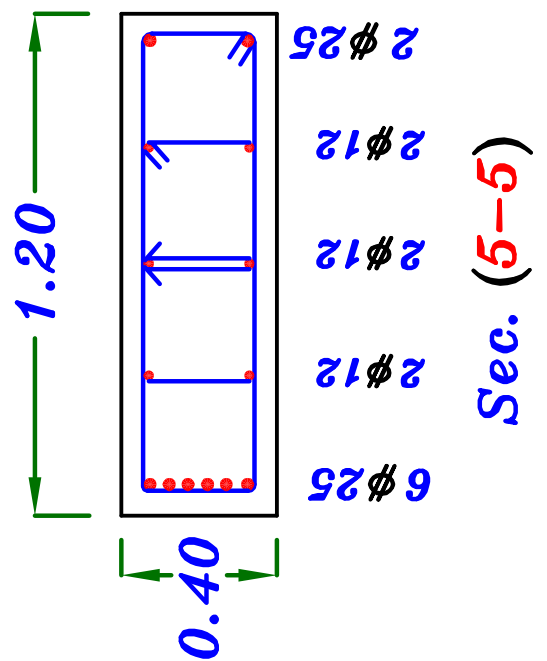
Sec. (1-1)



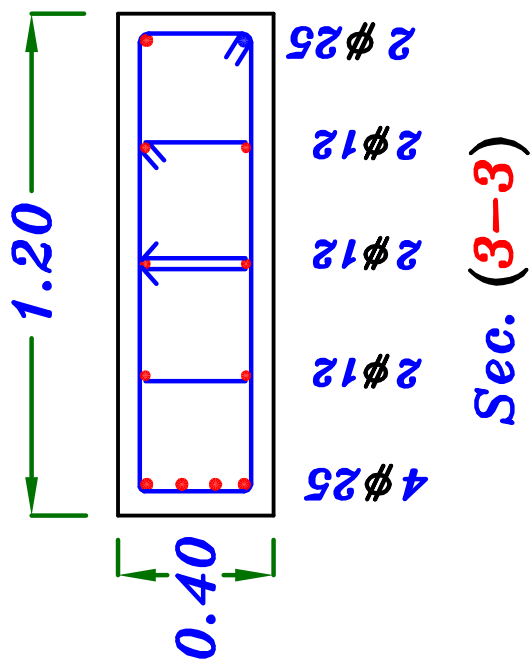
Sec. (4-4)



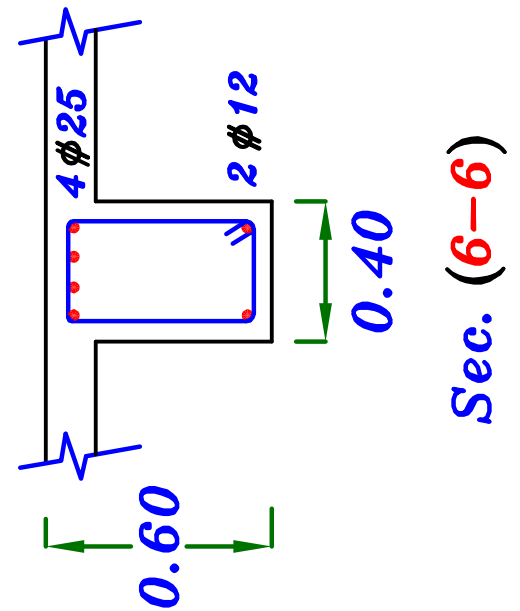
Sec. (2-2)



Sec. (5-5)



Sec. (3-3)



Sec. (6-6)

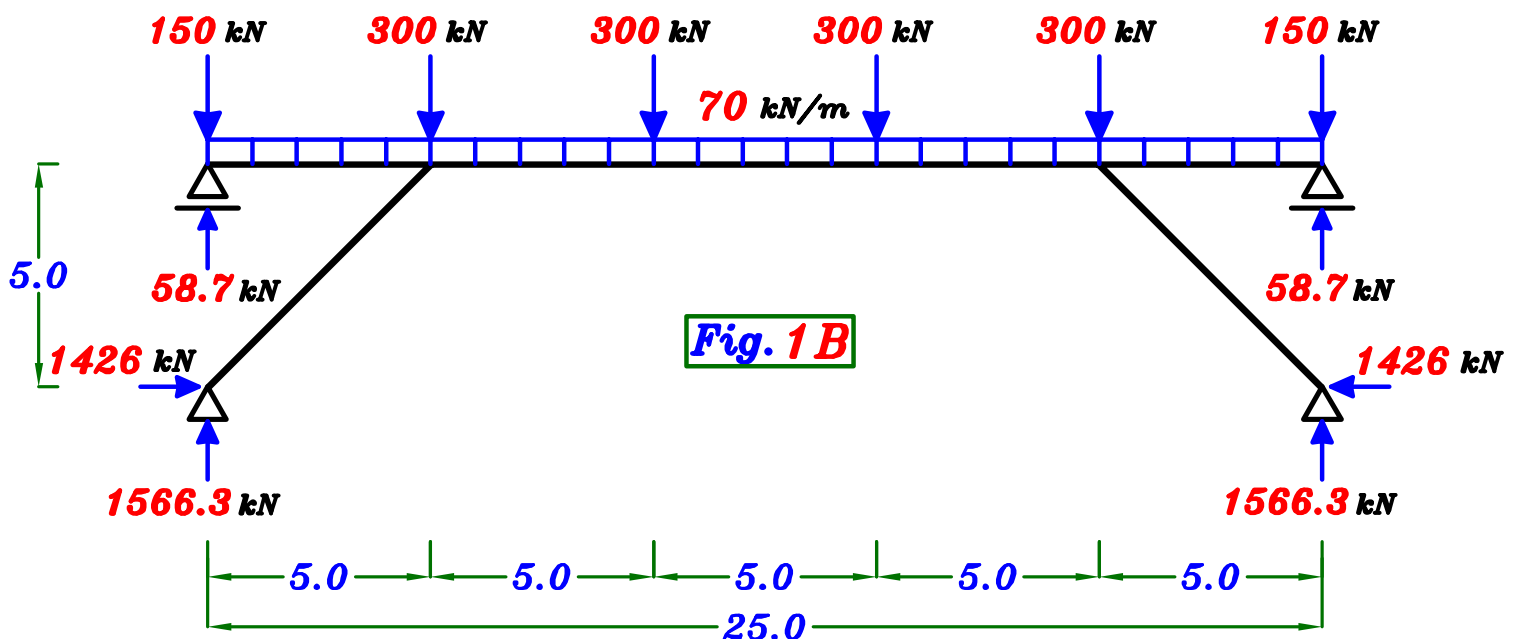
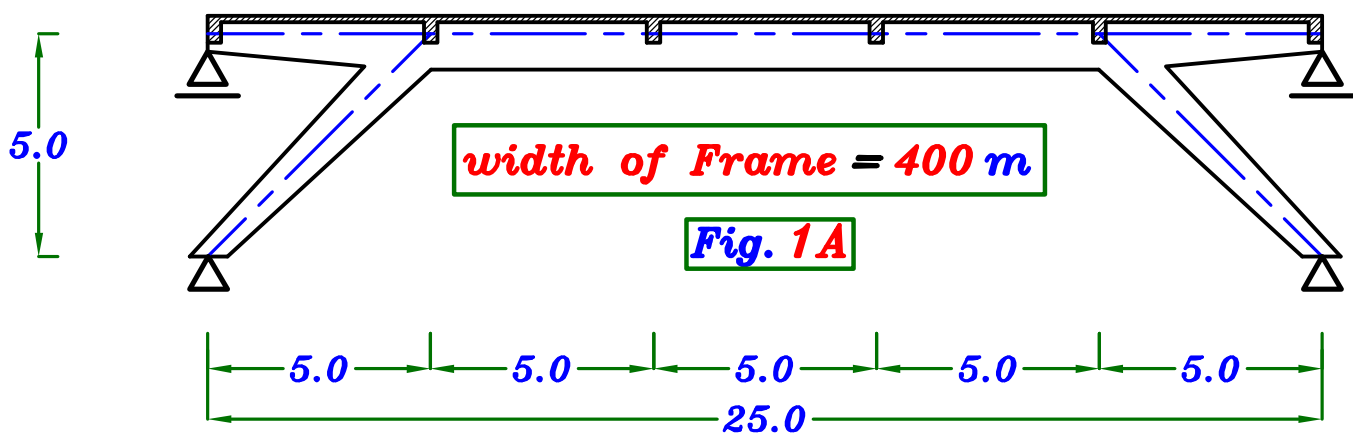
Example.

Fig. 1A shows a schematic elevation of a main Frame of a roadway concrete bridge. For the given geometrical and loading conditions. It is required to :

- 1- Draw a sectional elevation showing the concrete dimensions of different structural elements including the Foundation taking into consideration that the Frame are spaced by **6.0 meters**
- 2- Draw the **B.M.D. , N.F.D. & S.F.D.** For the main Frame using the given service (**working**) loads in **Fig. 1B**
- 3- Design the different concrete sections of the main Frame using ultimate limit design method
- 4- Check shear For the horizontal girder only using ultimate limit design method
- 5- Draw a sectional elevation (**Scale 1:50**) and cross sections (**Scale 1:25**) showing the reinforcement details of the main Frame using the moment of resistance.

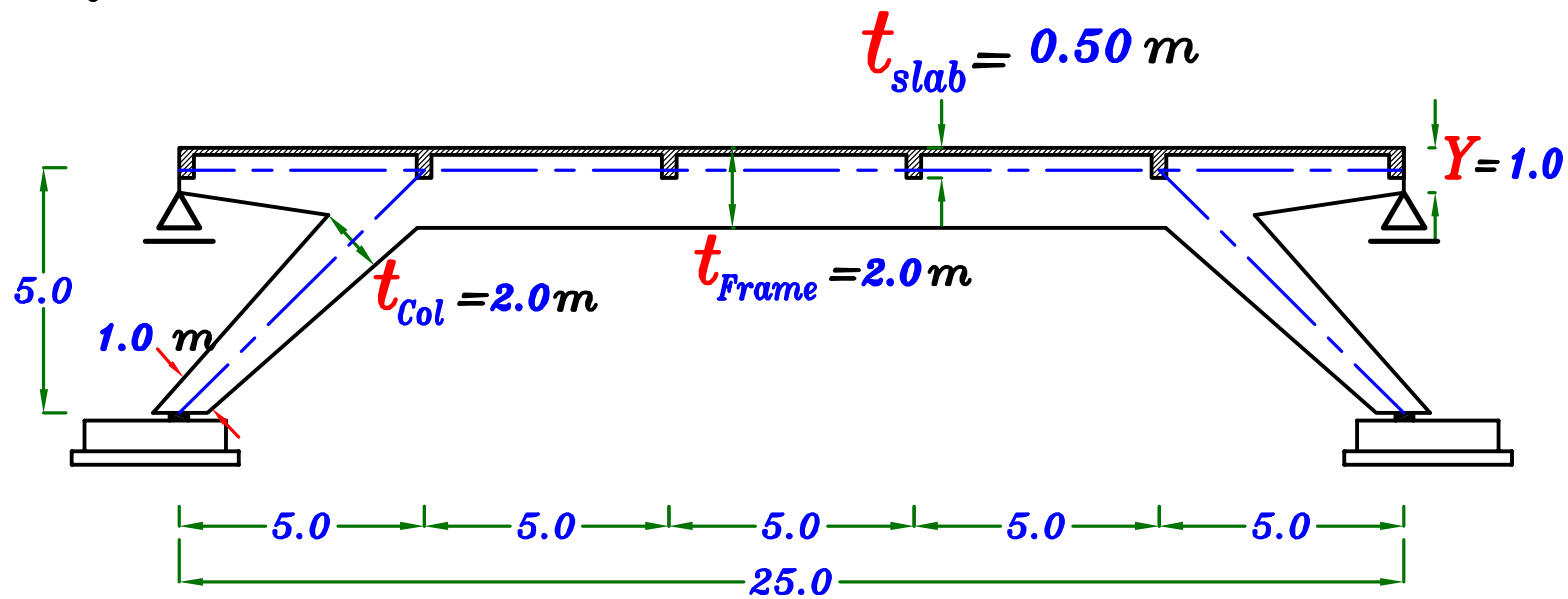
Concrete Grade. C 35 $F_{cu} = 35 \text{ MPa}$

Steel Grade: st. 52 $F_y = 360 \text{ MPa}$



Question (1)

- 1- Draw a sectional elevation showing the concrete dimensions of different structural elements including the Foundation taking into consideration that the Frame are spaced by **6.0 meters**



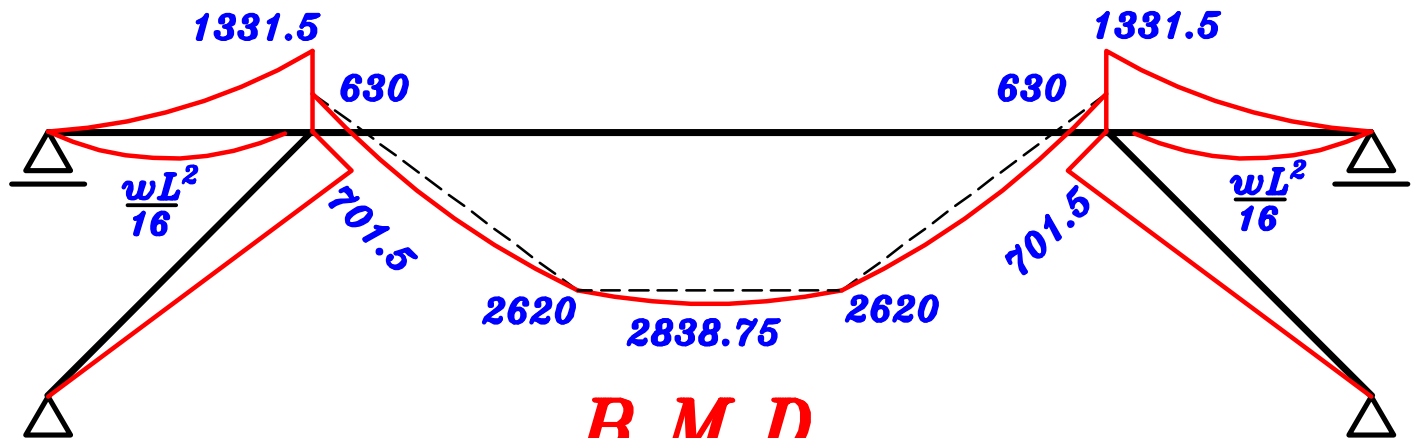
$$t_{Frame} = \frac{L}{12 \rightarrow 14} = \frac{25.0}{12 \rightarrow 14} = (1.78 \rightarrow 2.08) m = 2.0 m$$

$$Y = \frac{t_{Frame}}{2} = 1.0 m$$

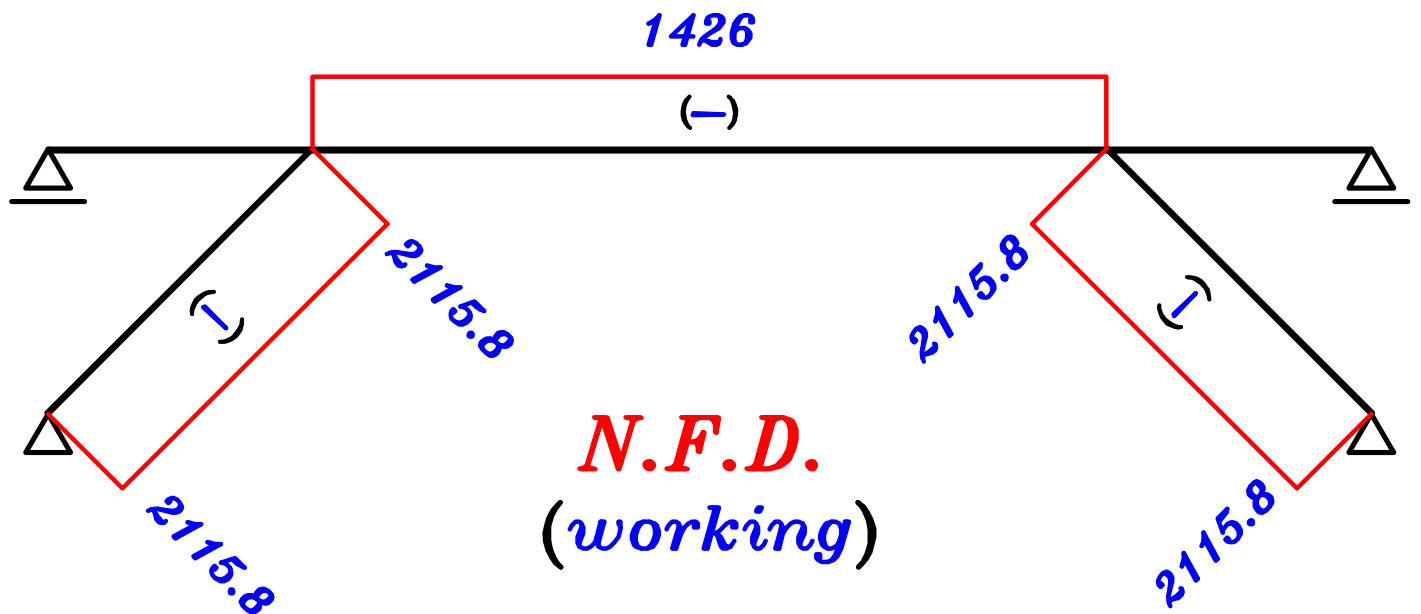
$$t_{col.} = t_{Frame} = 2.0 m$$

$$t_{secondary Beams} = \frac{spacing}{12} = \frac{6.0}{12} = 0.50 m$$

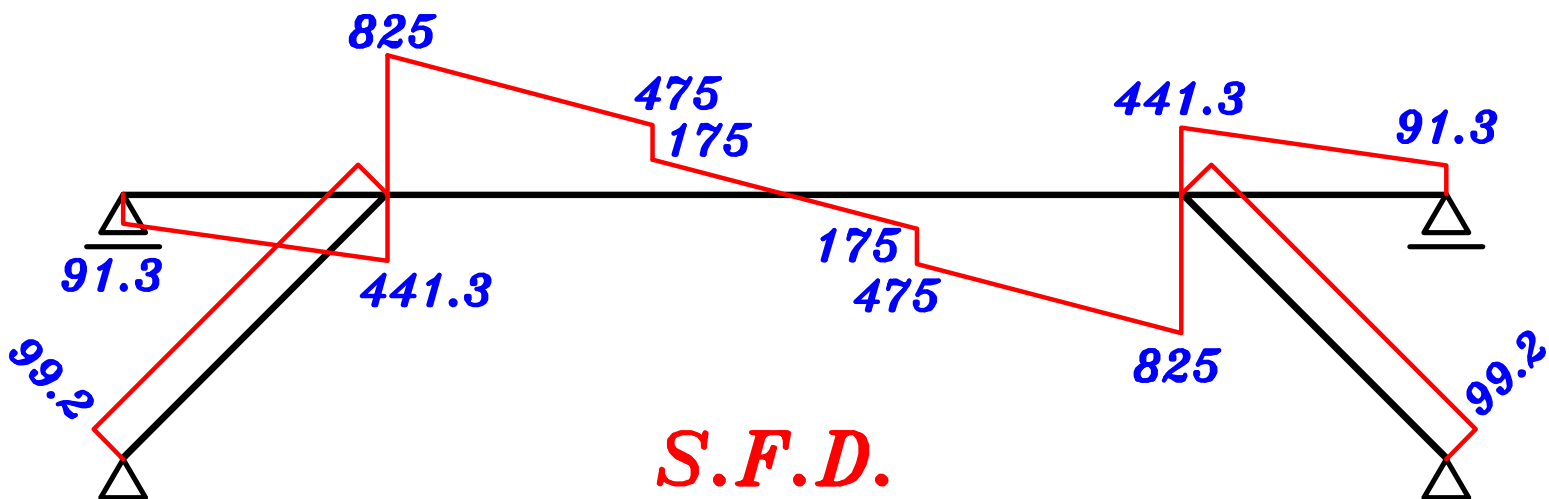
I.F.D. (working)



B.M.D.
(working)

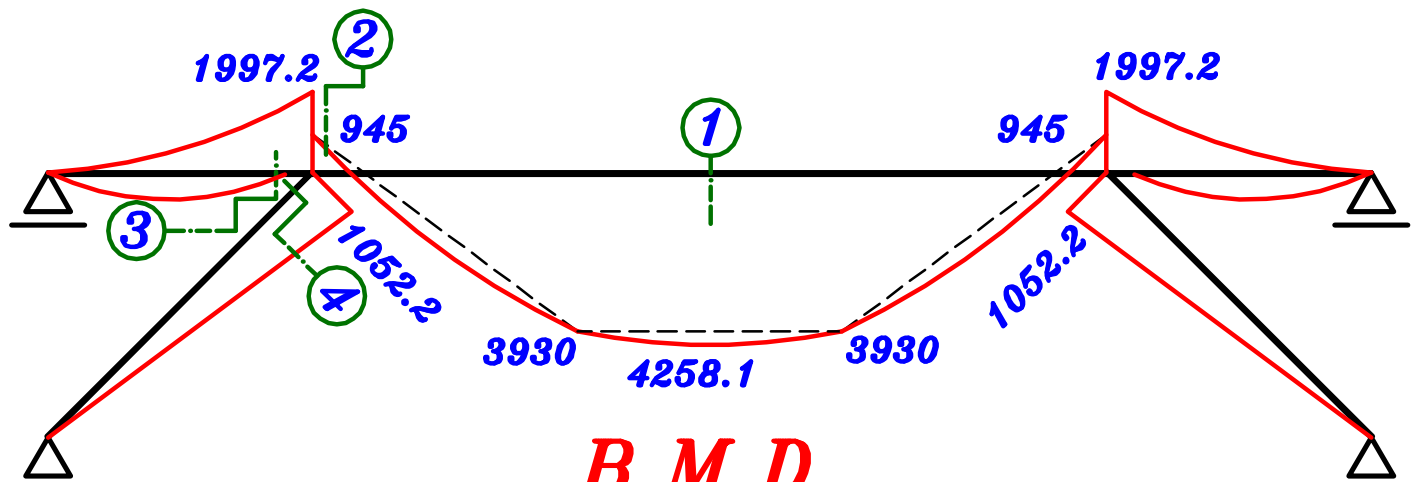


N.F.D.
(working)

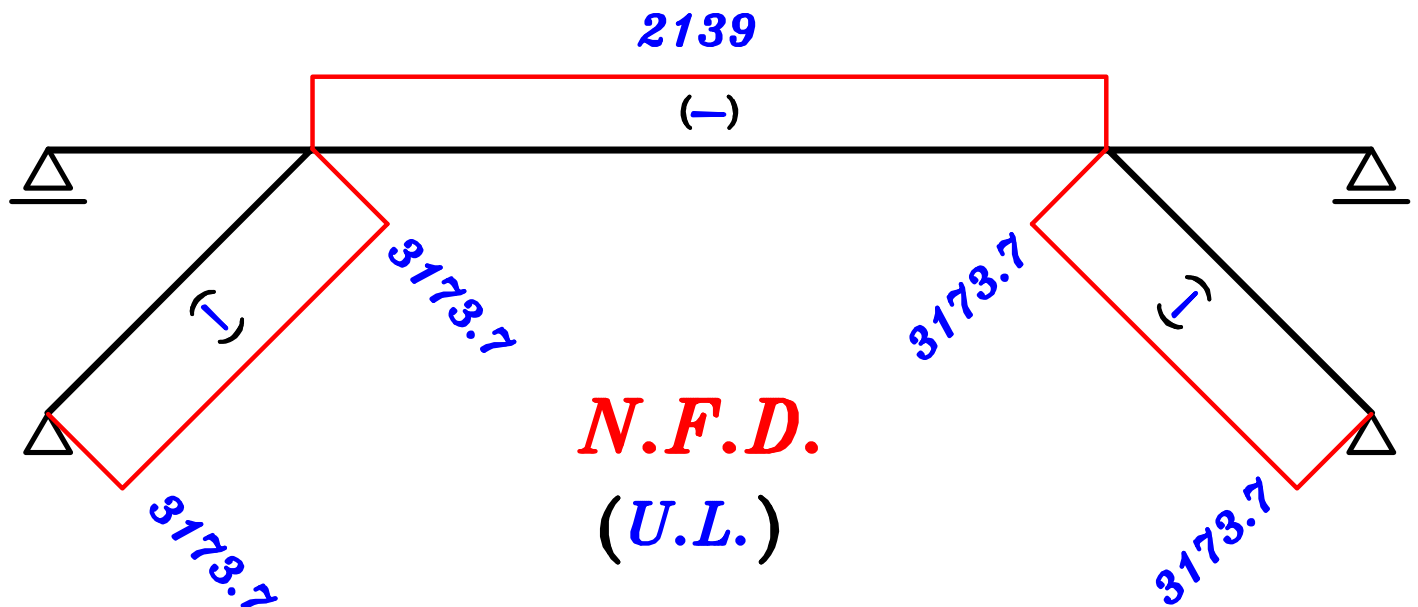


S.F.D.
(working)

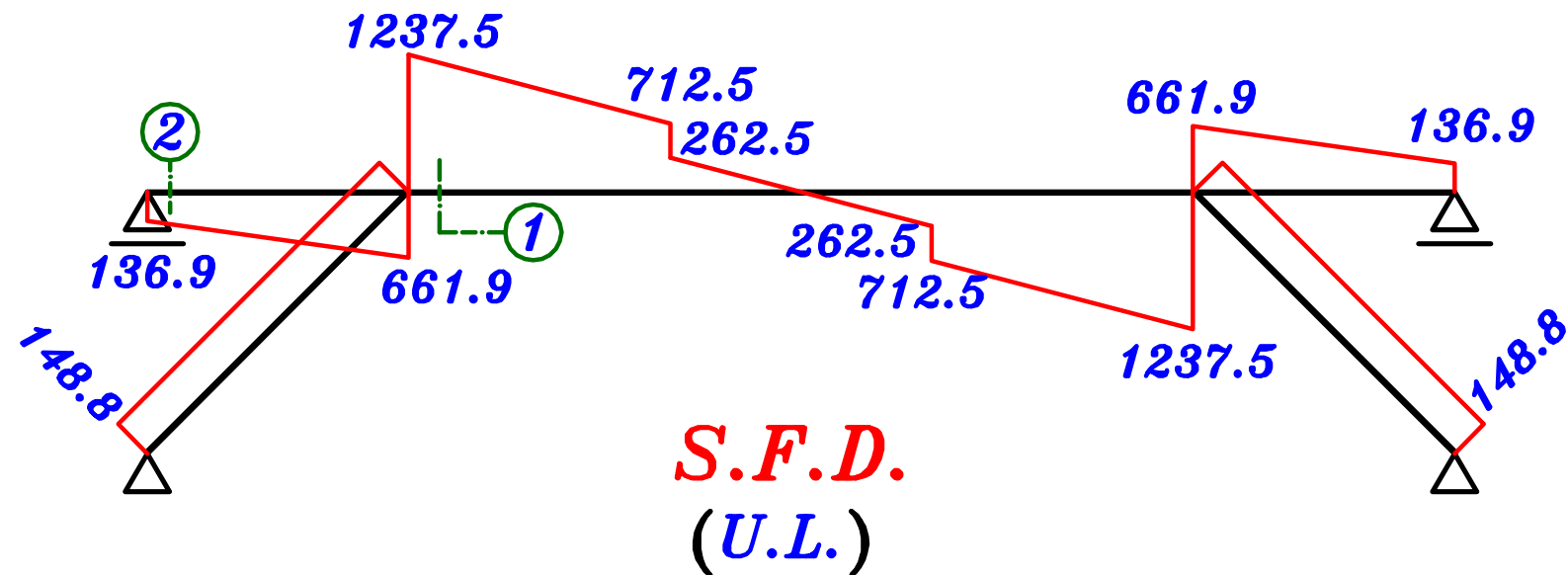
I.F.D. (U.L.)



B.M.D. (U.L.)



N.F.D. (U.L.)

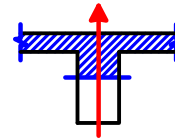


S.F.D. (U.L.)

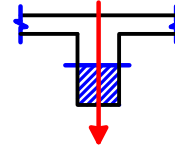
4 - Design the critical sections of the Frame For Bending and shear.

Concrete Dimensions الأبعاد التي تم فرضها لل
عاده نستخدمها في حساب الاوزان فقط و ليس شرط ان نأخذها معنا في التصميم .

Sec. ① $M_{U.L.} = 4258.1 \text{ kN.m}$ T-Sec.



Sec. ③ $M_{U.L.} = 1997.2 \text{ kN.m}$ R-Sec.



$\therefore M_T > 2 M_R \therefore \text{Design T-Sec. First.}$

Sec. ① $M = 4258.1 \text{ kN.m}$, $P = 2139 \text{ kN}$, $b = 400 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{4258.1 \cdot 10^6}{35 \cdot 400}} = 1930.2 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1930.2) = (2123.2 \rightarrow 2509.2) \text{ mm}$$

Take $d = 2200 \text{ mm}$, $t = 2200 + 100 = 2300 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{2139 \cdot 10^3}{35 \cdot 400 \cdot 2300} = 0.066 > 0.04 \therefore (\text{Don't neglect } P)$

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{4258.1}{2139} = 2.0 \text{ m} \quad \therefore \frac{e}{t} = \frac{2.0}{2.3} = 0.86 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 2.0 + \frac{2.30}{2} - 0.10 = 3.05 \text{ m}$$

$$M_s = P \cdot e_s = 2139 \cdot 3.05 = 6523.9 \text{ kN.m}$$

$$\therefore 2200 = C_1 \sqrt{\frac{6523.9 \cdot 10^6}{35 \cdot 400}} \longrightarrow C_1 = 3.22 \longrightarrow J = 0.762$$

$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \delta_s)}$$

$$\therefore A_s = \frac{6523.9 * 10^6}{0.762 * 360 * 2200} - \frac{2139 * 10^3}{(360 \setminus 1.15)} = 3977.1 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 3977.1 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{35}}{360} \right) 400 * 2200 = 3253.8 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 3977.1 \text{ mm}^2 \quad \textcircled{9 \phi 25}$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$

Sec. ② $M = 945 \text{ kN.m}$, $P = 2139 \text{ kN}$, $b = 400 \text{ mm}$
 $d = 2200 \text{ mm}$ (the same depth of sec. ①)

Check $\frac{P}{F_{cu} b t} = \frac{2139 * 10^3}{35 * 400 * 2300} = 0.066 > 0.04 \therefore (\text{Don't neglect } P)$

\therefore Design the Sec. on both **N.F.** & **B.M.**

$$e = \frac{M}{P} = \frac{945}{2139} = 0.44 \text{ m} \therefore \frac{e}{t} = \frac{0.44}{2.3} = 0.19 < 0.5 \xrightarrow{\text{Use}} \text{I.D.}$$

\therefore Use Interaction Diagram

$$\zeta = \frac{2300 - 200}{2300} = 0.90 \xrightarrow{\text{use}} \text{ECCS Design Aids Page 4-23}$$

$$\left. \begin{aligned} \frac{P_U}{F_{cu} b t} &= \frac{2139 * 10^3}{35 * 400 * 2300} = 0.066 \\ \frac{M_U}{F_{cu} b t^2} &= \frac{945 * 10^6}{35 * 400 * 2300^2} = 0.0127 \end{aligned} \right\} \rho < 1.0 \xrightarrow{\text{Take}} \rho = 1.0$$

$$\mu = \rho * F_{cu} * 10^{-4} = 1.0 * 35 * 10^{-4} = 3.5 * 10^{-3}$$

$$A_s = A_{s'} = \mu * b * t = 3.5 * 10^{-3} * 400 * 2300 = 3220 \text{ mm}^2$$

– Check $A_{s_{min.}} = \frac{0.8}{100} * b * t = \frac{0.8}{100} * 400 * 2300 = 7360 \text{ mm}^2$

$$A_{s_{Total}} = A_s + A_{s'} = 2 * 3220 = 6440 \text{ mm}^2 \therefore A_{s_{Total}} < A_{s_{min.}}$$

$$\therefore \text{take } A_s = A_{s'} = \frac{A_{s_{min.}}}{2} = \frac{7360}{2} = 3680 \text{ mm}^2 \quad \textcircled{8 \phi 25}$$

Sec. ③ $M = 1997.2 \text{ kN.m}$, $b = 400 \text{ mm}$

$d = 2200 \text{ mm}$ (the same depth of Sec. ①)

$$\therefore 2200 = C_1 \sqrt{\frac{1997.2 * 10^6}{35 * 400}} \rightarrow C_1 = 5.82 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1997.2 * 10^6}{0.826 * 360 * 2200} = 3052.9 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 3052.9 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{35}}{360} \right) 400 * 2200 = 3253.8 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$\left. \begin{aligned} A_{s_{min.}} &= \left(0.225 * \frac{\sqrt{35}}{360} \right) 400 * 2200 = 3253.8 \text{ mm}^2 \\ 1.3 A_{s_{req.}} &= 1.3 * 3052.9 = 3968.8 \text{ mm}^2 \end{aligned} \right\} \begin{array}{l} \text{الأقل} \\ = 3253.8 \text{ mm}^2 \end{array} \quad \textcircled{7 \# 25}$$

Sec. ④ $R\text{-Sec.}$ $M = 1052.2 \text{ kN.m}$, $P = 3173.7 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{1052.2 * 10^6}{35 * 400}} = 959.5 \text{ mm} \quad (\text{as } R\text{-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (959.5) = (1055.4 \rightarrow 1247.3) \text{ mm}$$

$$\therefore \text{Take } d = 1200 \text{ mm} , t = 1200 + 100 = 1300 \text{ mm}$$

$$\therefore t_{(Column)} < 0.8 t_{(Beam)} \xrightarrow{\text{Take}} t_{(Column)} = t_{(Beam)} = 2300 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{3173.7 * 10^3}{35 * 400 * 2300} = 0.098 > 0.04 \therefore (\text{Don't neglect } P)$$

\therefore Design the Sec. on both $N.F.$ & $B.M.$

$$e = \frac{M}{P} = \frac{1052.2}{3173.7} = 0.33 \text{ m} \quad \therefore \frac{e}{t} = \frac{0.33}{2.3} = 0.14 < 0.5 \xrightarrow{\text{Use}} \text{I.D.}$$

\therefore Use Interaction Diagram

$$\zeta = \frac{2300 - 200}{2300} = 0.90 \xrightarrow{\text{use}} \text{ECCS Design Aids Page 4-23}$$

$$\left. \begin{aligned} \frac{P_U}{F_{cu} b t} &= \frac{3173.7 \cdot 10^3}{35 \cdot 400 \cdot 2300} = 0.098 \\ \frac{M_U}{F_{cu} b t^2} &= \frac{1052.2 \cdot 10^6}{35 \cdot 400 \cdot 2300^2} = 0.0142 \end{aligned} \right\} \rho < 1.0 \xrightarrow{\text{Take}} \rho = 1.0$$

$$\mu = \rho \cdot F_{cu} \cdot 10^{-4} = 1.0 \cdot 35 \cdot 10^{-4} = 3.5 \cdot 10^{-3}$$

$$A_s = A_{s'} = \mu \cdot b \cdot t = 3.5 \cdot 10^{-3} \cdot 400 \cdot 2300 = 3220 \text{ mm}^2$$

$$\text{— Check } A_{s_{min.}} = \frac{0.8}{100} \cdot b \cdot t = \frac{0.8}{100} \cdot 400 \cdot 2300 = 7360 \text{ mm}^2$$

$$A_{s_{Total}} = A_s + A_{s'} = 2 \cdot 3220 = 6440 \text{ mm}^2 \quad \therefore A_{s_{Total}} < A_{s_{min.}}$$

$$\therefore \text{take } A_s = A_{s'} = \frac{A_{s_{min.}}}{2} = \frac{7360}{2} = 3680 \text{ mm}^2 \quad (8 \phi 25)$$

Check Shear.

— Allowable shear stress.

$$\text{— } q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{35}{1.5}} = 1.15 \text{ N/mm}^2$$

$$\text{— } q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{35}{1.5}} = 3.38 \text{ N/mm}^2$$

$$\text{Sec. ① } Q = 1237.5 \text{ kN}$$

$$\therefore \text{Actual shear stress.} = q_u = \frac{Q}{b d} = \frac{1237.5 \cdot 10^3}{400 \cdot 2200} = 1.40 \text{ N/mm}^2$$

$\therefore q_{cu} < q_u < q_{max}$. \therefore We need Stirrups more Than $5 \phi 8 \setminus m$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \setminus \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.40 - \frac{1.15}{2} = \frac{2 * 50.3 (240 \setminus 1.15)}{400 * S} \rightarrow S = 63.6 \text{ mm} < 100 \text{ mm}$$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

$$1.40 - \frac{1.15}{2} = \frac{2 * 78.5 (240 \setminus 1.15)}{400 * S} \rightarrow S = 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups} \setminus m = \frac{1000}{S} = \frac{1000}{100} = 10$$

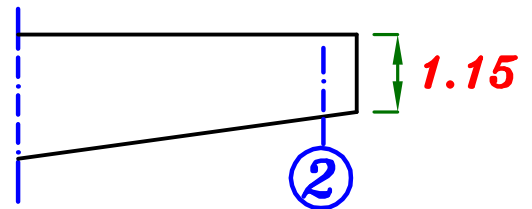
\therefore Use Stirrups $10 \phi 10 \setminus m$ 2 branches

Sec. ③ $Q = 136.9 \text{ kN}$

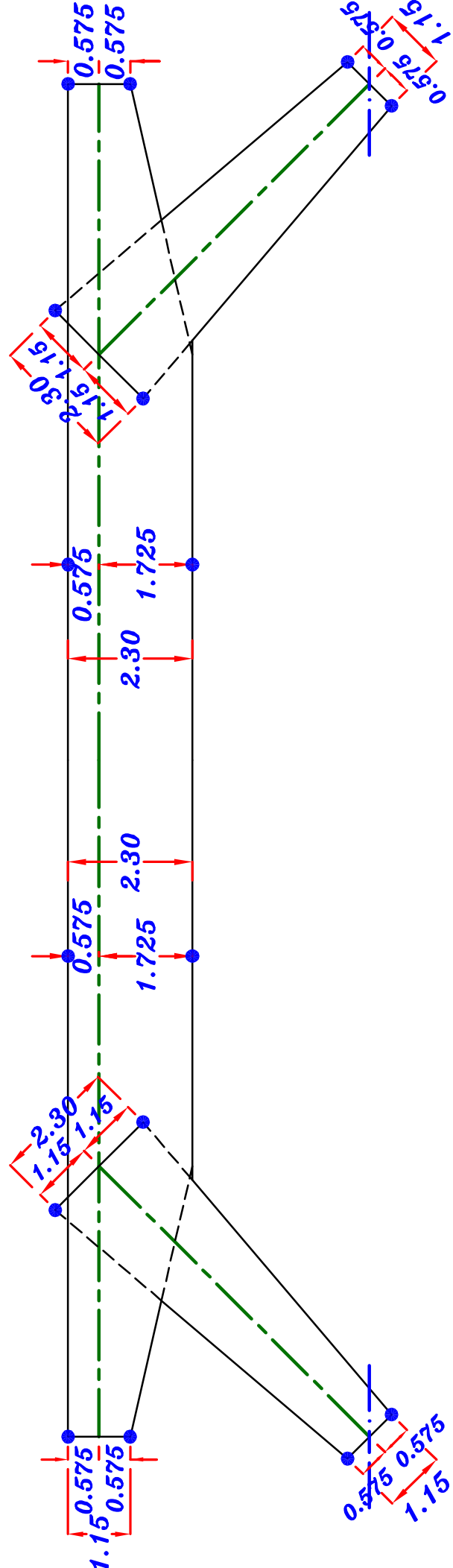
\therefore Actual shear stress. =

$$q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

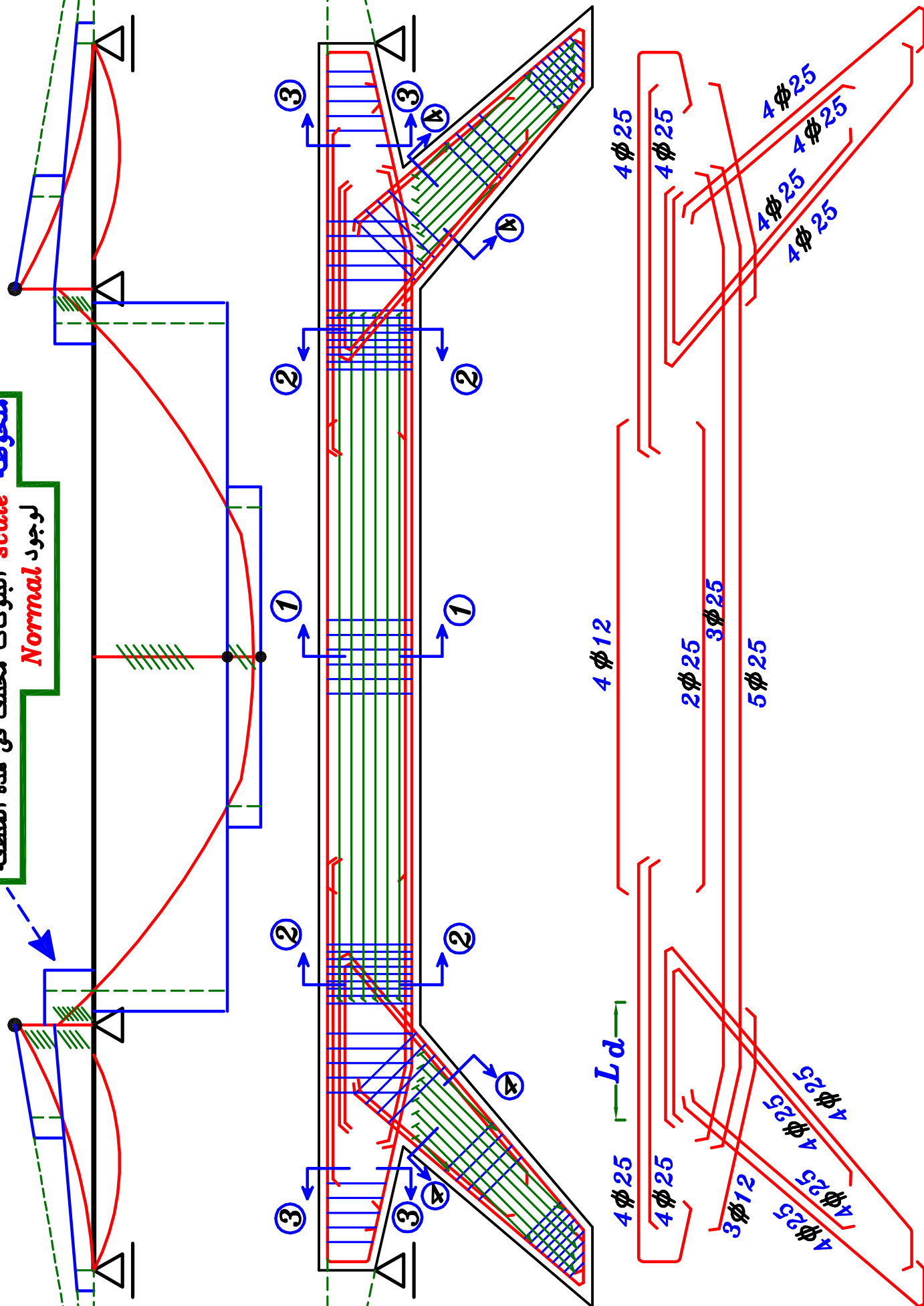
$$= \frac{136.9 * 10^3}{400 * 1050} - \text{ZERO} = 0.32 \text{ N} \setminus \text{mm}^2$$

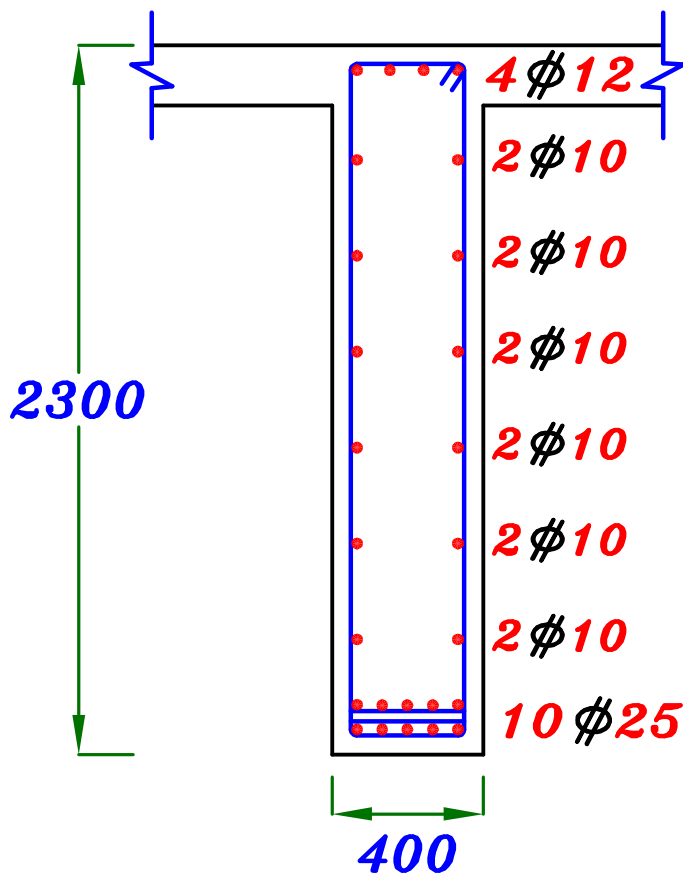


$\therefore q_u < q_{cu} \rightarrow$ Use min. stirrups $5 \phi 8 \setminus m$

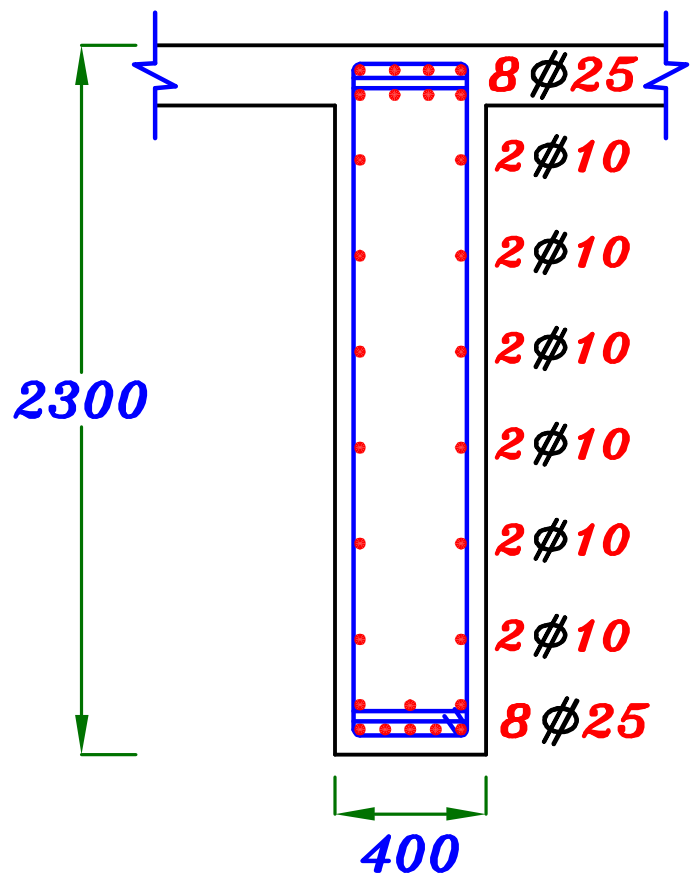


ملحوظة **scale** البلوكات مختلف في هذه المنطقة
 لوجود **Normal**

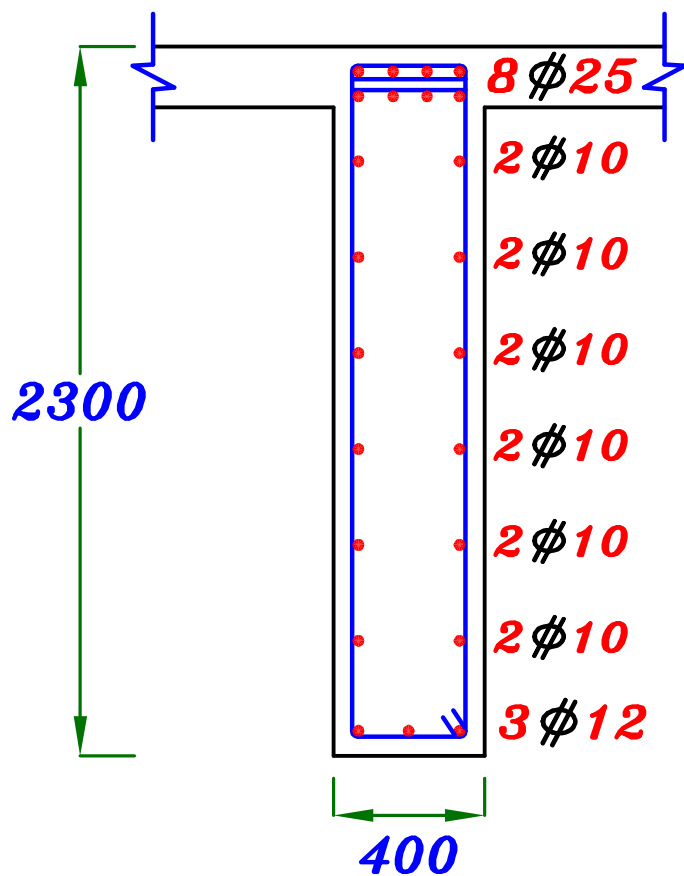




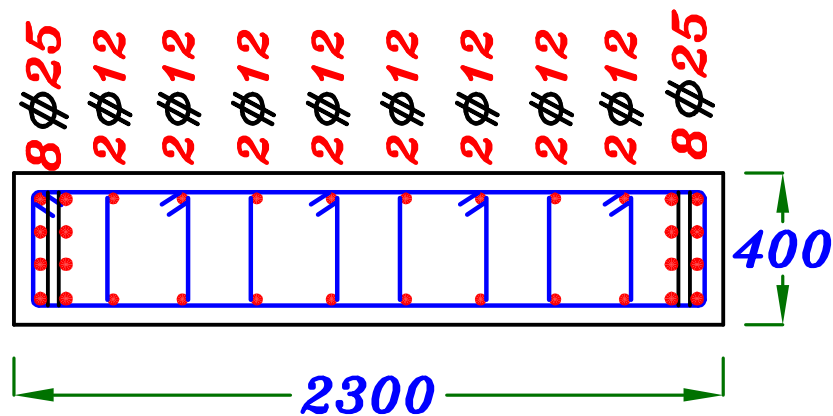
Sec. (1-1)



Sec. (2-2)



Sec. (3-3)



Sec. (4-4)

Example.

Question (1)

Fig. (1) shows a sectional elevation, statical system and load diagram For a reinforced concrete stadium ring Frame. The ring stadium is covered by reinforced concrete slabs supported by a system of secondary beams and Frames (**F**), spaced at **6.0 m**.

For an intermediate panel, **It is required to :**

- 1- Without any calculation but with reasonably assumed concrete dimensions, draw sectional For the ring Frame, Showing the dimensions of all concrete elements. to scale **1:50**
- 2- Draw **B.M.D., N.F.D. & S.F.D.** For case of **total load only** of an intermediate Frame (**F**) Using the given **Ultimate limit loads**.
- 3- Design the critical sections For the intermediate Frame (**F**), to satisfy both bending moment and normal Forces.
- 4- Design the critical sections For the intermediate Frame (**F**), to satisfy the shearing Force.
- 5- Using the **moment of resistance principle**. draw the details of reinforcement For the Frame in elevation (scale **1:50**) and cross sections (scale **1:20**)

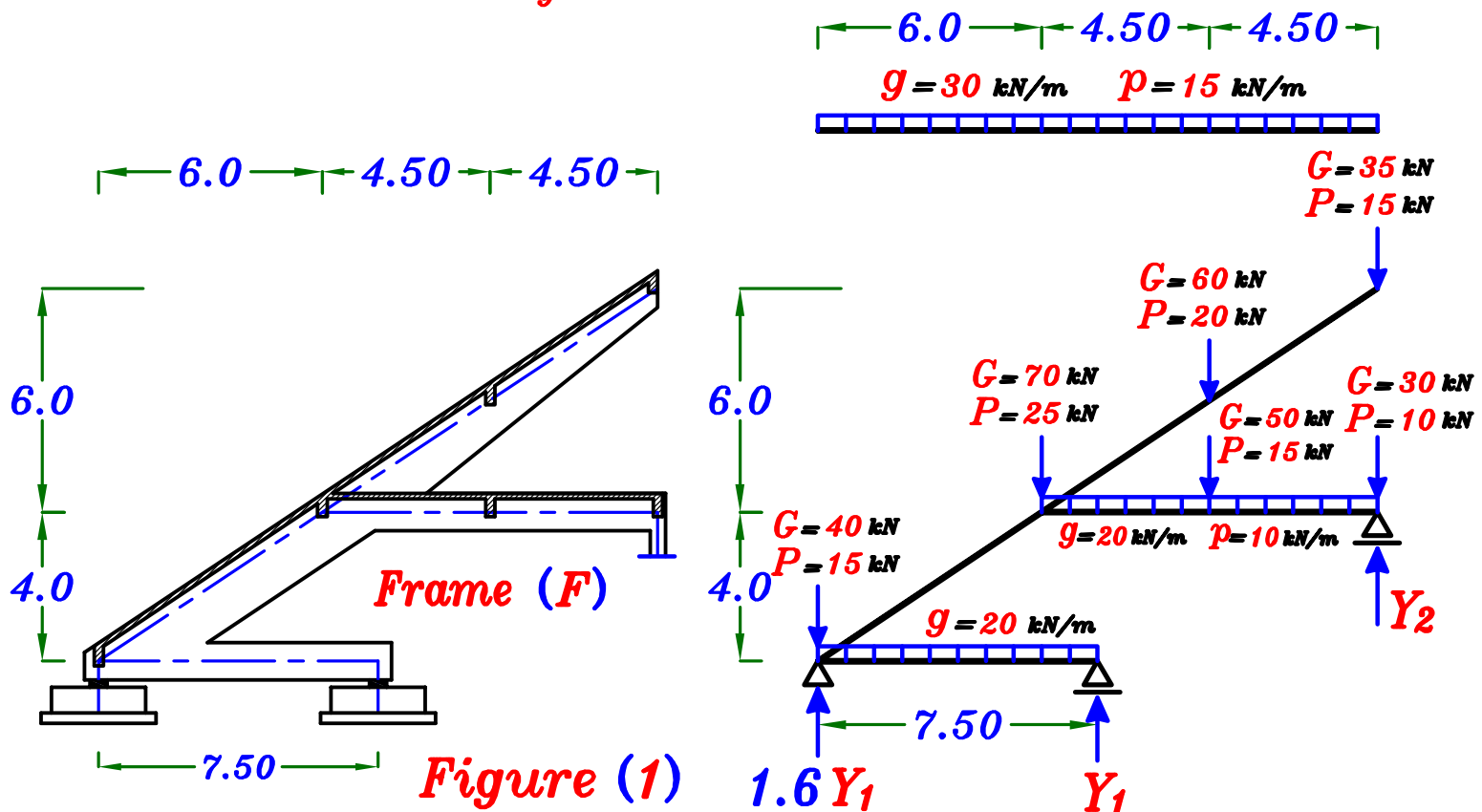
Data:

$t_s = 140 \text{ mm}$, Spacing = **6.0 m**

$b_{\text{(beam)}} = 250 \text{ mm}$, $b_{\text{(Frame)}} = 400 \text{ mm}$

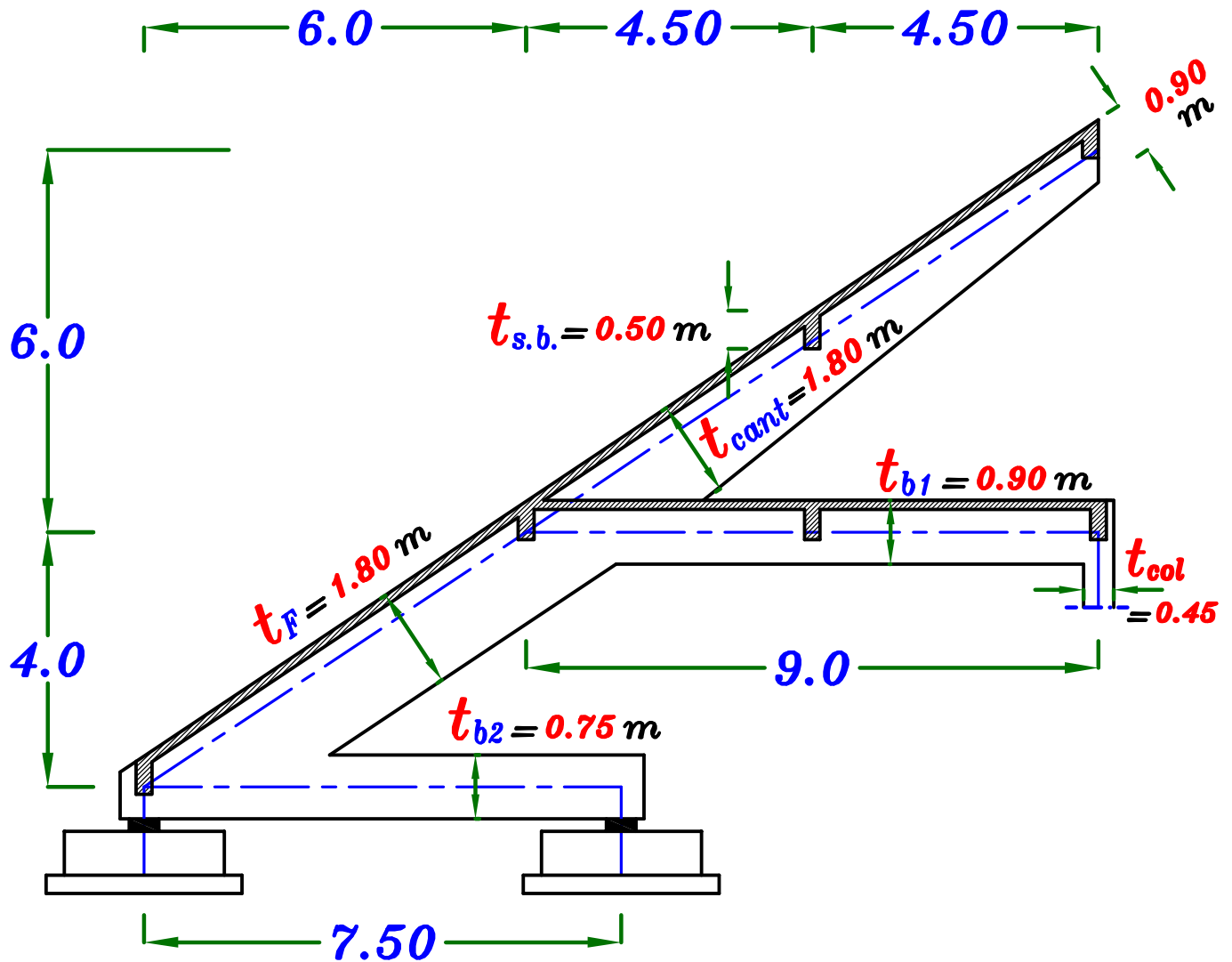
Concrete Grade. **C 30** $F_{cu} = 30 \text{ MPa}$

Steel Grade: **st. 52** $F_y = 360 \text{ MPa}$



Question (1)

- 1- Without any calculation but with reasonably assumed concrete dimensions, draw sectional For the ring Frame, Showing the dimensions of all concrete elements. to scale **1:50**



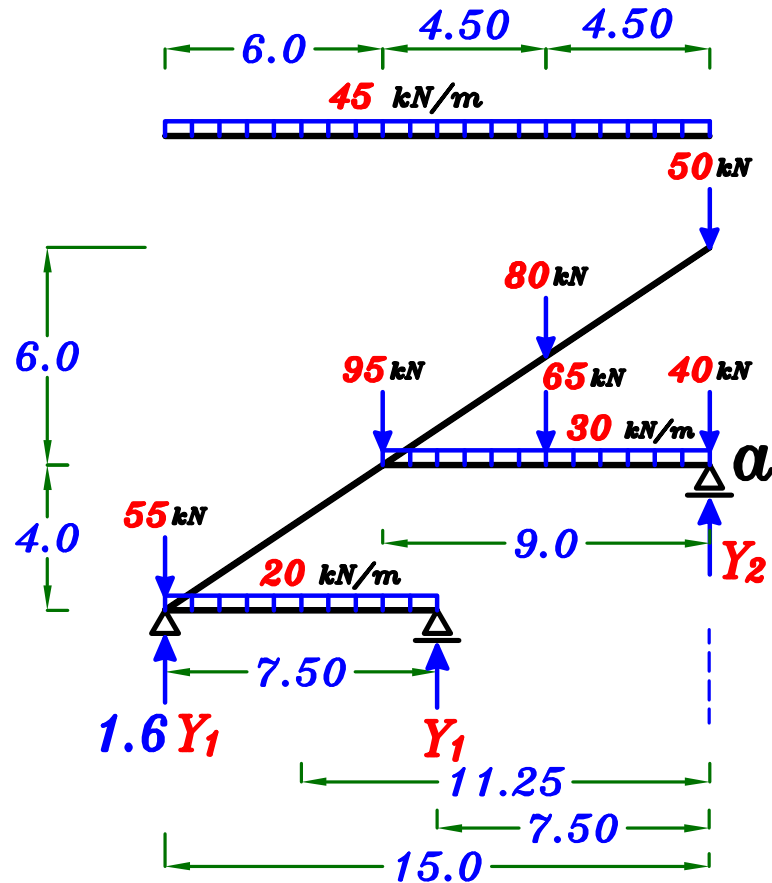
$$t_{b1} = \frac{L}{10} = \frac{9.0}{10} = 0.90 \text{ m} \quad , \quad t_{b2} = \frac{L}{10} = \frac{7.5}{10} = 0.75 \text{ m}$$

$$t_{cant.} = \frac{L}{5} = \frac{9.0}{5} = 1.80 \text{ m} \quad , \quad t_F \approx t_{cant.} \approx 1.80 \text{ m}$$

$$t_{col.} = \frac{t_{b1}}{2} = \frac{0.9}{2} = 0.45 \text{ m}$$

$$t_{s.b.} = \frac{\text{spacing}}{12} = \frac{6.0}{12} = 0.50 \text{ m}$$

2- Draw B.M.D., N.F.D. & S.F.D. For case of total load only of an intermediate Frame (F)
 Using the given **Ultimate limit loads**.

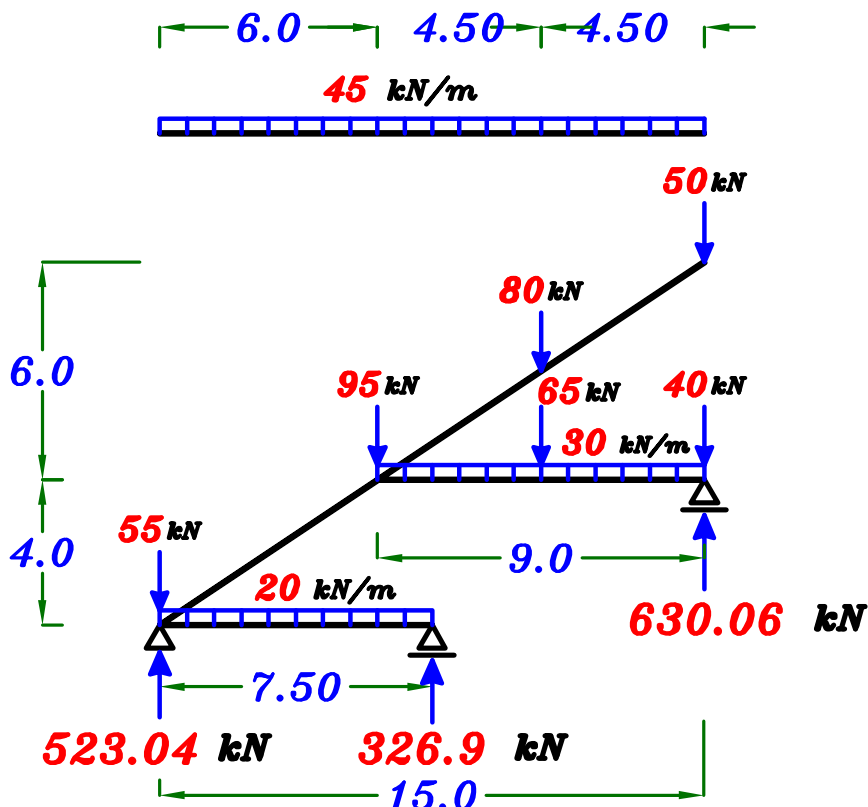


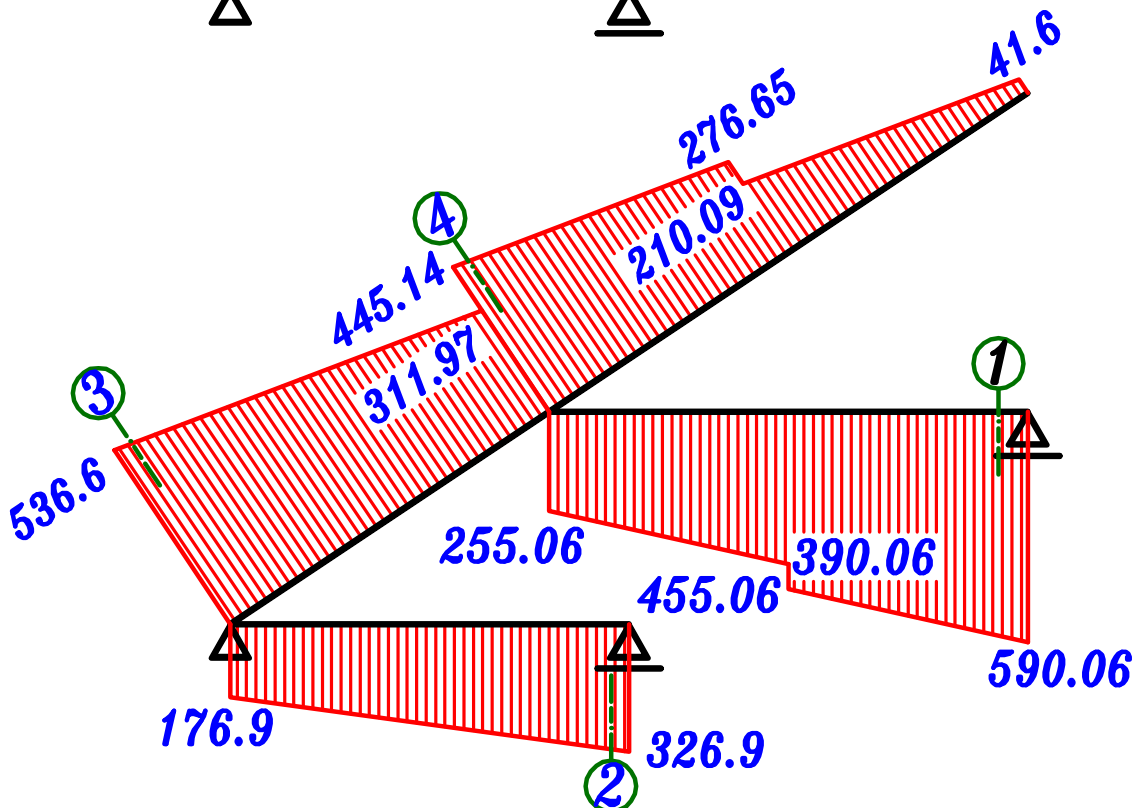
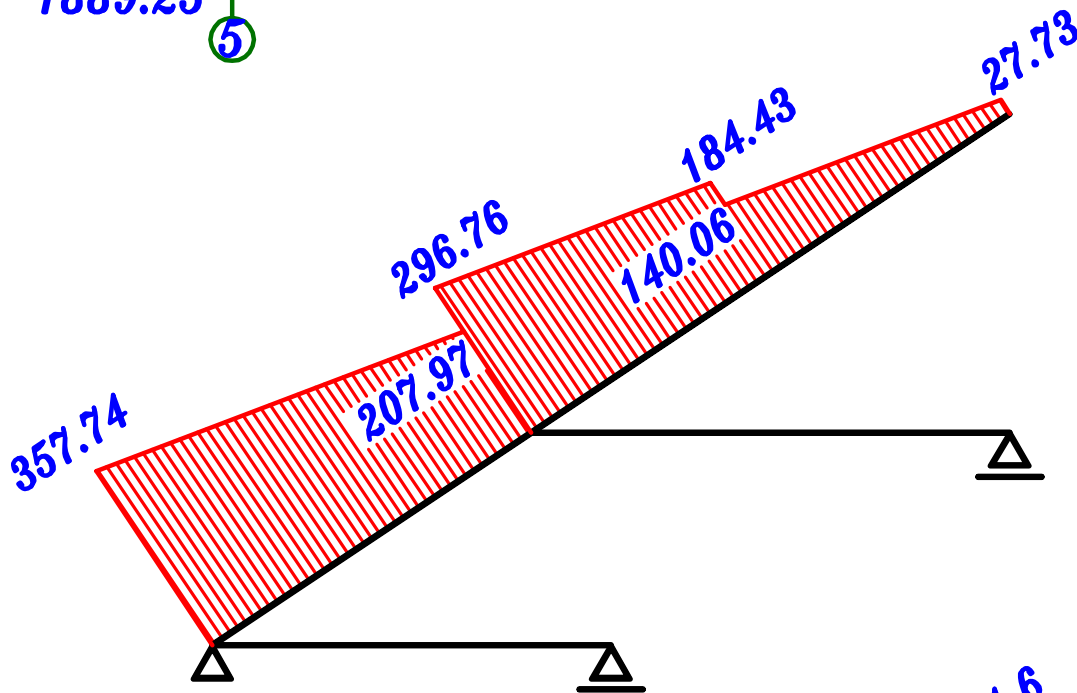
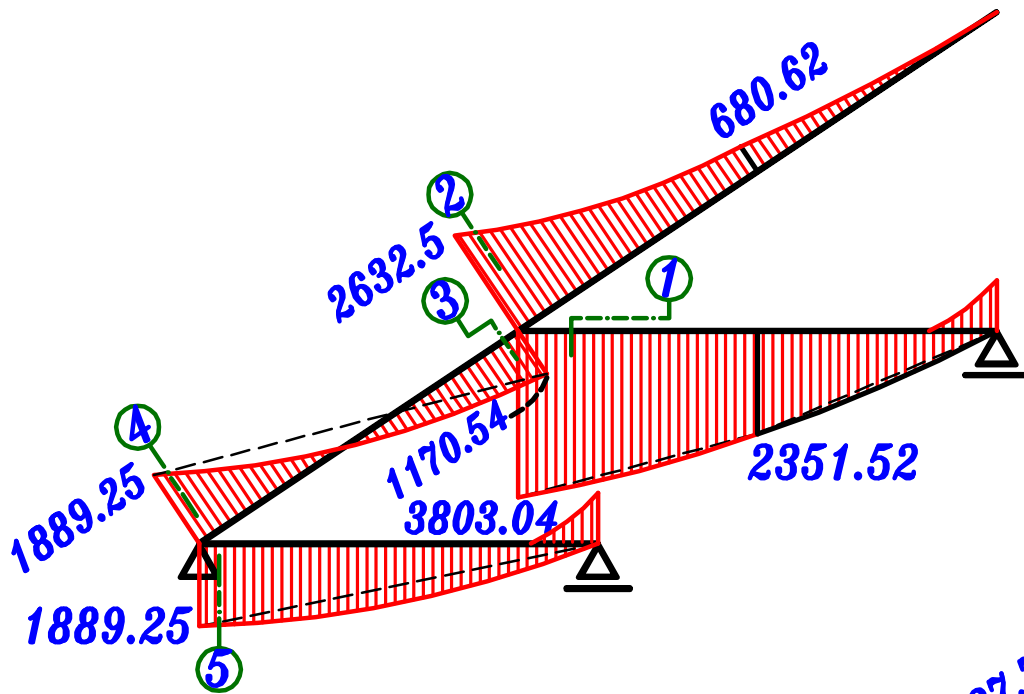
$$\sum M_{\alpha} = \text{Zero}$$

$$45 (15) (7.5) + 30 (9) (4.5) + 80 (4.5) + 65 (4.5) + 95 (9) + 20 (7.5) (11.25) + 55 (15) - (1.6 Y_1) (15) - (Y_1) (7.5) = \text{Zero}$$

$$Y_1 = 326.9 \text{ kN}$$

$$\sum Y = \text{Zero} \quad Y_2 = 630.06 \text{ kN}$$

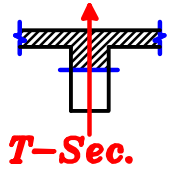




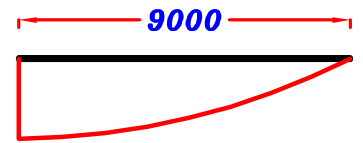
3-Design the critical sections For the intermediate Frame (F), to satisfy both bending moment and normal Forces.

Concrete Dimensions الأبعاد التي تم فرضها لا
عاده نستخدمها فى حساب الاوزان فقط و ليس شرط ان نأخذها معنا فى التصميم .

Sec. ① $M = 3803.04 \text{ kN.m}$, $P = \text{Zero kN}$, $b = 400 \text{ mm}$



$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = \text{Spacing} = 6.0 \text{ m} = 6000 \text{ mm} \\ 16 t_s + b = 16 * 140 + 400 = 2640 \text{ mm} \\ K \frac{L}{5} + b = 1.0 * \frac{9000}{5} + 400 = 2200 \text{ mm} \end{array} \right\}$$



$B = 2200 \text{ mm}$

Take $C_1 = 6.0 \rightarrow J = 0.826$

$$d = 6.0 \sqrt{\frac{3803.04 * 10^6}{30 * 2200}} = 1440.2 \text{ mm} \quad (\text{T-Sec.})$$

Take $d = 1500 \text{ mm}$, $t = 1500 + 100 = 1600 \text{ mm}$

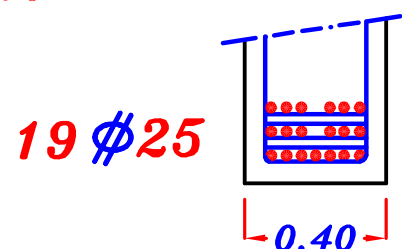
$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{3803.04 * 10^6}{0.826 * 360 * 1440.2} = 8880.2 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 8880.2 \text{ mm}^2$

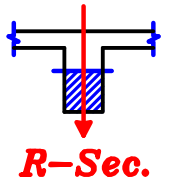
$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1500 = 2054 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 8880.2 \text{ mm}^2$ **19 ϕ 25**

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$



Sec. ② $M = 2632.5 \text{ kN.m}$, $P = 296.76 \text{ kN}$, $b = 400 \text{ mm}$



$$d_o = 3.5 \sqrt{\frac{2632.5 * 10^6}{30 * 400}} = 1639.3 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1639.3) = (1803.2 \rightarrow 2131) \text{ mm}$$

Take $d = 1900 \text{ mm}$, $t = 1900 + 100 = 2000 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{296.76 * 10^3}{30 * 400 * 2000} = 0.012 < 0.04 \therefore (\text{Neglect } P)$

\therefore Take $d = d_o = 1639.3 \text{ mm}$

\therefore Take $d = 1700 \text{ mm}$, $t = 1800 \text{ mm}$

$\therefore C_1 = 3.50 \rightarrow J = 0.78$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{2632.5 * 10^6}{0.780 * 360 * 1639.3} = 5718.9 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 5718.9 \text{ mm}^2$

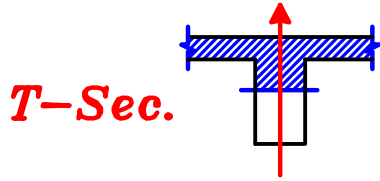
$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1700 = 2327.8 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 5718.9 \text{ mm}^2$ 12 ϕ 25

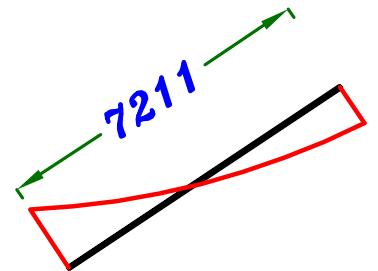
Sec. ③ $M = 1170.54 \text{ kN.m}$, $P = 207.97 \text{ kN}$, $b = 400 \text{ mm}$

$d = 1700 \text{ mm}$ (the same depth of Sec. ②)

Check $\frac{P}{F_{cu} b t} = \frac{207.97 * 10^3}{30 * 400 * 1800} = 0.0096 < 0.04 \therefore (\text{Neglect } P)$



$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = \text{Spacing} = 6.0 \text{ m} = 6000 \text{ mm} \\ 16 t_s + b = 16 * 140 + 400 = 2640 \text{ mm} \\ K \frac{L}{5} + b = 0.8 * \frac{7211}{5} + 400 = 1553.7 \text{ mm} \end{array} \right\}$$



$B = 1553.7 \text{ mm}$

$$\therefore 1700 = C_1 \sqrt{\frac{1170.54 * 10^6}{30 * 1553.7}} \rightarrow C_1 = 10.7 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1170.54 * 10^6}{0.826 * 360 * 1700} = 2315.5 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2315.5 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1700 = 2327.8 \text{ mm}^2$$

$\therefore \mu_{min.} b d > A_{s_{req.}}$ Use $A_{s_{min.}}$

$$A_{s_{min.}} = 0.225 * \frac{\sqrt{F_{cu}}}{F_y} b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1900 = 2327.8$$

الأقل = 2327.8

$$1.3 A_{s_{req.}} = 1.3 * 2315.5 = 3010.1$$

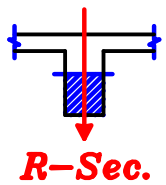
الأكثر = 3010.1

st. 360/520 $\frac{0.15}{100} b d = \frac{0.15}{100} * 400 * 1900 = 1140$

$= 2327.8 \text{ mm}^2$

5 # 25

Sec. ④ $M = 1889.25 \text{ kN.m}$, $P = 357.74 \text{ kN}$, $b = 400 \text{ mm}$



$d = 1700 \text{ mm}$ (the same depth of Sec. ②)

Check $\frac{P}{F_{cu} b t} = \frac{357.74 * 10^3}{30 * 400 * 1800} = 0.016 < 0.04 \therefore (\text{Neglect } P)$

$\therefore 1700 = C_1 \sqrt{\frac{1889.25 * 10^6}{30 * 400}} \rightarrow C_1 = 4.28 \rightarrow J = 0.813$

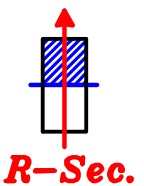
$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1889.25 * 10^6}{0.813 * 360 * 1700} = 3797.0 \text{ mm}^2$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 3797.0 \text{ mm}^2$

$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1700 = 2327.8 \text{ mm}^2$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 3797.0 \text{ mm}^2$ **8 ϕ 25**

Sec. ⑤ $M = 1889.25 \text{ kN.m}$, $P = \text{Zero}$ kN , $b = 400 \text{ mm}$



Take $C_1 = 3.5 \rightarrow J = 0.78$

$d = 3.5 \sqrt{\frac{1889.25 * 10^6}{30 * 400}} = 1388.7 \text{ mm}$ (R-Sec.)

Take $d = 1400 \text{ mm}$, $t = 1400 + 100 = 1500 \text{ mm}$

$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1889.25 * 10^6}{0.780 * 360 * 1388.7} = 4844.9 \text{ mm}^2$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 4844.9 \text{ mm}^2$

$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 400 * 1400 = 1917 \text{ mm}^2$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 4844.9 \text{ mm}^2$ **10 ϕ 25**

4-Design the critical sections For the intermediate Frame (F)
to satisfy the shearing Force.

Check Shear.

– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{30}{1.5}} = 3.13 \text{ N/mm}^2$$

Sec. ① $Q = 590.06 \text{ kN}$, $d = 1500 \text{ mm}$

$$q_u = \frac{Q}{b d} = \frac{590.06 * 10^3}{400 * 1500} = 0.98 \text{ N/mm}^2$$

$\therefore q_u < q_{cu} \longrightarrow$ Use min. stirrups $5\phi 8 \setminus m'$

Sec. ② $Q = 326.9 \text{ kN}$, $d = 1400 \text{ mm}$

$$q_u = \frac{Q}{b d} = \frac{326.9 * 10^3}{400 * 1400} = 0.583 \text{ N/mm}^2$$

$\therefore q_u < q_{cu} \longrightarrow$ Use min. stirrups $5\phi 8 \setminus m'$

Sec. ③ $Q = 536.6 \text{ kN}$, $d = 1700 \text{ mm}$

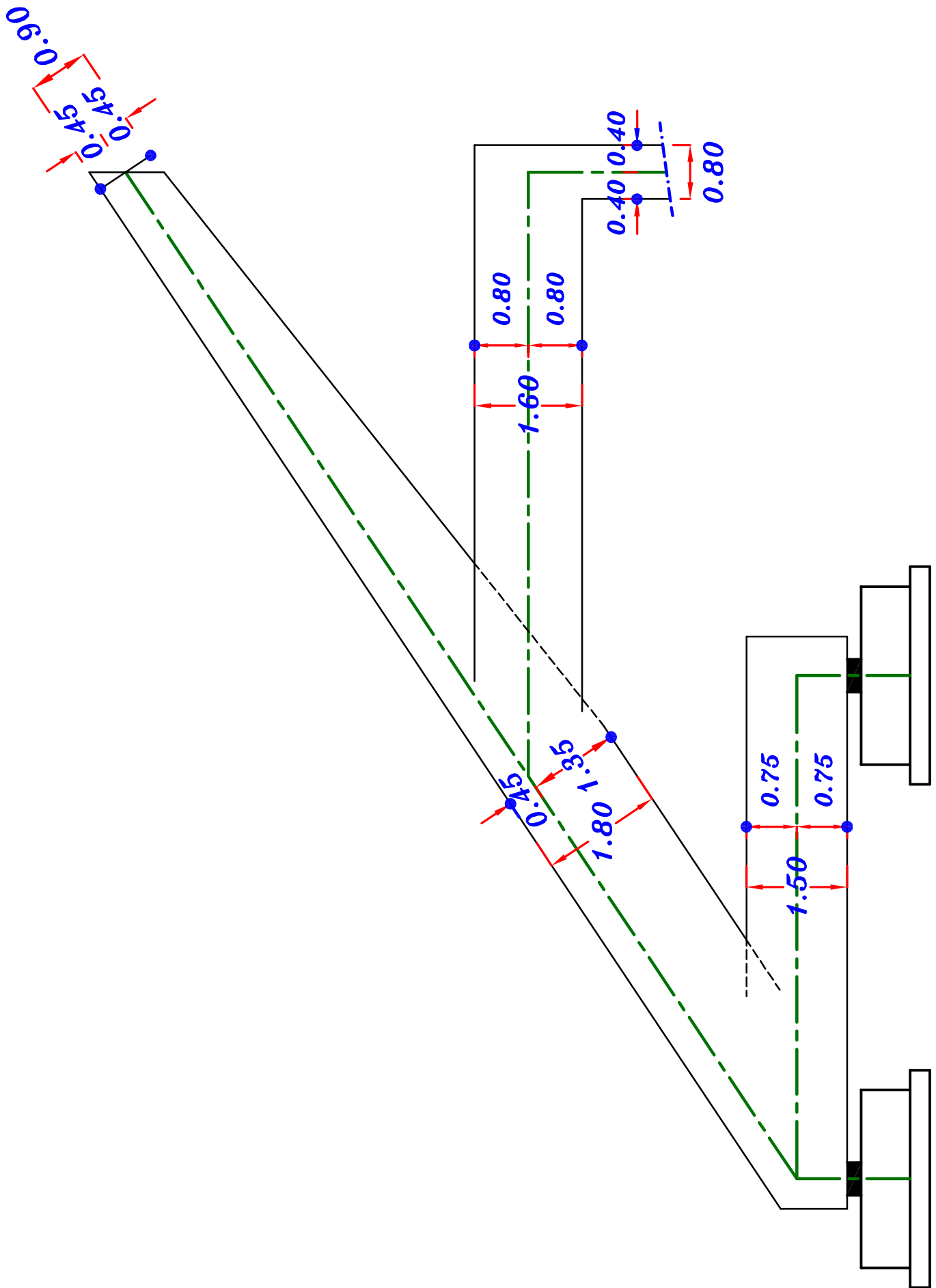
$$q_u = \frac{Q}{b d} = \frac{536.6 * 10^3}{400 * 1700} = 0.79 \text{ N/mm}^2$$

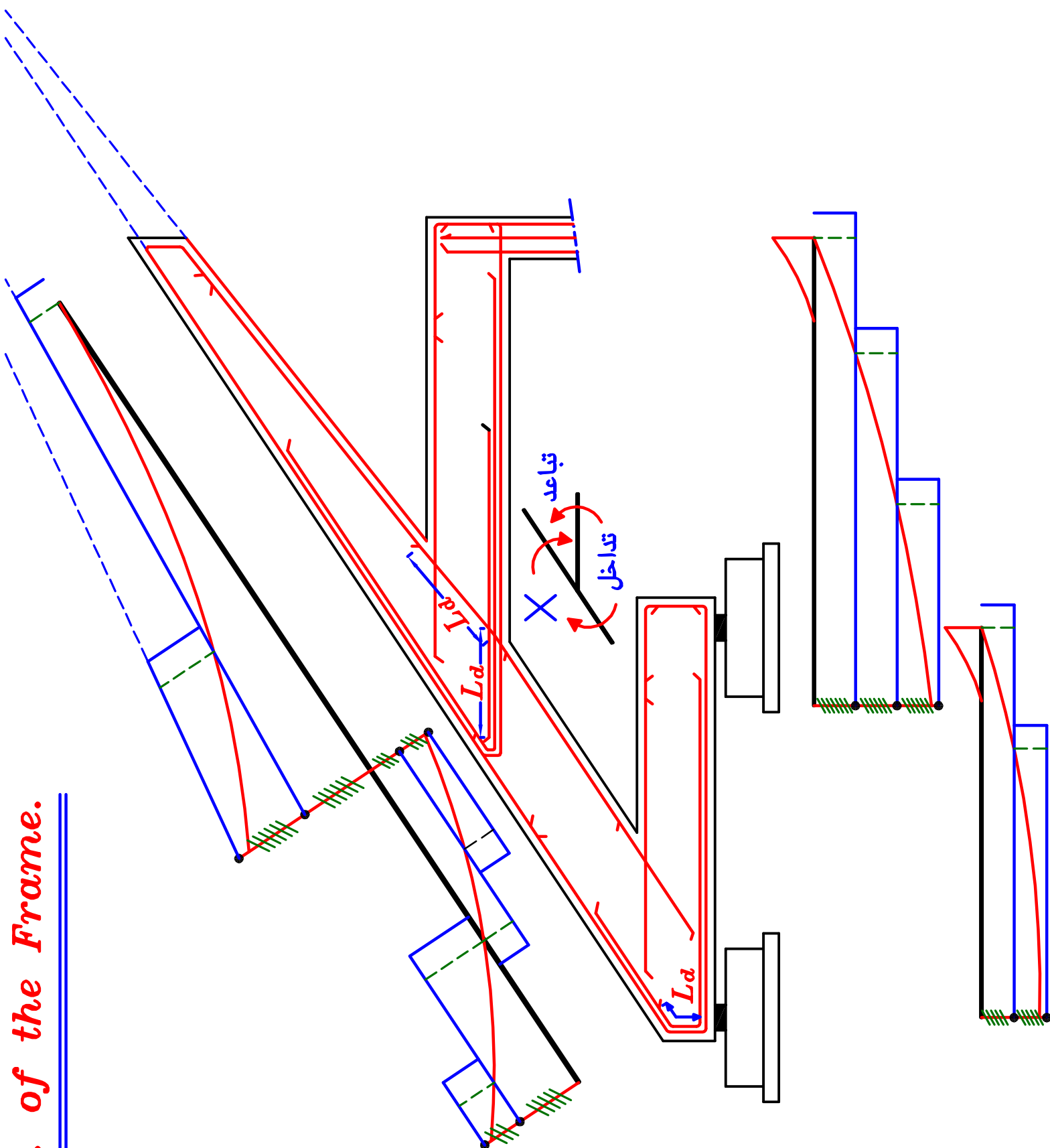
$\therefore q_u < q_{cu} \longrightarrow$ Use min. stirrups $5\phi 8 \setminus m'$

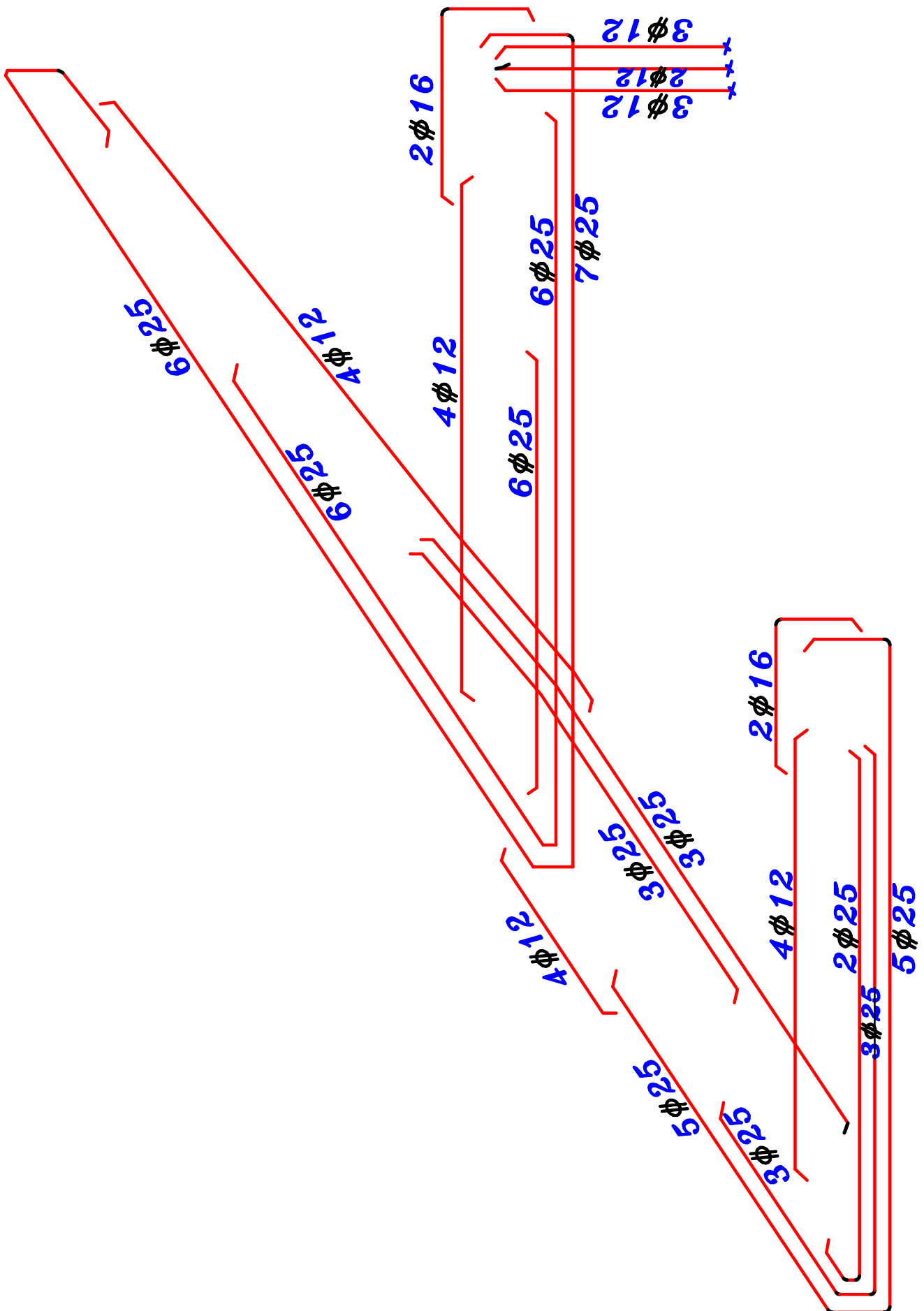
Sec. ④ $Q = 445.14 \text{ kN}$, $d = 1700 \text{ mm}$

$$q_u = \frac{Q}{b d} = \frac{445.14 * 10^3}{400 * 1700} = 0.65 \text{ N/mm}^2$$

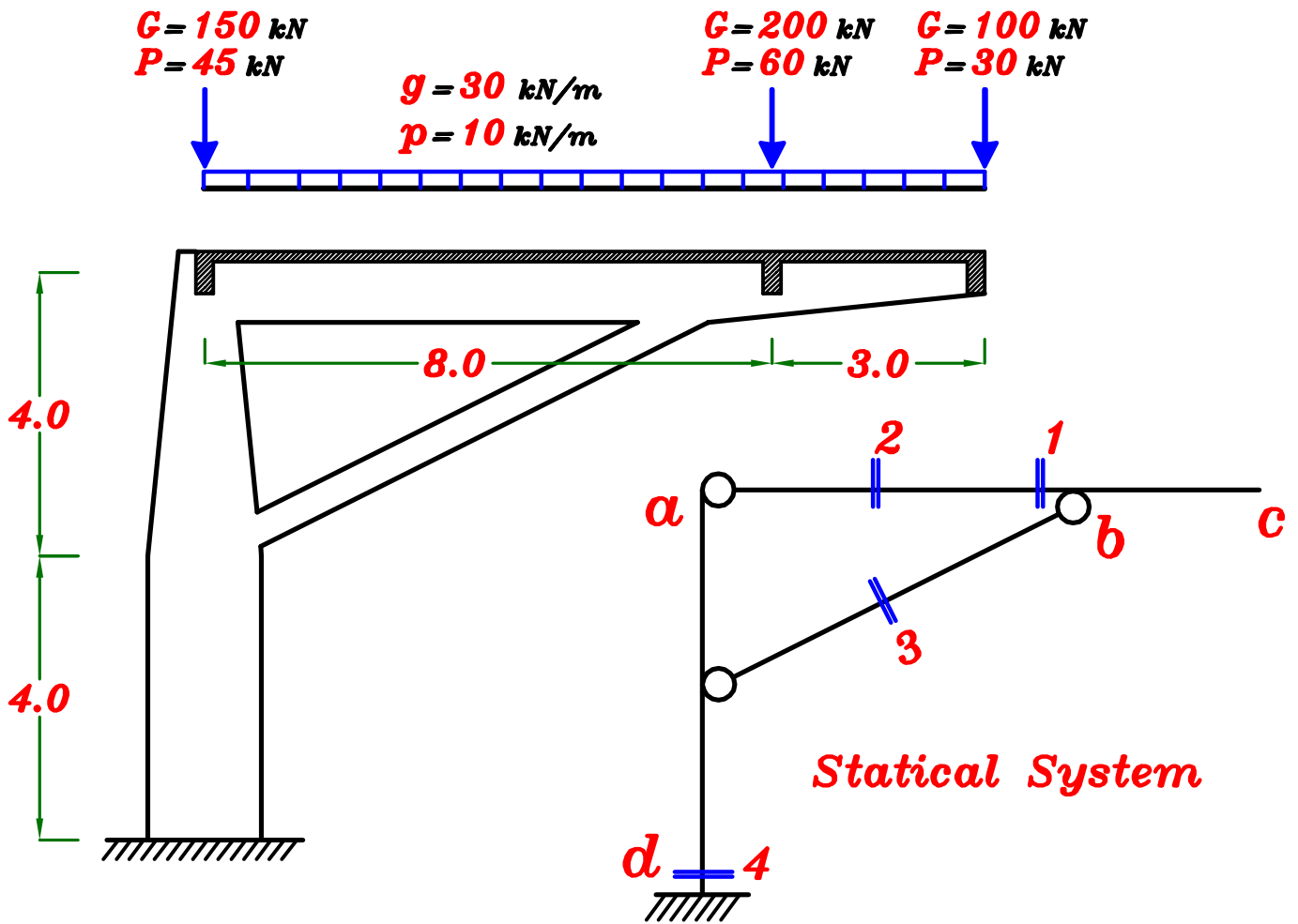
$\therefore q_u < q_{cu} \longrightarrow$ Use min. stirrups $5\phi 8 \setminus m'$







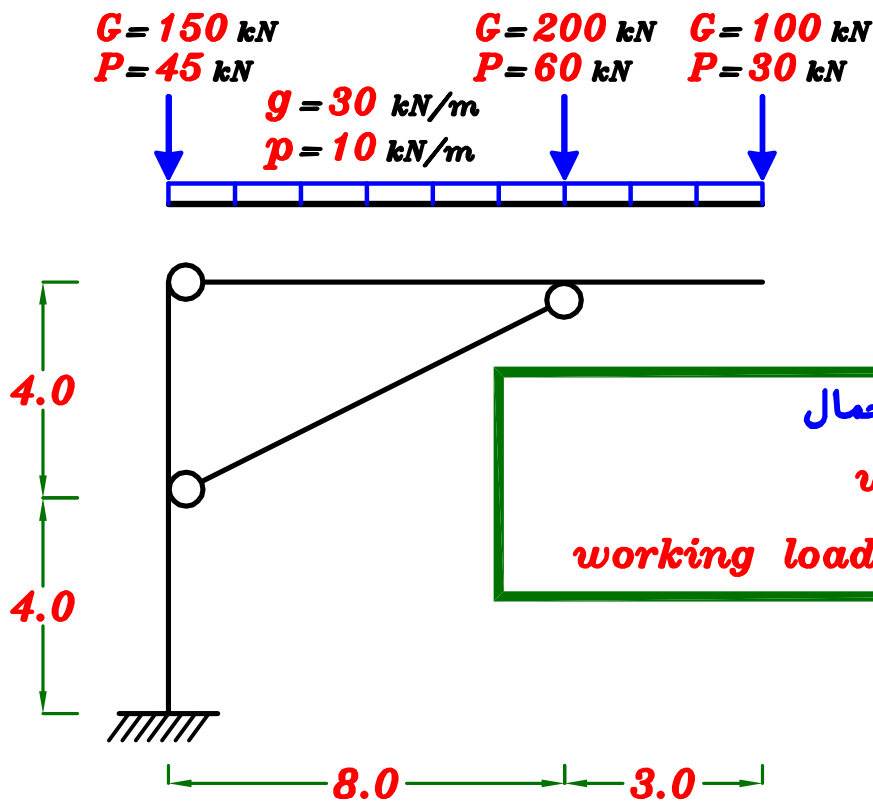
Example.



The Figure shows the concrete dimensions and static system of a repeated Frame used as a car shed. The spacing between Frames is 6.0 m and each Frame carries a group of secondary beams as shown in the Figure. It is required to:

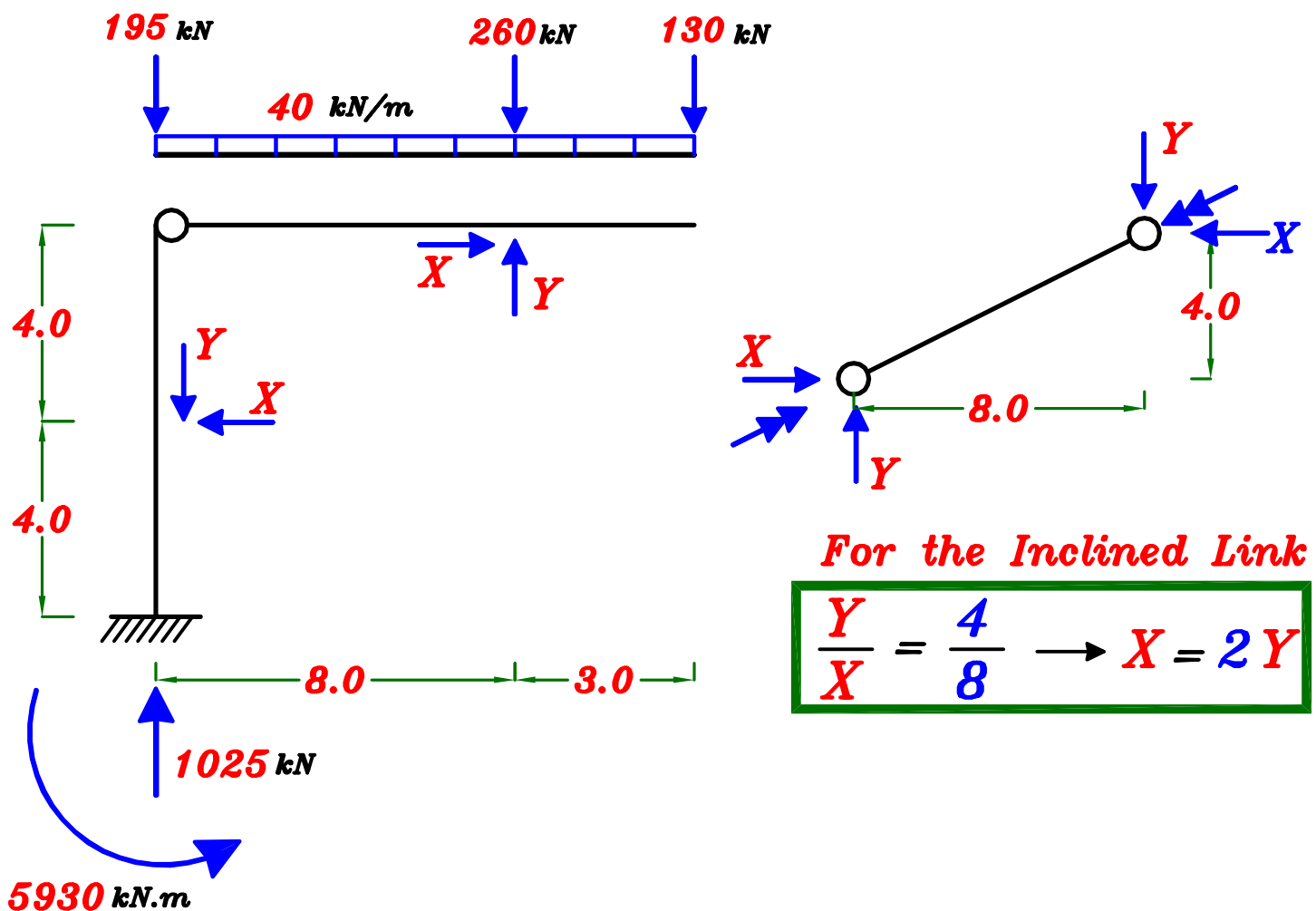
- 1- Draw the **S.F.D.**, **N.F.D.** & **B.M.D.** For one intermediate Frame.
- 2- Assuming that the column (**a d**) is an unbraced column, calculate the bending moments on the column **in & out** of plane due to buckling.
- 3- Design the critical sections (**1→4**) of the Frame.
- 4- Draw the shear stress diagram of members **a-b-c** and design its critical sections For shear.
- 5- Draw the details of the reinforcement of the Frame using the moment of resistance diagram For the bars curtailment For members **a-b-c** and **a-d** in elevation to scale **1:50** and in sections to scale **1:20**

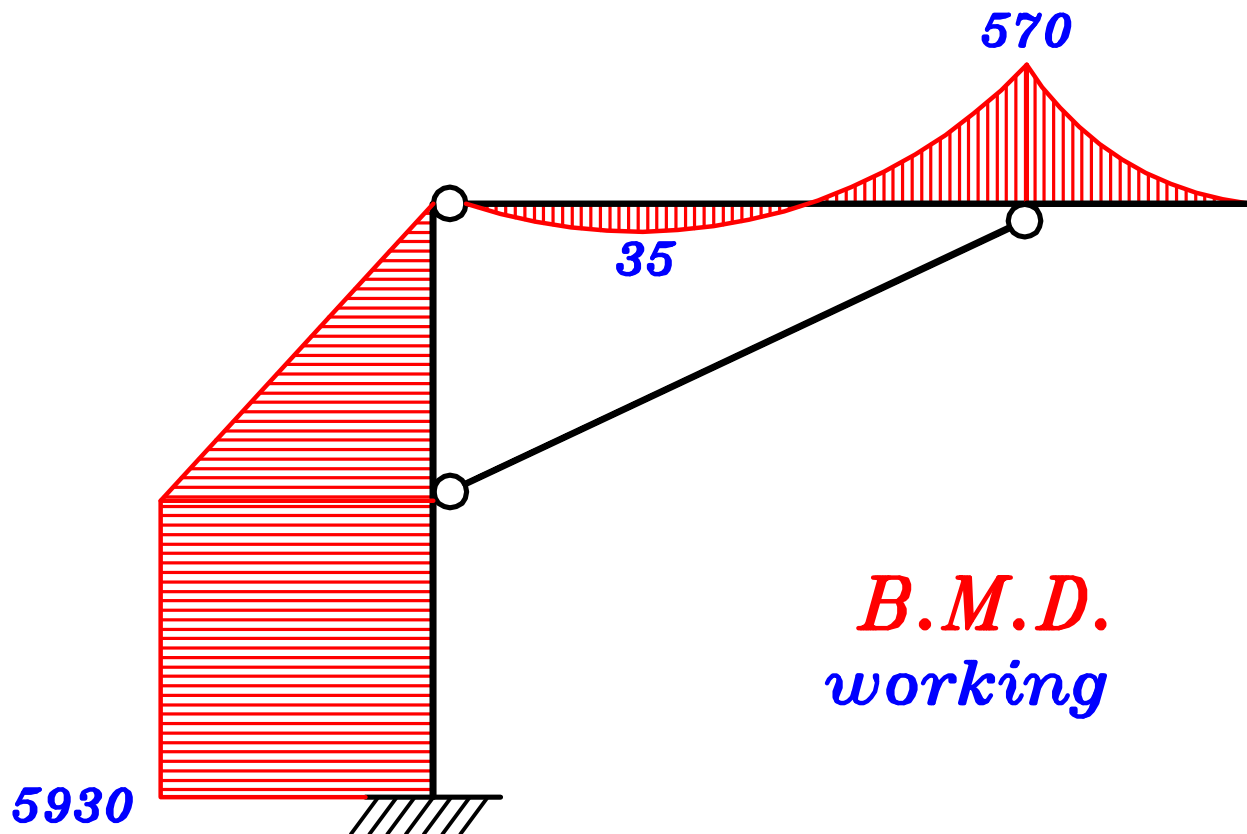
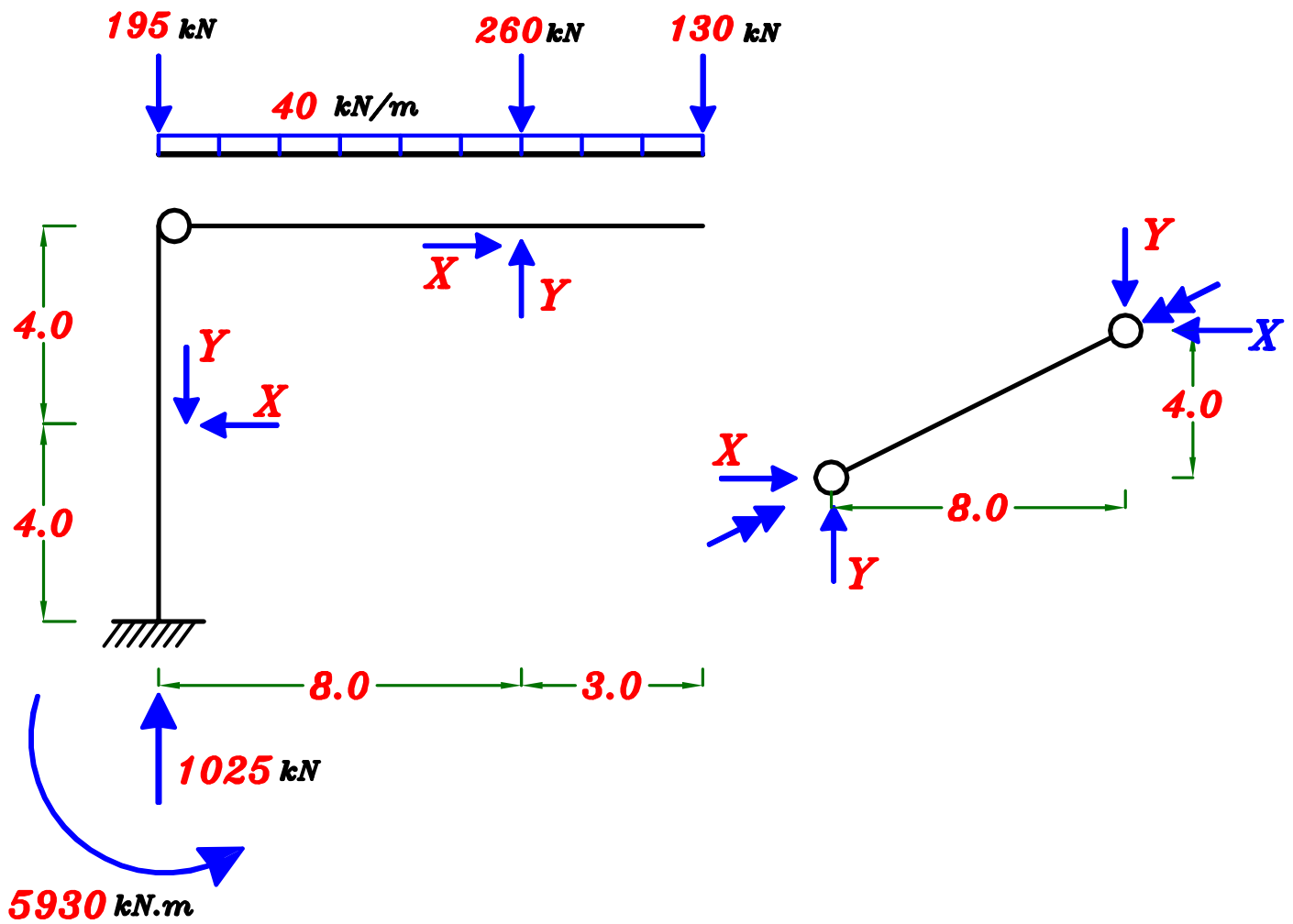
- Use **$F_{cu} = 35$ MPa** • Steel used is St. **400/600** • **$b = 450$ mm (Frame)**
- **Slabs thickness = 150 mm** • **Floor Cover = 2.0 kN/m²** • **Live Load = 1.0 kN/m²**

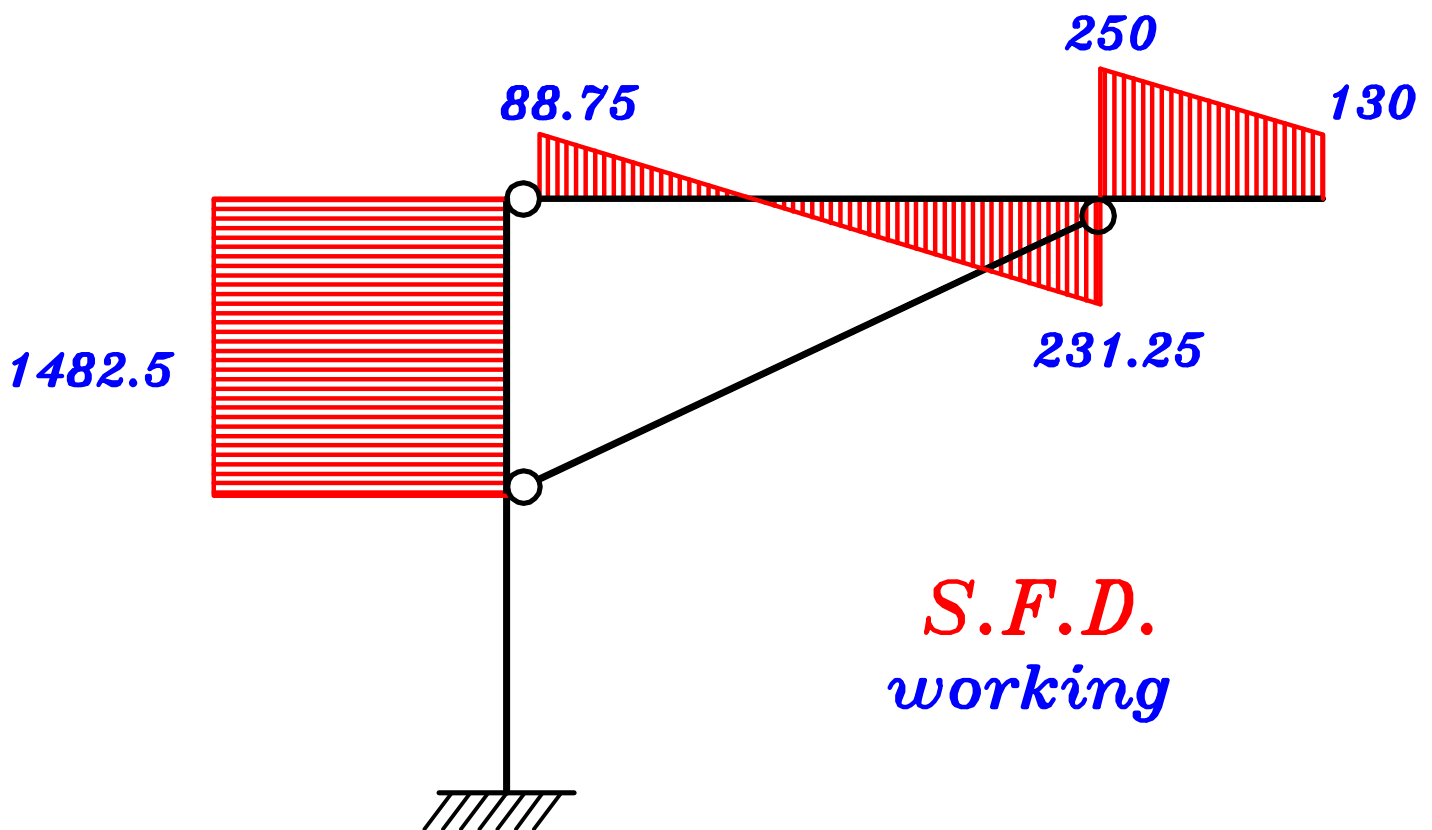
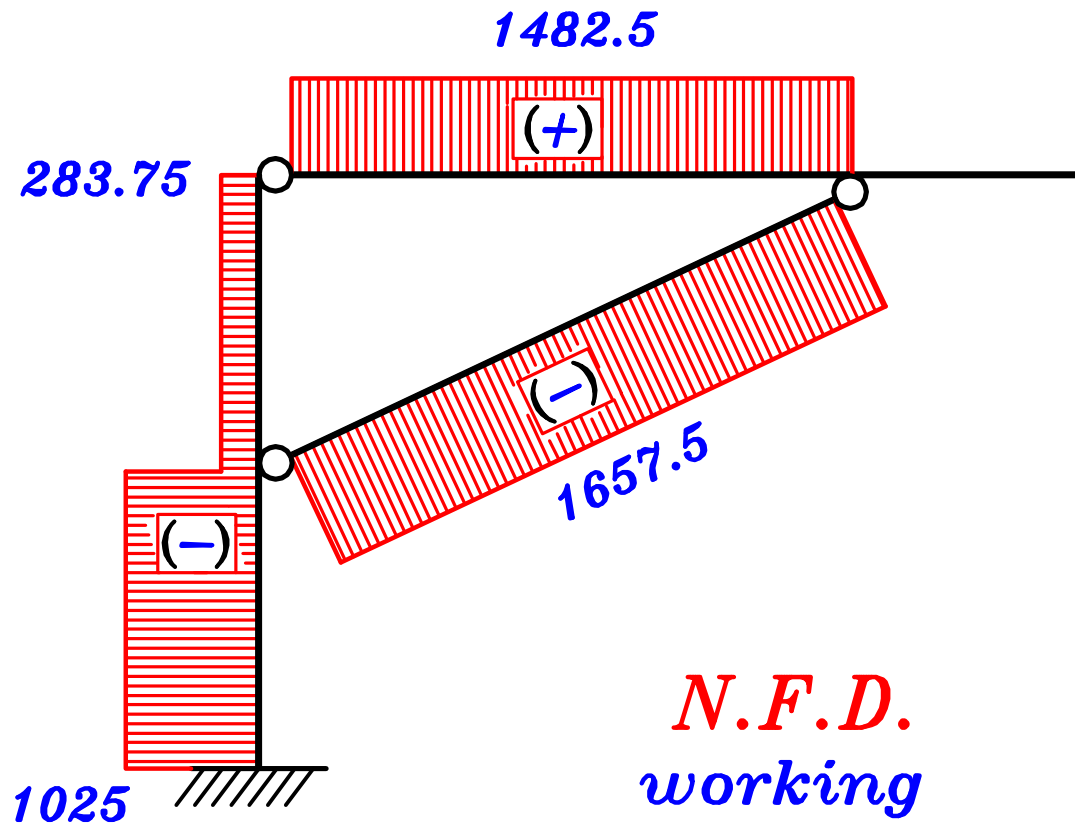


1- Draw the *S.F.D.*, *N.F.D.* & *B.M.D.* For one intermediate Frame.

بما انه لم يتم طلب عمل حالات تحميل على ال *Frame* اذا سنأخذ كل الاحمال *Total*







2- Assuming that the column (**a d**) is an unbraced column, calculate the bending moments on the column **in & out** of plane due to buckling.

توجد معلومات ناقصة سنحتاج لفرضها

١- عمق الكمره ال **secondary** $t_{s.b.} = \frac{\text{spacing}}{12} = \frac{6.0}{12} = 0.50 \text{ m}$

٢- تخانه عمود ال **Frame**

يمكن فرض الابعاد لكن يفضل ان نفرض الابعاد التى نضمن ان تجعل العمود **safe**

مع كلا من ال **Bending & Normal**

لذا سنصمم العمود اولا على M_{ext}, P و نحدد الابعاد ثم نعمل **check buckling** على هذه الابعاد .

R-Sec. , $M = 5930 * 1.5 = 8895 \text{ kN.m}$, $P = 1025 * 1.5 = 1537.5 \text{ kN}$

$d_o = 3.5 \sqrt{\frac{8895 * 10^6}{35 * 450}} = 2630 \text{ mm}$ (as **R-Sec.**)

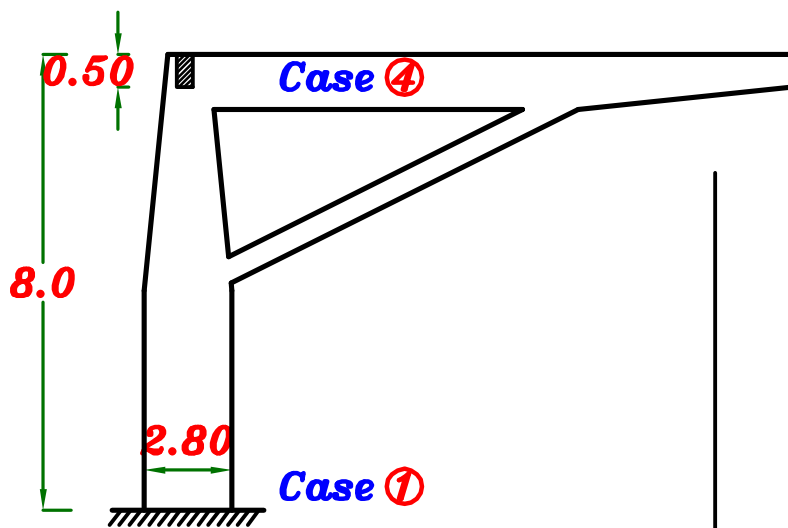
$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (2630) = (2893 \rightarrow 3419) \text{ mm}$

\therefore Take $d = 2900 \text{ mm}$, $t = 3000 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{1537.5 * 10^3}{35 * 450 * 3000} = 0.032 < 0.04$ (**Neglect P**)

\therefore Take $d = 2700 \text{ mm}$, $t = 2800 \text{ mm}$

Buckling In plane

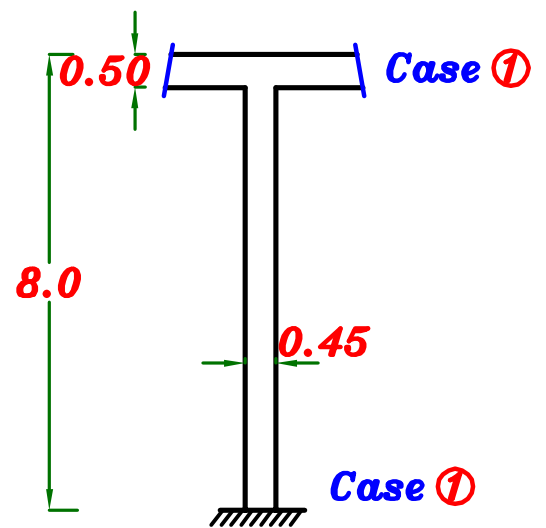


Upper Case ④
Lower Case ① } $k = 2.2$

$$H_o = 8.0 \text{ m}$$

$$\lambda_{b_{in}} = \frac{2.2 * 8.0}{2.8} = 6.28 < 10$$

Buckling Out of plane



Upper Case ①
Lower Case ① } $k = 1.2$

$$H_o = 8.0 - 0.5 = 7.50 \text{ m}$$

$$\lambda_{b_{out}} = \frac{1.2 * 7.5}{0.45} = 20 > 10$$

Take the bigger value of $\lambda_b = 20$ (Out of plane)

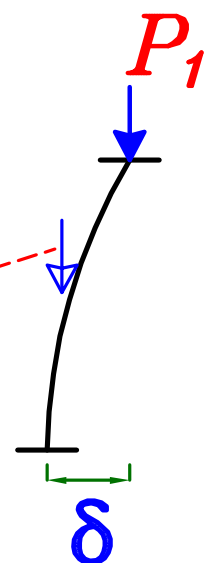
$$\delta = \frac{(\lambda_b)^2 * b}{2000} = \frac{20.0^2 * 0.45}{2000} = 0.09 \text{ m}$$

$$P_1 = 283.75 * 1.5 = 425.62 \text{ kN}$$

اعمل تأثير ال buckling
لهذا الحمل

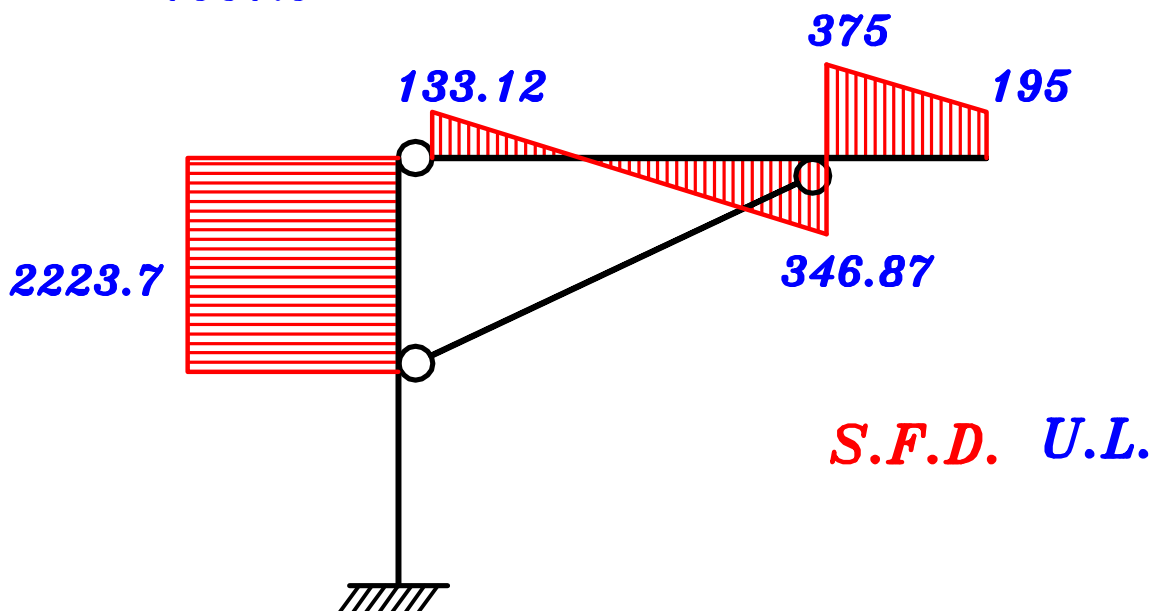
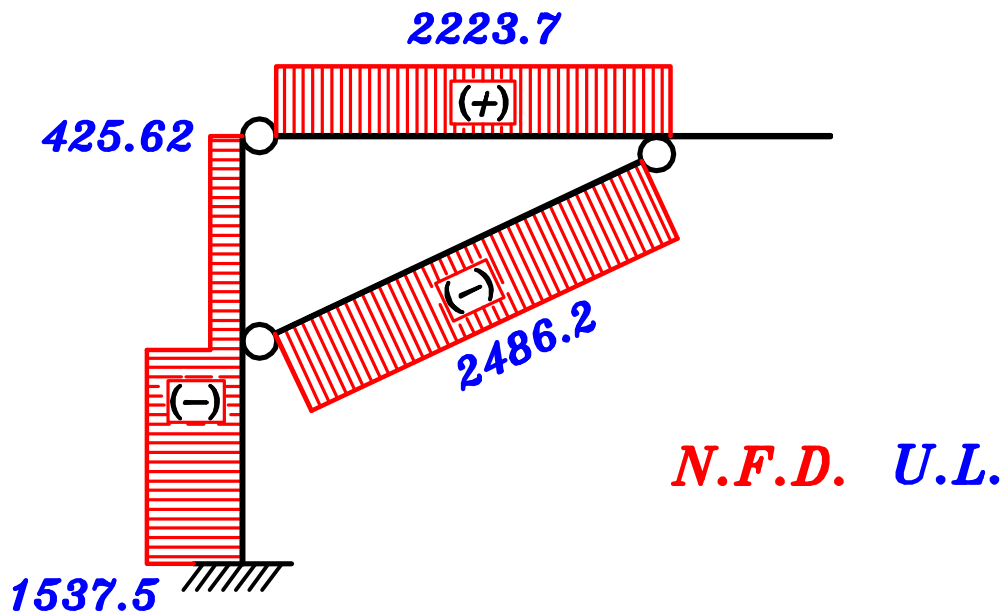
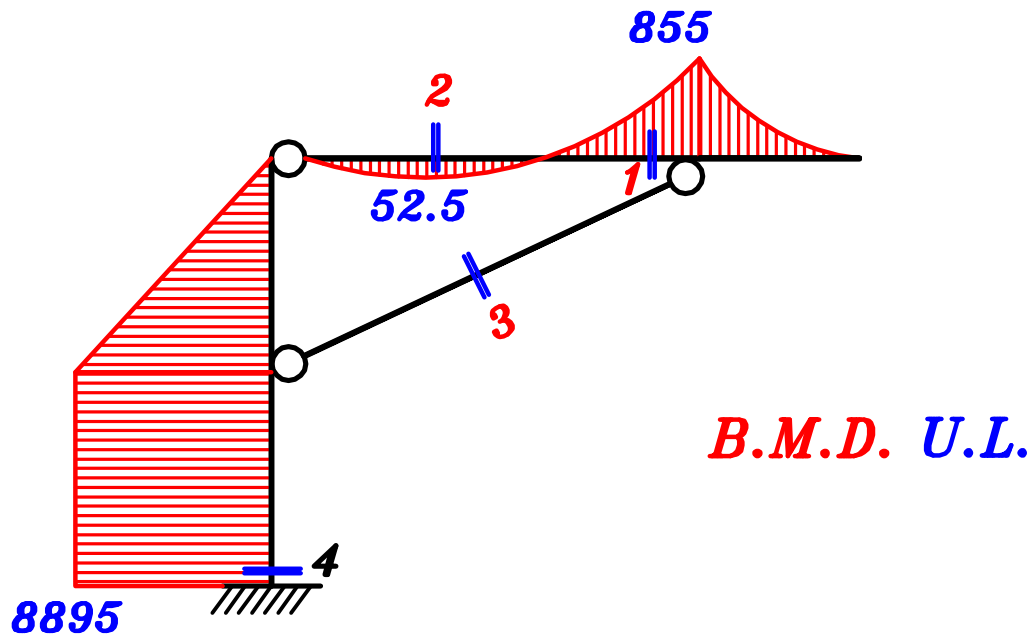
$$M_{add.} = P_1 * \delta = 425.62 * 0.09 = 38.30 \text{ kN.m}$$

اعلى P و ليس شرط
ان تكون اكبر P



3- Design the critical sections (1→4) of the Frame.

Internal Forces Diagrams



Sec. ① $M = 855 \text{ kN.m}$, $T = 2223.7 \text{ kN}$, $b = 450 \text{ mm}$ **R-Sec.**

$$d_o = 3.5 \sqrt{\frac{855 * 10^6}{35 * 450}} = 815.5 \text{ mm}$$

$$d = (0.9 \rightarrow 1.0) d_o = (0.9 \rightarrow 1.0) (815.5) = (733.9 \rightarrow 815.5) \text{ mm}$$

Take $d = 850 \text{ mm}$, $t = 900 \text{ mm}$

$$e = \frac{M}{T} = \frac{855}{2223.7} = 0.384 \text{ m} \quad \therefore \frac{e}{t} = \frac{0.384}{0.90} = 0.42 < 0.5$$

Small Eccentricity.

$$a = \frac{t}{2} - c - e = \frac{0.90}{2} - 0.05 - 0.384 = 0.016 \text{ m}$$

$$b = \frac{t}{2} - c + e = \frac{0.90}{2} - 0.05 + 0.384 = 0.784 \text{ m}$$

$$\therefore T_1 (a + b) = T (b) \quad \text{بأخذ العزم عند } T_2$$

$$T_1 (0.80) = 2223.7 (0.784) \longrightarrow T_1 = 2179.2 \text{ kN}$$

$$\therefore T = T_1 + T_2 \quad \therefore 2223.7 = 2179.2 + T_2 \longrightarrow T_2 = 44.5 \text{ kN}$$

$$A_{s1} = \frac{T_1}{(F_y / \gamma_s)} = \frac{2179.2 * 10^3}{(400 / 1.15)} = 6265.2 \text{ mm}^2$$

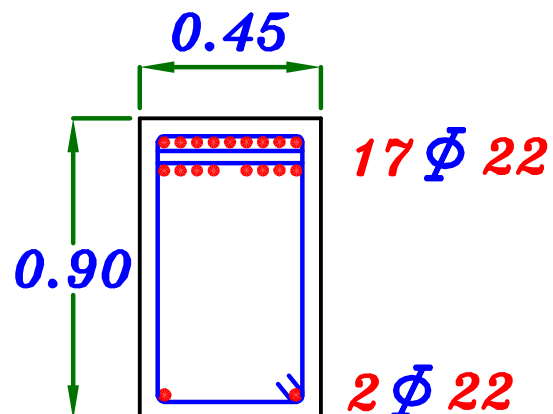
17 Φ 22

$$A_{s2} = \frac{T_2}{(F_y / \gamma_s)} = \frac{44.5 * 10^3}{(400 / 1.15)} = 127.9 \text{ mm}^2$$

2 Φ 22

$$\therefore n = \frac{b - 25}{\phi + 25}$$

$$= \frac{450 - 25}{22 + 25} = 9.04 = 9.0$$



Sec. ② $M = 52.5 \text{ kN.m}$, $T = 2223.7 \text{ kN}$, $b = 450 \text{ mm}$ R-Sec.

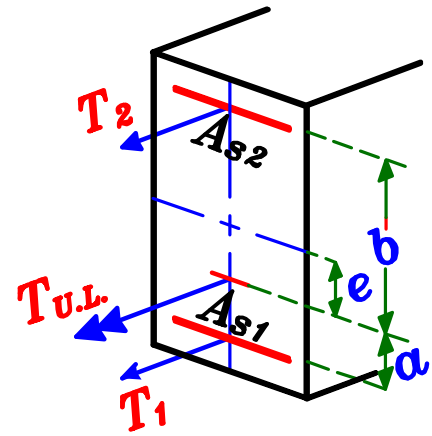
$$e = \frac{M}{T} = \frac{52.5}{2223.7} = 0.023 \text{ m} \quad \therefore \frac{e}{t} = \frac{0.023}{0.90} = 0.026 < 0.5$$

Small Eccentricity.

$$a = \frac{t}{2} - c - e = \frac{0.90}{2} - 0.05 - 0.023 = 0.377 \text{ m}$$

$$b = \frac{t}{2} - c + e = \frac{0.90}{2} - 0.05 + 0.023 = 0.423 \text{ m}$$

$$\therefore T_1 (a + b) = T (b) \quad \boxed{T_2 \text{ بأخذ العزم عند } T_2}$$

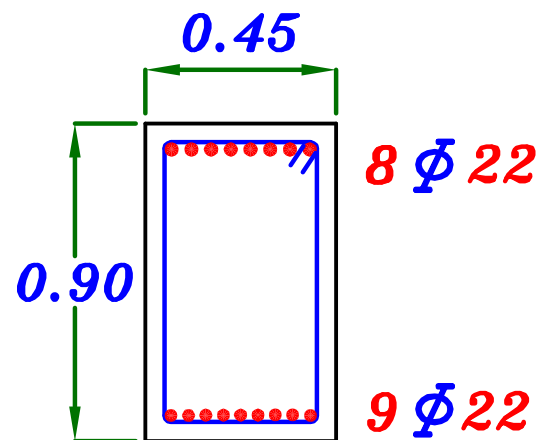


$$T_1 (0.80) = 2223.7 (0.423) \longrightarrow \boxed{T_1 = 1175.8 \text{ kN}}$$

$$\therefore T = T_1 + T_2 \quad \therefore 2223.7 = 1175.8 + T_2 \longrightarrow \boxed{T_2 = 1047.9 \text{ kN}}$$

$$A_{s1} = \frac{T_1}{(F_y / \phi_s)} = \frac{1175.8 * 10^3}{(400 / 1.15)} = 3380.4 \text{ mm}^2 \quad \boxed{9 \phi 22}$$

$$A_{s2} = \frac{T_2}{(F_y / \phi_s)} = \frac{1047.9 * 10^3}{(400 / 1.15)} = 3012.7 \text{ mm}^2 \quad \boxed{8 \phi 22}$$



Sec. ③ $P = 2486.2 \text{ kN}$, $(b * \frac{t}{2}) = (450 * 450)$

Neglect effect of buckling

$$A_c = 450 * 450 = 202500 \text{ mm}^2$$

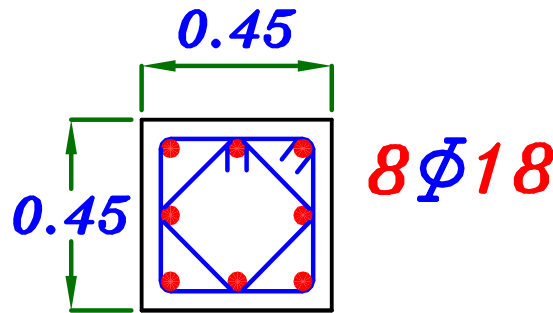
$$\therefore P_{u.L.} = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

$$\therefore 2486.2 * 10^3 = 0.35 (202500) (35) + 0.67 A_s (400)$$

$$\therefore A_s = 20.80 \text{ mm}^2 < A_{smin}$$

$$A_{smin} = \frac{0.8}{100} * A_c = \frac{0.8}{100} * 202500 = 1620 \text{ mm}^2$$

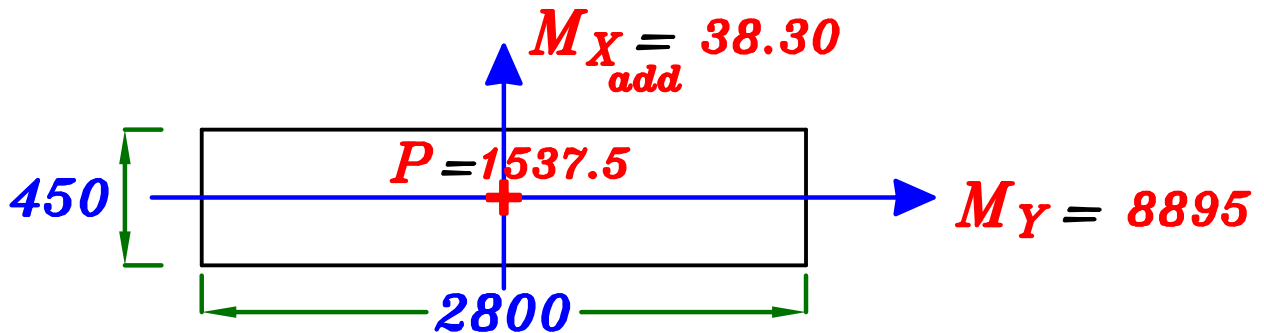
$$\therefore A_s < A_{smin} \rightarrow A_s = A_{smin} = 1620 \text{ mm}^2$$



8Φ18

Sec. ④ $b = 450 \text{ mm}$, $t = 2800 \text{ mm}$ R-Sec.

$$P = 1537.5 \text{ kN.m} \quad M_Y = 8895 \text{ kN.m} \quad M_{X_{add}} = 38.30 \text{ kN.m}$$



لان قيمه M_X اقل كثيرا من M_Y فمن الممكن فى الامتحان افعال قيمه M_X

Neglect M_X because it is too small.

Design the section on :

$$P = 1537.5 \text{ kN.m}, M_Y = 8895 \text{ kN.m}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{1537.5 * 10^3}{35 * 450 * 2800} = 0.035 < 0.04 \quad (\text{Neglect } P)$$

$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} B}} \therefore 2700 = c_1 \sqrt{\frac{8895 * 10^6}{35 * 450}} \rightarrow c_1 = 3.60 \rightarrow J = 0.786$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{8895 * 10^6}{0.786 * 400 * 2700} = 10478 \text{ mm}^2$$

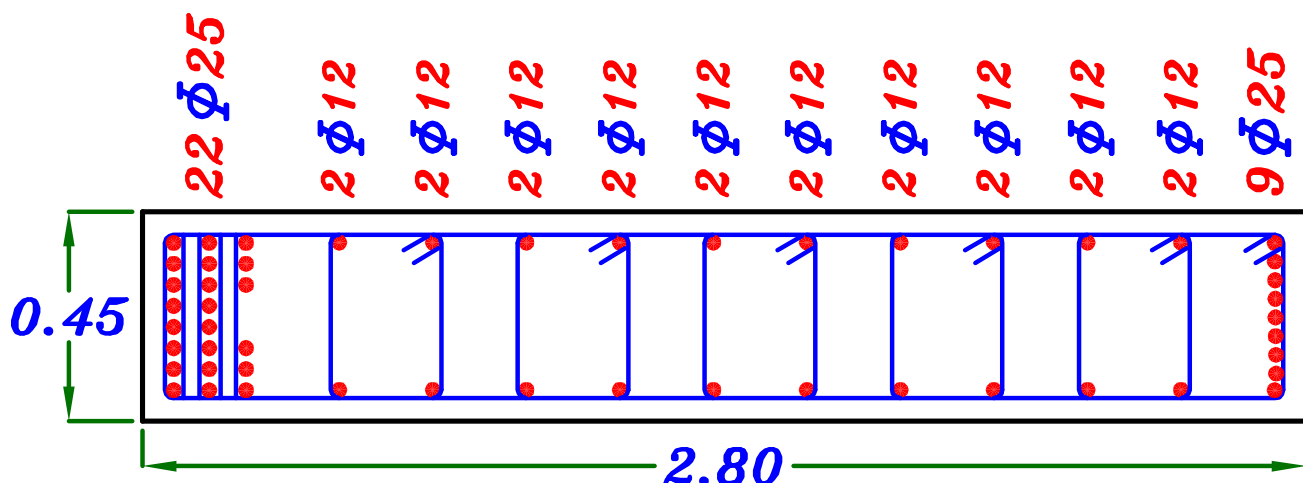
$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 10478 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{35}}{400} \right) 450 * 2800 = 4193 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 10478 \text{ mm}^2 \quad (22\phi 25)$$

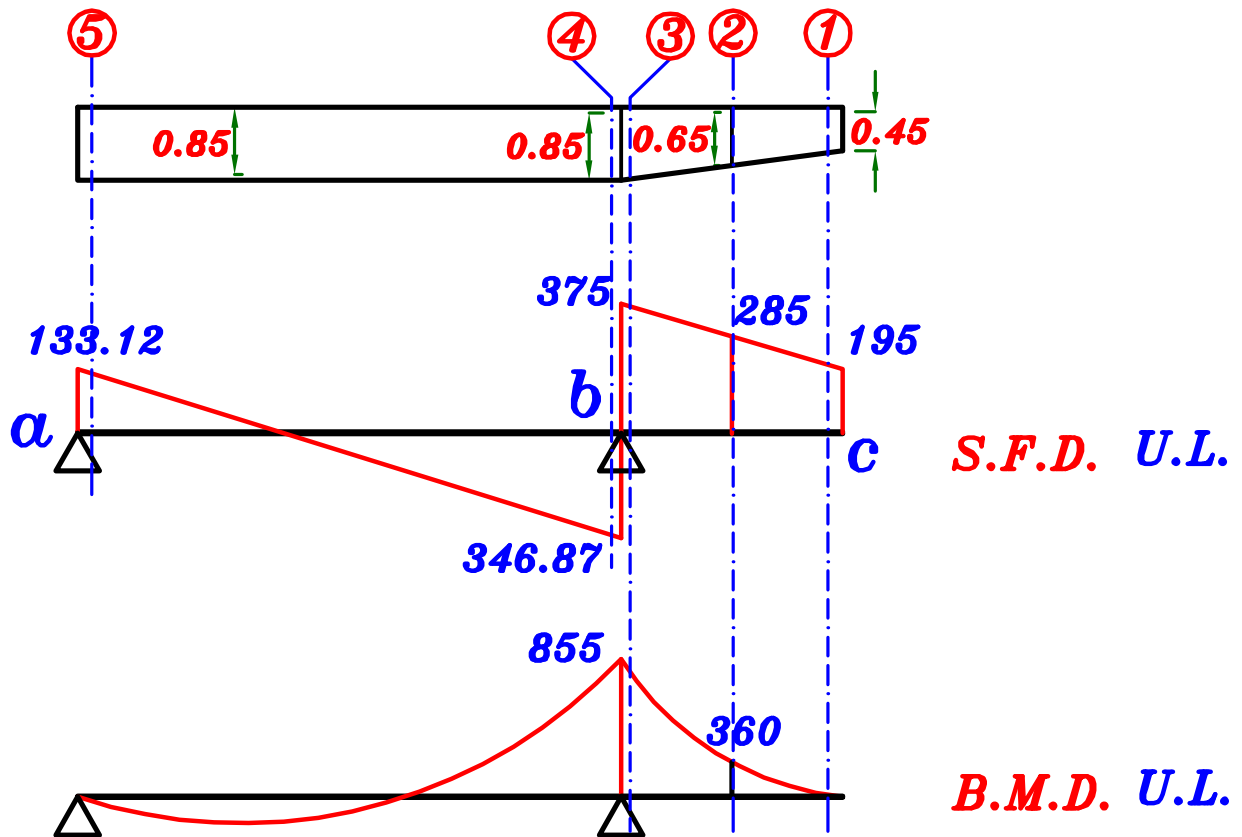
$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{450 - 25}{25 + 25} = 8.50 = 8.0 \text{ bars}$$

$$\text{Stirrup Hangers} = 0.4 A_s = 0.4 (10478) = 4191.2 \text{ mm}^2 \quad (9\phi 25)$$



4- Draw the shear stress diagram of members a-b-c and design its critical sections For shear.

لرسم ال **Shear Stress Diagram** سنحسب ال **stress** عند ثلاث نقاط للجزء المائل و نوصل بينهم بمنحنى و نقطتين عند الجزء الافقى و نوصل بينهم بخط.



For inclined part.

$$\tan \beta = \frac{0.9 - 0.5}{3.0} = 0.133$$

$$q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

Point ①

$$Q = 195 \text{ kN.} \quad M = \text{Zero kN.m} \quad d = 450 \text{ mm}$$

$$q = \frac{195 * 10^3}{450 * 450} - \text{Zero} = 0.963 \text{ N/mm}^2$$

Point ②

$$Q = 285 \text{ kN.} \quad M = 360 \text{ kN.m} \quad d = 650 \text{ mm}$$

$$q = \frac{285 * 10^3}{450 * 650} - \frac{360 * 10^6 * (0.133)}{450 * 650^2} = 0.722 \text{ N/mm}^2$$

Point ③

$$Q = 375 \text{ kN.} \quad M = 855 \text{ kN.m} \quad d = 850 \text{ mm}$$

$$q = \frac{375 * 10^3}{450 * 850} - \frac{855 * 10^6 * (0.133)}{450 * 850^2} = 0.630 \text{ N/mm}^2$$

For straight part.

$$q_u = \frac{Q}{b d}$$

Point ④

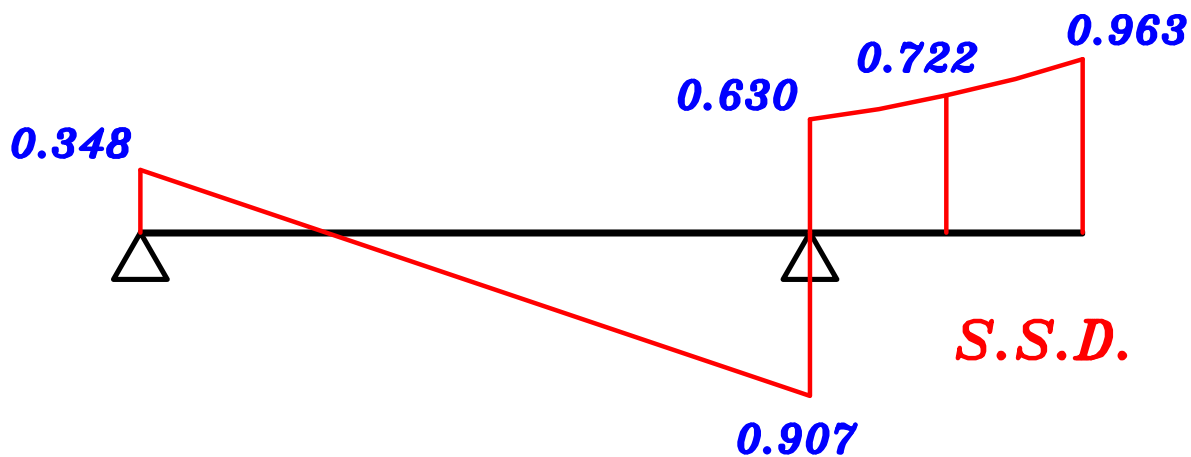
$$Q = 346.87 \text{ kN.} \quad d = 850 \text{ mm}$$

$$q = \frac{346.87 * 10^3}{450 * 850} = 0.907 \text{ N/mm}^2$$

Point ⑤

$$Q = 133.12 \text{ kN.} \quad d = 850 \text{ mm}$$

$$q = \frac{133.12 * 10^3}{450 * 850} = 0.348 \text{ N/mm}^2$$

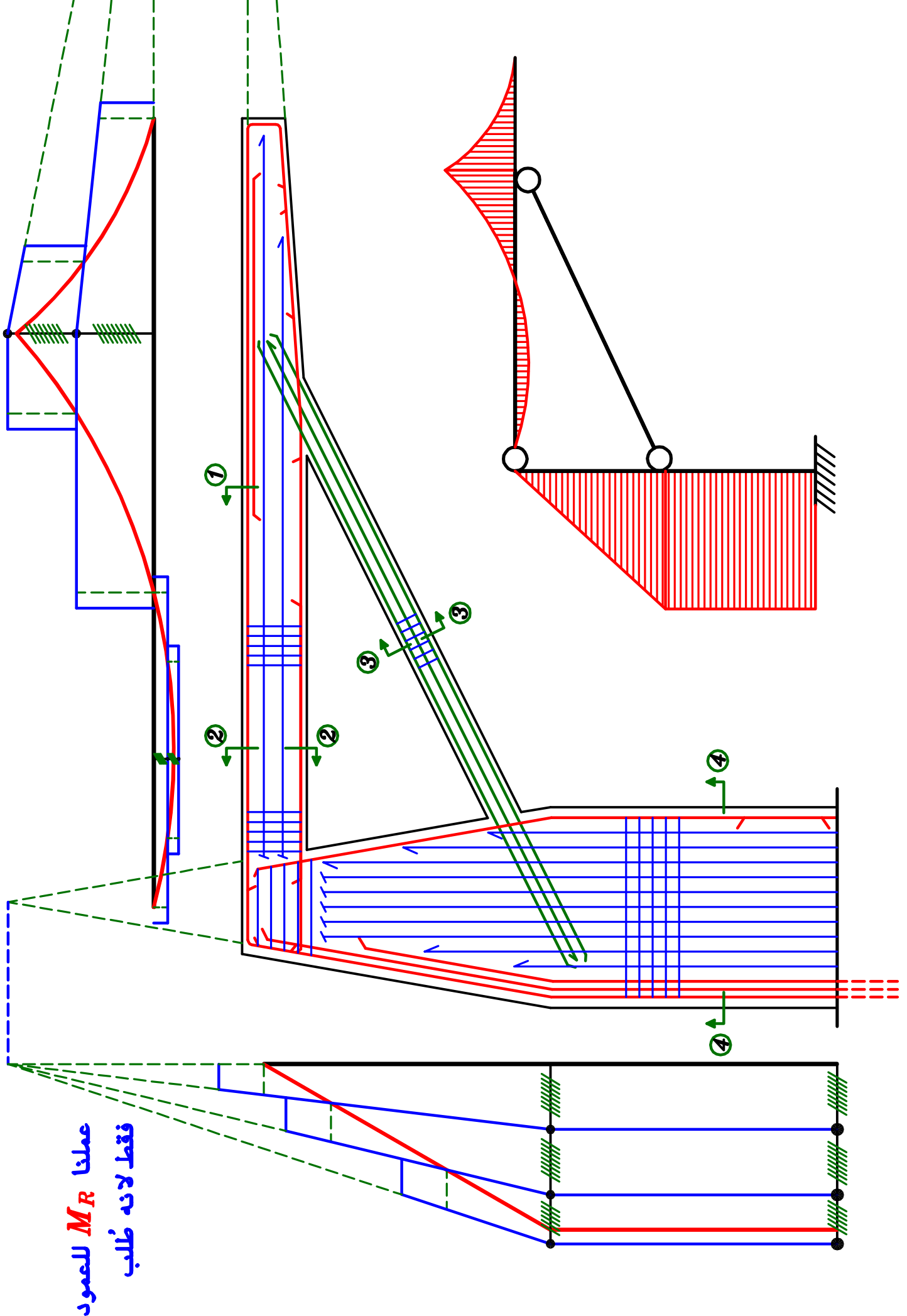


Check Shear. – Allowable shear stress.

$$q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{35}{1.5}} = 1.16 \text{ N/mm}^2$$

∴ All sections have stresses less than q_{cu}

∴ Stirrups For all sections are $5\phi 8 \text{ m}^2$ 2 branches





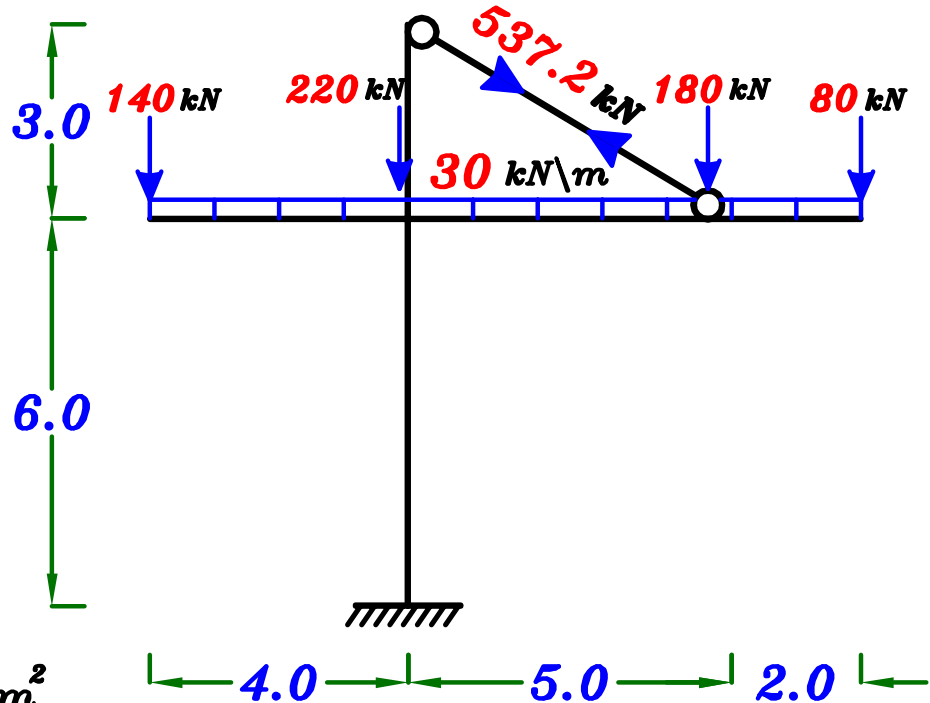
Example.

Data.

$$b_{(Frame)} = 350 \text{ mm}$$

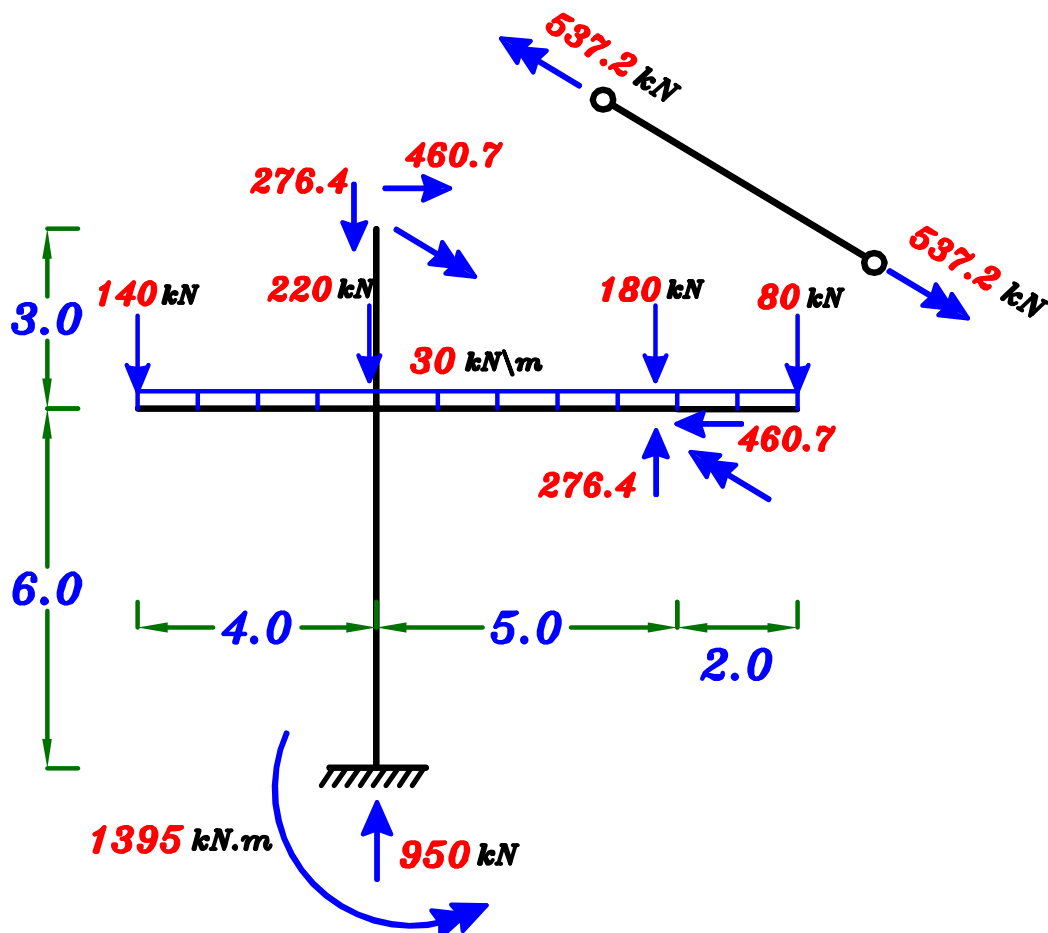
st. 360/520

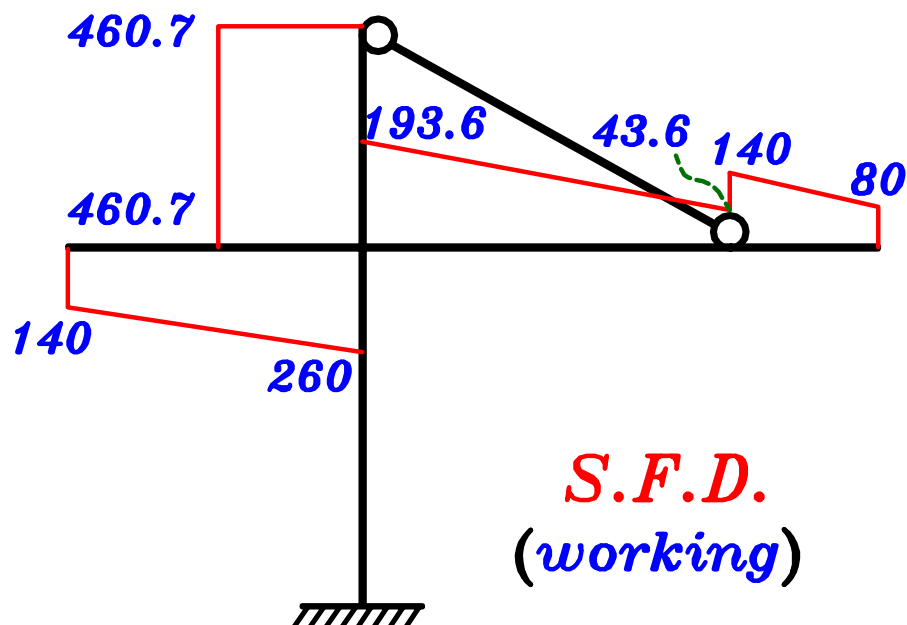
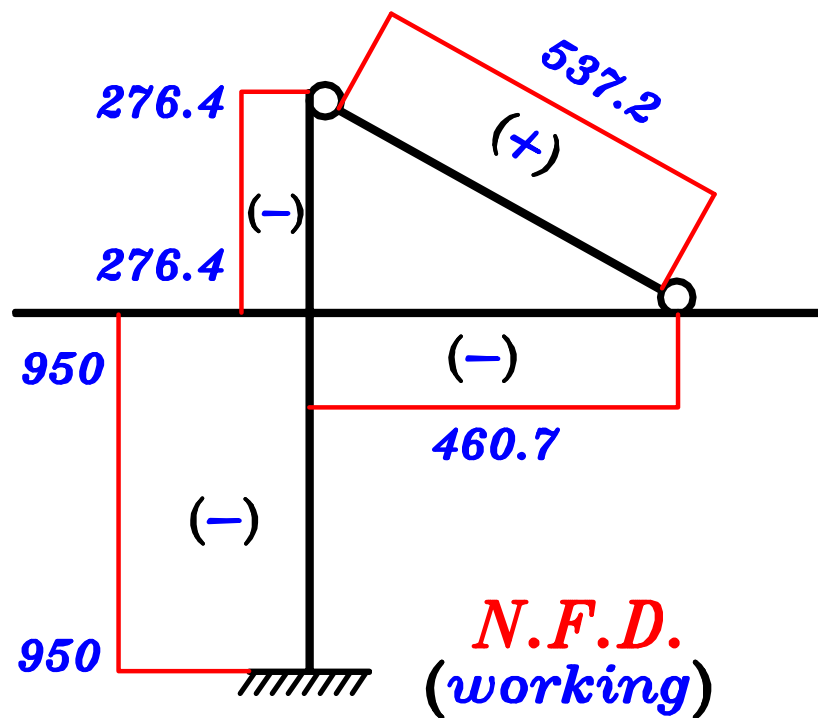
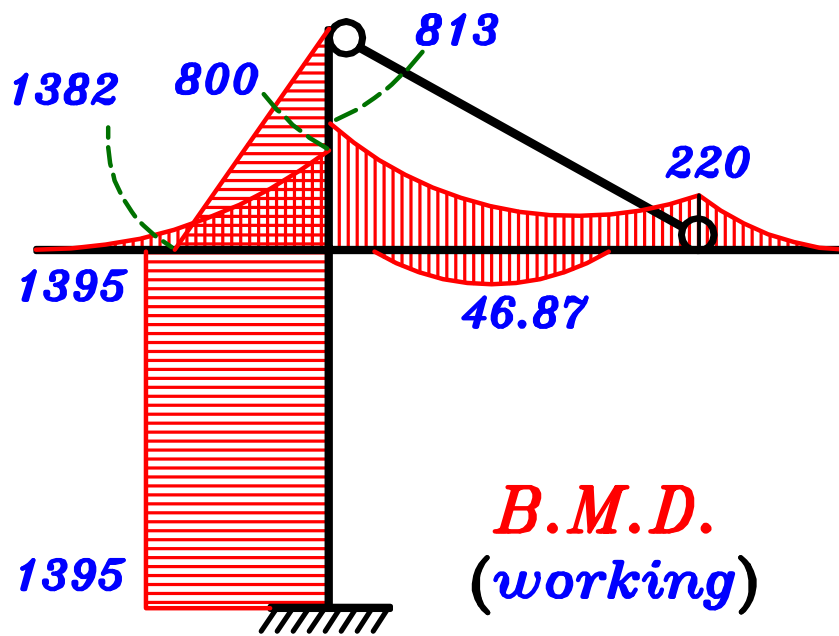
$$C = 30 = F_{cu} = 30 \text{ N/mm}^2$$

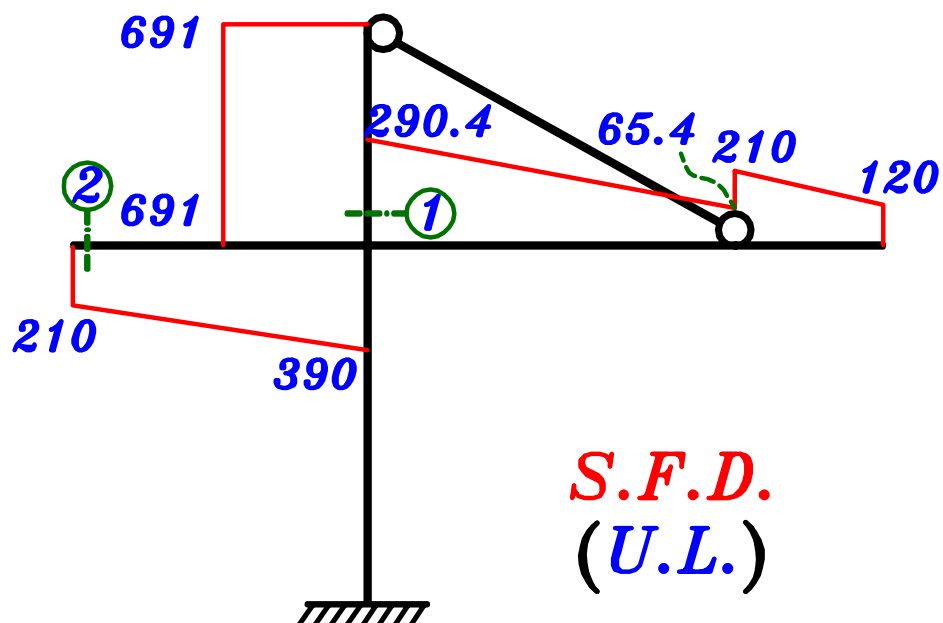
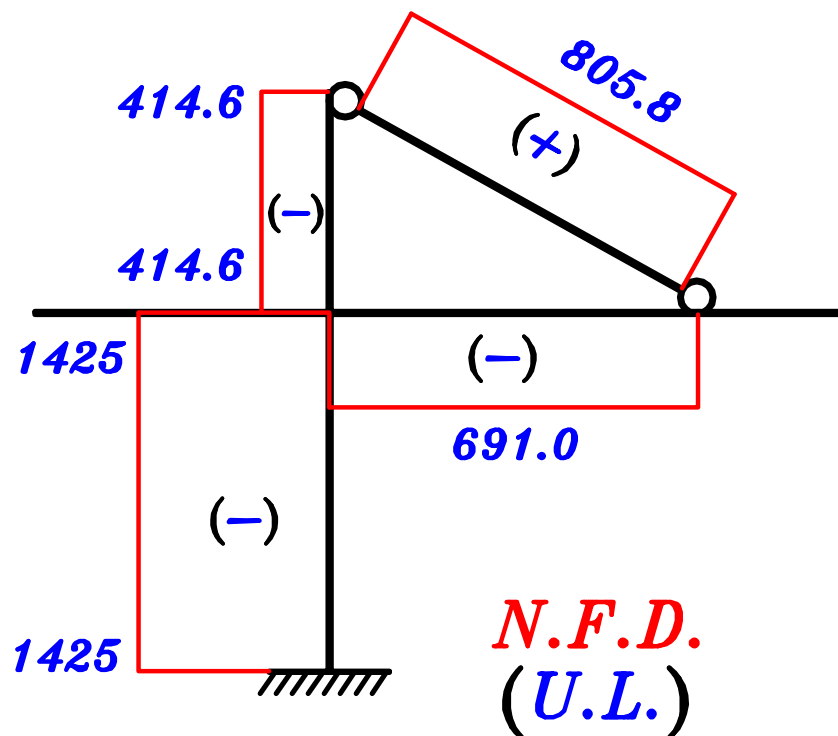
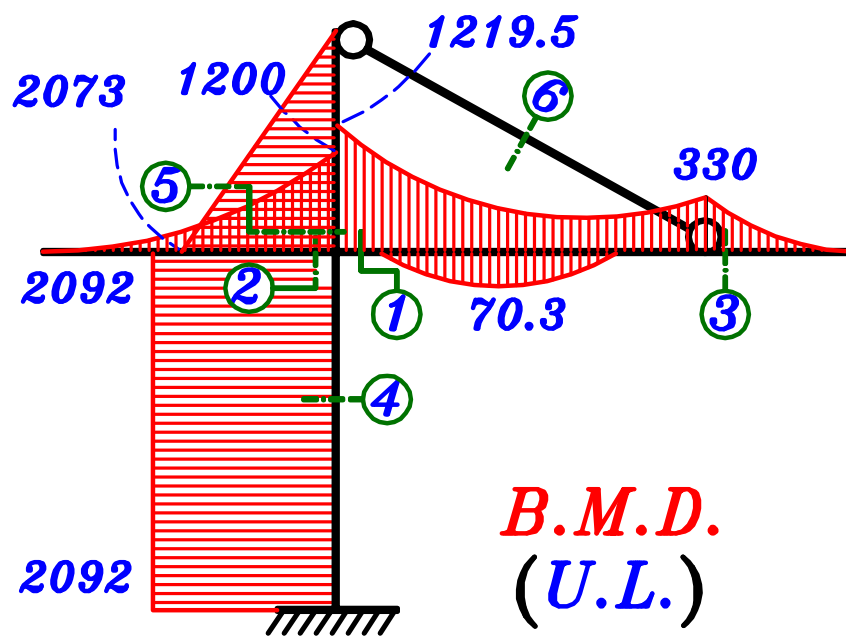


Req.

- 1 - Draw B.M.D. , N.F.D. & S.F.D.
- 2 - Design the critical sections of the Frame For Bending and shear.
- 3 - Draw the details of reinforcement For intermediate Frame (**F**) in elevation to scale 1:50 and cross sections to scale 1:25







2 - Design the critical sections of the Frame For Bending and shear.

Sec. ① $M = 1219.5 \text{ kN.m}$, $P = 691.0 \text{ kN}$, $b = 350 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{1219.5 * 10^6}{30 * 350}} = 1192.8 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1192.8) = (1312.1 \rightarrow 1550.6) \text{ mm}$$

\therefore Take $d = 1400 \text{ mm}$, $t = 1500 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{691.0 * 10^3}{30 * 350 * 1500} = 0.0438 > 0.04$ (Don't neglect P)

\therefore Design the Sec. on both $N.F.$ & $B.M.$

$$e = \frac{M}{P} = \frac{1219.5}{691.0} = 1.76 \text{ m} \quad \therefore \frac{e}{t} = \frac{1.76}{1.5} = 1.17 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.76 + \frac{1.50}{2} - 0.10 = 2.41 \text{ m}$$

$$M_s = P * e_s = 691.0 * 2.41 = 1665.3 \text{ kN.m}$$

$$\therefore 1400 = C_1 \sqrt{\frac{1665.3 * 10^6}{30 * 350}} \rightarrow C_1 = 3.51 \rightarrow J = 0.78$$

$$\begin{aligned} \therefore A_s &= \frac{M_s}{J F_y d} - \frac{N_{U.L.}}{(F_y \setminus \delta_s)} \\ &= \frac{1665.3 * 10^6}{0.780 * 350 * 1400} - \frac{691.0 * 10^3}{(360 \setminus 1.15)} = 2149.8 \text{ mm}^2 \end{aligned}$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2149.8 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1400 = 1677.4 \text{ mm}^2$$

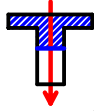
$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 2149.8 \text{ mm}^2$ **6 ϕ 22**

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{22 + 25} = 6.91 = 6.0 \text{ bars}$$

Sec. ② $M = 1200$ kN.m , $P = \text{Zero}$ kN , $b = 350$ mm

$d = 1400$ mm (the same depth of sec. ①)

The sec. is R-sec.



$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \therefore 1400 = c_1 \sqrt{\frac{1200 * 10^6}{30 * 350}} \rightarrow c_1 = 4.14 \rightarrow J = 0.808$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1200 * 10^6}{0.808 * 360 * 1400} = 2946.7 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2946.7 \text{ mm}^2$

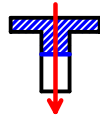
$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1400 = 1677.4 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2946.7 \text{ mm}^2 \quad \text{8 } \phi 22$$

Sec. ③ $M = 330$ kN.m , $P = \text{Zero}$ kN , $b = 350$ mm

$d = 1400$ mm (the same depth of sec. ①)

The sec. is R-sec.



$$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \therefore 1400 = c_1 \sqrt{\frac{330 * 10^6}{30 * 350}} \rightarrow c_1 = 7.89 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{330 * 10^6}{0.826 * 360 * 1400} = 792.7 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 792.7 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1400 = 1677.4 \text{ mm}^2$$

$$\mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$A_{s_{min.}} = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1400 = 1677.4 \text{ mm}^2 \quad \left. \begin{array}{l} \text{الأقل} \\ 1.3 A_{s_{req.}} = 1.3 * 792.7 = 1030.5 \text{ mm}^2 \end{array} \right\} = 1030.5 \text{ mm}^2 \quad \text{3 } \phi 22$$

Sec. ④ $M = 2092 \text{ kN.m}$, $P = 1425 \text{ kN}$, $b = 350 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{2092 * 10^6}{30 * 350}} = 1562.2 \text{ mm (as R-Sec.)}$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1562.2) = (1718.5 \rightarrow 2030) \text{ mm}$$

$$\therefore \text{Take } \boxed{d = 1800 \text{ mm}} , \boxed{t = 1900 \text{ mm}}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{1425 * 10^3}{30 * 350 * 1900} = 0.071 > 0.04 \text{ (Don't neglect } P \text{)}$$

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{2092}{1425} = 1.47 \text{ m} \therefore \frac{e}{t} = \frac{1.47}{1.90} = 0.77 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.47 + \frac{1.90}{2} - 0.10 = 2.32 \text{ m}$$

$$M_s = P * e_s = 1425 * 2.32 = 3306 \text{ kN.m}$$

$$\therefore 1800 = C_1 \sqrt{\frac{3306 * 10^6}{30 * 350}} \rightarrow C_1 = 3.20 \rightarrow J = 0.76$$

$$\begin{aligned} \therefore A_s &= \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \delta_s)} \\ &= \frac{3306 * 10^6}{0.780 * 360 * 1800} - \frac{1425 * 10^3}{(360 \setminus 1.15)} = 1988.7 \text{ mm}^2 \end{aligned}$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 1988.7 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1800 = 2156.6 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$\left. \begin{aligned} A_{s_{min.}} &= \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1800 = 2156.6 \text{ mm}^2 \\ 1.3 A_{s_{req.}} &= 1.3 * 1988.7 = 2585.3 \text{ mm}^2 \end{aligned} \right\} \text{الأقل} = 2156.6 \text{ mm}^2 \quad \boxed{6 \text{ } \Phi \text{ } 22}$$

Sec. ⑤ $M = 2073 \text{ kN.m}$, $P = 414.6 \text{ kN}$, $b = 350 \text{ mm}$

(Take the same depth of Sec. ④)

∴ Take $d = 1800 \text{ mm}$, $t = 1900 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{414.6 * 10^3}{30 * 350 * 1900} = 0.020 < 0.04$ (Neglect P)

∴ $d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \therefore 1800 = c_1 \sqrt{\frac{2073 * 10^6}{30 * 350}} \rightarrow c_1 = 4.05 \rightarrow J = 0.805$

∴ $A_s = \frac{M_{U.L.}}{J F_y d} = \frac{2073 * 10^6}{0.805 * 360 * 1800} = 3974 \text{ mm}^2$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 3974 \text{ mm}^2$

$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1800 = 2156.6 \text{ mm}^2$

∴ $A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 3974 \text{ mm}^2$

11 ϕ 22

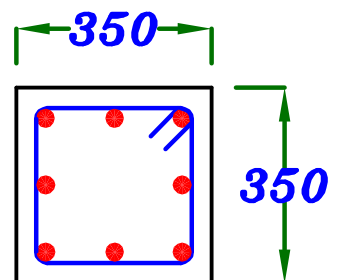
Sec. ⑥ $T = 805.8 \text{ kN}$

لانه $Link \text{ member}$ و عليه قوى $Tension$ فقط
فلن يحتاج الى ابعاد كبيره فمن الممكن اخذ الابعاد $(b * b)$

$A_c = (b * b) (350 * 350)$

$A_s = \frac{T}{F_y \gamma_s} = \frac{805.8 * 10^3}{360 \setminus 1.15} = 2574.7 \text{ mm}^2$

8 ϕ 22



8 ϕ 22

Check Shear.

– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{30}{1.5}} = 3.0 \text{ N/mm}^2$$

Sec. ① $Q = 691 \text{ kN}$

$$\therefore \text{Actual shear stress.} = q_u = \frac{Q}{b d} = \frac{691 * 10^3}{350 * 1800} = 1.09 \text{ N/mm}^2$$

$\therefore q_{cu} < q_u < q_{max.} \therefore$ We need Stirrups more Than $5 \phi 8 \text{ m}$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.09 - \frac{1.07}{2} = \frac{2 * 50.3 (240 \delta_s)}{350 * S} \rightarrow S = 108.1 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

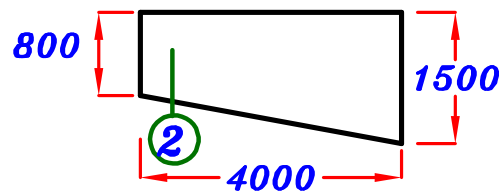
$$\therefore \text{No. of stirrups/m} = \frac{1000}{S} = \frac{1000}{108.1} = 9.25 = 10$$

\therefore Use Stirrups $10 \phi 8 \text{ m}$ 2 branches

Sec. ② $Q = 210 \text{ kN}$

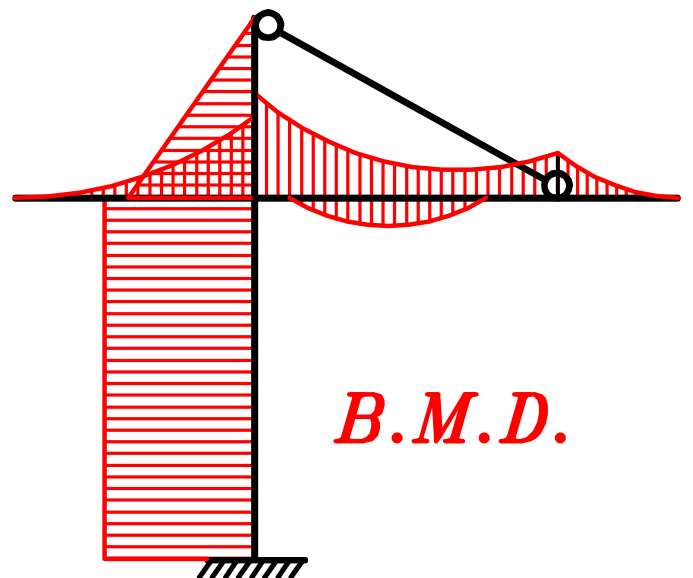
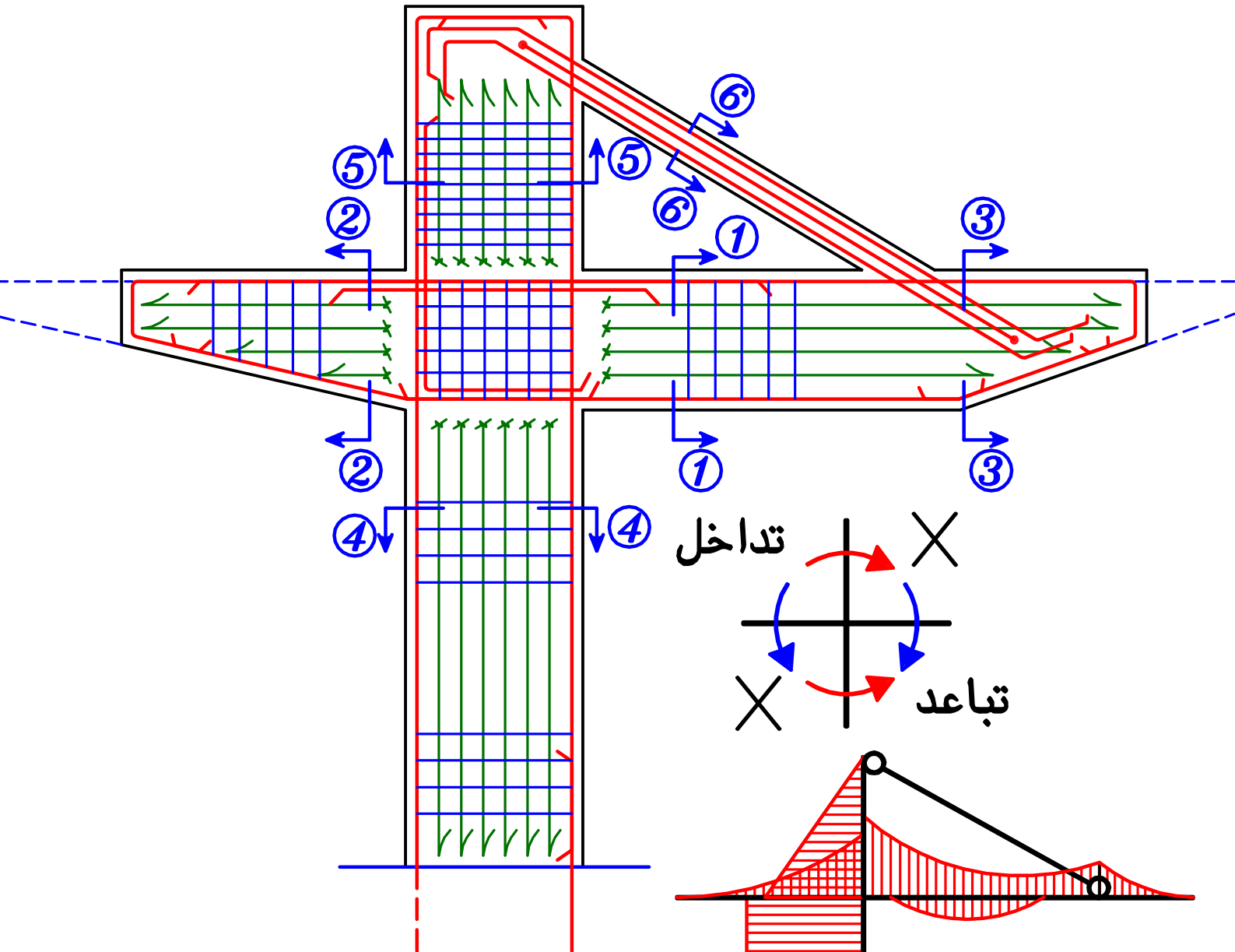
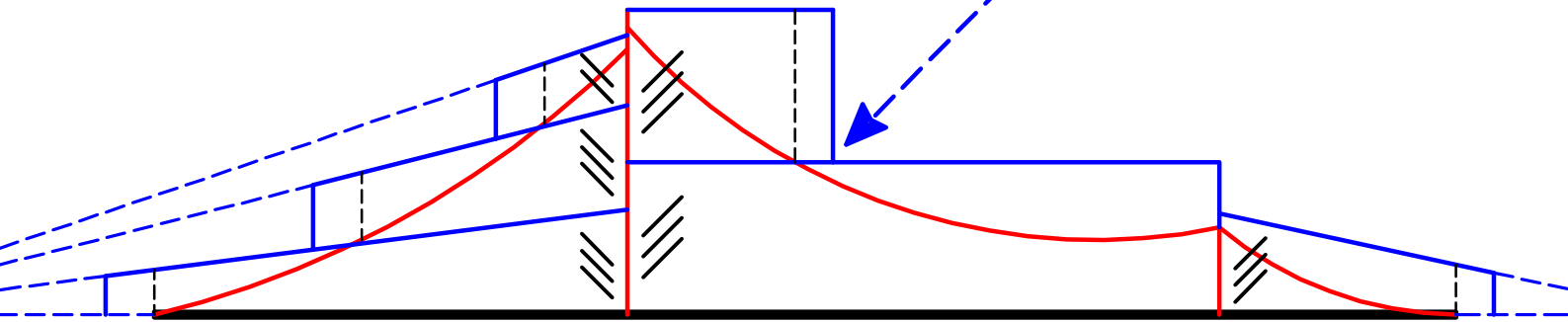
$$\text{Actual shear stress.} = q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

$$q_u = \frac{210 * 10^3}{350 * 750} - \text{ZERO} = 0.80 \text{ N/mm}^2$$

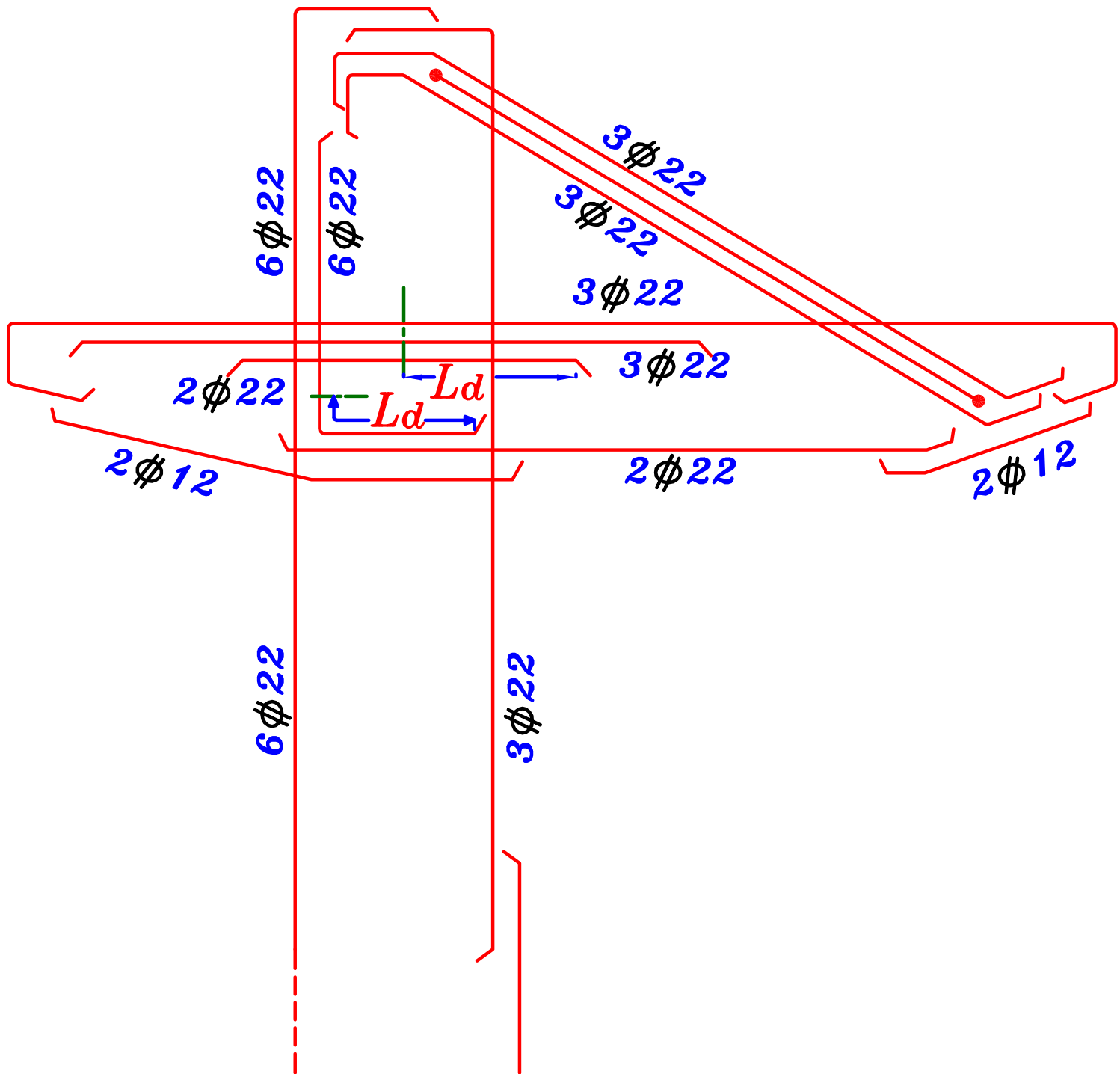


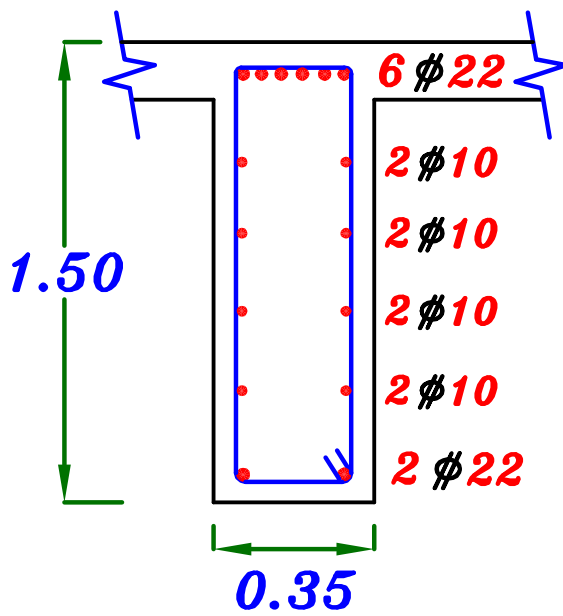
$\therefore q_u < q_{cu} \rightarrow$ Use min. stirrups $5 \phi 8 \text{ m}$

ملحوظه **scale** البلوكات مختلف في هذه المنطقه
 لوجود **Normal**

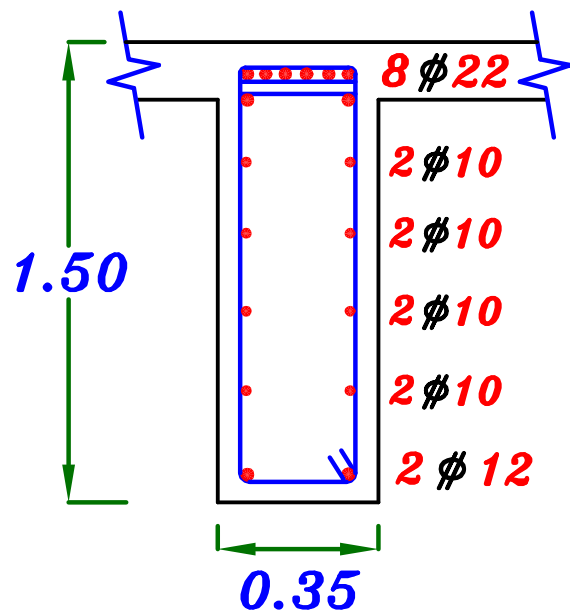


B.M.D.

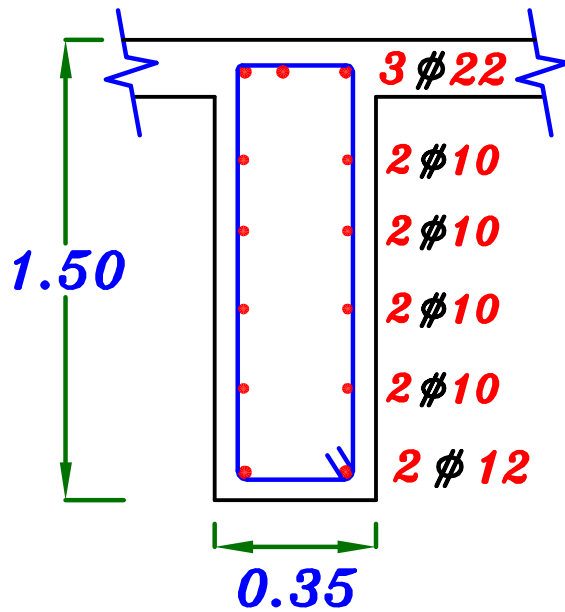




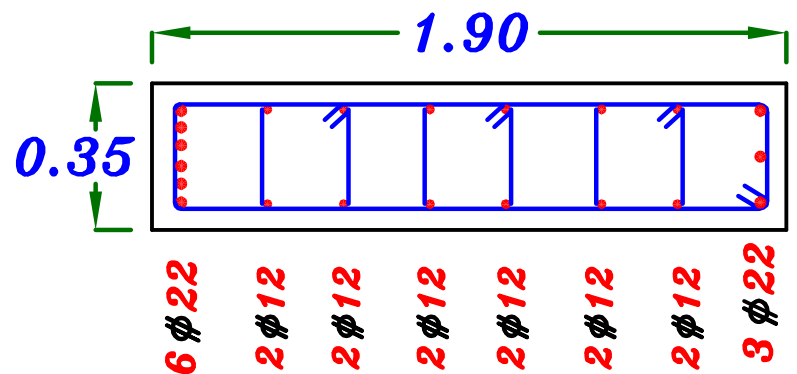
Sec. (1-1)



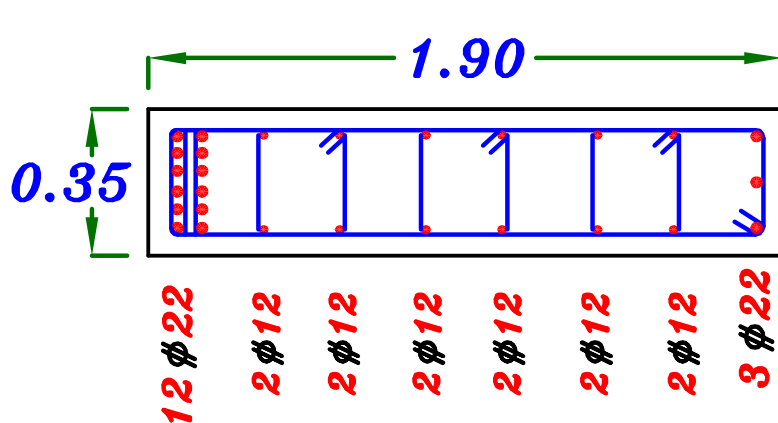
Sec. (2-2)



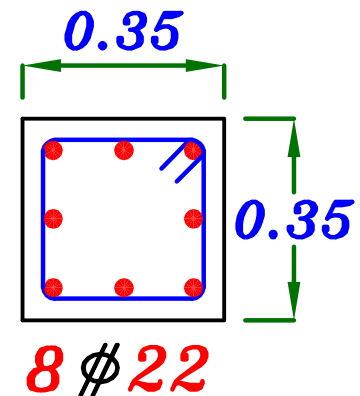
Sec. (3-3)



Sec. (4-4)



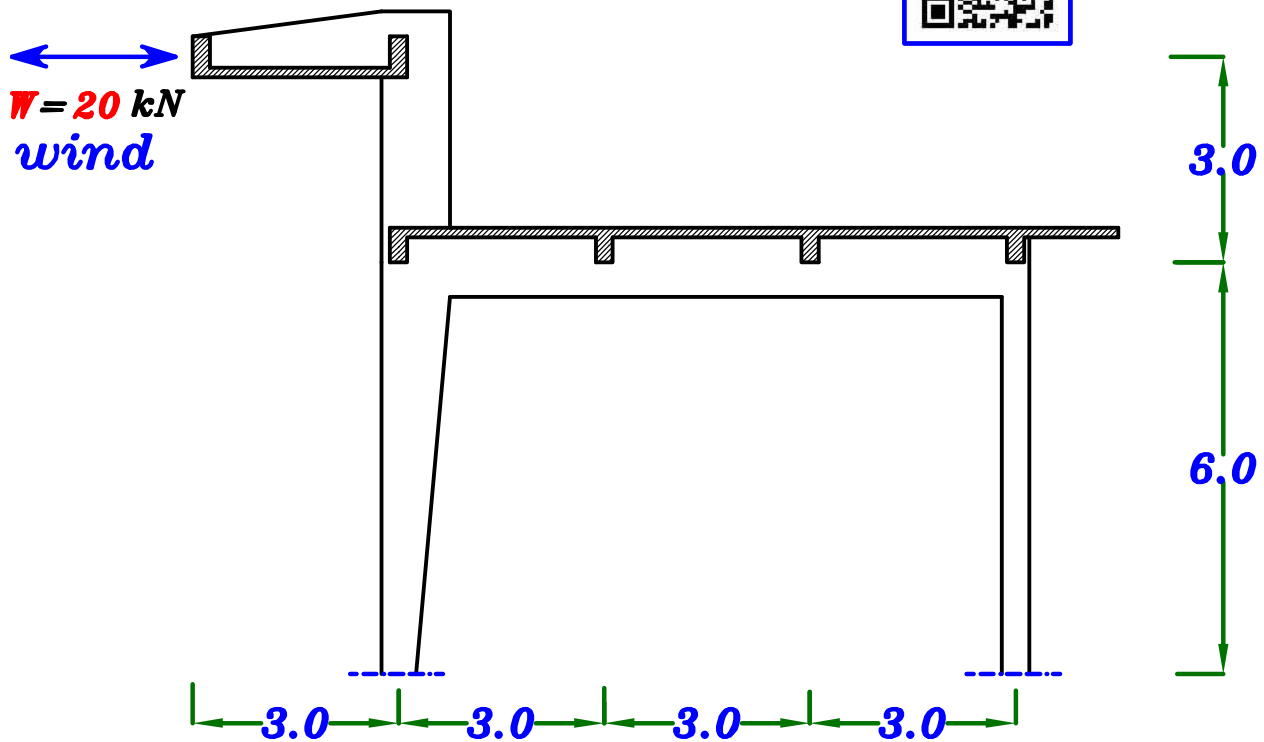
Sec. (5-5)



Sec. (6-6)

RFT. of Max – Max B.M. For Frames.

Example.



Data.

$$F_{cu} = 25 \text{ N/mm}^2$$

$$F_y = 360 \text{ N/mm}^2$$

$$t_s = 120 \text{ mm}$$

$$\text{Spacing} = 6.0 \text{ m}$$

$$b_{(\text{Beams})} = 250 \text{ mm}$$

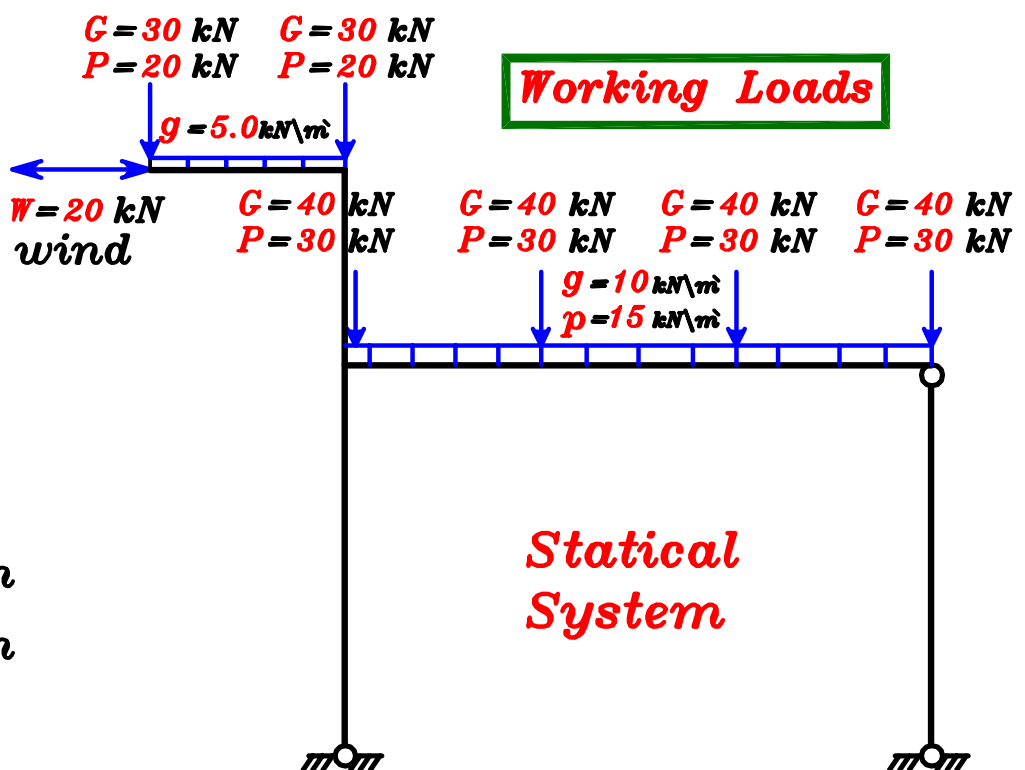
$$b_{(\text{Frames})} = 350 \text{ mm}$$

Req.

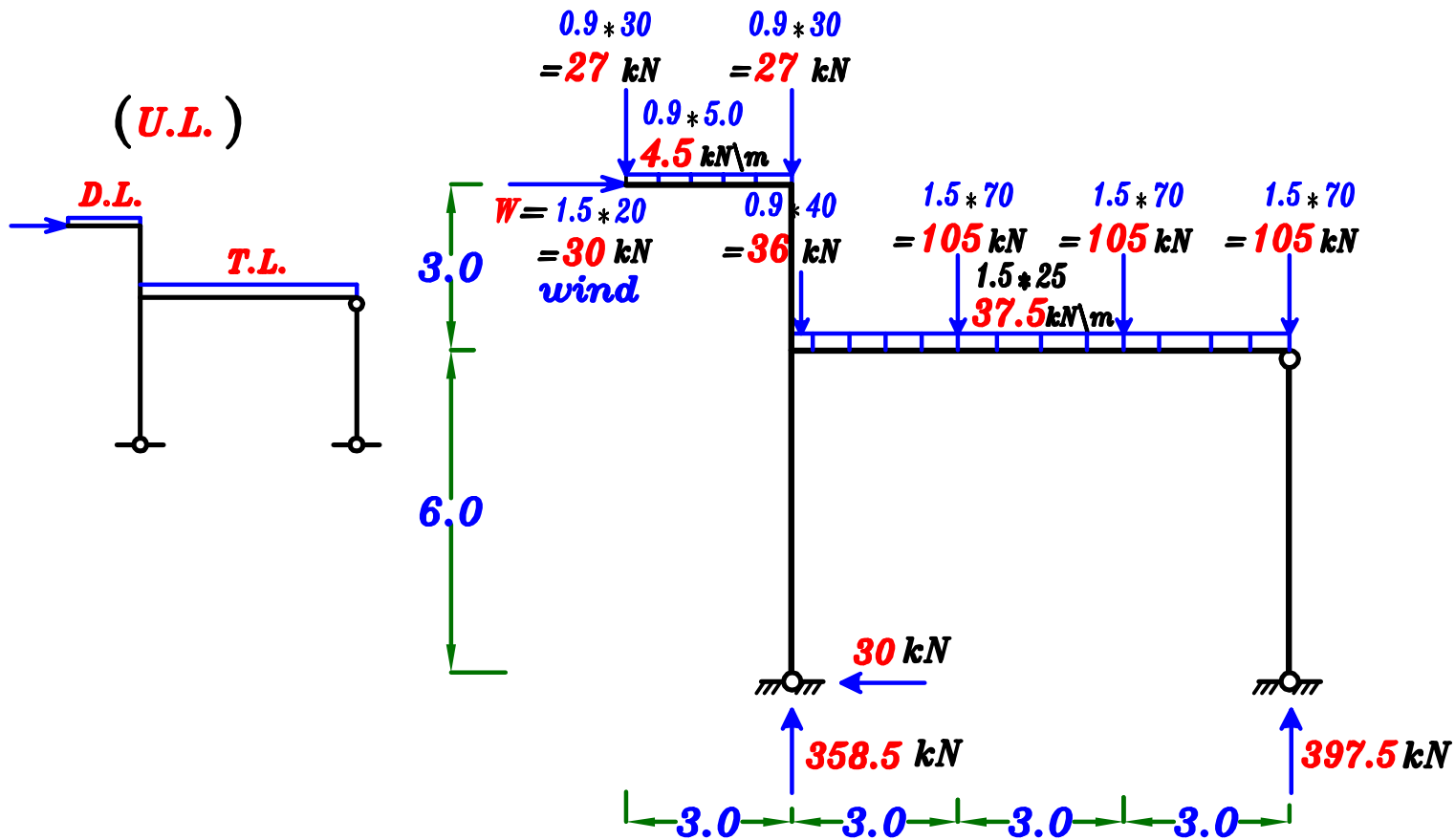
① Draw max–max U.L. B.M.D.

② Design the intermediate Frame & Draw Details of RFT. to scale (1:50) and cross sec. to scale (1:20)

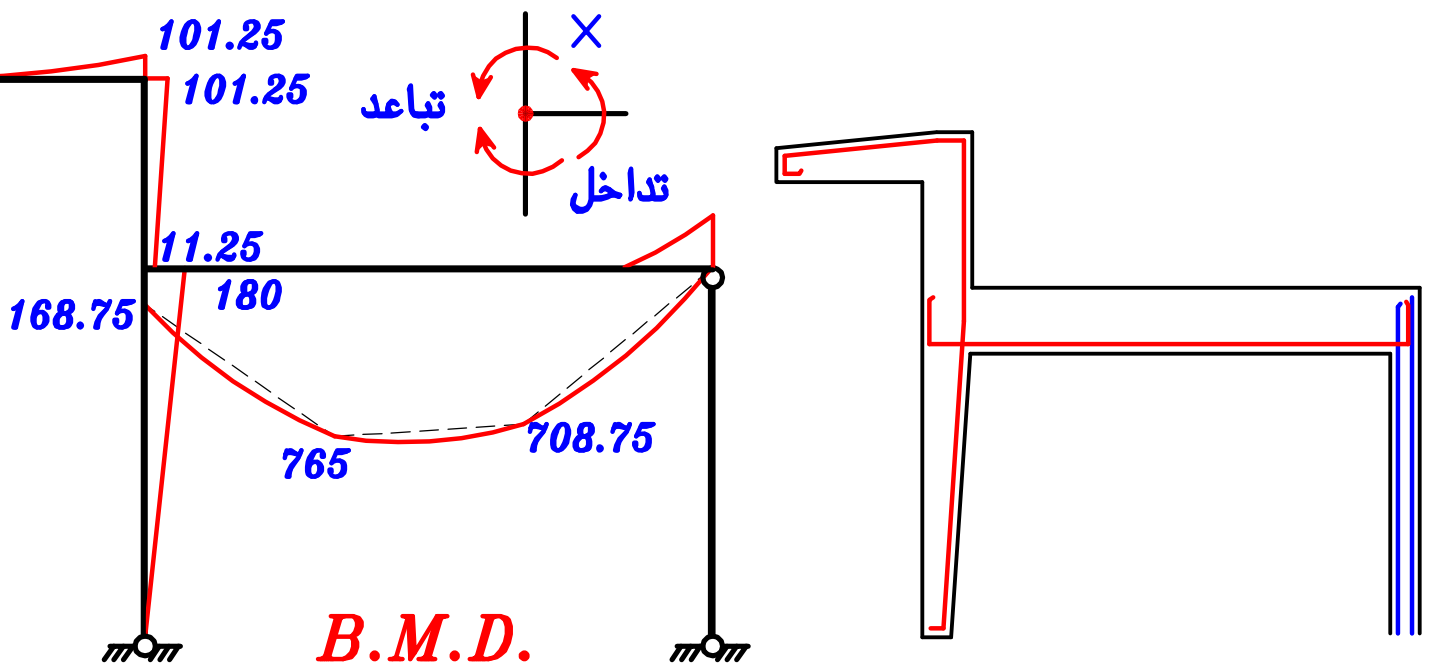
(Curtailement of steel RFT. is to be made by moment of Resistance Method)

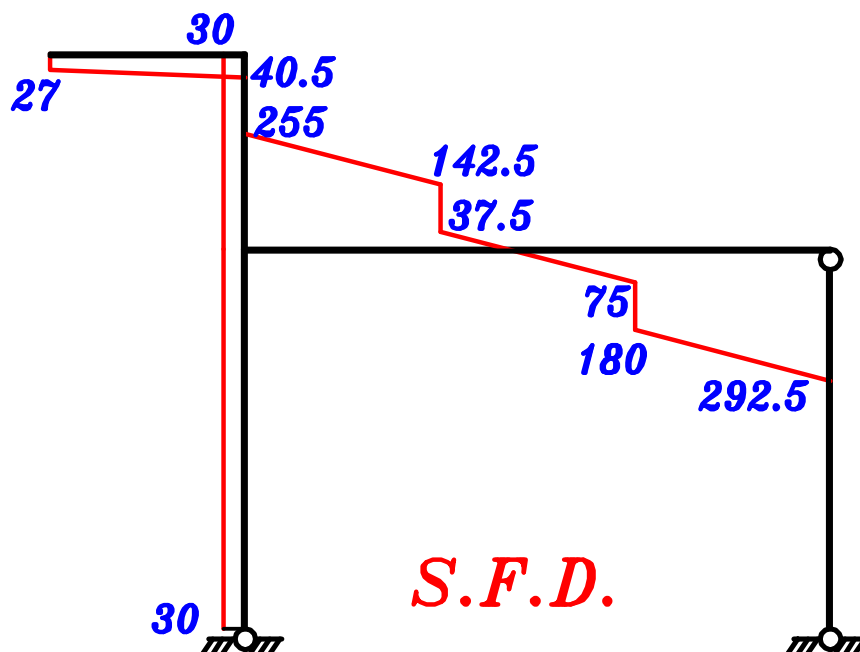
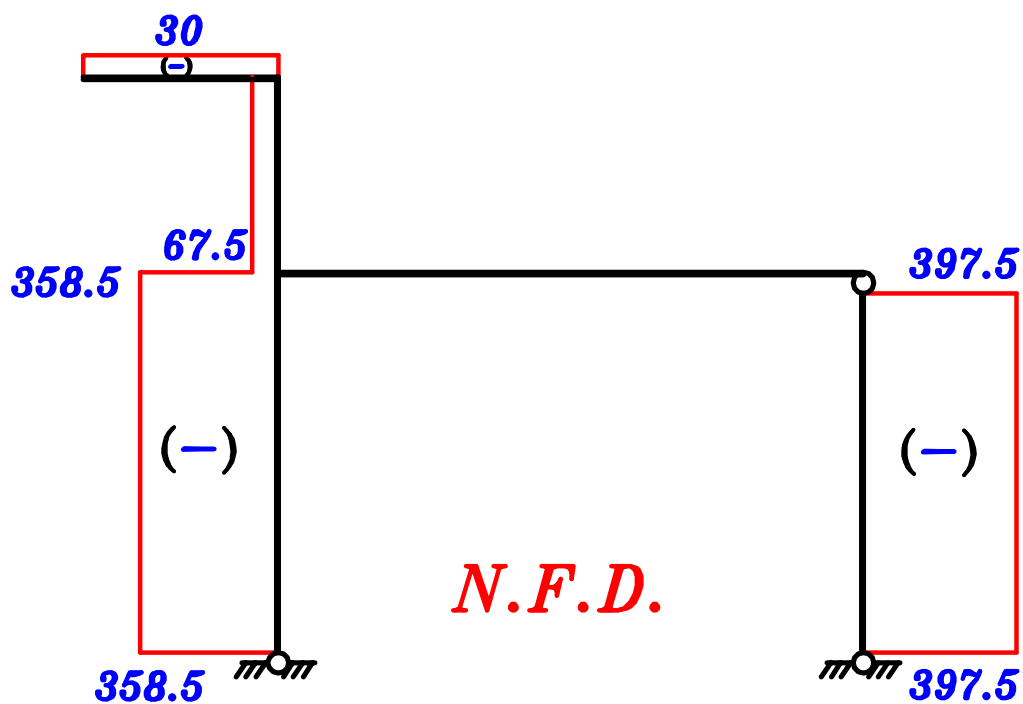
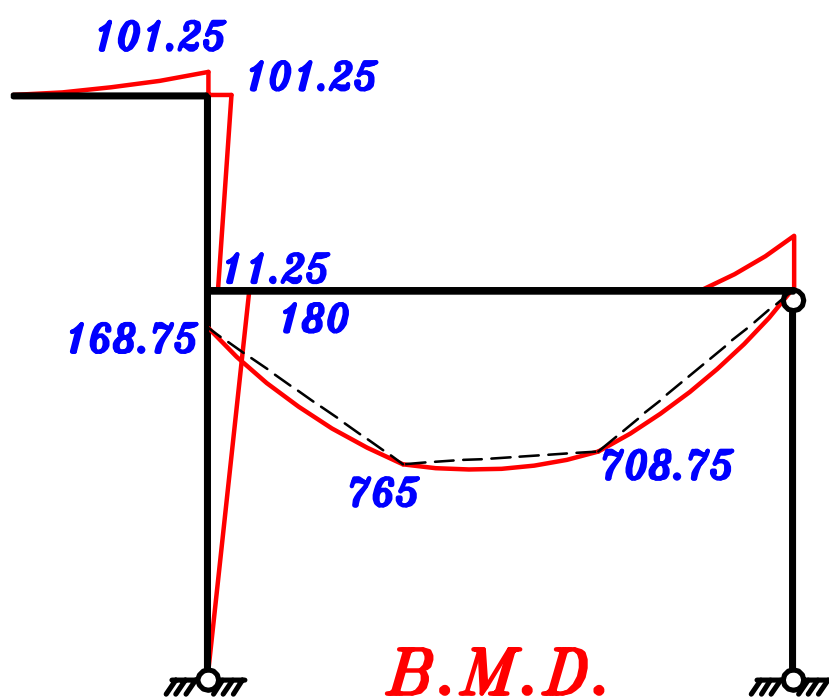


***I.F.D* s**



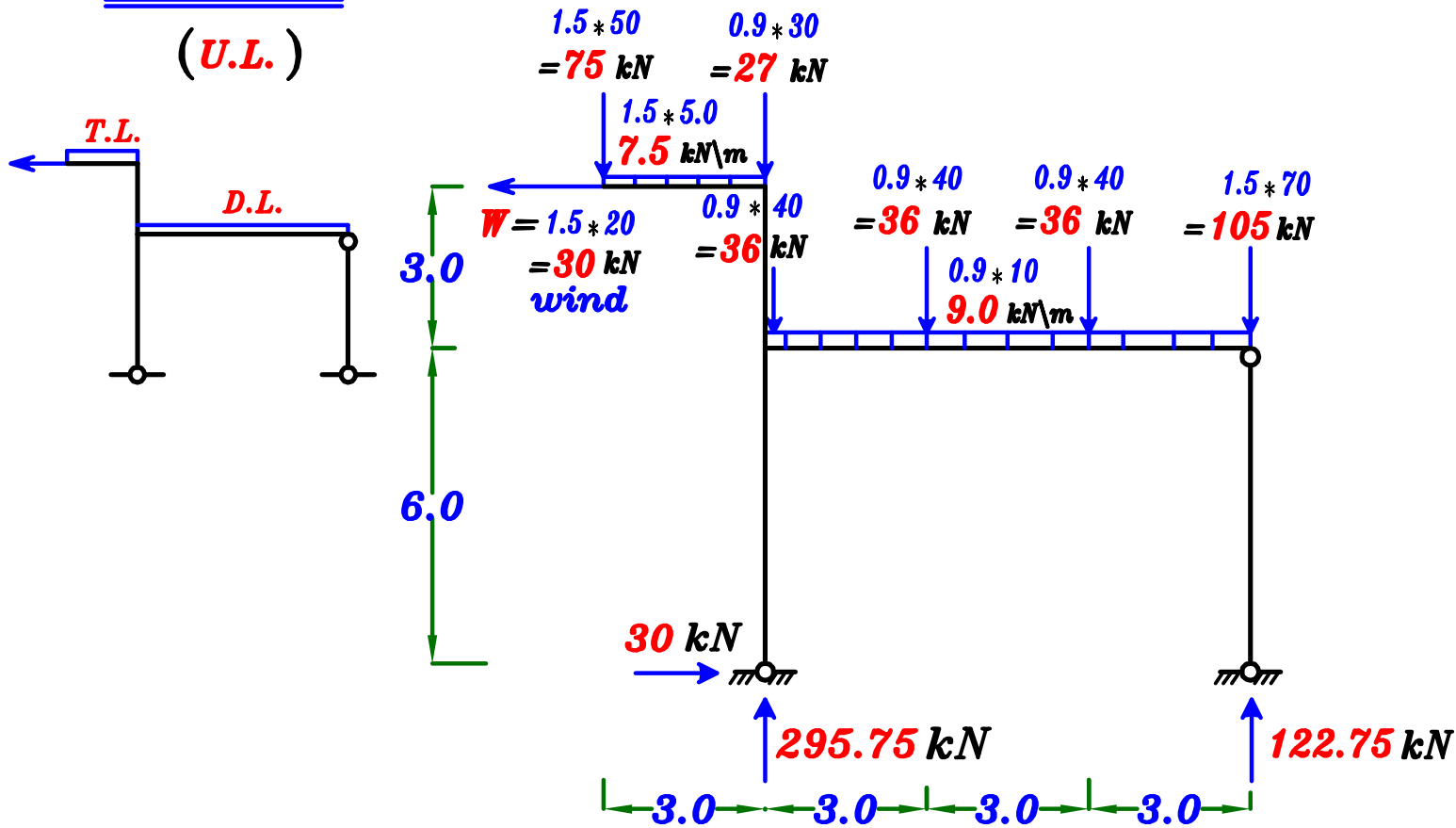
الاحمال المركزه فوق الاعمده لا يكون لها أى تأثير على قيم ال **B.M.** و ال **S.F.**
ولكن يكون لها تأثير على قيم ال **N.F.** على الاعمده و للتصميم يفضل للاعمد التى عليها **B.M. & N.F.**
أن نضع فوقها **D.L.** حيث كلما قلت قيمه ال **N.F.** زادت كميه حديد التسليح
أما الاعمد التى عليها **N.F.** فقط مثل **Link member** فنضع فوقها **T.L.** لزياده كميه حديد التسليح



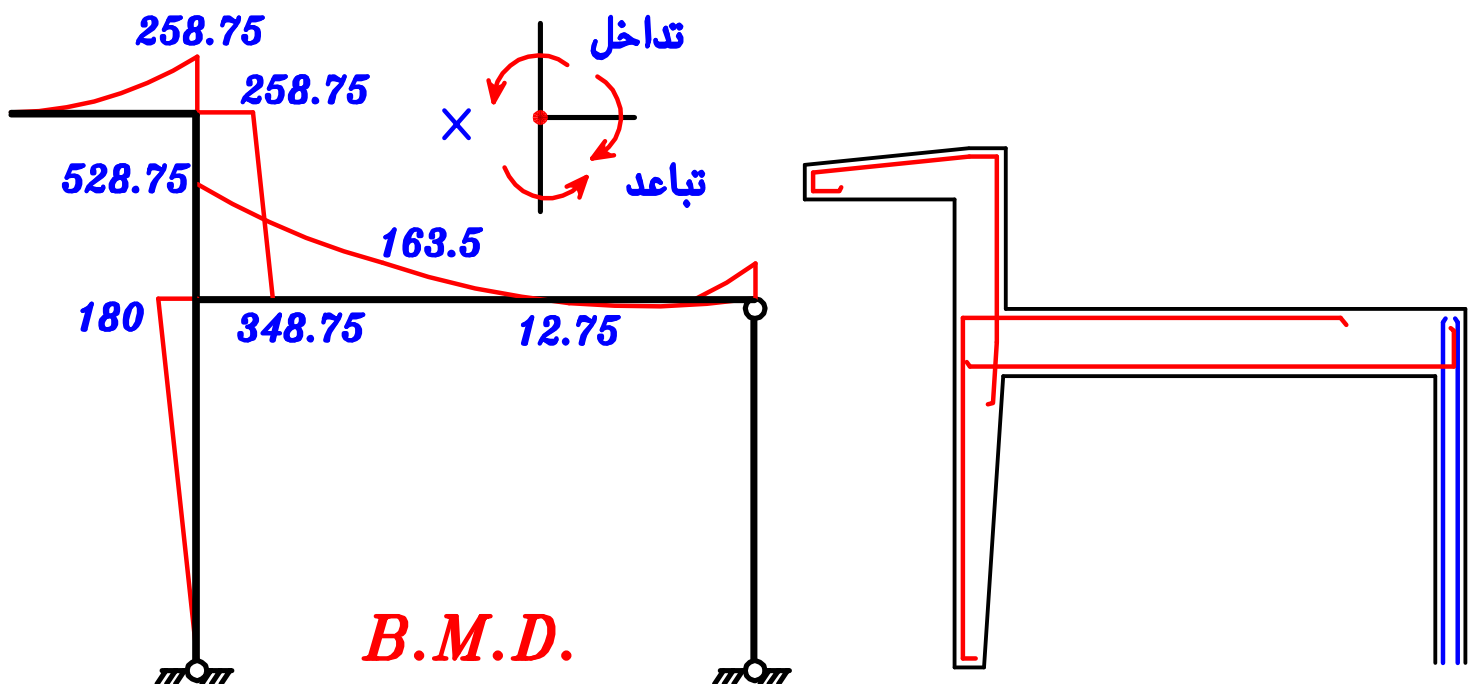


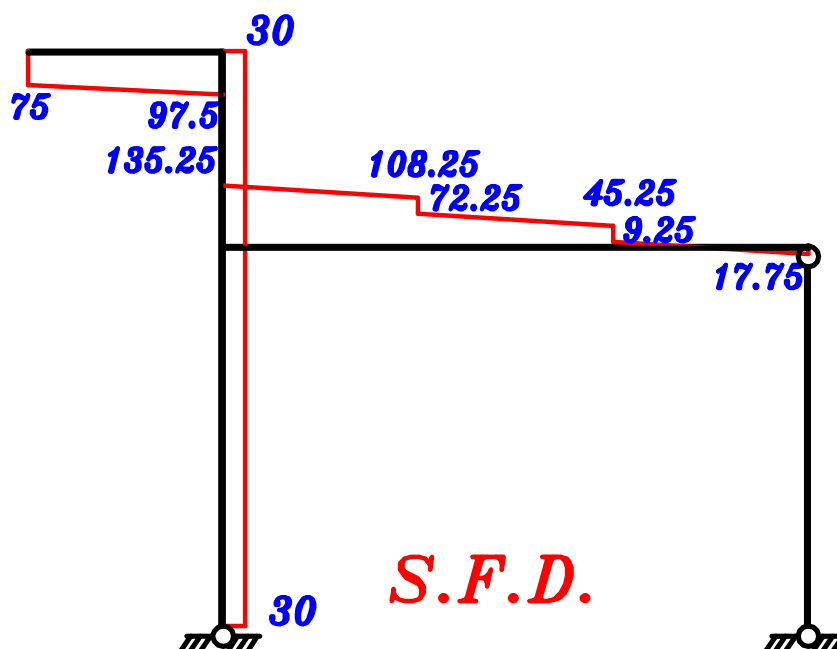
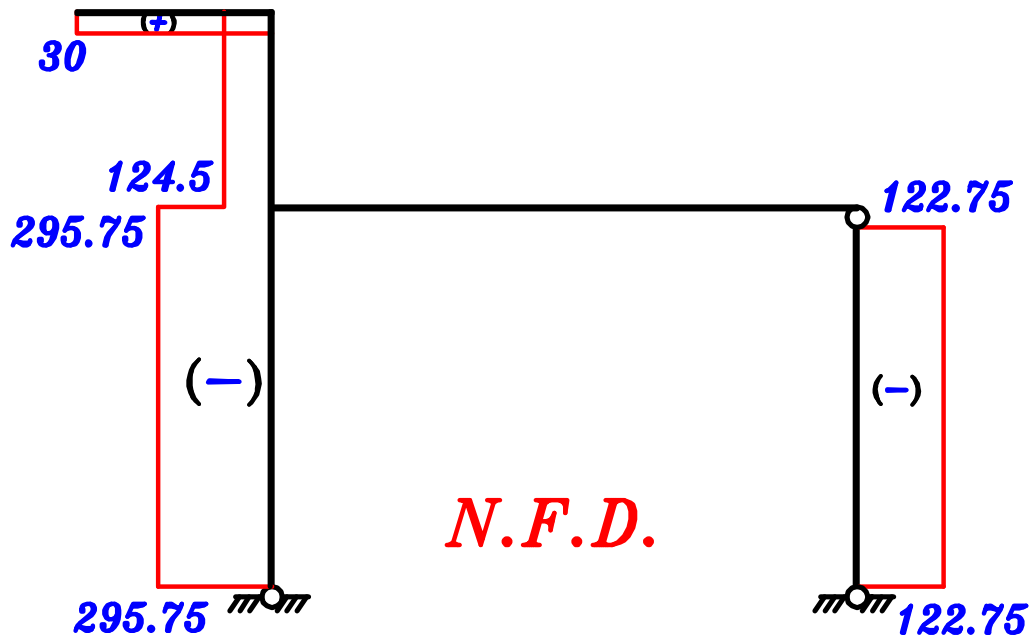
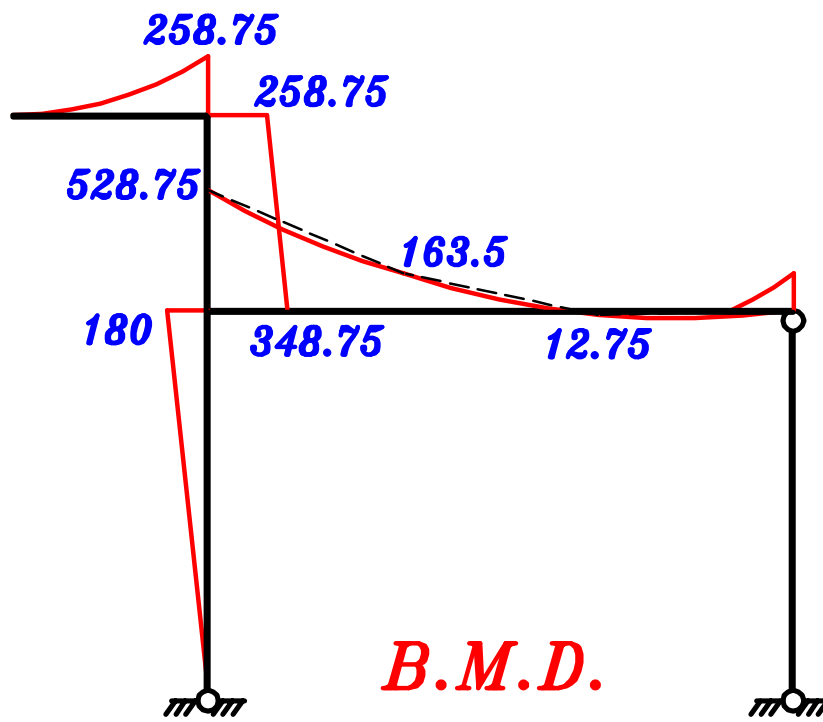
I.F.D

(U.L.)

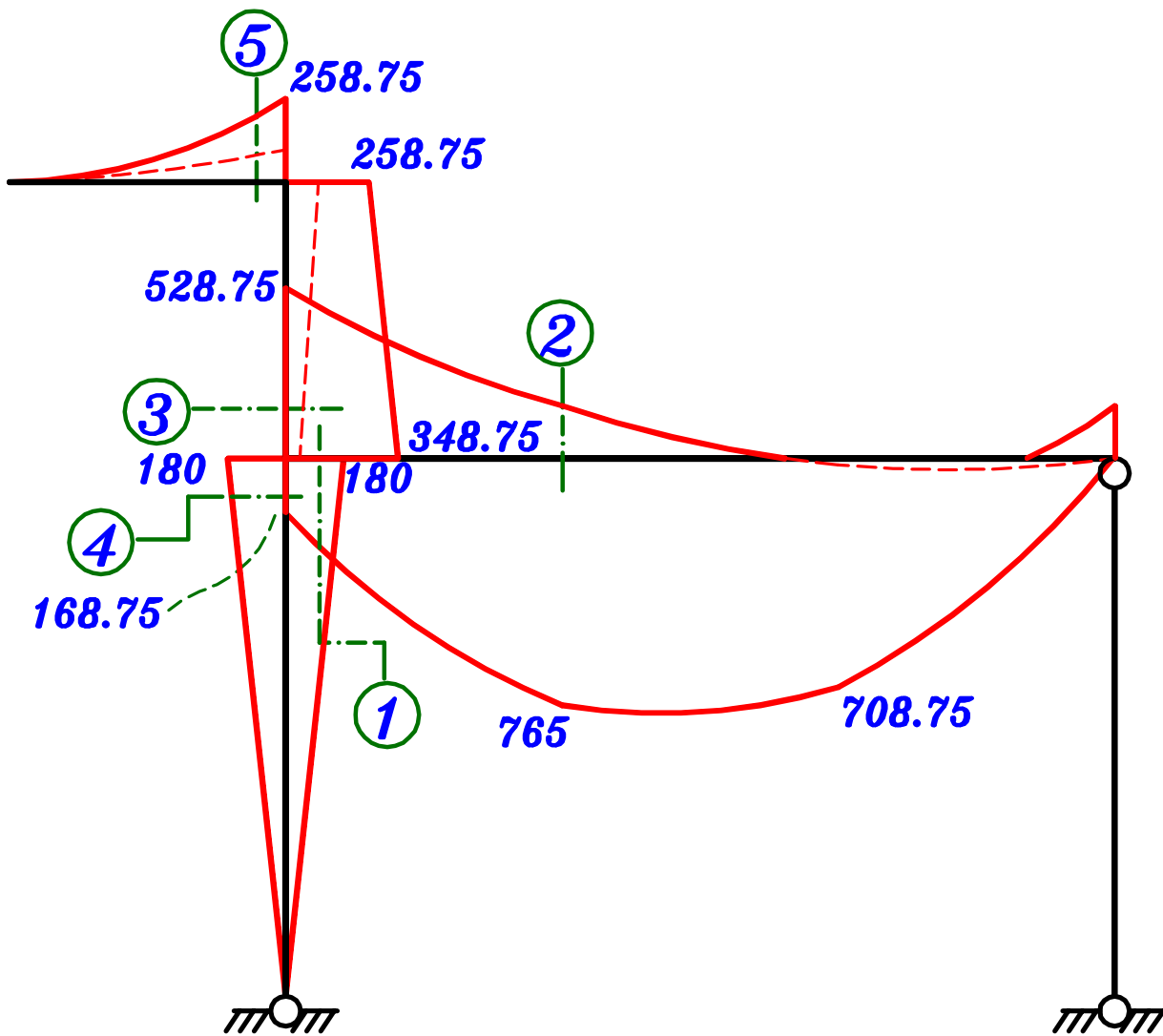


الاحمال المركزة فوق الاعمده لا يكون لها أى تأثير على قيم ال **B.M.** و ال **S.F.**
 و لكن يكون لها تأثير على قيم ال **N.F.** على الاعمده و للتصميم يفضل للاعمد التى عليها **B.M. & N.F.**
 أن نضع فوقها **D.L.** حيث كلما قلت قيمة ال **N.F.** زادت كمية حديد التسليح
 أما الاعمد التى عليها **N.F.** فقط مثل **Link member** فنضع فوقها **T.L.** لزيادة كمية حديد التسليح





$(max-max)$ B.M.D. (U.L.)

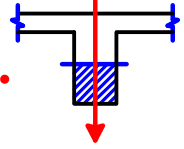


نرسم $max-max$ B.M.D. لتحديد $critical$ sections
و عند تصميم أى قطاع نحدد العزم المصمم عليه من أى حالة تحميل و نأخذ قيمه ال $Normal$
عليه من نفس حالة التحميل و ليس شرط أن يكون ال $Normal$ الاكبر

لا نرسم التسليح على شكل ال $max-max$ B.M.D.
و لكن نرسم التسليح لى حالة تحميل أولا ثم نكمل التسليح من حالة التحميل الاخرى

Design of Sections.

Sec. ① $M = 528.75 \text{ kN.m}$, $b = 350 \text{ mm}$ **R-Sec.**



Take $C_1 = 3.50 \rightarrow J = 0.78$

- Get $d = C_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}} = 3.50 \sqrt{\frac{528.75 \cdot 10^6}{25 \cdot 350}} = 860.37 \text{ mm}$

- Take $d = 900 \text{ mm}$, $t = 950 \text{ mm}$

- Get $A_s = \frac{M_{u.L.}}{J F_y d} = \frac{528.75 \cdot 10^6}{0.78 \cdot 360 \cdot 860.37} = 2188.6 \text{ mm}^2$

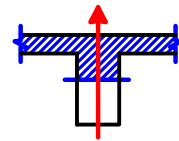
Check $A_{s_{min.}}$ $A_{s_{req.}} = 2188.6 \text{ mm}^2$

$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 350 \cdot 900 = 984.3 \text{ mm}^2$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2188.6 \text{ mm}^2$ **7 ϕ 20**

$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{20 + 25} = 7.22 = 7.0 \text{ bars}$

Sec. ② $M_{u.L.} = 765 \text{ kN.m}$ **T-Sec.**



Take $d = 900 \text{ mm}$ (The same d of Sec. ①)

$B = \left\{ \begin{array}{l} \text{C.L. - C.L.} = \text{Spacing} = 6.0 \text{ m} = 6000 \text{ mm} \\ 16 t_s + b = 16 \cdot 120 + 350 = 2270 \text{ mm} \\ K \frac{L}{5} + b = 1.0 \cdot \frac{9000}{5} + 350 = 2150 \text{ mm} \end{array} \right\}$

$K = 1.0$

$B = 2150 \text{ mm}$

$$\therefore d = C_1 \sqrt{\frac{M_{U.L.}}{F_{cu} B}} \therefore 900 = C_1 \sqrt{\frac{765 * 10^6}{25 * 2150}} \rightarrow C_1 = 7.54 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{765 * 10^6}{0.826 * 360 * 900} = 2858.5 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2858.5 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 900 = 984.3 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2858.5 \text{ mm}^2 \quad (10 \phi 20)$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 2858.5 \quad (4 \phi 12)$$

Sec. ③ $M = 348.75 \text{ kN.m}$, $P = 124.5 \text{ kN}$, $b = 350 \text{ mm}$

Take $C_1 = 3.50 \rightarrow J = 0.78$

$$d_o = 3.5 \sqrt{\frac{348.75 * 10^6}{25 * 350}} = 698.75 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (698.75) = (768.6 \rightarrow 908.3) \text{ mm}$$

Take $d = 900 \text{ mm}$, $t = 900 + 50 = 950 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{124.5 * 10^3}{25 * 350 * 900} = 0.015 < 0.04 \therefore (\text{neglect } P)$

$$\therefore d = d_o = 698.75 \text{ mm} \quad \boxed{d = 700 \text{ mm}} , \quad \boxed{t = 750 \text{ mm}}$$

$$\therefore t_{(Column)} < 0.8 t_{(Beam)} \xrightarrow{\text{Take}} t_{(Column)} = t_{(Beam)} = 950 \text{ mm}$$

$$\therefore d = c_1 \sqrt{\frac{M_{u.l.}}{F_{cu} b}} \therefore 900 = c_1 \sqrt{\frac{348.75 * 10^6}{25 * 350}} \rightarrow c_1 = 4.50 \rightarrow J = 0.819$$

$$\therefore A_s = \frac{M_{u.l.}}{J F_y d} = \frac{348.75 * 10^6}{0.819 * 360 * 900} = 1314.2 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1314.2 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 900 = 984.3 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1314.2 \text{ mm}^2 \quad \text{5 } \phi \text{ 20}$$

Sec. ④ $M = 180 \text{ kN.m}$, $P = 295.75 \text{ kN}$, $b = 350 \text{ mm}$

$d = 900 \text{ mm}$ (the same depth of Sec. ③)

Check $\frac{P}{F_{cu} b t} = \frac{295.75 * 10^3}{25 * 350 * 950} = 0.035 < 0.04 \therefore (\text{neglect } P)$

$$\therefore d = c_1 \sqrt{\frac{M_{u.l.}}{F_{cu} b}} \therefore 900 = c_1 \sqrt{\frac{180 * 10^6}{25 * 350}} \rightarrow c_1 = 6.27 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{u.l.}}{J F_y d} = \frac{180 * 10^6}{0.826 * 360 * 900} = 672.59 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 672.6 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 900 = 984.27 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$A_{s_{min.}} = 0.225 * \frac{\sqrt{F_{cu}}}{F_y} b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 900 = 984.27$$

$$1.3 A_{s_{req.}} = 1.3 * 672.6 = 874.37$$

$$\text{st. 360/520} \quad \frac{0.15}{100} b d = \frac{0.15}{100} * 350 * 900 = 472.5 \text{ mm}^2$$

الأقل = 874.37
الأكبر = 874.37 mm²

3 ϕ 20

Sec. ⑤ $M = 258.75 \text{ kN.m}$, $T = 30.0 \text{ kN}$, $b = 350 \text{ mm}$

Take $C_1 = 3.50 \rightarrow J = 0.78$

$$d_o = 3.5 \sqrt{\frac{258.75 \cdot 10^6}{25 \cdot 350}} = 601.8 \text{ mm (as R-Sec.)}$$

$$d = (0.9 \rightarrow 1.0) d_o = (0.9 \rightarrow 1.0) (601.8) = (541.7 \rightarrow 601.8) \text{ mm}$$

Take $d = 550 \text{ mm}$, $t = 550 + 50 = 600 \text{ mm}$

$$e = \frac{M}{T} = \frac{258.75}{30.0} = 8.625 \text{ m} \quad \therefore \frac{e}{t} = \frac{8.625}{0.6} = 14.37 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e - \frac{t}{2} + c = 8.625 - \frac{0.60}{2} + 0.05 = 8.375 \text{ m}$$

$$M_s = T \cdot e_s = 30.0 \cdot 8.375 = 251.25 \text{ kN.m}$$

$$\therefore d = c_1 \sqrt{\frac{M_s}{F_{cu} b}} \quad \therefore 550 = c_1 \sqrt{\frac{251.25 \cdot 10^6}{25 \cdot 350}} \rightarrow c_1 = 3.24 \rightarrow J = 0.764$$

$$\begin{aligned} \therefore A_s &= \frac{M_s}{J F_y d} + \frac{T_{u.l.}}{(F_y \setminus \delta_s)} \\ &= \frac{251.25 \cdot 10^6}{0.764 \cdot 360 \cdot 550} + \frac{30.0 \cdot 10^3}{(360 \setminus 1.15)} = 1756.75 \text{ mm}^2 \end{aligned}$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1756.75 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 350 \cdot 700 = 765.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1756.75 \text{ mm}^2 \quad \boxed{6 \phi 20}$$

$$Y = \left\{ \begin{array}{l} \frac{t}{2} = \frac{600}{2} = 300 \text{ mm} \\ t_b = \frac{\text{spacing}}{12} = \frac{6000}{12} = 500 \text{ mm} \\ t - \frac{L_c}{3} = 600 - \frac{3000}{3} = -400 \text{ mm} \end{array} \right\}$$

$$Y = 500 \text{ mm}$$

Sec. ⑥ (350 * 450) Axially Loaded Column. $P = 397.5 \text{ kN}$

$$\therefore P_{u.l.} = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

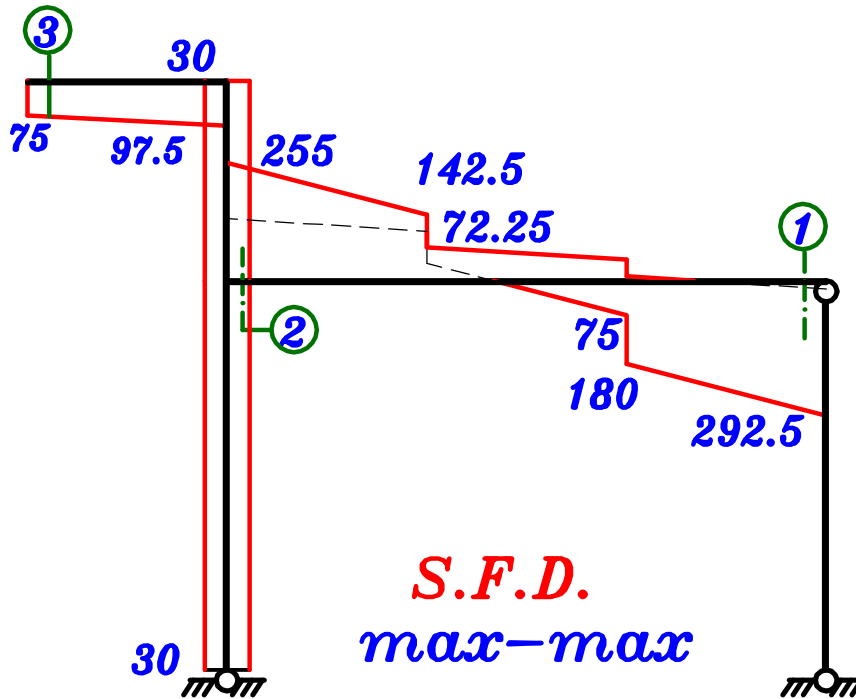
$$\therefore 397.5 * 10^3 = 0.35 (350 * 450) (25) + 0.67 A_s (360)$$

$$\therefore A_s = - 4065.6 \text{ mm}^2 = (-Ve) \text{ Value}$$

$$\therefore A_s = A_{s_{min.}} = \frac{0.8}{100} * 350 * 450 = 1260 \text{ mm}^2$$

12 ϕ 12

Check Shear.



– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{25}{1.5}} = 2.85 \text{ N/mm}^2$$

Sec. ① $Q = 292.5 \text{ kN}$

$$\therefore \text{Actual shear stress.} = q_v = \frac{Q}{b d} = \frac{292.5 * 10^3}{350 * 900} = 0.92 \text{ N/mm}^2$$

$$q_v < q_{cu} \longrightarrow \text{Use min. stirrups } \boxed{5 \phi 8 \setminus m}$$

Sec. ② $Q = 255 \text{ kN}$

$$\therefore \text{Actual shear stress.} = q_v = \frac{Q}{b d} = \frac{255 * 10^3}{350 * 900} = 0.81 \text{ N/mm}^2$$

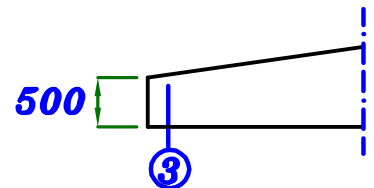
$$q_v < q_{cu} \longrightarrow \text{Use min. stirrups } \boxed{5 \phi 8 \setminus m}$$

Sec. ③ $Q = 75.0 \text{ kN}$

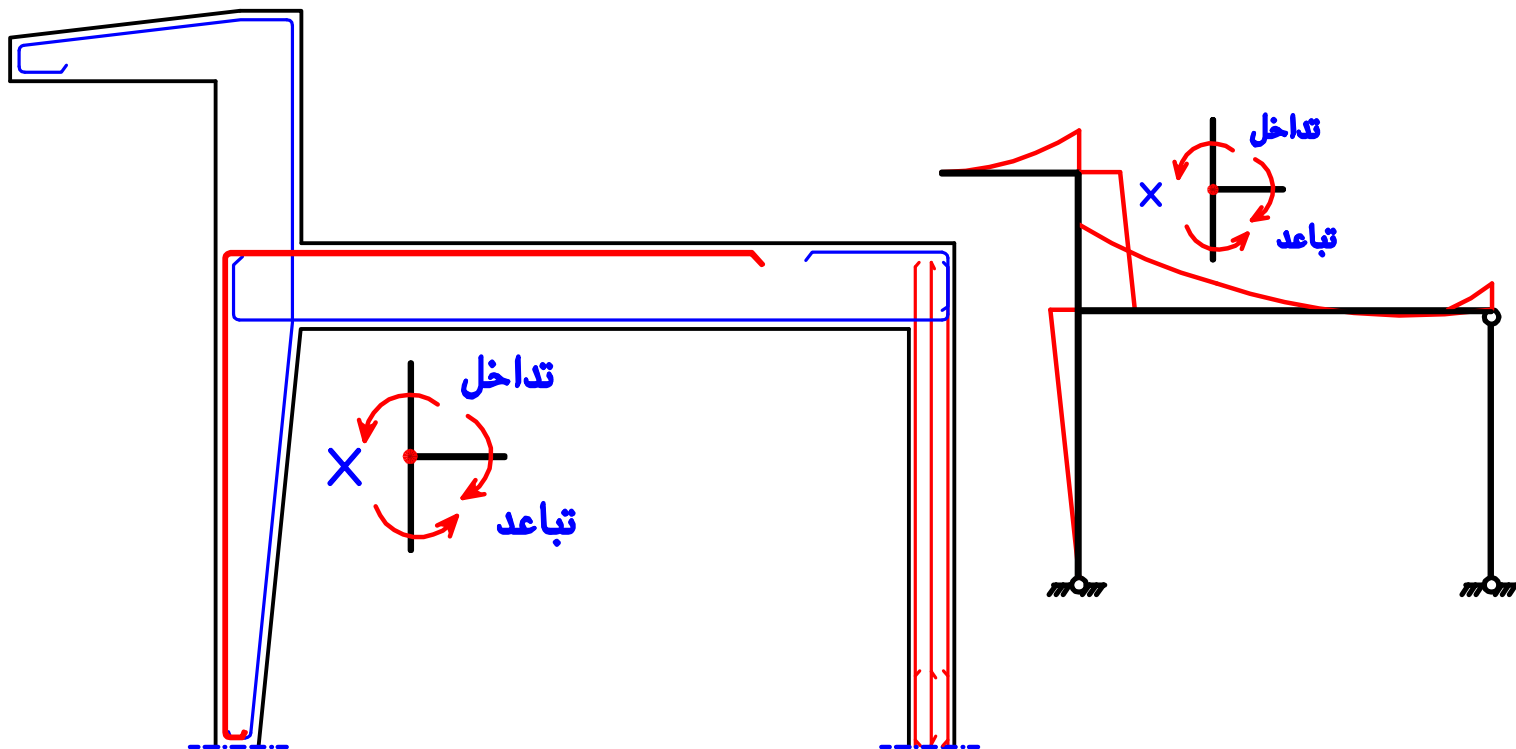
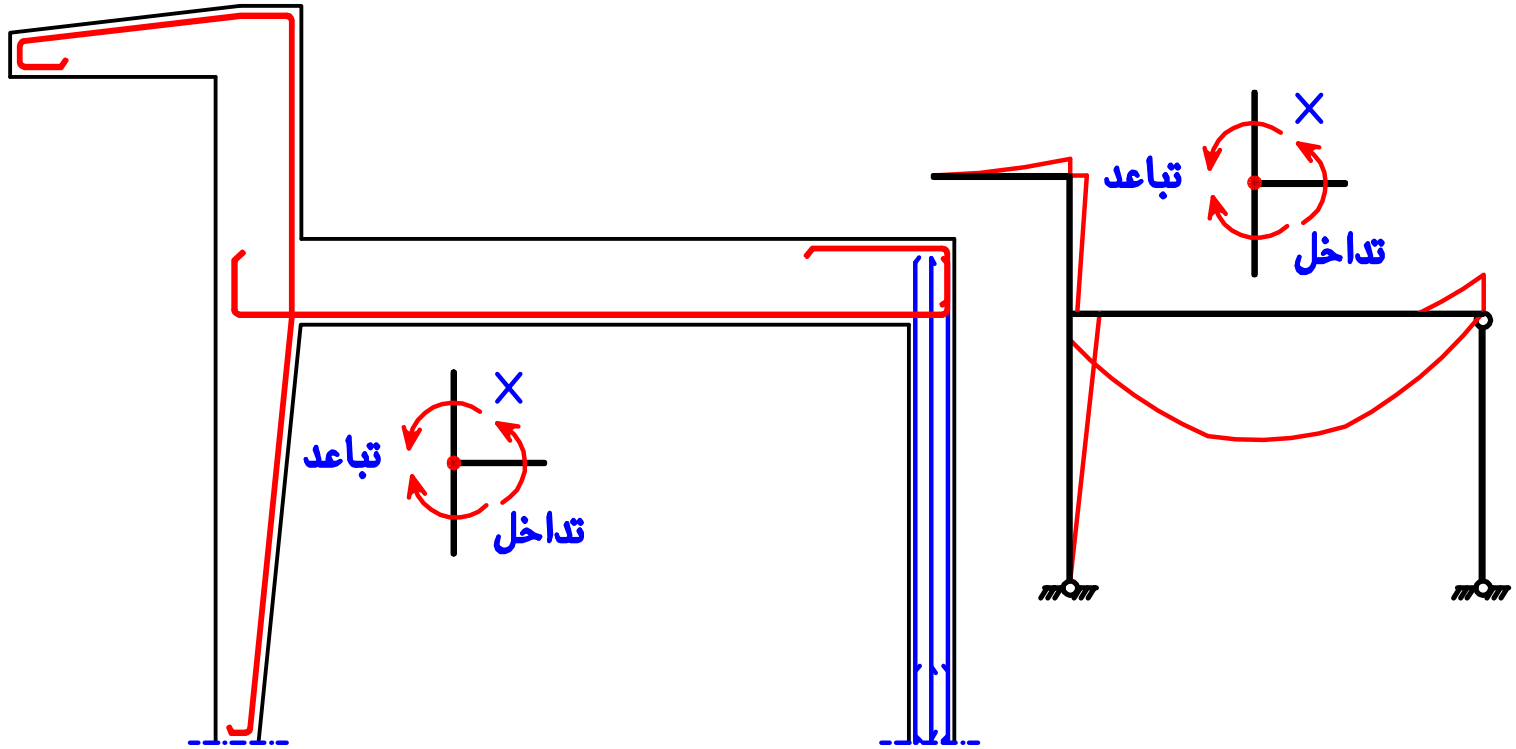
$$\therefore \text{Actual shear stress.} = q_v = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

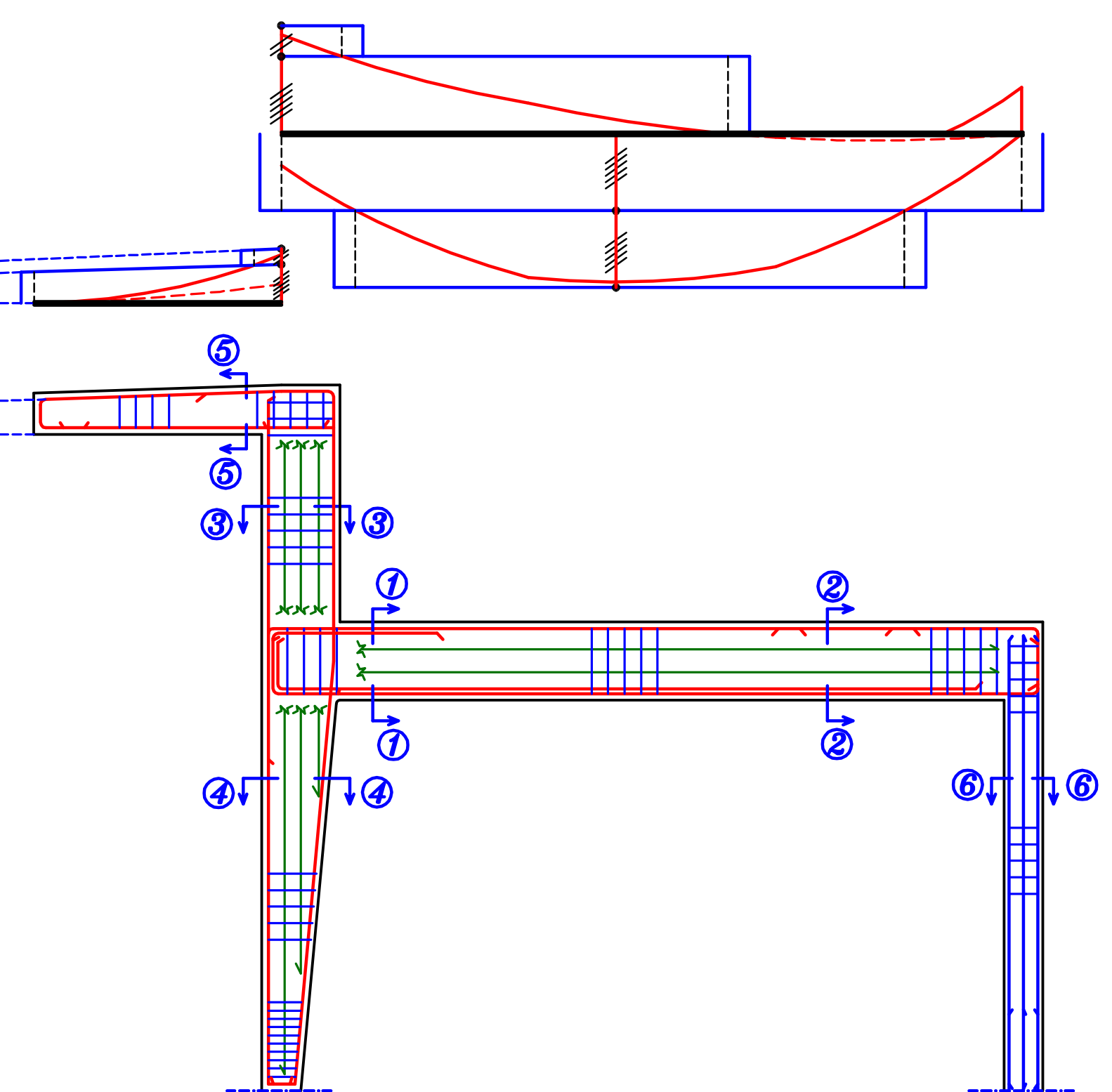
$$= \frac{75.0 * 10^3}{350 * 450} - \text{ZERO} = 0.47 \text{ N/mm}^2$$

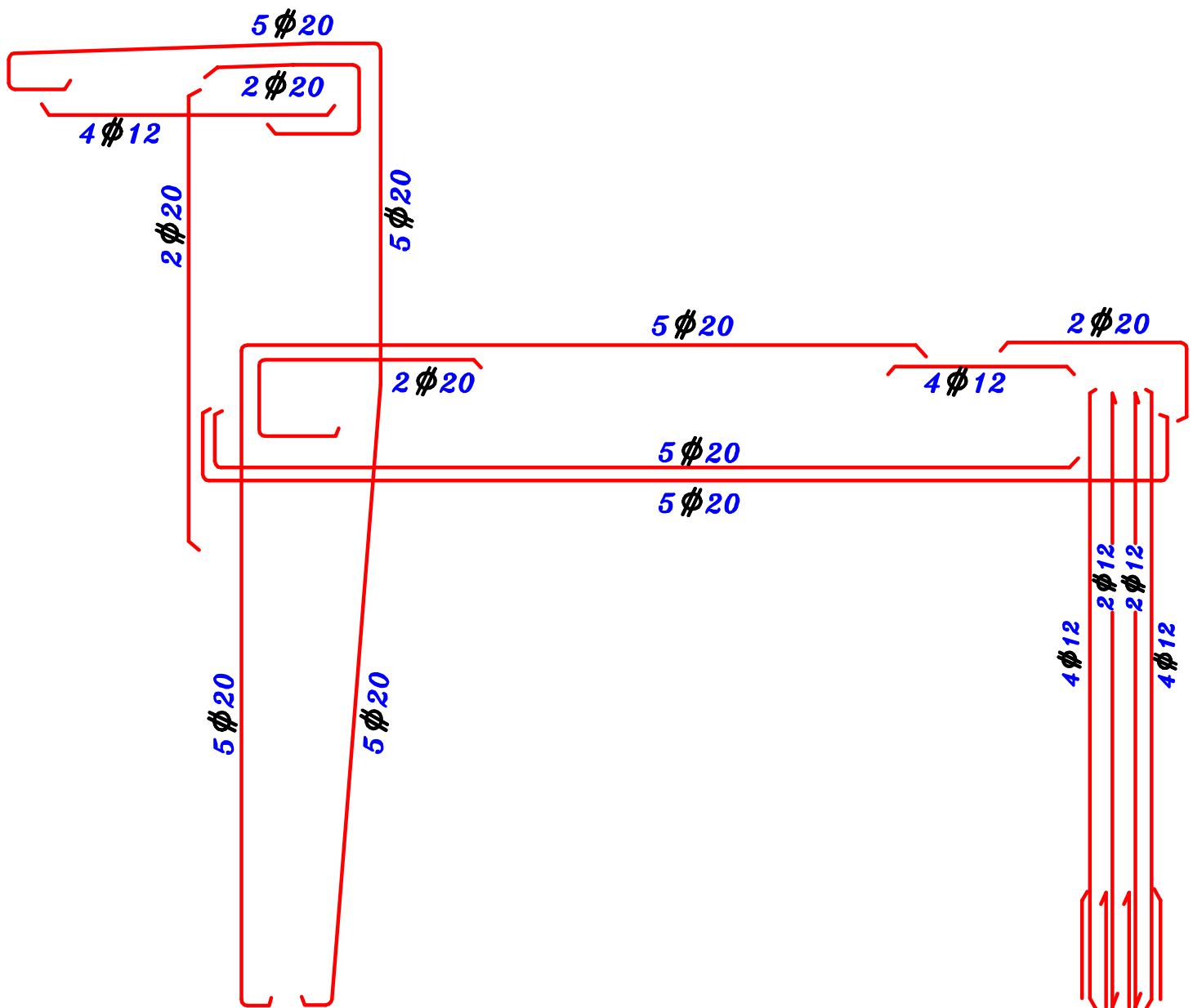
$$\therefore q_v < q_{cu} \longrightarrow \text{Use min. stirrups } \boxed{5 \phi 8 \setminus m}$$

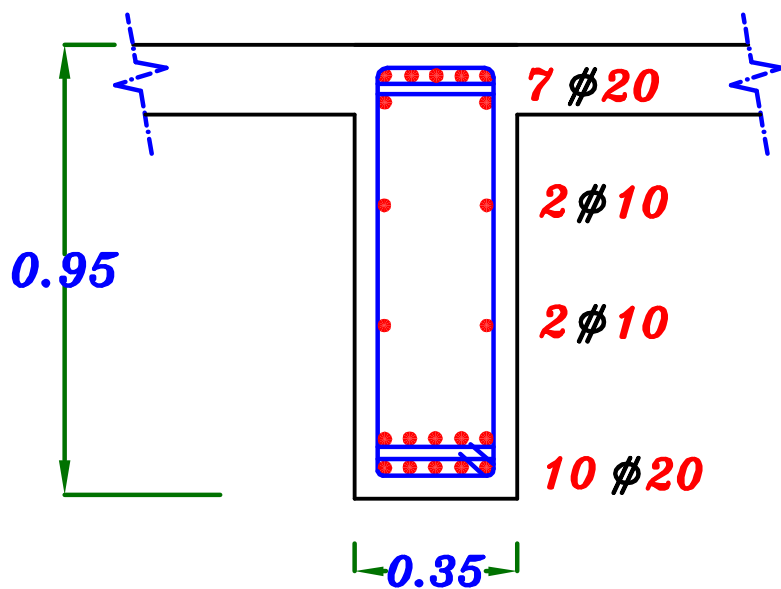


لا نرسم التسليح على شكل الـ *max-max B.M.D.* ولكن نرسم التسليح لى حاله تحميل أولا ثم نكمل التسليح من حاله التحميل الاخرى

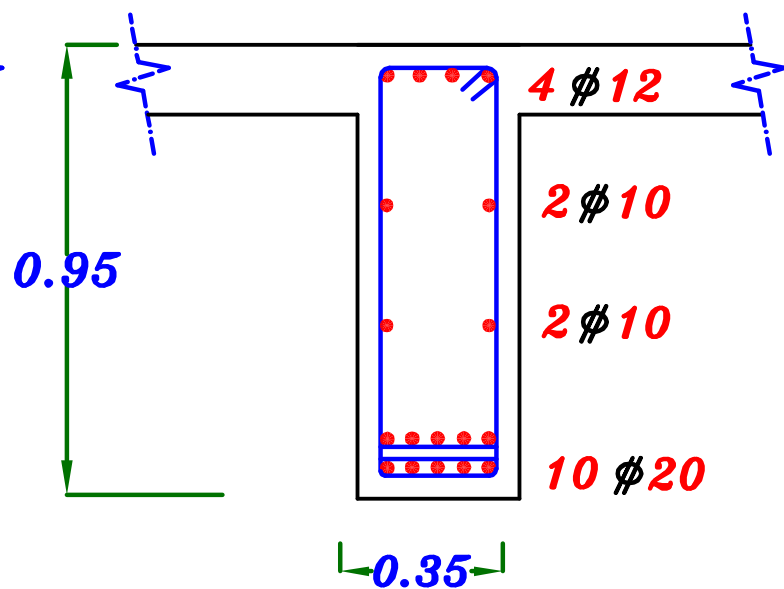




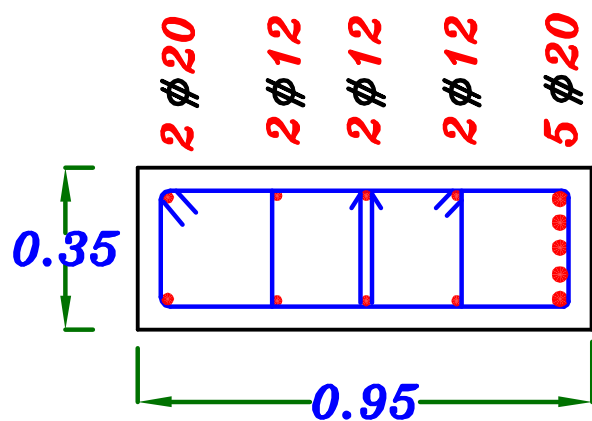




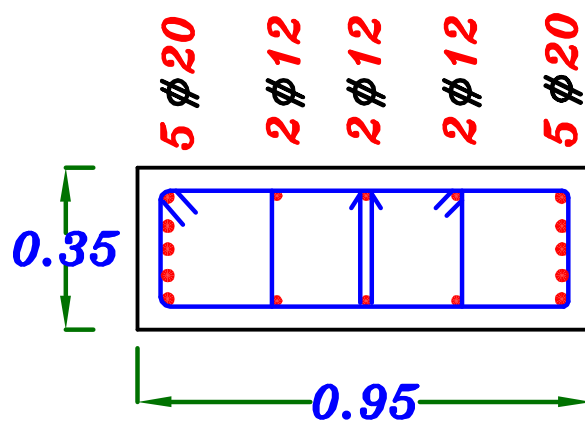
Sec. (1-1)



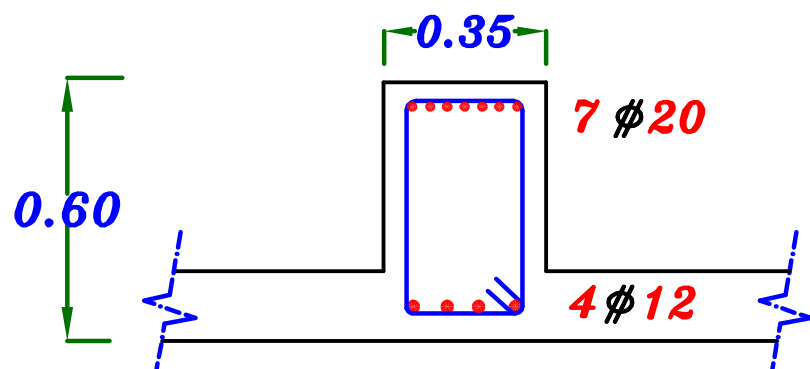
Sec. (2-2)



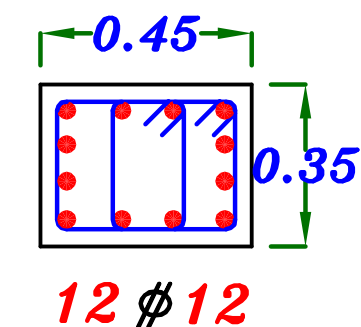
Sec. (3-3)



Sec. (4-4)

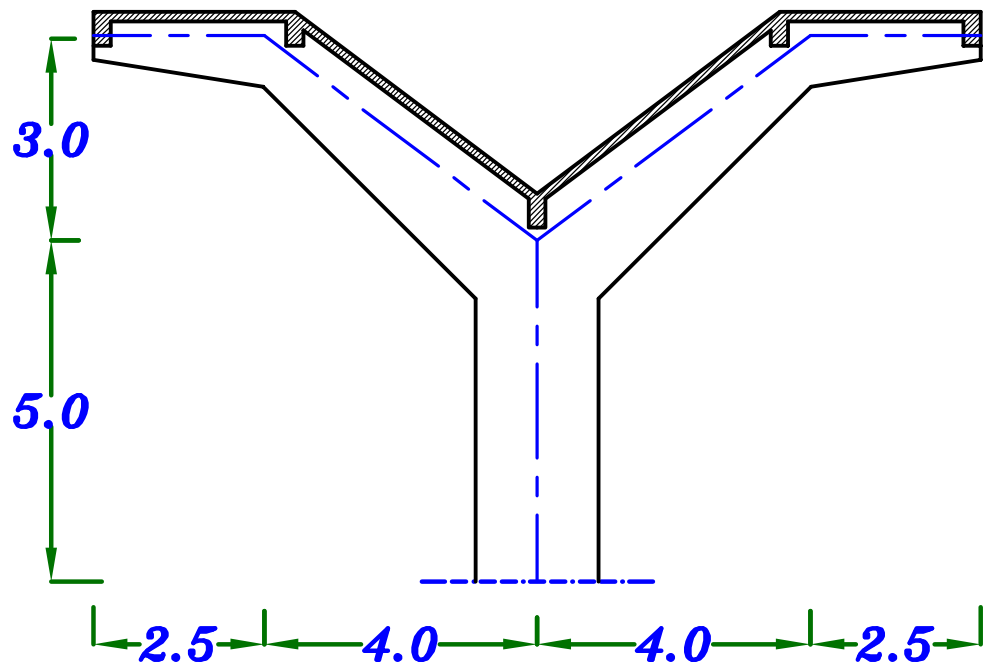


Sec. (5-5)



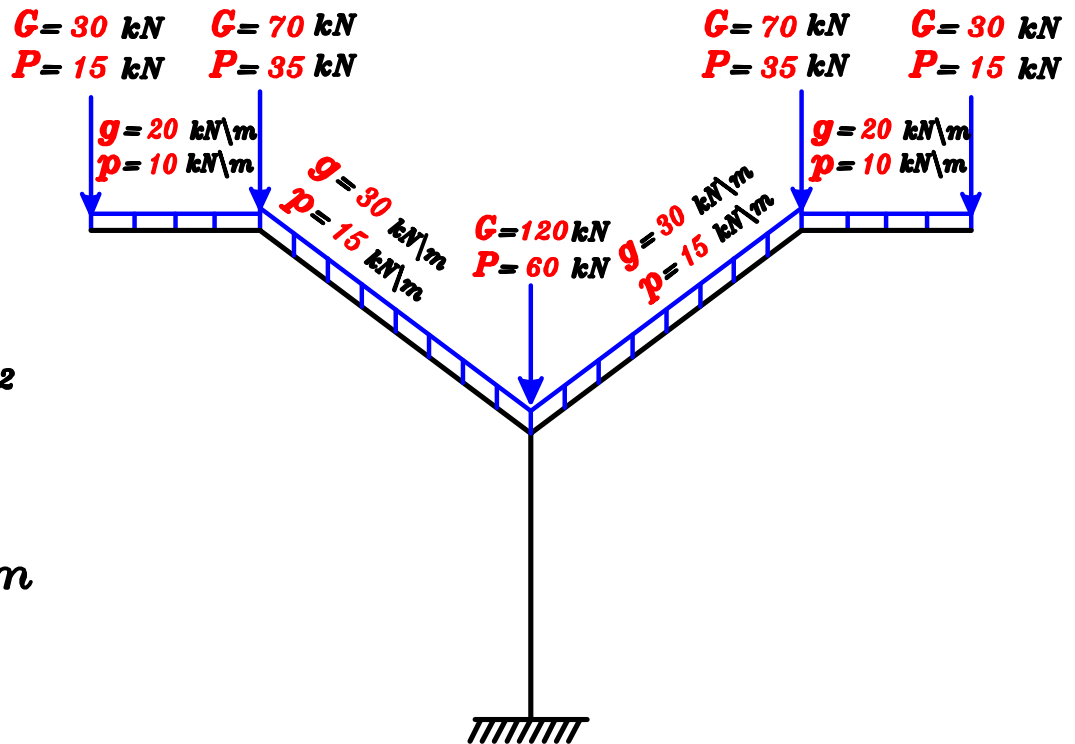
Sec. (6-6)

Example.



Data.

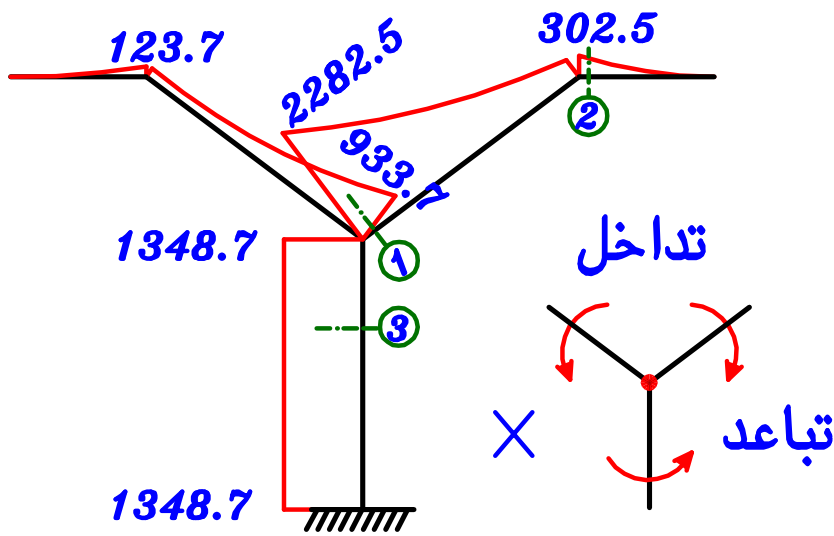
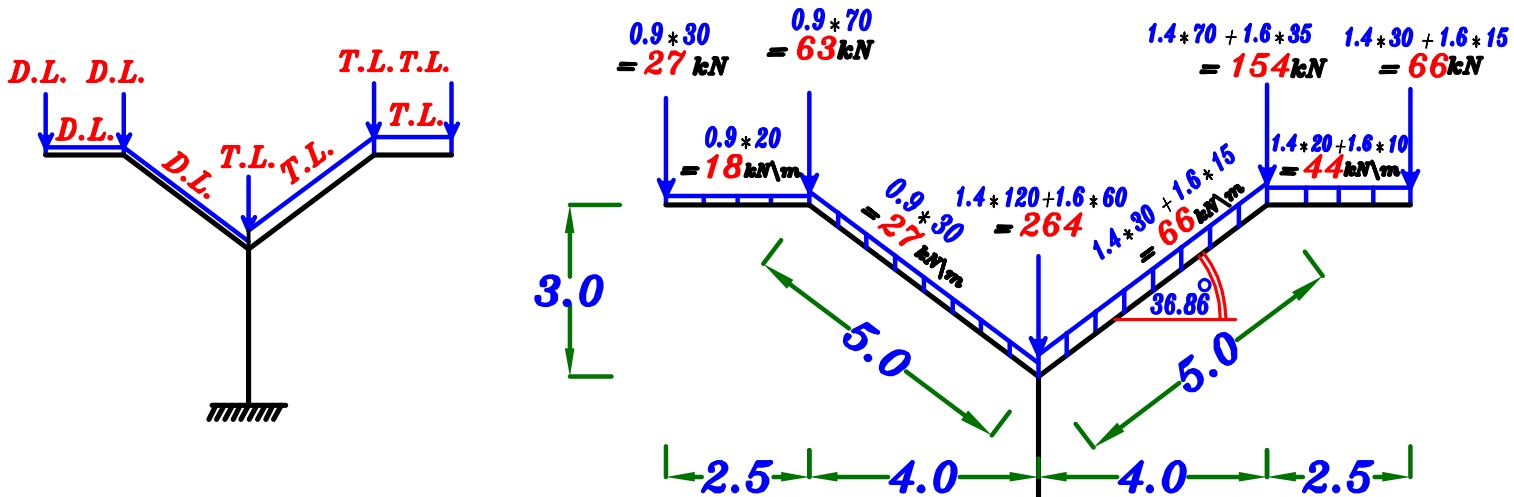
$$F_{cu} = 25 \text{ N/mm}^2$$
$$F_y = 360 \text{ N/mm}^2$$
$$t_s = 120 \text{ mm}$$
$$\text{Spacing} = 5.0 \text{ m}$$



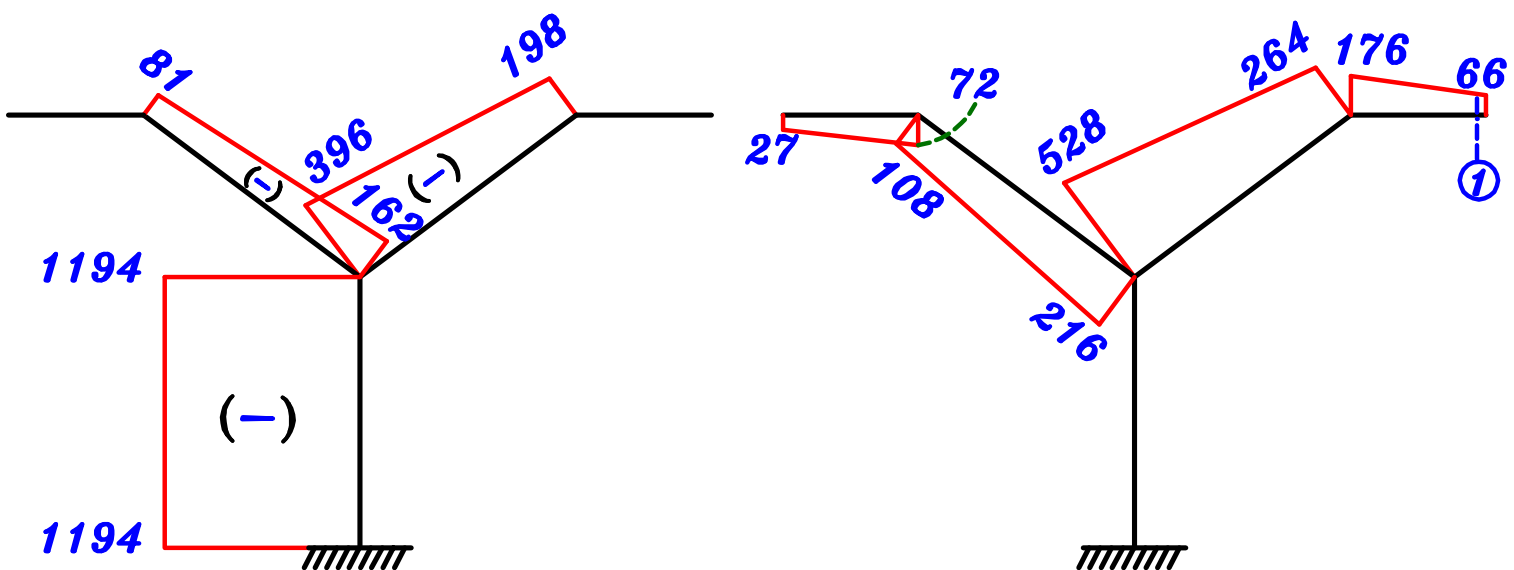
Req.

- ① Draw the Internal Forces Diagrams For the Frame due to the given working Loads. (**max-max I.F.D.**)
- ② Design the Frame.
using U.L. design method in bending.
- ③ Draw Details of RFT. For Frame. in elevation to scale **1:50** and cross-section to scale **1:10** making curtailment of steel using Moment of Resistance Method.

1- max (-ve) B.M.D.



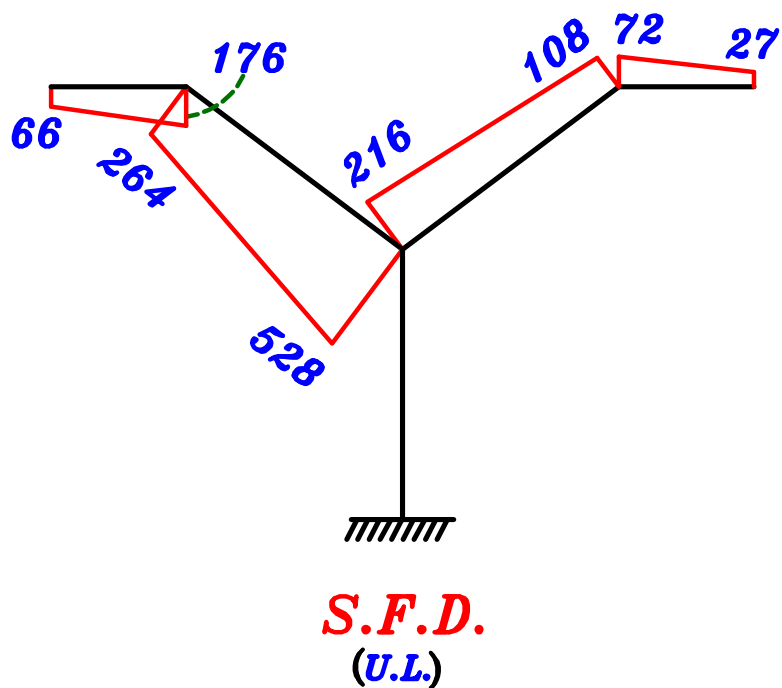
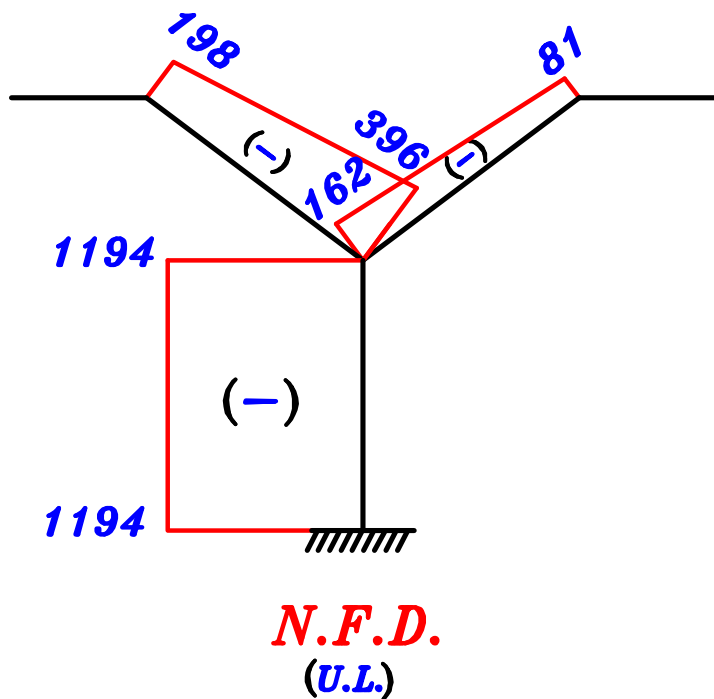
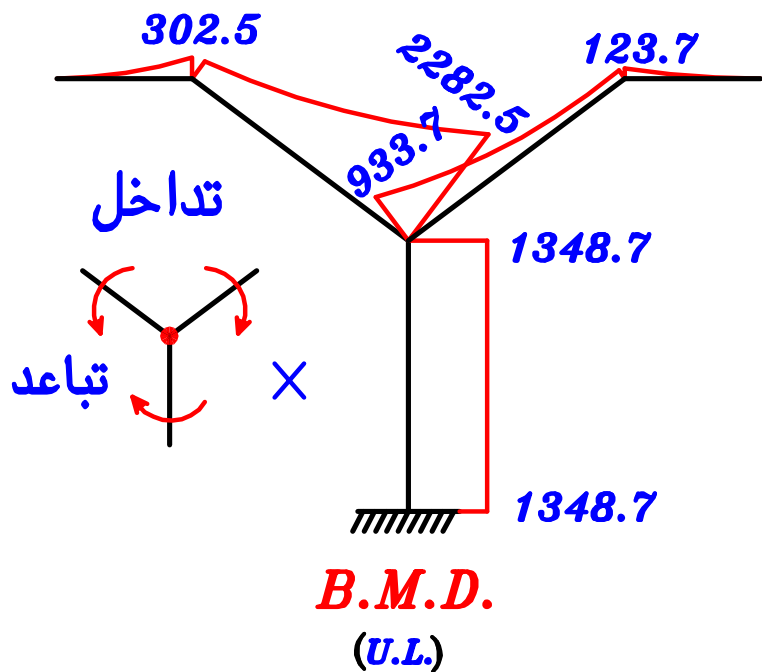
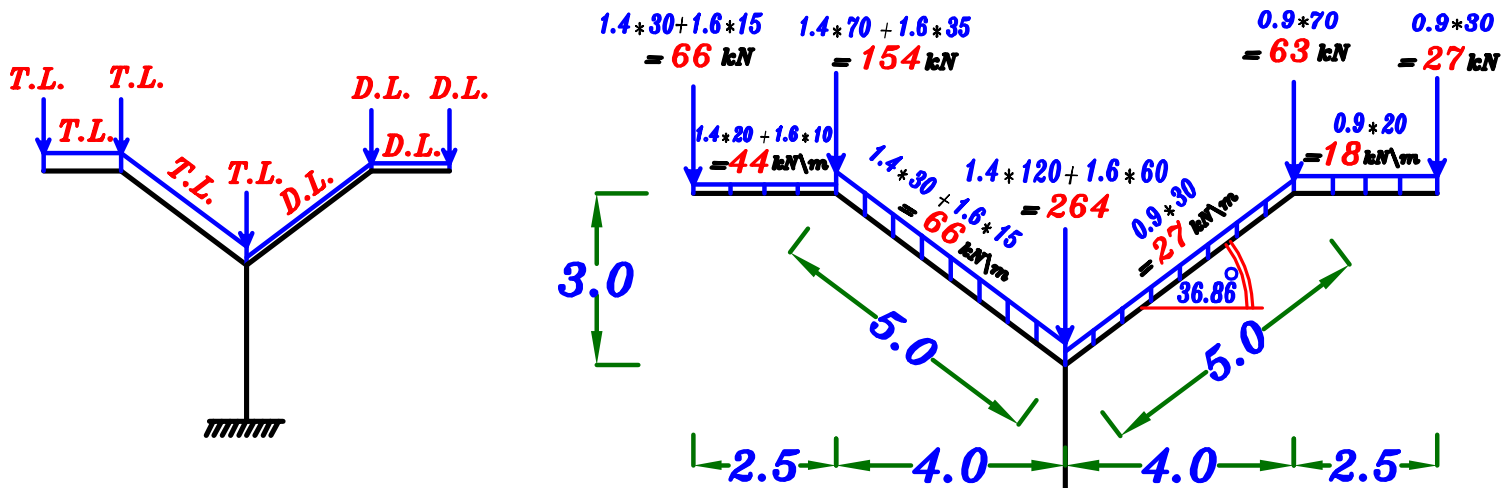
B.M.D.
(U.L.)



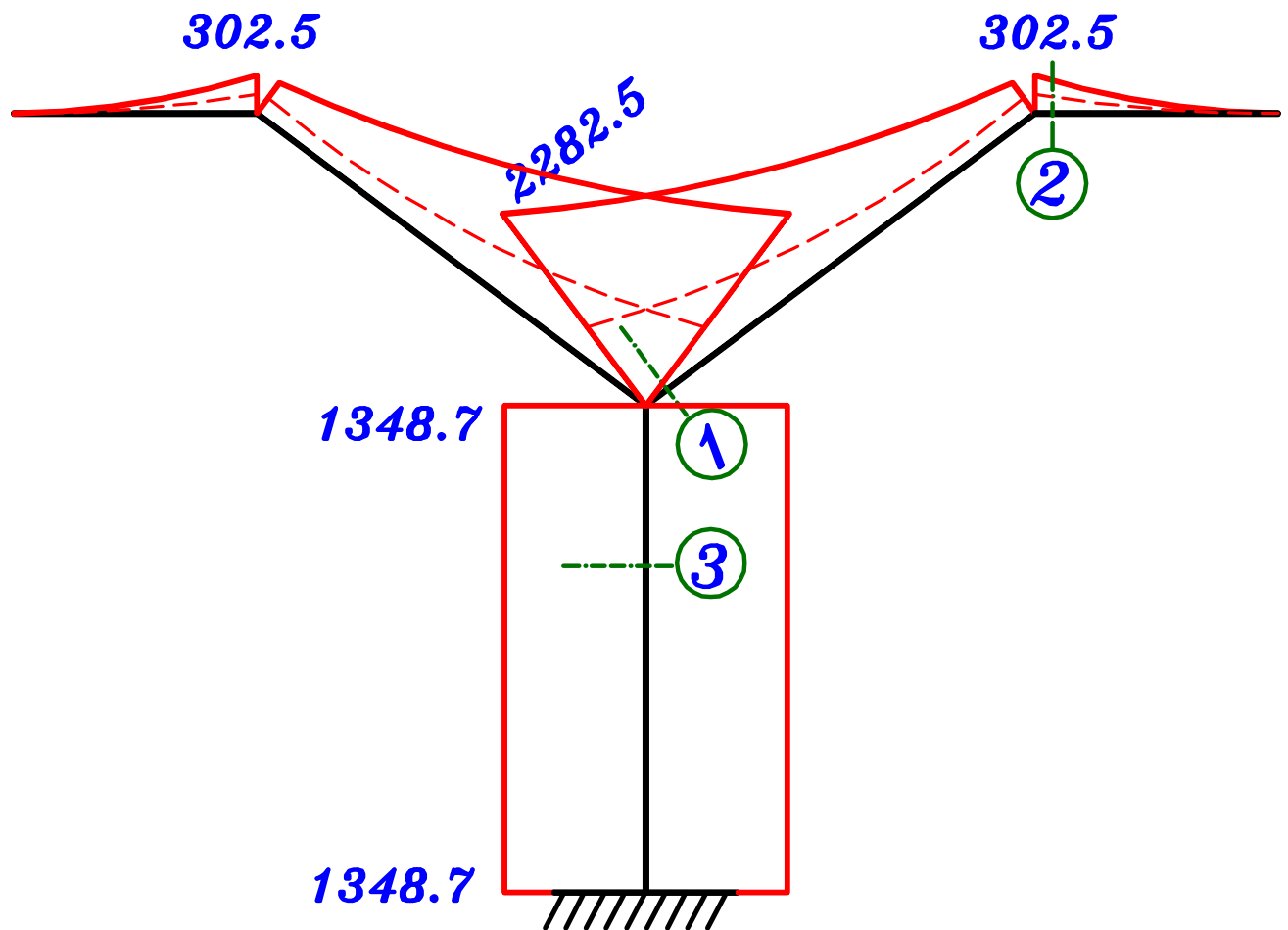
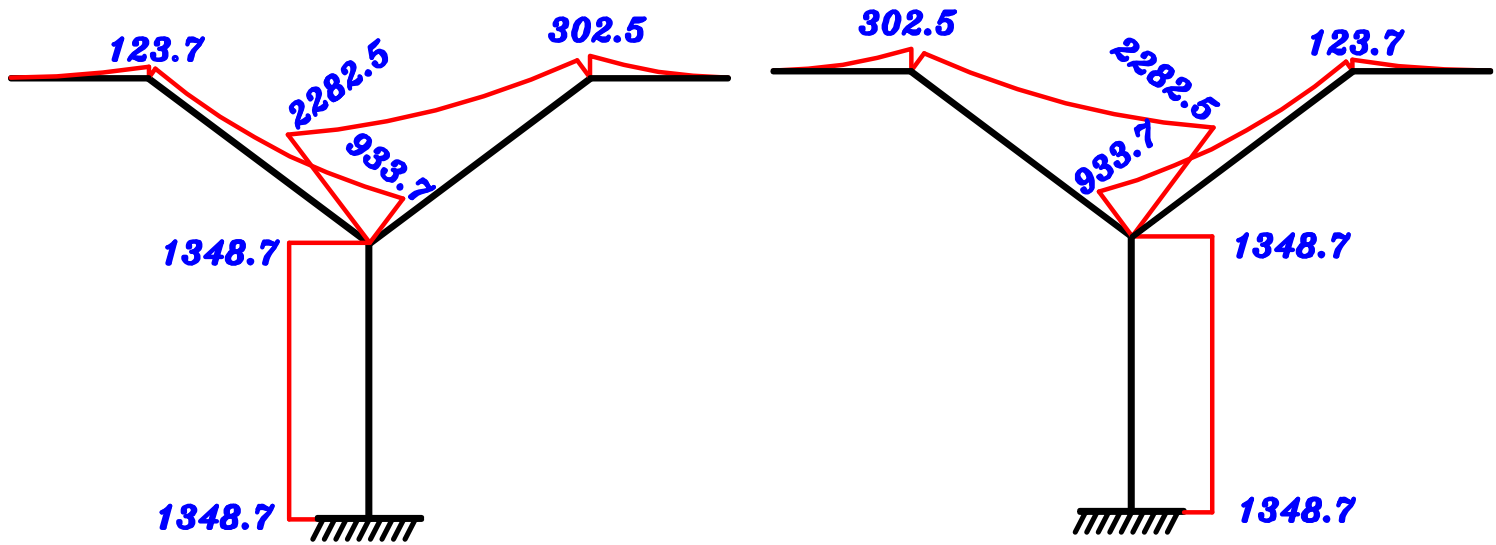
N.F.D.
(U.L.)

S.F.D.
(U.L.)

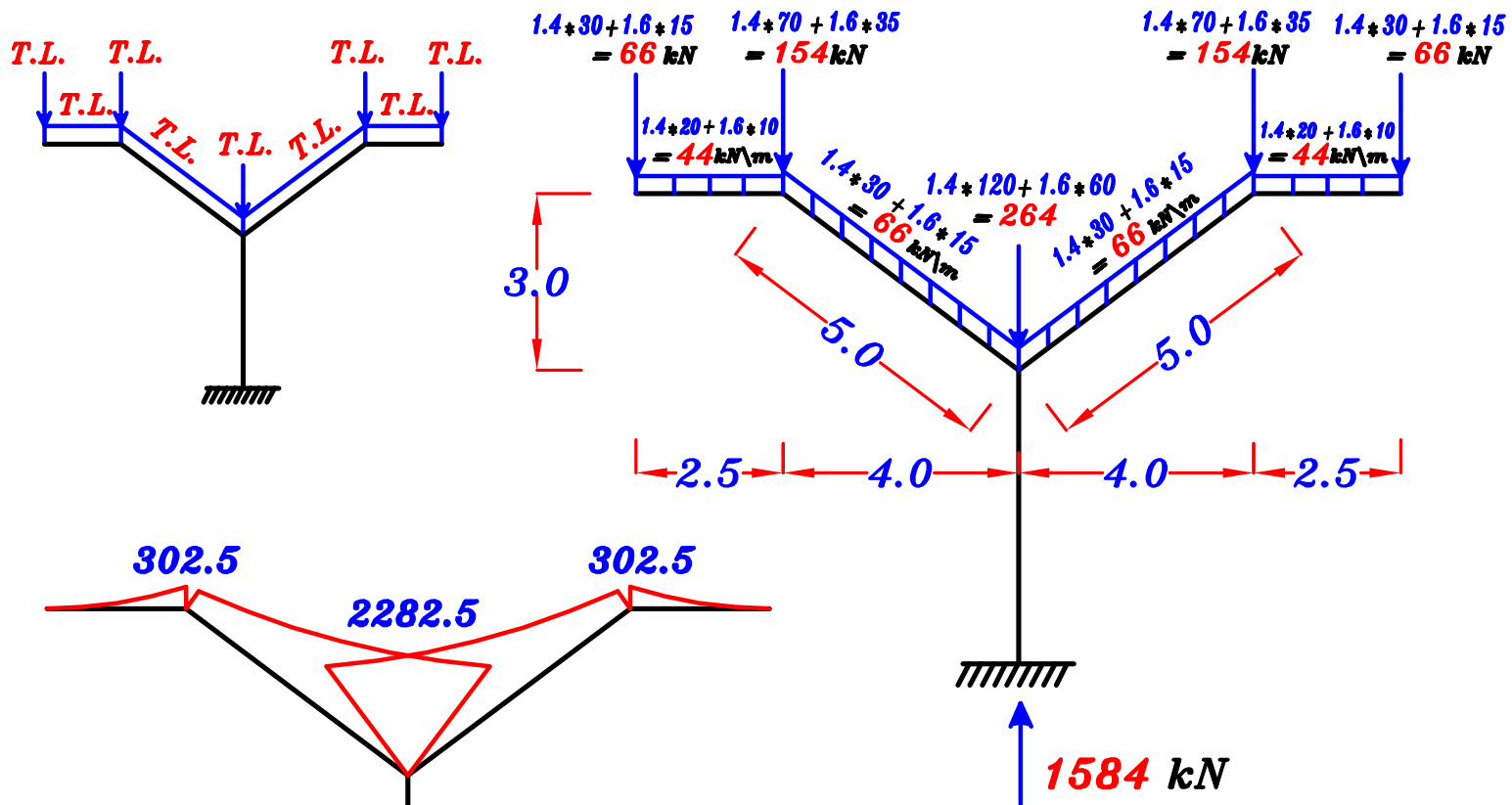
2- max (+ve) B.M.D.



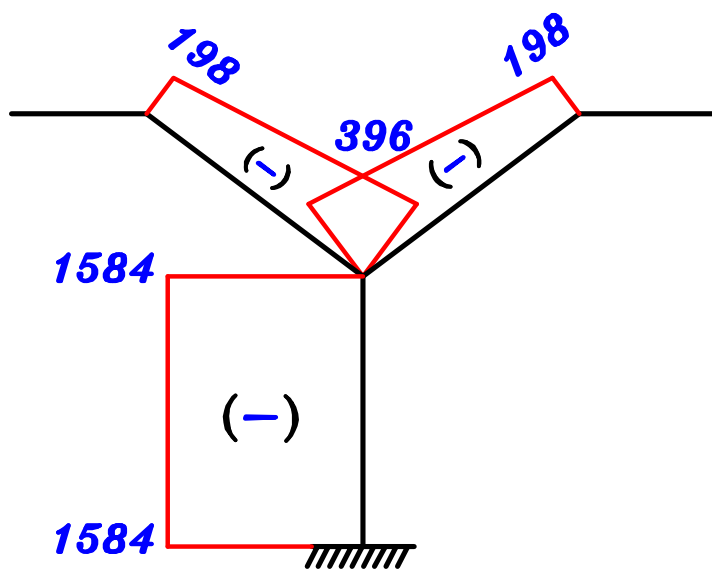
max-max B.M.D.



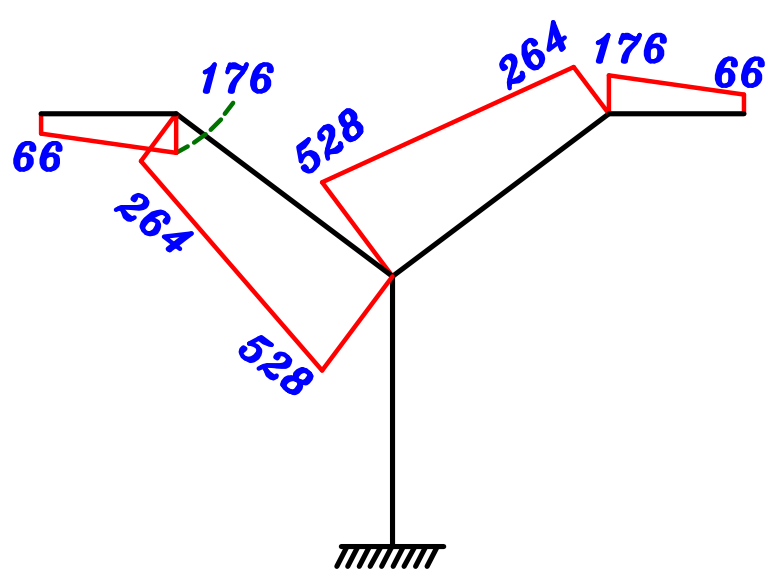
max N.F.D. (Not a critical case)



B.M.D.
(U.L.)



N.F.D.
(U.L.)



S.F.D.
(U.L.)

Design of Sections.

Sec. ① $M = 2282.5 \text{ kN.m}$, $P = 396 \text{ kN}$, $b = 400 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{2282.5 \cdot 10^6}{25 \cdot 400}} = 1672.1 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1672.1) = (1839.3 \rightarrow 2173) \text{ mm}$$

Take $d = 1900 \text{ mm}$, $t = 1900 + 100 = 2000 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{396 \cdot 10^3}{25 \cdot 400 \cdot 2000} = 0.0198 < 0.04 \therefore (\text{neglect } P)$

\therefore Take $d = d_o = 1672.1 \text{ mm}$

\therefore Take $d = 1700 \text{ mm}$, $t = 1800 \text{ mm}$

\therefore The sec. still R-sec. $C_1 = 3.50 \rightarrow J = 0.78$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{2282.5 \cdot 10^6}{0.780 \cdot 360 \cdot 1672.1} = 4861 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 4861 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 400 \cdot 1700 = 2125 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 4861 \text{ mm}^2$

$10 \phi 25$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$

Stirrup Hangers = $(0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 4861$ $5 \phi 12$

Sec. ② $M_{U.L.} = 302.5 \text{ kN.m}$ *R-Sec.*

Take $t = \frac{t_1}{2} = \frac{1.80}{2} = 0.90 \text{ m}$

\therefore Take $d = 850 \text{ mm}$, $t = 900 \text{ mm}$

$\therefore d = c_1 \sqrt{\frac{M_{U.L.}}{F_{cu} b}} \therefore 850 = c_1 \sqrt{\frac{302.5 \cdot 10^6}{25 \cdot 400}} \rightarrow c_1 = 4.88 \rightarrow J = 0.826$

$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{302.5 \cdot 10^6}{0.826 \cdot 360 \cdot 850} = 1196 \text{ mm}^2$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1196 \text{ mm}^2$

$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 400 \cdot 850 = 1062 \text{ mm}^2$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 1196 \text{ mm}^2$ $3 \phi 25$

$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$

Stirrup Hangers = $(0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 1196$ $2 \phi 12$

$Y = \left\{ \begin{array}{l} \frac{t}{2} = \frac{900}{2} = 450 \text{ mm} \\ t_b = \frac{\text{spacing}}{12} = \frac{5000}{12} = 416.6 \text{ mm} \\ t - \frac{L_c}{3} = 900 - \frac{2500}{3} = 66.6 \text{ mm} \end{array} \right\}$ $Y = 450 \text{ mm}$



Sec. ③ R-Sec. $M = 1348.7 \text{ kN.m}$, $P = 1194 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{1348.7 \cdot 10^6}{25 \cdot 400}} = 1285.3 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1285.3) = (1413.8 \rightarrow 1670.9) \text{ mm}$$

$$\therefore \text{Take } d = 1500 \text{ mm} , t = 1600 \text{ mm}$$

$$\xrightarrow{\text{Take}} t_{(\text{Column})} = t_{(\text{Beam})} = 1800 \text{ mm} \quad \text{للتسهيل}$$

$$\text{Check } \frac{P}{F_u b t} = \frac{1194 \cdot 10^3}{25 \cdot 400 \cdot 1800} = 0.066 > 0.04 \quad (\text{Don't neglect } P)$$

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{1348.7}{1194} = 1.129 \text{ m} \therefore \frac{e}{t} = \frac{1.129}{1.80} = 0.627 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.129 + \frac{1.80}{2} - 0.10 = 1.929 \text{ m}$$

$$M_s = P \cdot e_s = 1194 \cdot 1.929 = 2303.2 \text{ kN.m}$$

$$\therefore 1700 = C_1 \sqrt{\frac{2303.2 \cdot 10^6}{25 \cdot 400}} \rightarrow C_1 = 3.54 \rightarrow J = 0.783$$

$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \backslash \delta_s)}$$

$$= \frac{2303.2 \cdot 10^6}{0.783 \cdot 360 \cdot 1700} - \frac{1194 \cdot 10^3}{(360 \backslash 1.15)} = 992.2 \text{ mm}^2$$

$$\text{Check } A_{s_{\min.}} \quad A_{s_{\text{req.}}} = 992.2 \text{ mm}^2$$

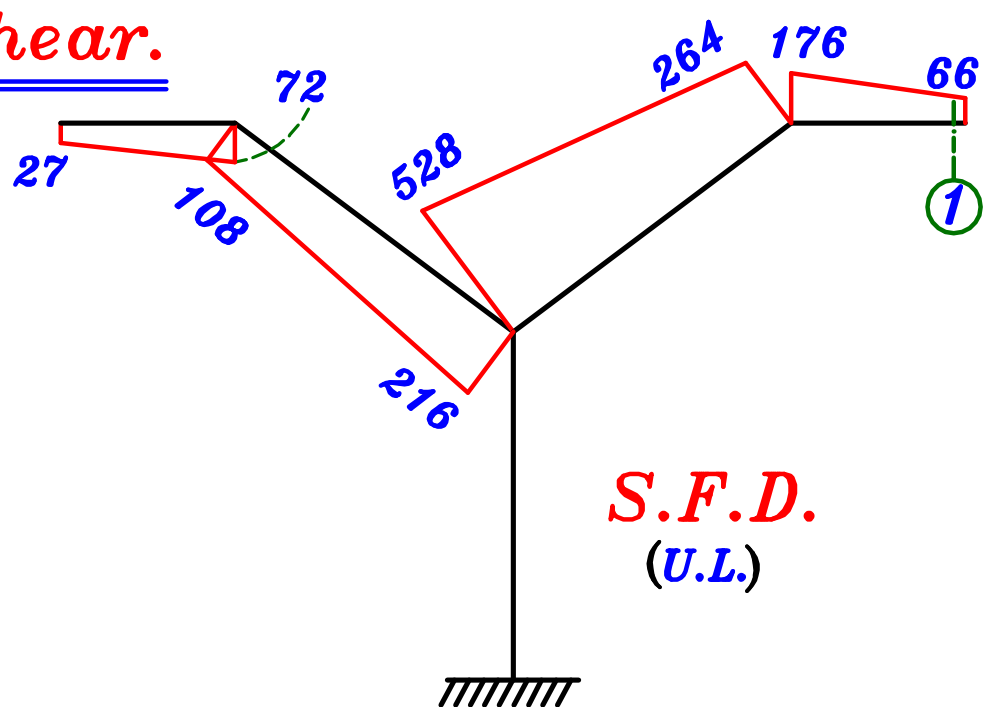
$$\mu_{\min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 400 \cdot 1700 = 2125 \text{ mm}^2$$

$$\therefore \mu_{\min.} b d > A_{s_{\text{req.}}} \xrightarrow{\text{Use}} A_{s_{\min.}}$$

$$A_{s_{\min.}} = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 400 \cdot 1700 = 2125 \text{ mm}^2 \quad \left. \vphantom{A_{s_{\min.}}} \right\} \text{الأقل}$$

$$1.3 A_{s_{\text{req.}}} = 1.3 \cdot 992.2 = 1289.9 \text{ mm}^2 \quad \left. \vphantom{1.3 A_{s_{\text{req.}}}} \right\} = 1289.9 \text{ mm}^2 \quad (4 \phi 25)$$

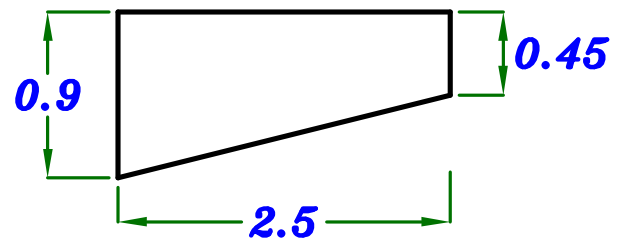
Check shear.



– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{25}{1.5}} = 2.85 \text{ N/mm}^2$$



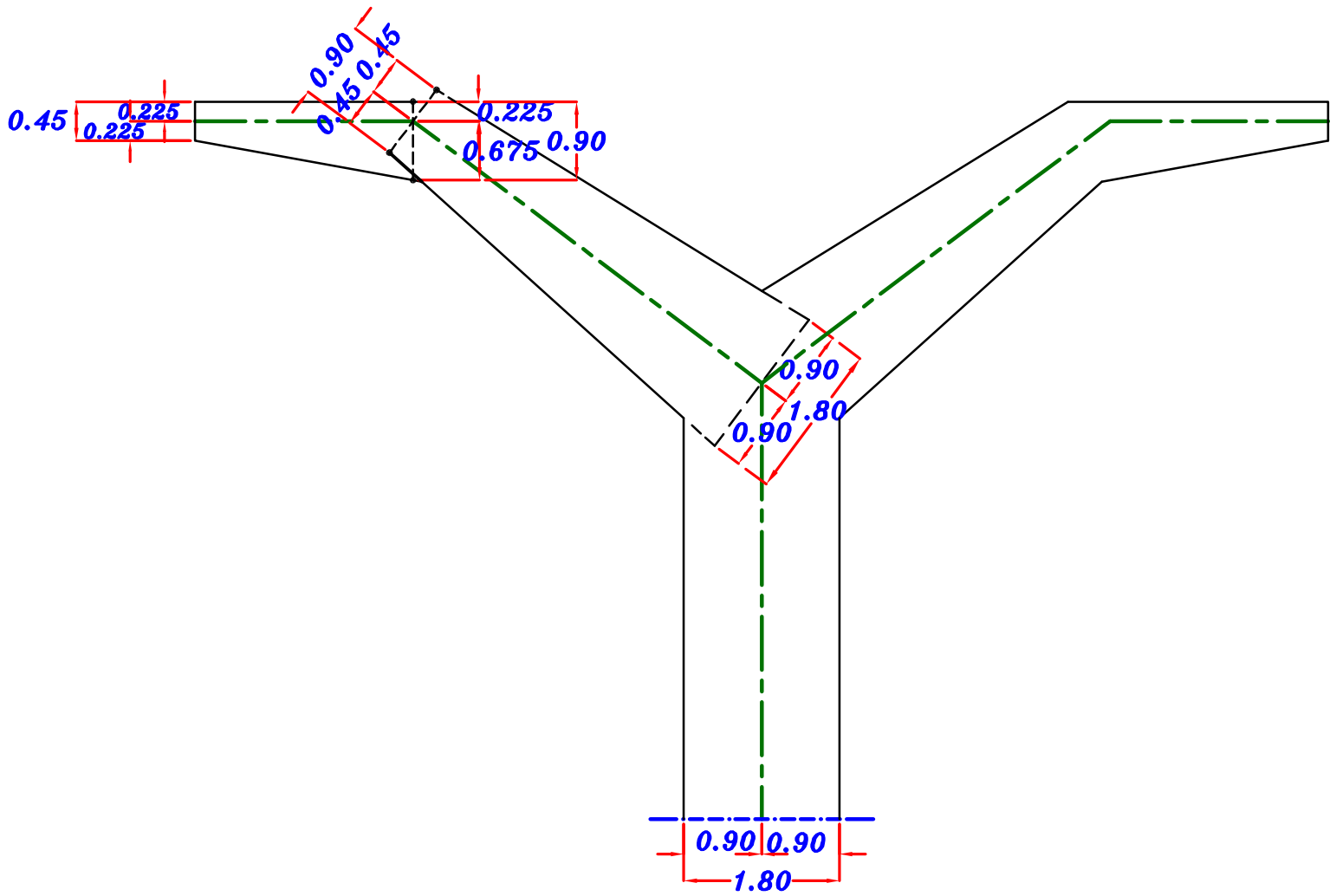
Sec. ① $Q = 66.0 \text{ kN}$ $\tan \beta = 0.18$

$$\therefore \text{Actual shear stress.} = q_U = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

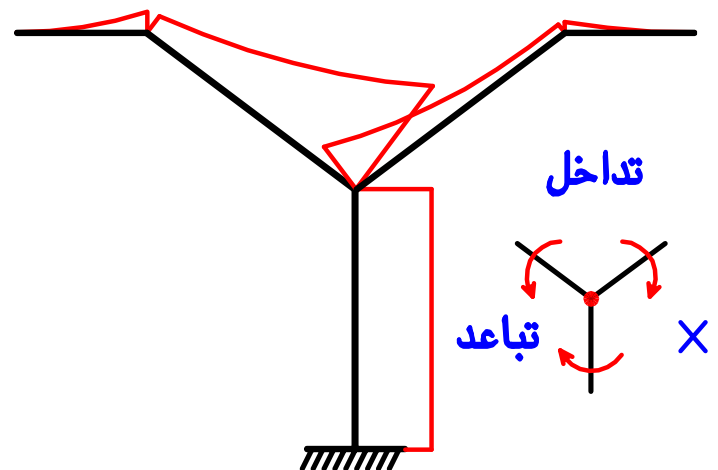
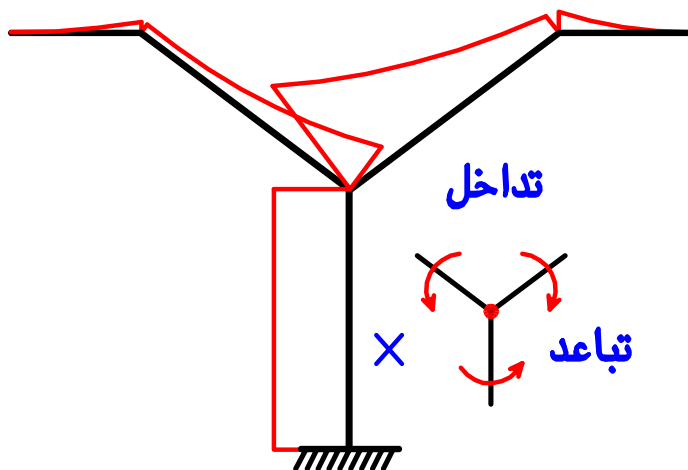
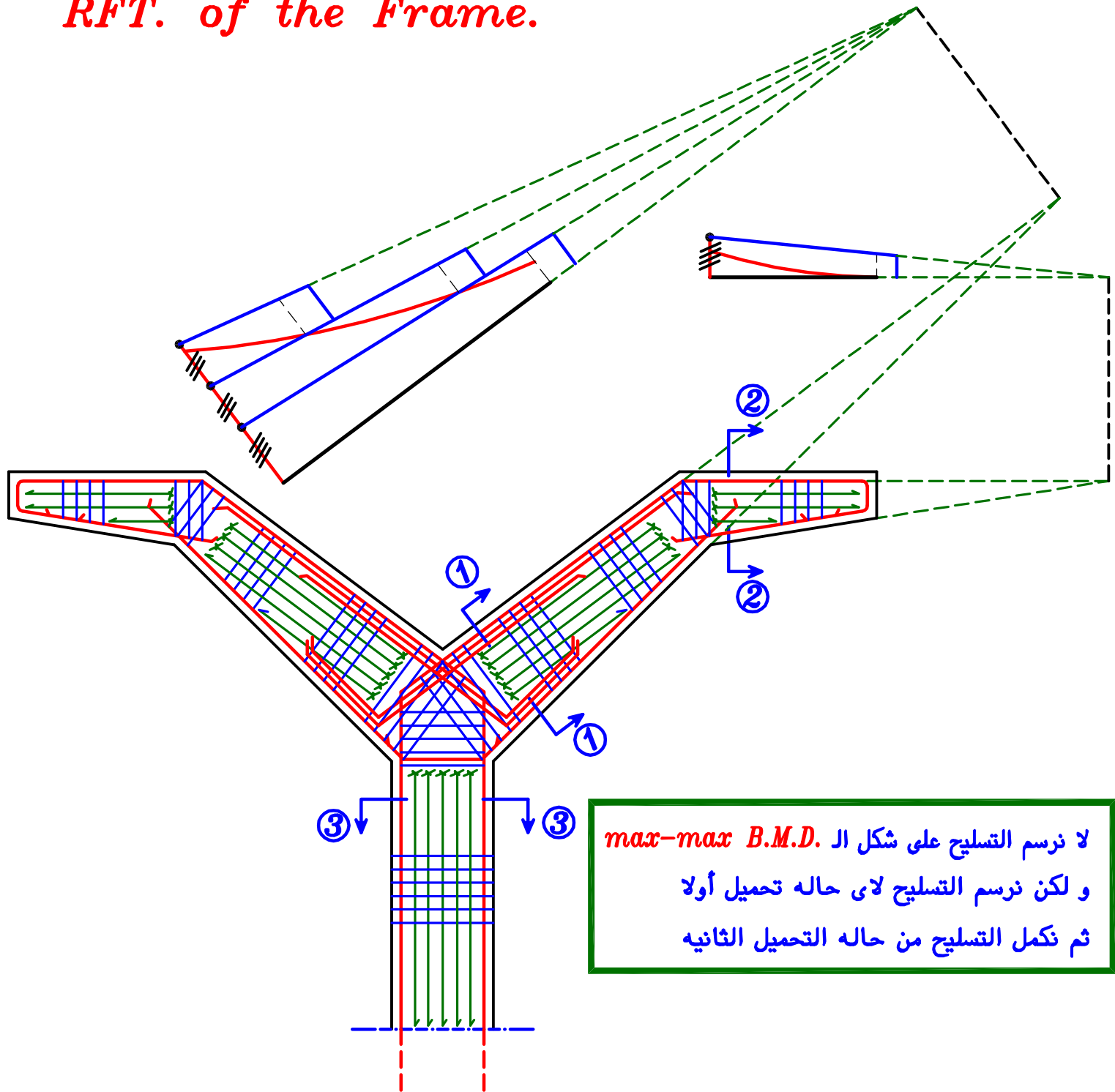
$$q_U = \frac{66.0 * 10^3}{400 * 400} - \text{ZERO} = 0.412 \text{ N/mm}^2$$

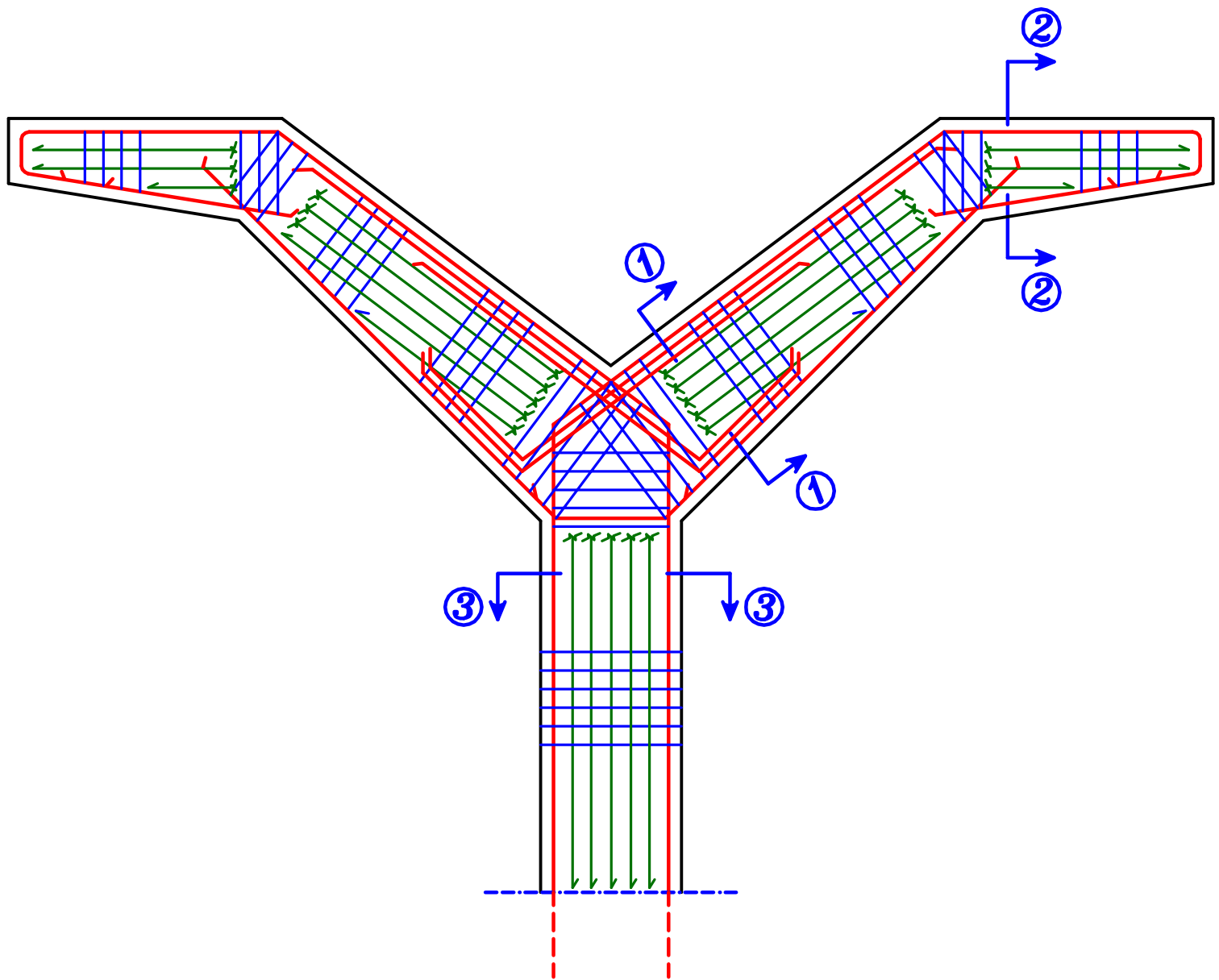
$$\therefore q_U < q_{cu} \longrightarrow \text{Use min. stirrups}$$

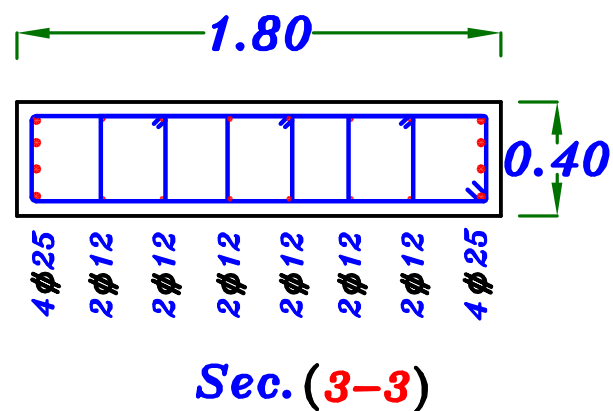
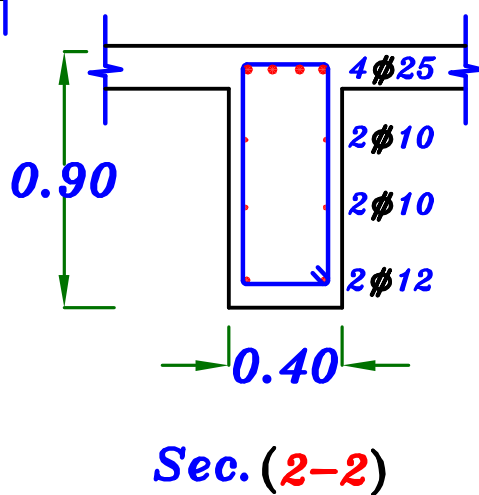
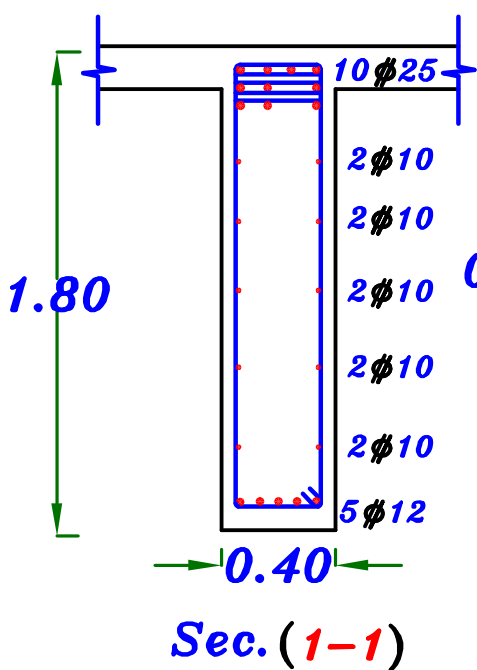
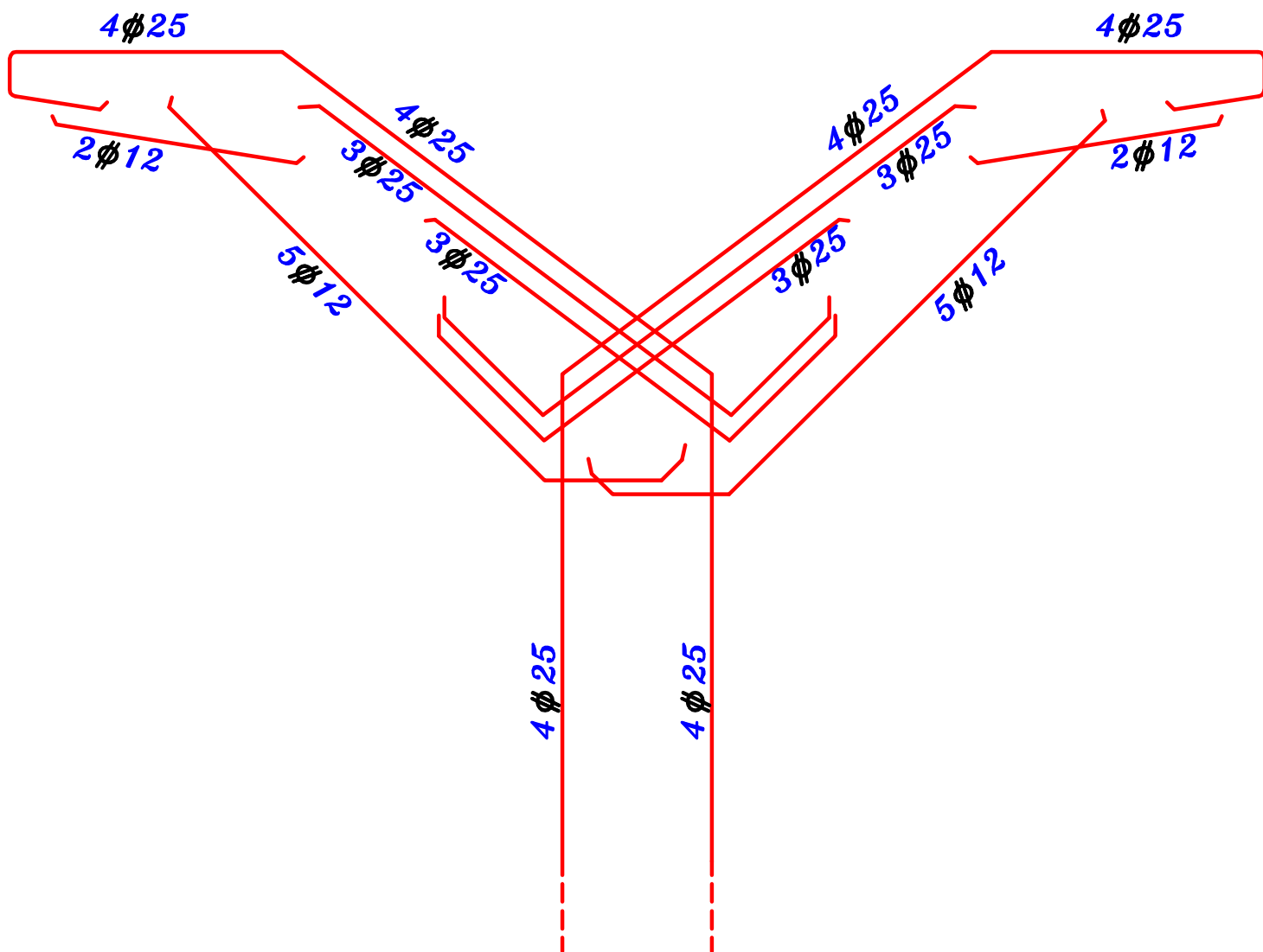
$$5 \phi 8 \text{ m'}$$



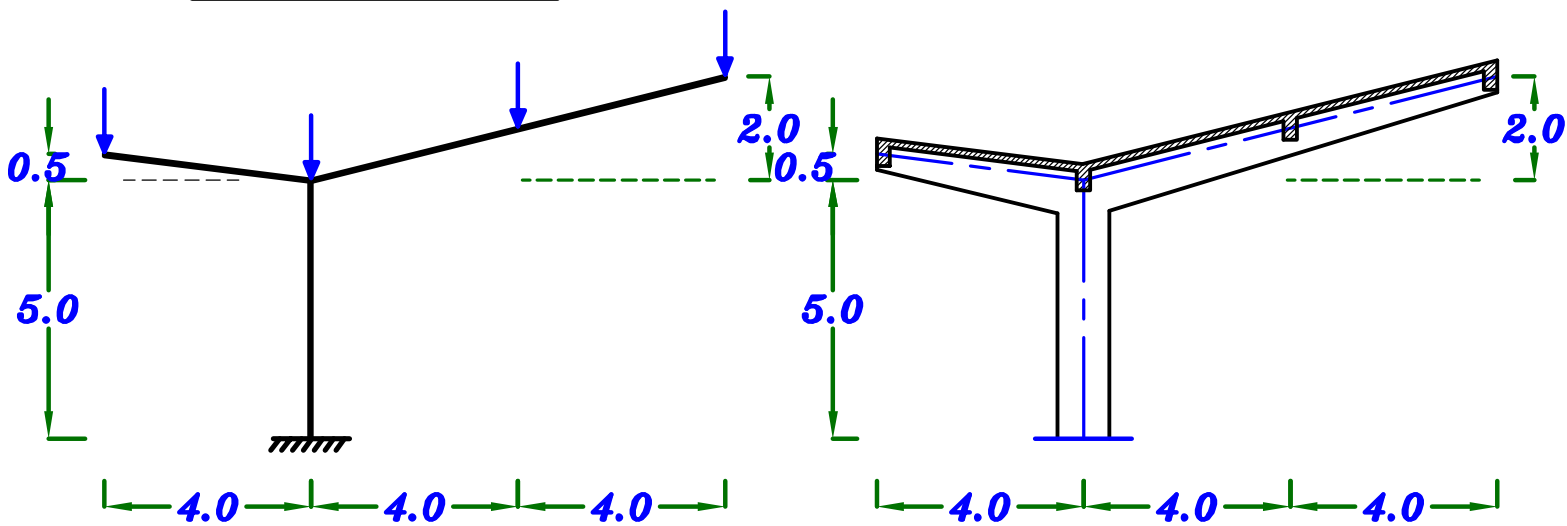
RFT. of the Frame.







Example.



Data.

$$F_{cu} = 30 \text{ N/mm}^2 \quad F_y = 400 \text{ N/mm}^2$$

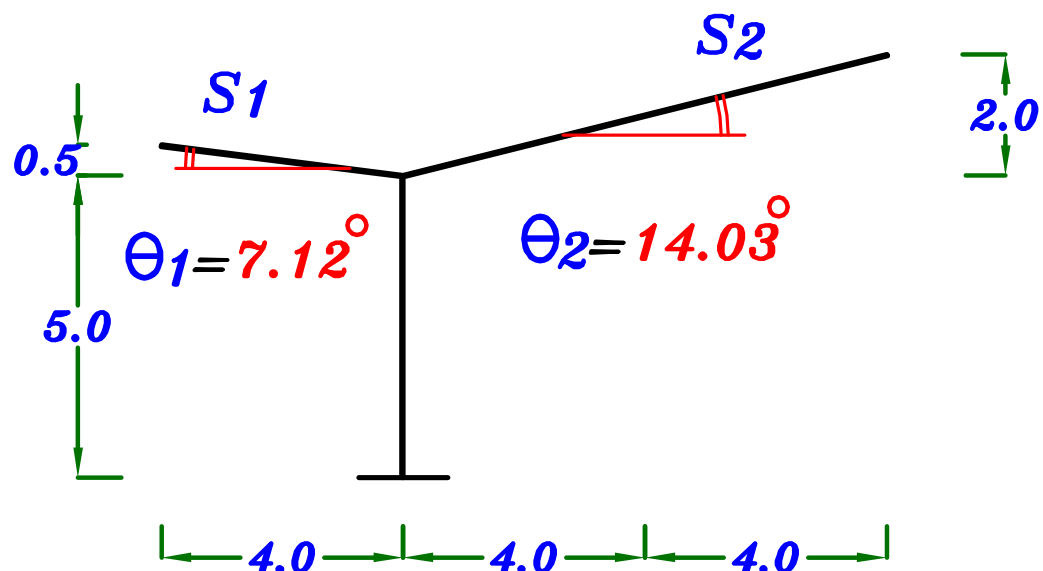
$$t_s = 140 \text{ mm} \quad L.L. = 1.50 \text{ kN/m}^2 \quad F.C. = 2.0 \text{ kN/m}^2$$

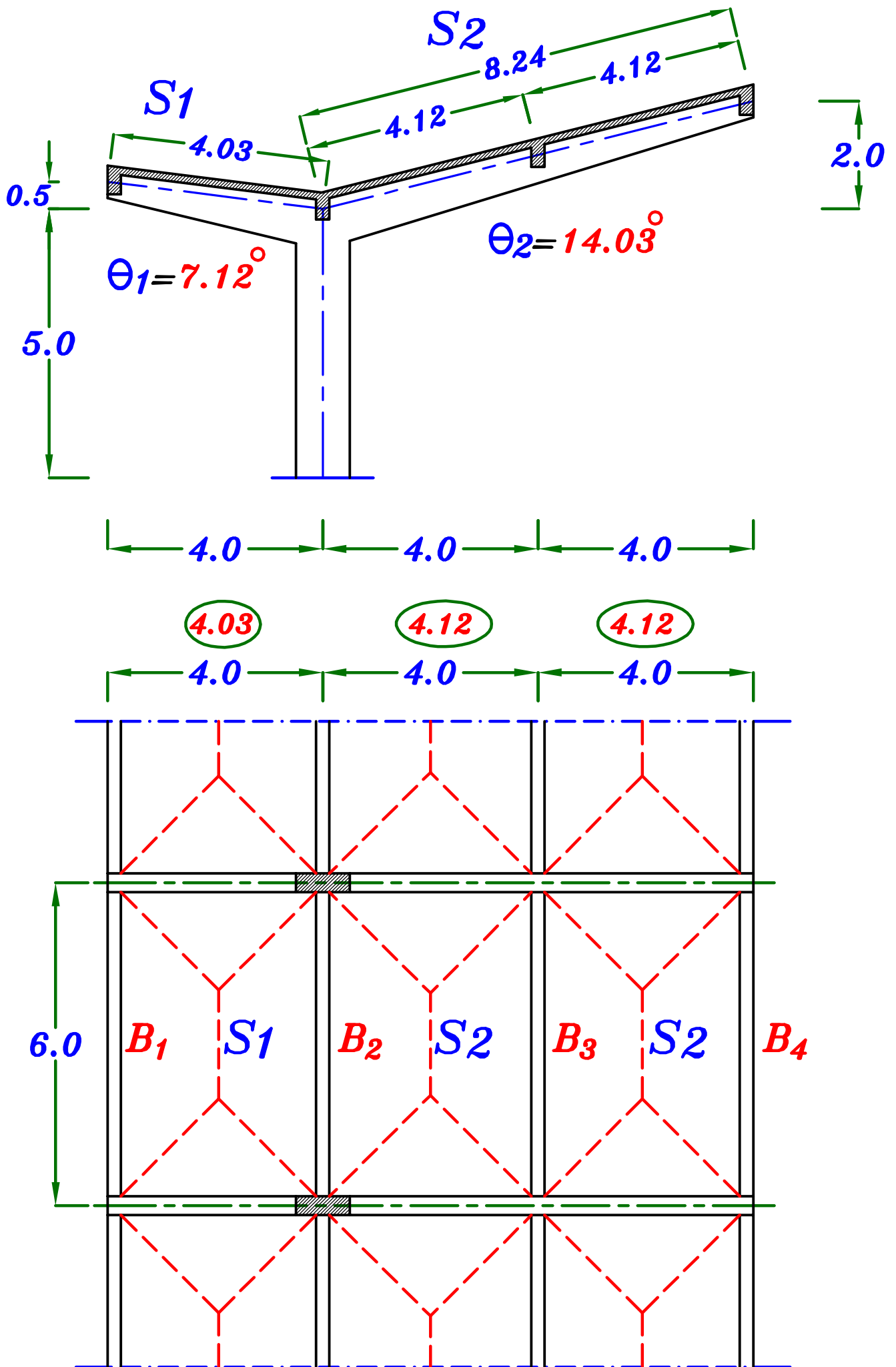
$$\text{Spacing} = 6.0 \text{ m}$$

Required.

- 1— Make Load distribution and draw max-max B.M.D. , N.F.D. & S.F.D.
- 2— Design the critical sections of the Frame.
- 3— Draw Details of RFT. of the Frame.

Solution.





g_s, p_s

$$g_s = t_s * \delta_c + F.C. = 0.14 * 25 + 2.0 = 5.50 \text{ kN/m}^2$$

$$p_{si1} = L.L. * \cos \theta = 1.5 * \cos 7.12^\circ = 1.49 \text{ kN/m}^2 \text{ ----- Slab } S_1$$

$$p_{si2} = L.L. * \cos \theta = 1.5 * \cos 14.03^\circ = 1.455 \text{ kN/m}^2 \text{ ----- Slab } S_2$$

B_1 Load For Shear.

$$\text{For Trapezoid 1 } C_{a1} = 1 - \frac{1}{2} \left(\frac{L_s}{L} \right) = 1 - \frac{1}{2} \left(\frac{4.03}{6.0} \right) = 0.664$$

$$g_a = 0.W. + C_{a1} g_s \frac{L_s}{2} = 3.0 + (0.664) (5.50) \left(\frac{4.03}{2} \right) = 10.35 \text{ kN/m}$$

$$p_a = C_{a1} p_{si1} \frac{L_s}{2} = (0.664) (1.49) \left(\frac{4.03}{2} \right) = 2.0 \text{ kN/m}$$

$$w_a = g_a + p_a = 10.35 + 2.0 = 12.35 \text{ kN/m}$$

$$R_1 = g_a * \text{Spacing} = 10.35 * 6.0 = 62.1 \text{ kN} \text{ ----- D.L.}$$

$$= w_a * \text{Spacing} = 12.35 * 6.0 = 74.1 \text{ kN} \text{ ----- T.L.}$$

$$R_1 = 62.1 \text{ kN} \text{ ----- D.L.}$$
$$= 74.1 \text{ kN} \text{ ----- T.L.}$$

B_2 Load For Shear. $C_{a1} = 0.664$

$$\text{For Trapezoid 2 } C_{a2} = 1 - \frac{1}{2} \left(\frac{L_s}{L} \right) = 1 - \frac{1}{2} \left(\frac{4.12}{6.0} \right) = 0.656$$

$$g_a = 0.W. + C_{a1} g_s \frac{L_s}{2} + C_{a2} g_s \frac{L_s}{2}$$

$$= 3.0 + (0.664) (5.50) \left(\frac{4.03}{2} \right) + (0.656) (5.50) \left(\frac{4.12}{2} \right) = 17.79 \text{ kN/m}$$

$$p_a = C_{a1} p_{si1} \frac{L_s}{2} + C_{a2} p_{si2} \frac{L_s}{2} = (0.664) (1.49) \left(\frac{4.03}{2} \right) + (0.656) (1.455) \left(\frac{4.12}{2} \right) = 3.96 \text{ kN/m}$$

$$w_a = g_a + p_a = 17.79 + 3.96 = 21.75 \text{ kN/m}$$

$$R_2 = g_a * \text{Spacing} = 17.79 * 6.0 = 106.74 \text{ kN} \text{ ----- D.L.}$$

$$= w_a * \text{Spacing} = 21.75 * 6.0 = 130.5 \text{ kN} \text{ ----- T.L.}$$

$$R_2 = 106.74 \text{ kN} \text{ ----- D.L.}$$
$$= 130.5 \text{ kN} \text{ ----- T.L.}$$

B₃ Load For Shear.

For Trapezoid 2 $C_{a2} = 0.656$

$$g_a = 0.W. + 2C_{a2}g_s \frac{L_s}{2} = 3.0 + 2(0.656)(5.50)\left(\frac{4.12}{2}\right) = 17.86 \text{ kN/m}$$

$$p_a = 2C_{a2}p_{si2} \frac{L_s}{2} = 2(0.656)(1.455)\left(\frac{4.12}{2}\right) = 3.93 \text{ kN/m}$$

$$w_a = g_a + p_a = 17.86 + 3.93 = 21.79 \text{ kN/m}$$

$$R_3 = g_a * \text{Spacing} = 17.86 * 6.0 = 107.16 \text{ kN} \text{ ----- D.L.}$$

$$= w_a * \text{Spacing} = 21.79 * 6.0 = 130.74 \text{ kN} \text{ ----- T.L.}$$

$$\begin{aligned} R_3 &= 107.16 \text{ kN} \text{ --- D.L.} \\ &= 130.74 \text{ kN} \text{ --- T.L.} \end{aligned}$$

B₄ Load For Shear.

For Trapezoid 2 $C_{a2} = 0.656$

$$g_a = 0.W. + C_{a2}g_s \frac{L_s}{2} = 3.0 + (0.656)(5.50)\left(\frac{4.12}{2}\right) = 10.43 \text{ kN/m}$$

$$p_a = C_{a2}p_{si2} \frac{L_s}{2} = (0.656)(1.455)\left(\frac{4.12}{2}\right) = 1.96 \text{ kN/m}$$

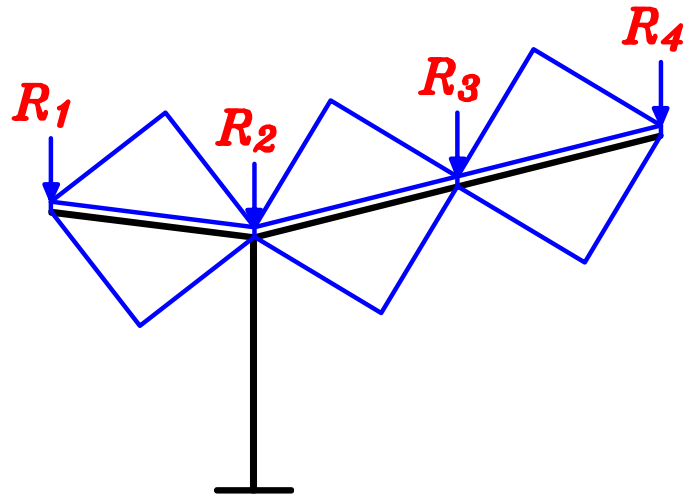
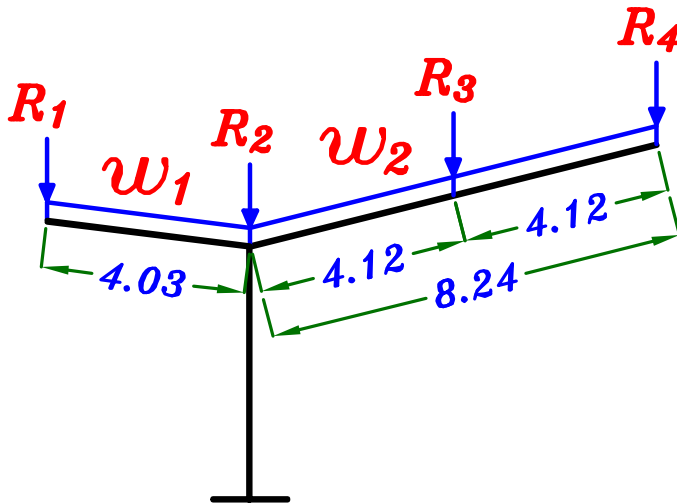
$$w_a = g_a + p_a = 10.43 + 1.96 = 12.39 \text{ kN/m}$$

$$R_4 = g_a * \text{Spacing} = 10.43 * 6.0 = 62.58 \text{ kN} \text{ ----- D.L.}$$

$$= w_a * \text{Spacing} = 12.39 * 6.0 = 74.34 \text{ kN} \text{ ----- T.L.}$$

$$\begin{aligned} R_4 &= 62.58 \text{ kN} \text{ --- D.L.} \\ &= 74.34 \text{ kN} \text{ --- T.L.} \end{aligned}$$

Loads on the Frame.



$$\underline{\underline{(w_1)}} \quad \frac{\sum \text{area}}{\text{span}} = \frac{2 \left(\frac{1}{2} (4.03) \left(\frac{4.03}{2} \right) \right)}{4.03} = 2.015$$

$$g_1 = g_a = g_e = o.w. + \frac{\sum \text{area}}{\text{span}} * g_s = 6.0 + 2.015 (5.50) = 17.08 \text{ kN/m}$$

$$p_1 = p_a = p_e = \frac{\sum \text{area}}{\text{span}} * p_{si1} = 2.015 (1.49) = 3.0 \text{ kN/m}$$

$$w_1 = w_a = w_e = g_1 + p_1 = 17.08 + 3.0 = 20.08 \text{ kN/m}$$

$$\boxed{g_1 = 17.08 \text{ kN/m} \text{ --- D.L.}}$$

$$\boxed{w_1 = 20.08 \text{ kN/m} \text{ --- T.L.}}$$

$$\underline{\underline{(w_2)}} \quad \frac{\sum \text{area}}{\text{span}} = \frac{4 \left(\frac{1}{2} (4.12) \left(\frac{4.12}{2} \right) \right)}{8.24} = 2.06$$

$$g_2 = g_a = g_e = o.w. + \frac{\sum \text{area}}{\text{span}} * g_s = 6.0 + 2.06 (5.50) = 17.33 \text{ kN/m}$$

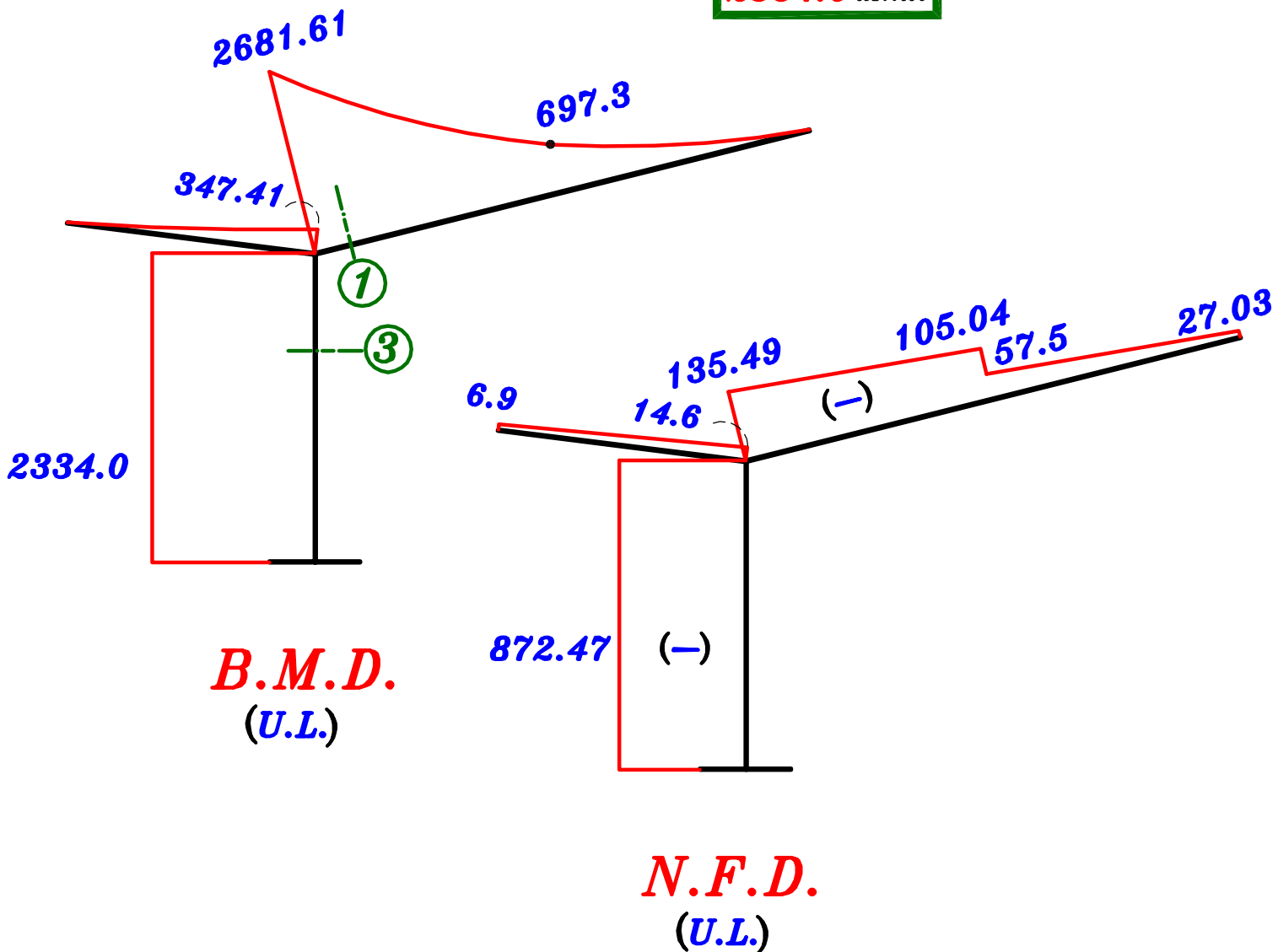
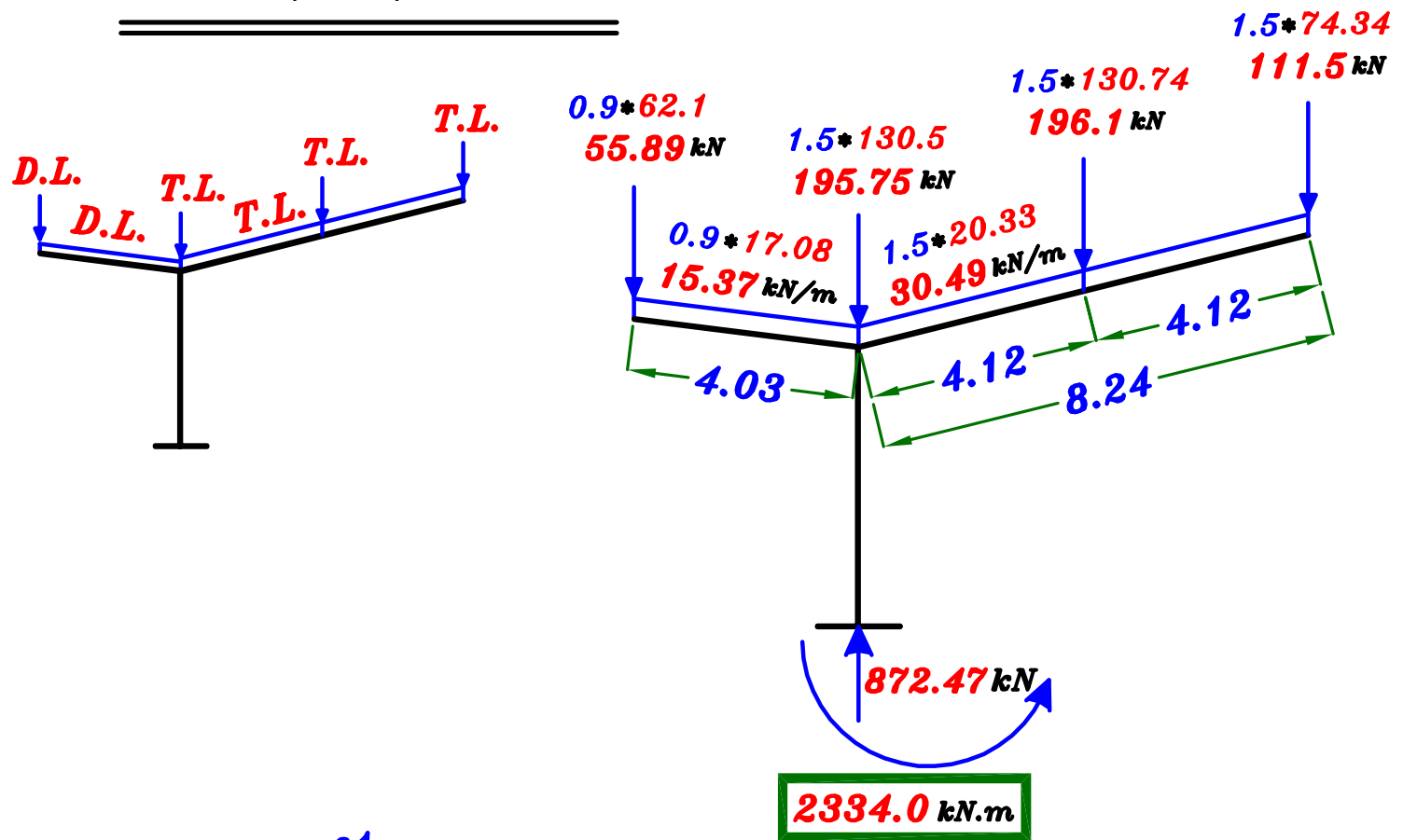
$$p_2 = p_a = p_e = \frac{\sum \text{area}}{\text{span}} * p_{si2} = 2.06 (1.455) = 3.0 \text{ kN/m}$$

$$w_2 = w_a = w_e = g_1 + p_1 = 17.33 + 3.0 = 20.33 \text{ kN/m}$$

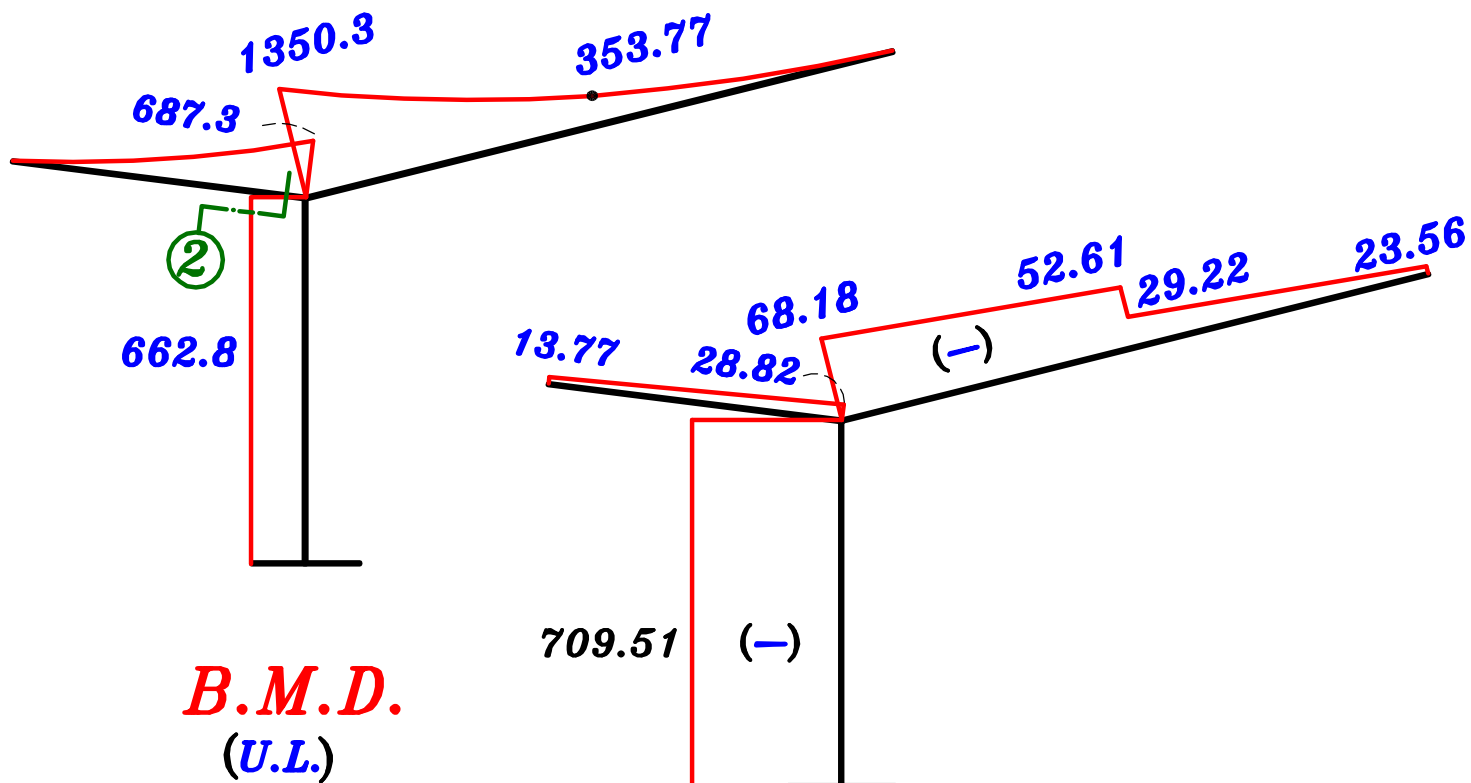
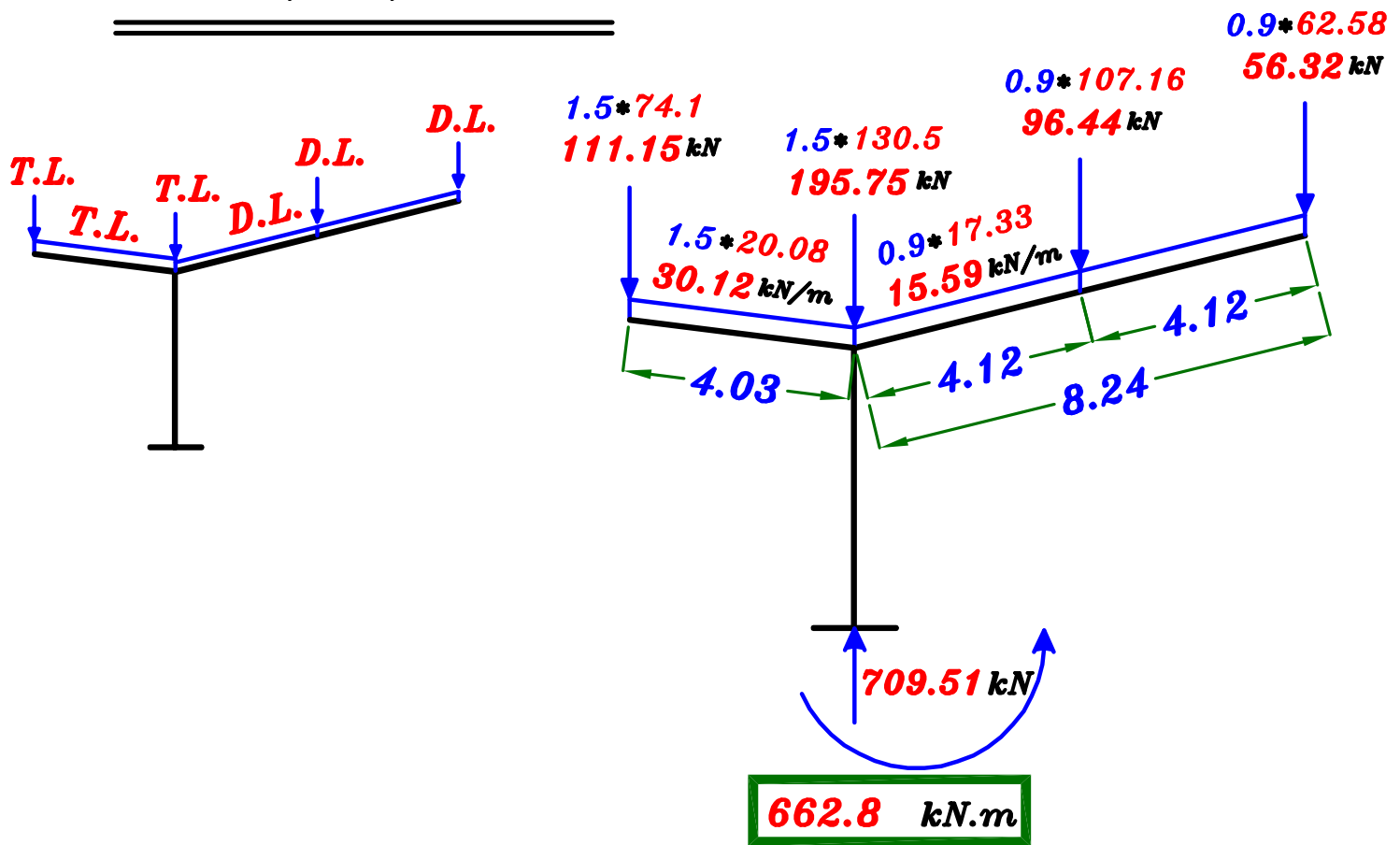
$$\boxed{g_2 = 17.33 \text{ kN/m} \text{ --- D.L.}}$$

$$\boxed{w_2 = 20.33 \text{ kN/m} \text{ --- T.L.}}$$

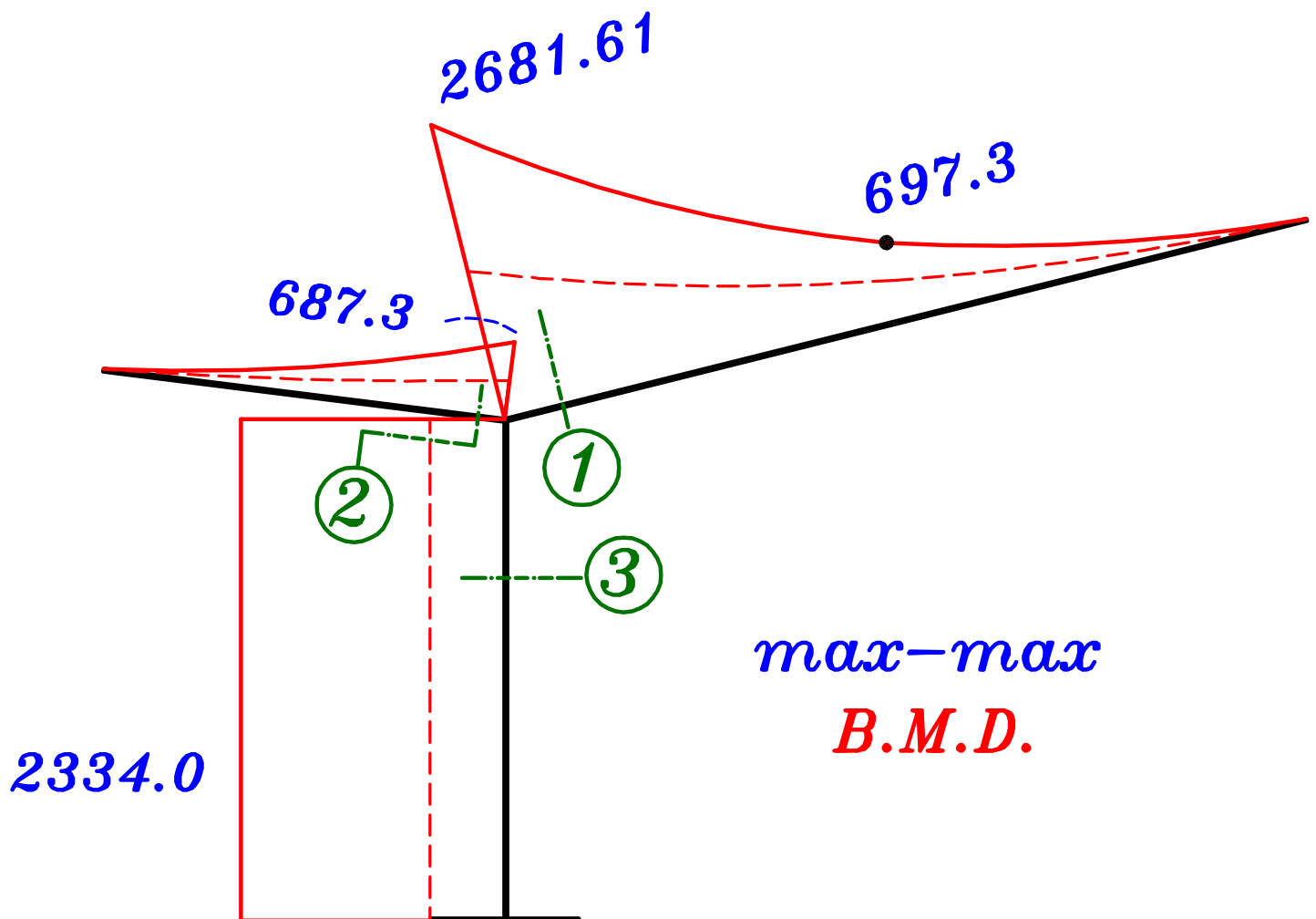
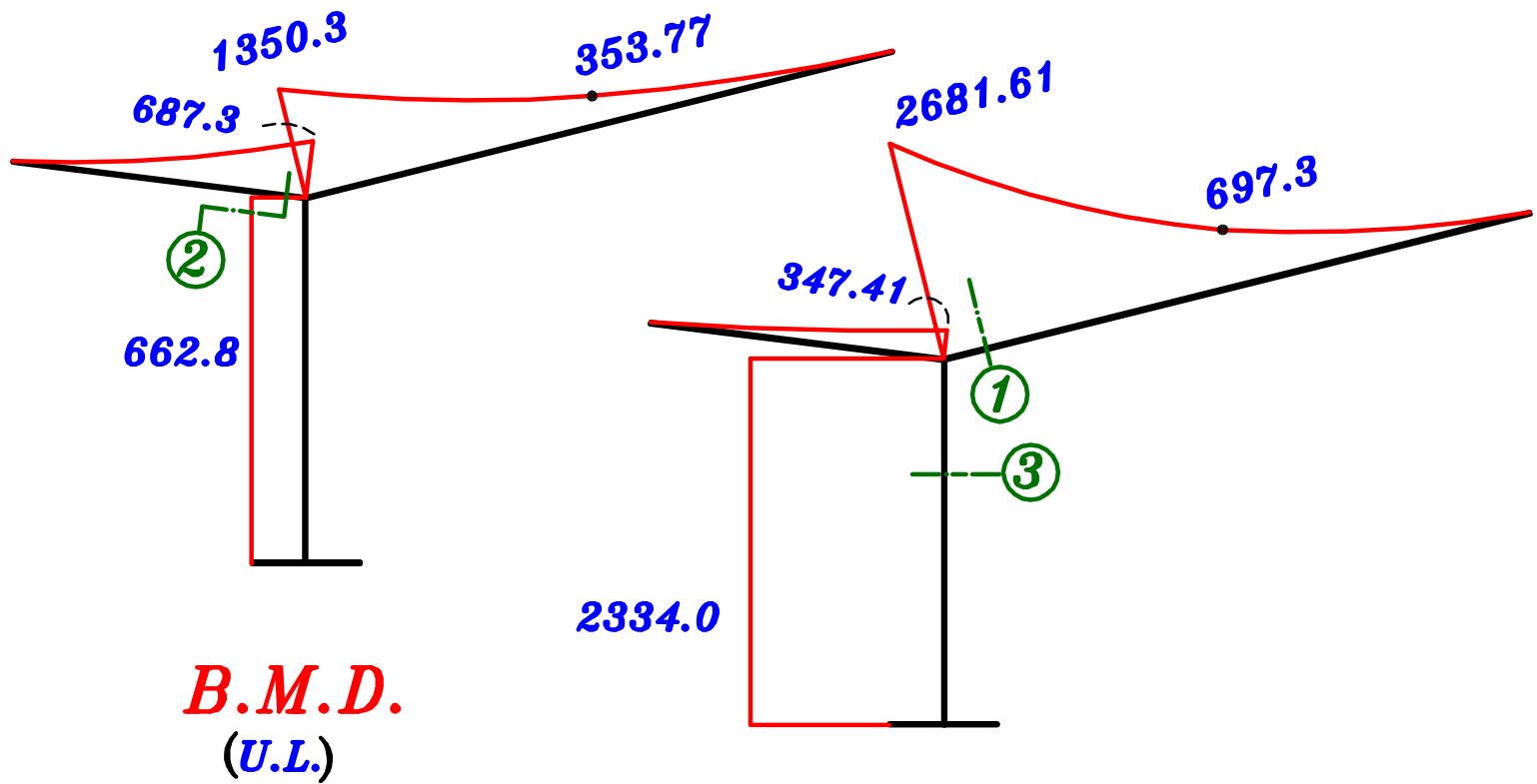
1- $\max (-Ve)$ *B.M.D.*



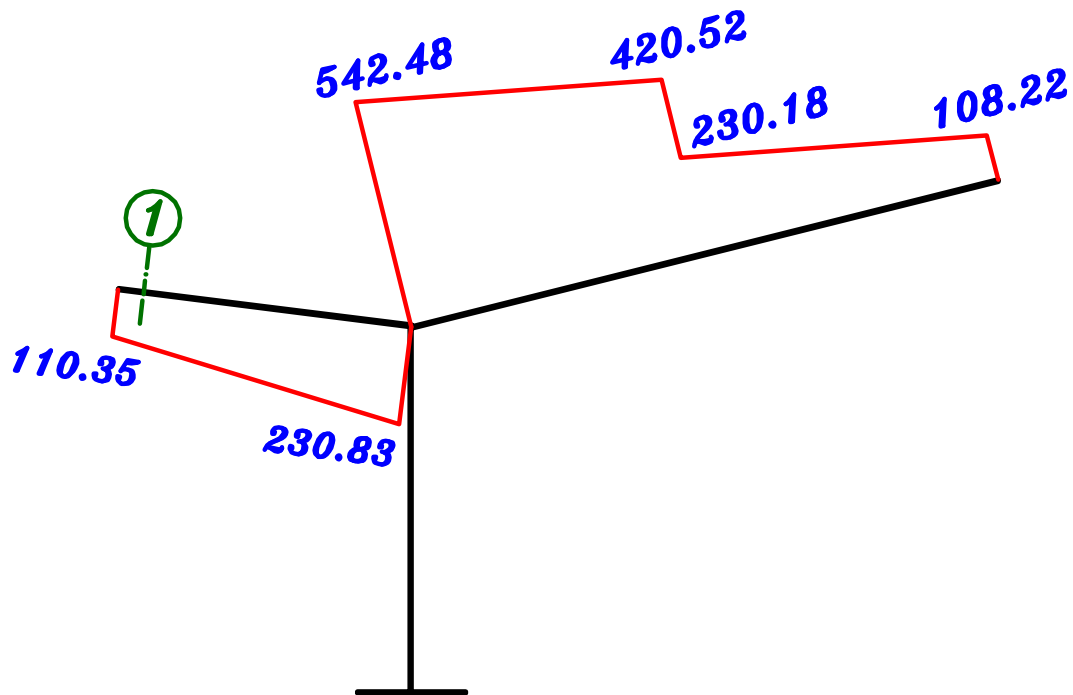
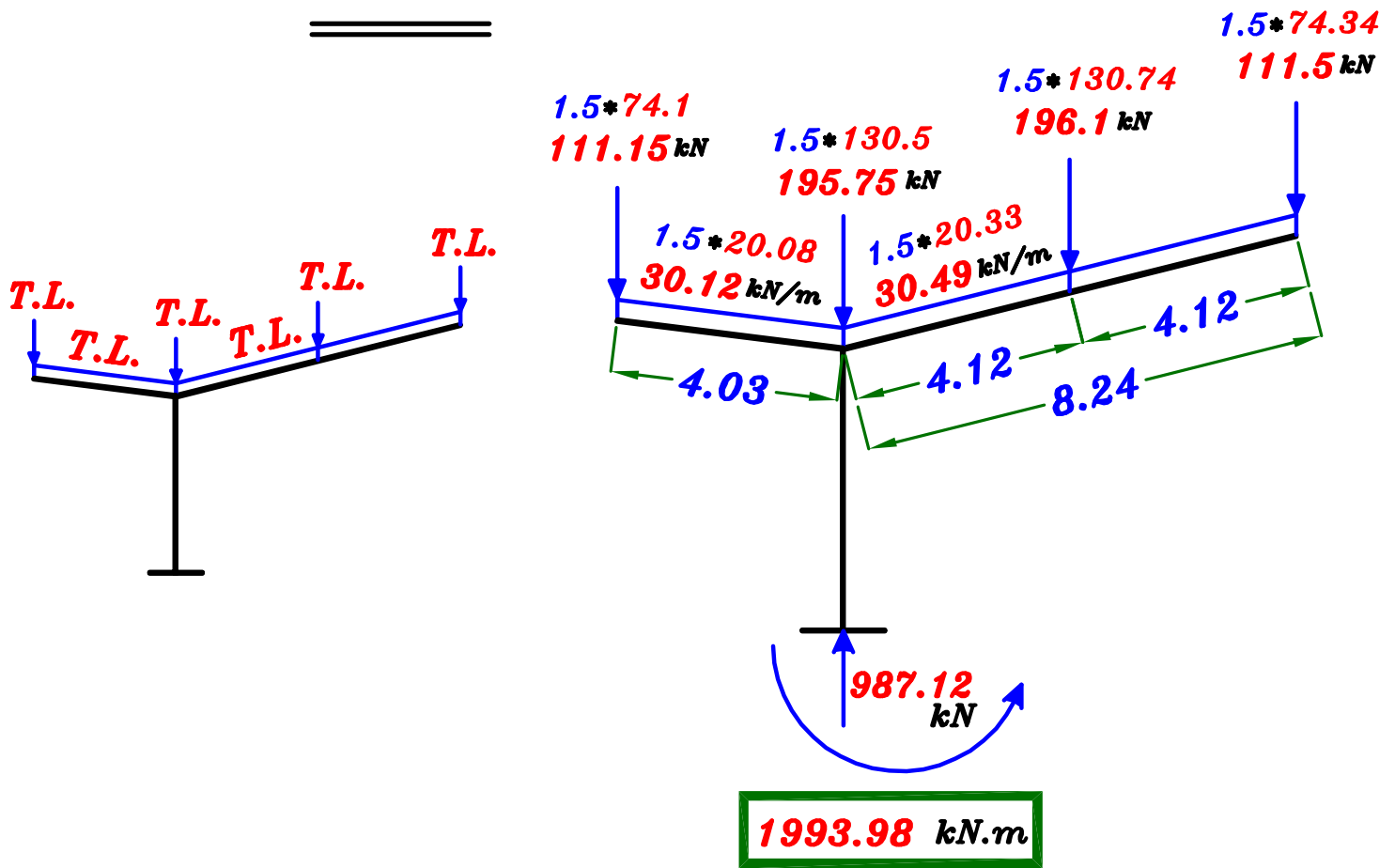
2- max (-Ve) B.M.D.



max-max B.M.D.



S.F.D.



S.F.D.
(U.L.)

Design of Sections.

Sec. ① $M = 2681.61 \text{ kN.m}$, $P = 135.49 \text{ kN}$, $b = 350 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{2681.61 \cdot 10^6}{30 \cdot 350}} = 1768.7 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1768.7) = (1945.5 \rightarrow 2299) \text{ mm}$$

Take $d = 2000 \text{ mm}$, $t = 2000 + 100 = 2100 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{135.49 \cdot 10^3}{30 \cdot 350 \cdot 2100} = 0.0062 < 0.04 \therefore (\text{neglect } P)$

\therefore Take $d = d_o = 1768.7 \text{ mm}$

\therefore Take $d = 1800 \text{ mm}$, $t = 1900 \text{ mm}$

\therefore The sec. still R-sec. $C_1 = 3.50 \rightarrow J = 0.78$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{2681.61 \cdot 10^6}{0.780 \cdot 400 \cdot 1768.7} = 4859.4 \text{ mm}^2$$

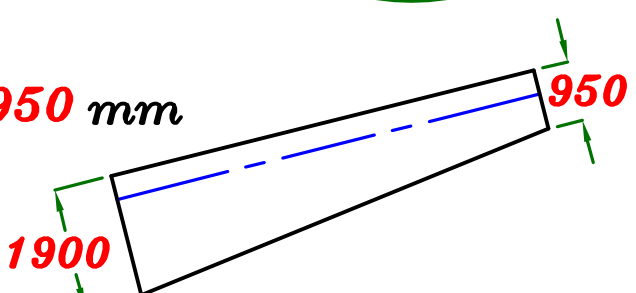
Check $A_{s_{min.}}$ $A_{s_{req.}} = 4859.4 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{30}}{400} \right) 350 \cdot 1800 = 1941 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore$ Take $A_s = A_{s_{req.}} = 4859.4 \text{ mm}^2$ **10 ϕ 25**

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{25 + 25} = 6.50 = 6.0 \text{ bars}$$

Stirrup Hangers = $(0.1 \rightarrow 0.2) A_s = (0.1 \rightarrow 0.2) 4859.4$ **5 ϕ 12**

$$Y = \left\{ \begin{array}{l} \frac{t}{2} = \frac{1900}{2} = 950 \text{ mm} \\ t_b = \frac{\text{spacing}}{12} = \frac{6000}{12} = 500 \text{ mm} \end{array} \right\} = 950 \text{ mm}$$


Sec. ② $M = 687.3$ kN.m , $P = 28.82$ kN , $b = 350$ mm

$$d_o = 3.5 \sqrt{\frac{687.3 * 10^6}{30 * 350}} = 895.0 \text{ mm (as R-Sec.)}$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (895.4) = (985.0 \rightarrow 1164.1) \text{ mm}$$

$$\text{Take } d = 1000 \text{ mm , } t = 1000 + 100 = 1100 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{28.82 * 10^3}{30 * 350 * 1100} = 0.0025 < 0.04 \therefore (\text{neglect } P)$$

$$\therefore \text{Take } d = d_o = 895.0 \text{ mm}$$

$$\therefore \text{Take } \boxed{d = 900 \text{ mm}} , \boxed{t = 950 \text{ mm}}$$

$$\therefore \text{The sec. still R-sec. } C_1 = 3.50 \rightarrow J = 0.78$$

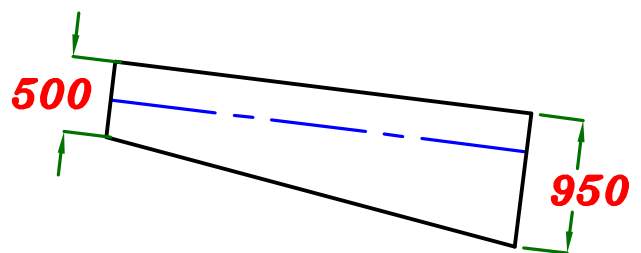
$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{687.3 * 10^6}{0.780 * 400 * 895.0} = 2461.32 \text{ mm}^2$$

$$\text{Check } \underline{A_{s_{min.}}} \quad A_{s_{req.}} = 2461.32 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{400} \right) 350 * 900 = 970.5 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2461.32 \text{ mm}^2 \quad \textcircled{6 \phi 25}$$

$$Y = \left\{ \begin{array}{l} \frac{t}{2} = \frac{950}{2} = 475 \text{ mm} \\ t_b = \frac{\text{spacing}}{12} = \frac{6000}{12} = 500 \text{ mm} \end{array} \right\} = 500 \text{ mm}$$



Sec. ③ $M = 2334.0 \text{ kN.m}$, $P = 872.47 \text{ kN}$, $b = 350 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{2334.0 \cdot 10^6}{30 \cdot 350}} = 1650.2 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1650.2) = (1815.2 \rightarrow 2145.2) \text{ mm}$$

Take $d = 1900 \text{ mm}$, $t = 1900 + 100 = 2000 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{872.47 \cdot 10^3}{30 \cdot 350 \cdot 2000} = 0.0415 > 0.04$ (Don't neglect P)

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{2334.0}{872.47} = 2.67 \text{ m} \therefore \frac{e}{t} = \frac{2.67}{2.0} = 1.33 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 2.67 + \frac{2.0}{2} - 0.10 = 3.57 \text{ m}$$

$$M_s = P \cdot e_s = 872.47 \cdot 3.57 = 3114.7 \text{ kN.m}$$

$$\therefore 1900 = C_1 \sqrt{\frac{3114.7 \cdot 10^6}{30 \cdot 350}} \rightarrow C_1 = 3.48 \rightarrow J = 0.779$$

$$A_s = \frac{M_s}{J F_y d} - \frac{P_{u.l.}}{(F_y \setminus \delta_s)}$$

$$= \frac{3114.7 \cdot 10^6}{0.779 \cdot 400 \cdot 1900} - \frac{872.47 \cdot 10^3}{(400 \setminus 1.15)} = 2752.6 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2752.6 \text{ mm}^2$

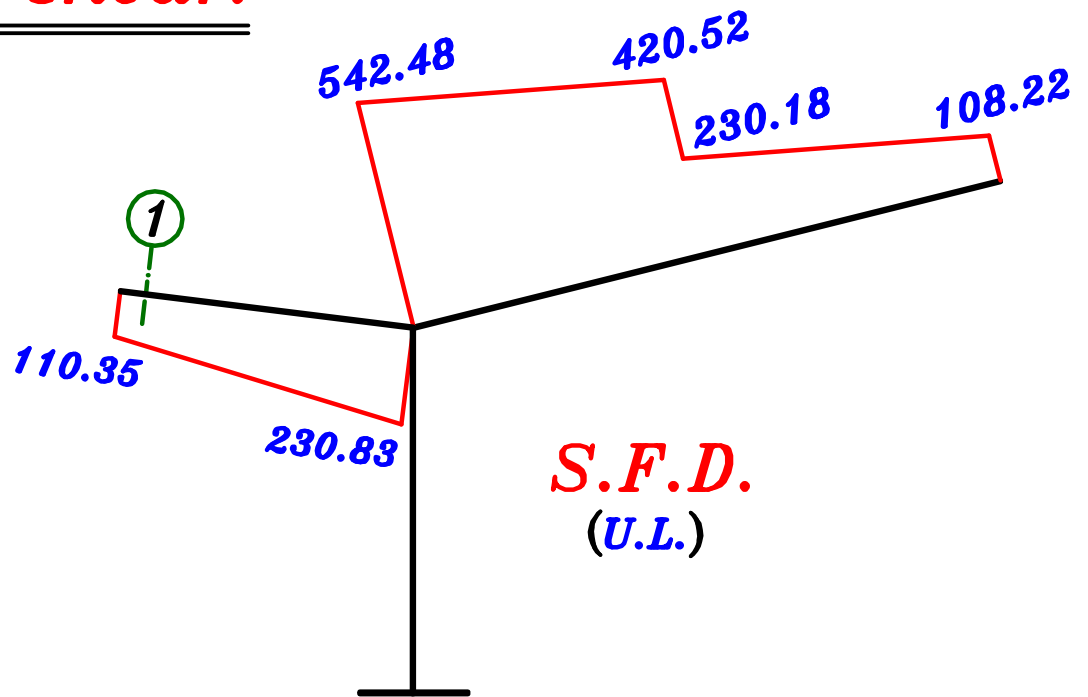
$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{30}}{400} \right) 350 \cdot 1900 = 2048.8 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2752.6 \text{ mm}^2 \quad \textcircled{6 \phi 25}$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{25 + 25} = 6.50 = 6.0 \text{ bars}$$

$$\text{Stirrup Hangers} \approx 0.4 A_s \approx 0.4 (2752.6) = 1101 \text{ mm}^2 \quad \textcircled{3 \phi 25}$$

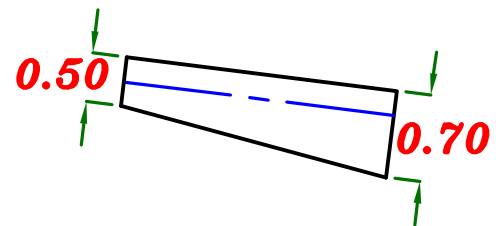
Check shear.



– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{30}{1.5}} = 3.13 \text{ N/mm}^2$$

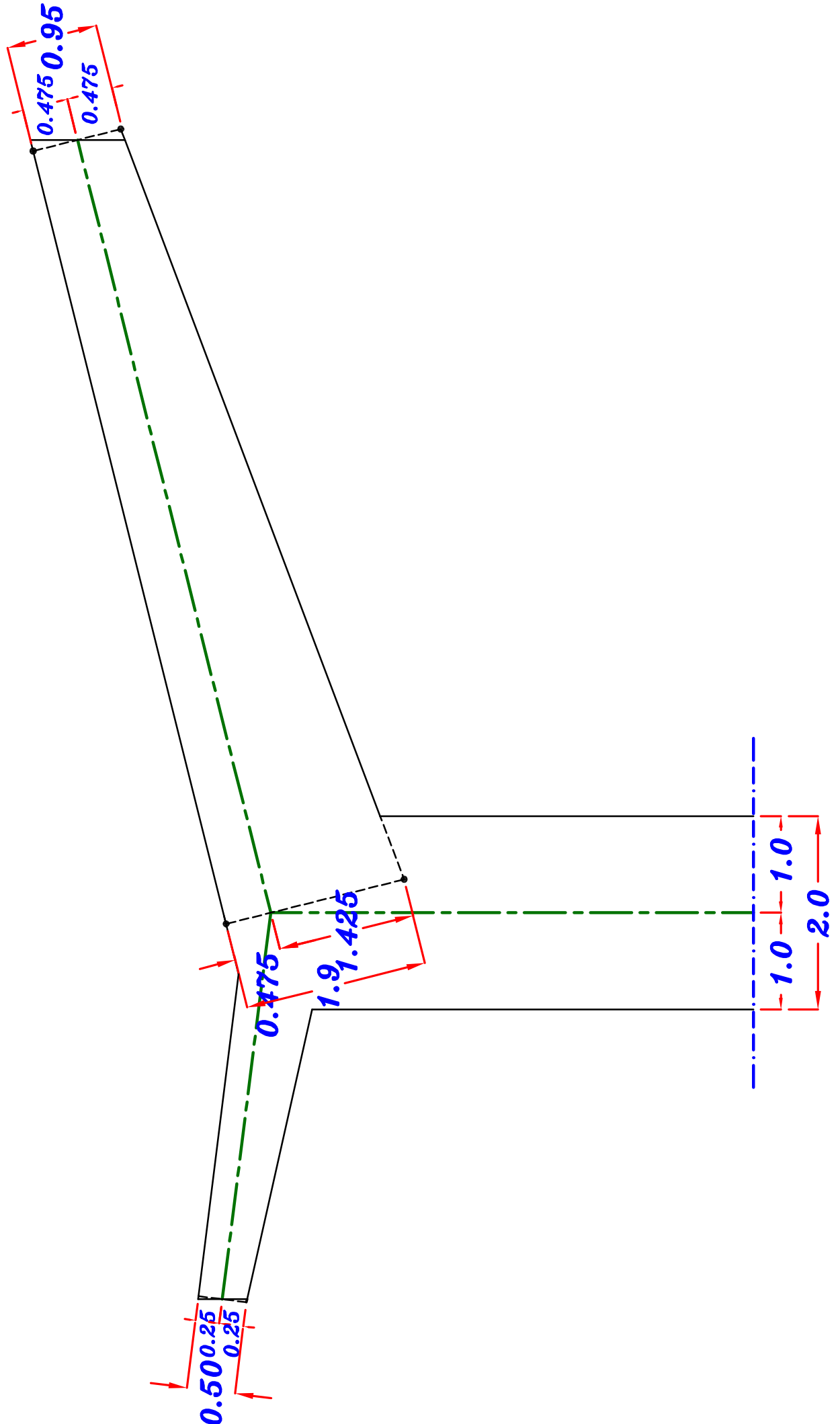


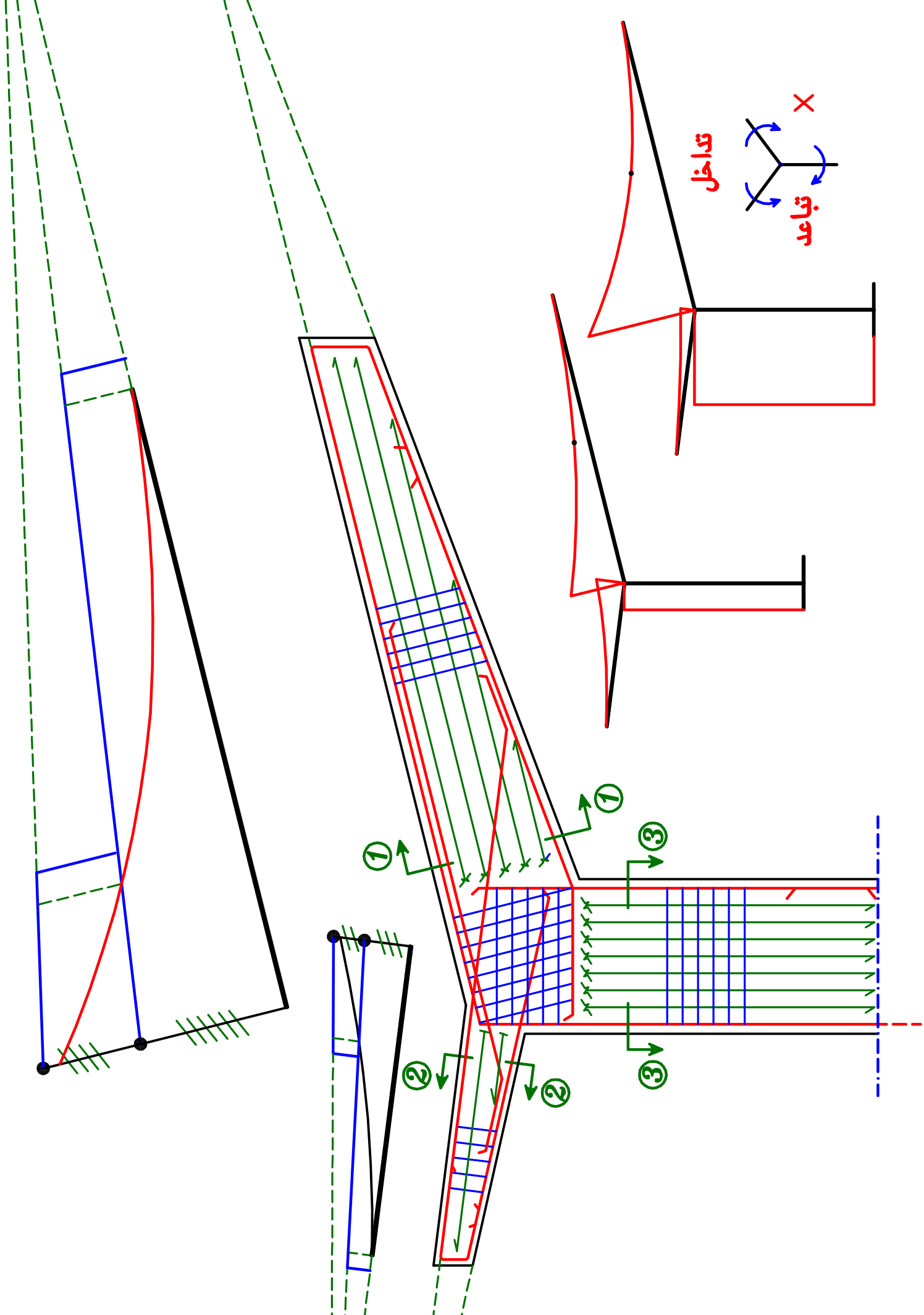
Sec. ① $Q = 110.35 \text{ kN}$

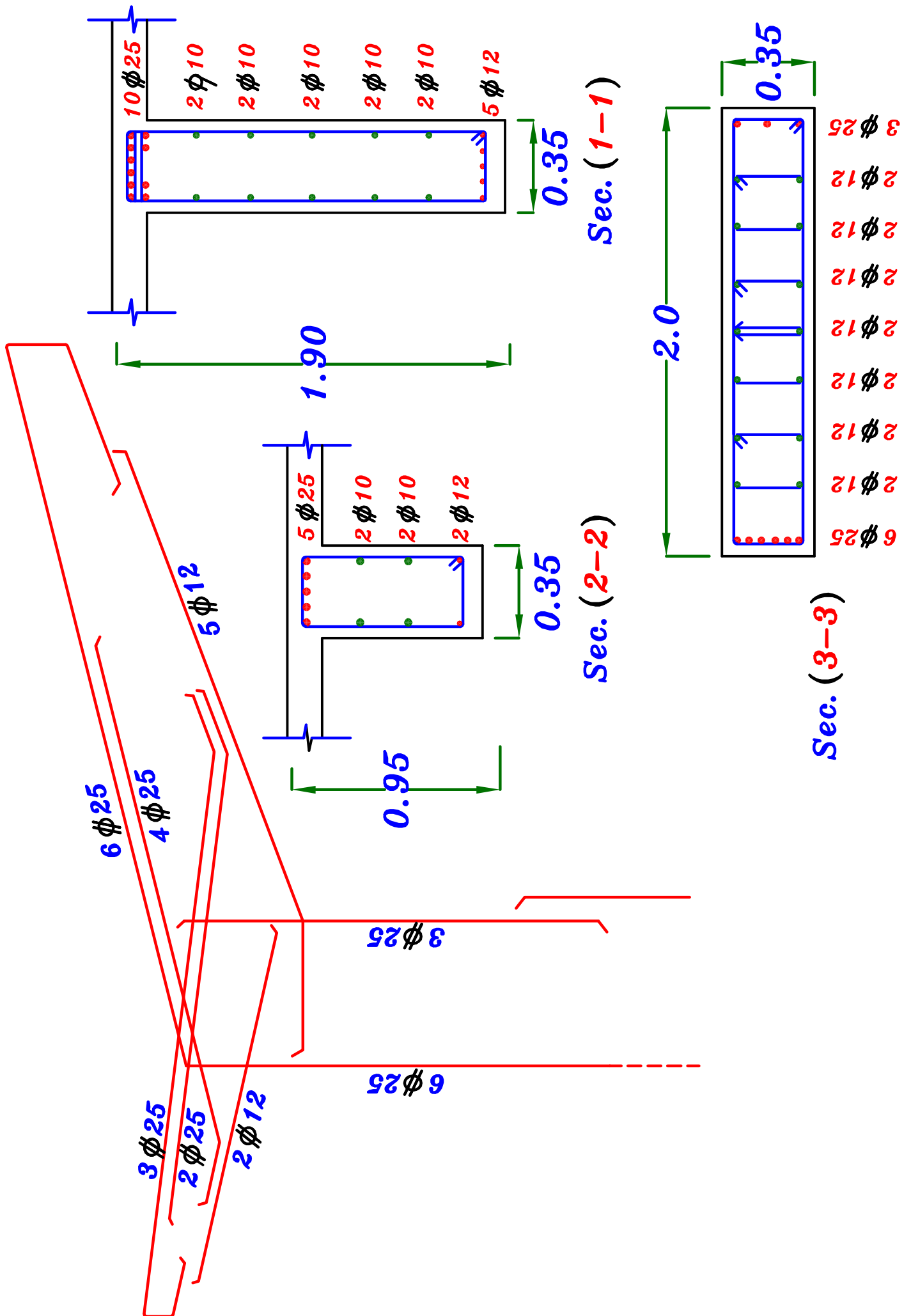
$$\therefore \text{Actual shear stress.} = q_U = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$

$$q_U = \frac{110.35 * 10^3}{350 * 450} - \text{ZERO} = 0.70 \text{ N/mm}^2$$

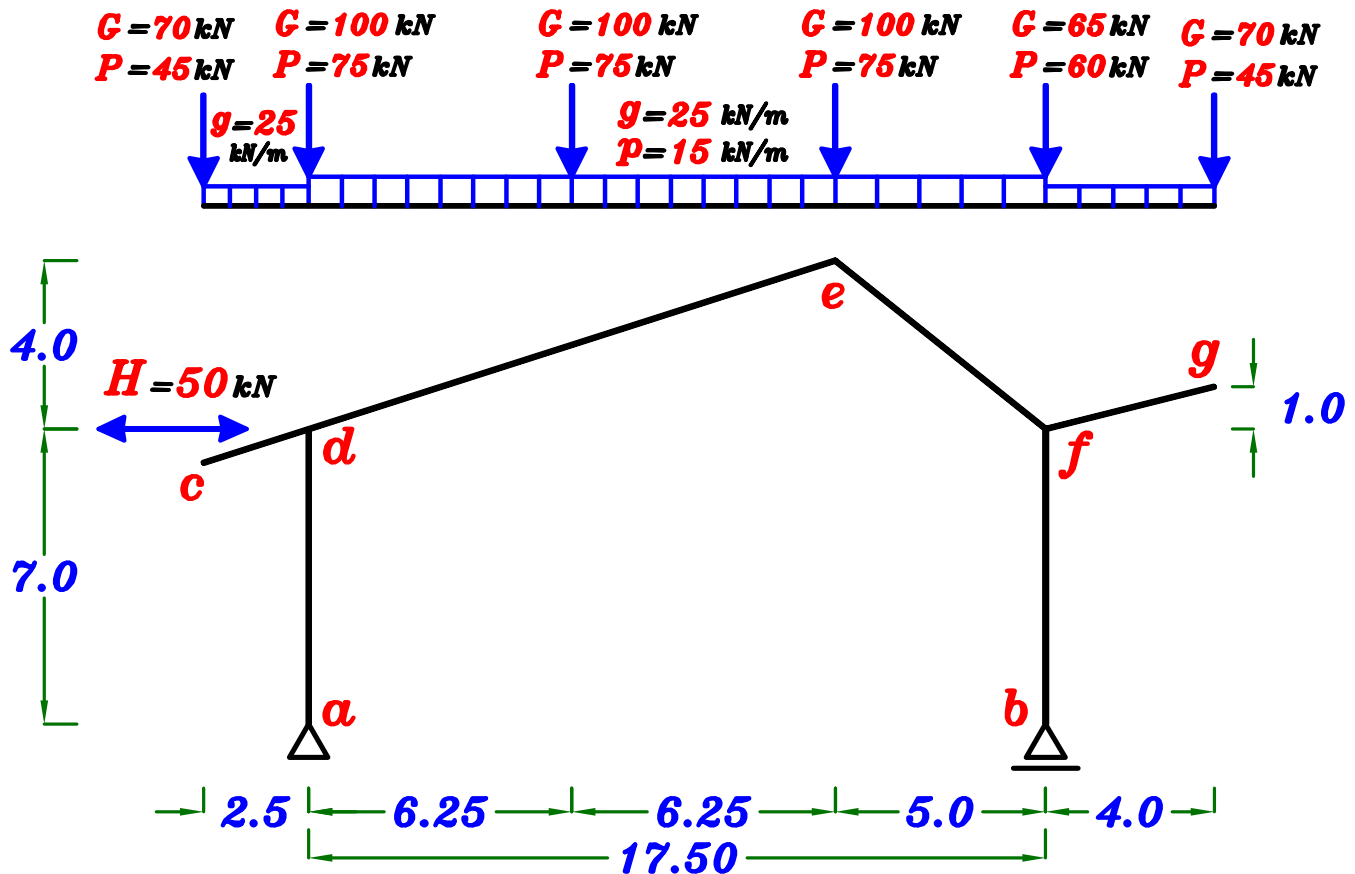
$$\therefore q_U < q_{cu} \longrightarrow \text{Use min. stirrups } \boxed{5 \phi 8 \setminus m'}$$







Example.



The Figure shows a statical system and load diagram For a reinforced concrete shed. The shed is covered with reinforced concrete slabs supported on a system of secondary beams and Frames (**F**), spaced at **6.0 m**. Each Frame is subjected also to a horizontal wind (**H**) as shown on the load diagram. For an intermediate panel.

It is required to:

- 1- Draw the absolute **B.M.D** considering the directions of wind load (**H**). of an intermediate Frame (**F**), **using given working loads**.
- 2- Draw the **N.F.D** and **S.F.D** For case of total load only, neglecting the wind load (**H**).
- 3- Design the critical sections (**at least Four sections**) For the intermediate Frame (**F**). to satisfy both bending moments and normal Forces.
- 4- Check shear stresses at joint (**f**) .
- 5- Consider the effect of buckling condition in the design of column (**a-d**).
- 6- Draw the details of reinforcement For the Frame, considering **the moment of resistance principle** For girder part (**c-d-e-f-g**) in elevation (**to scale 1:50**) and cross section (**to scale 1:20**).

Design Data:

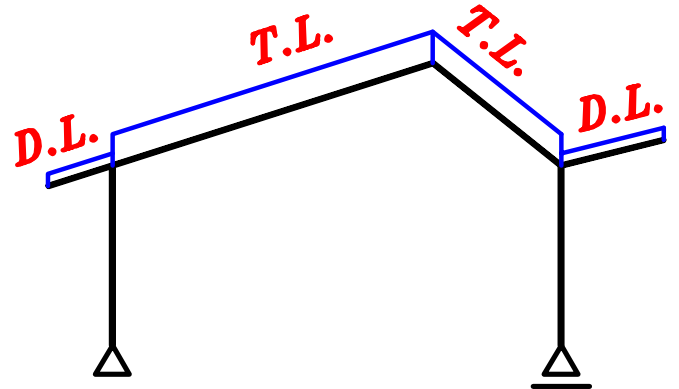
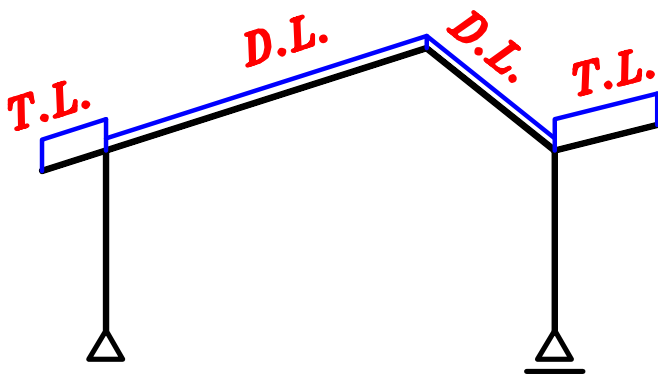
$$t_s = 140 \text{ mm} \quad b(\text{beams}) = 250 \text{ mm} \quad b(\text{Frame}) = 350 \text{ mm}$$

Spacing between Frames = **6.0 m**

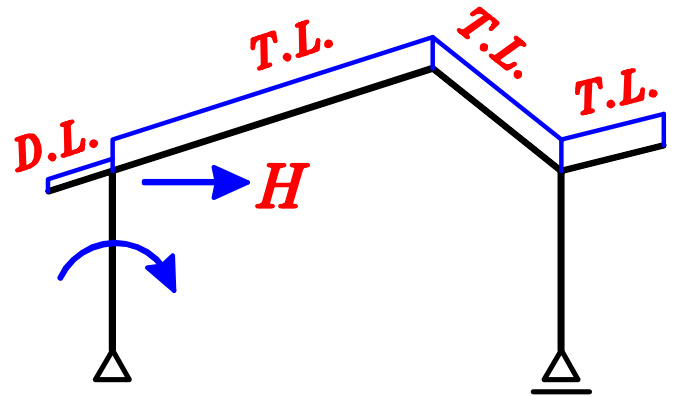
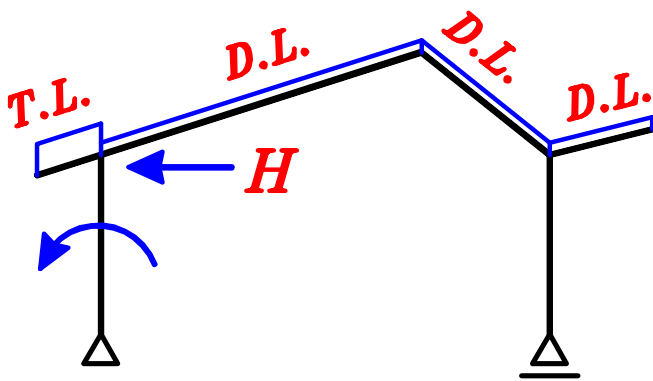
C 30 & Steel 360/520

1 – Draw the absolute **B.M.D** considering the directions of wind load (**H**). of an intermediate Frame (**F**), using given working loads.

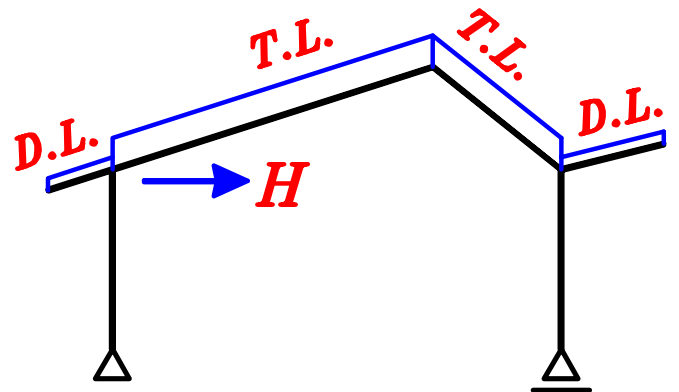
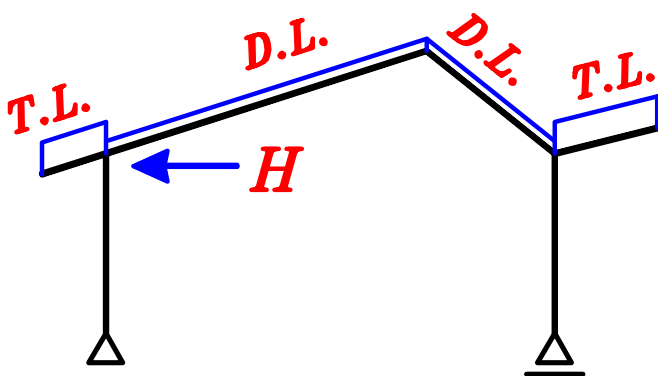
حالات التحميل الاساسيه لل Frame

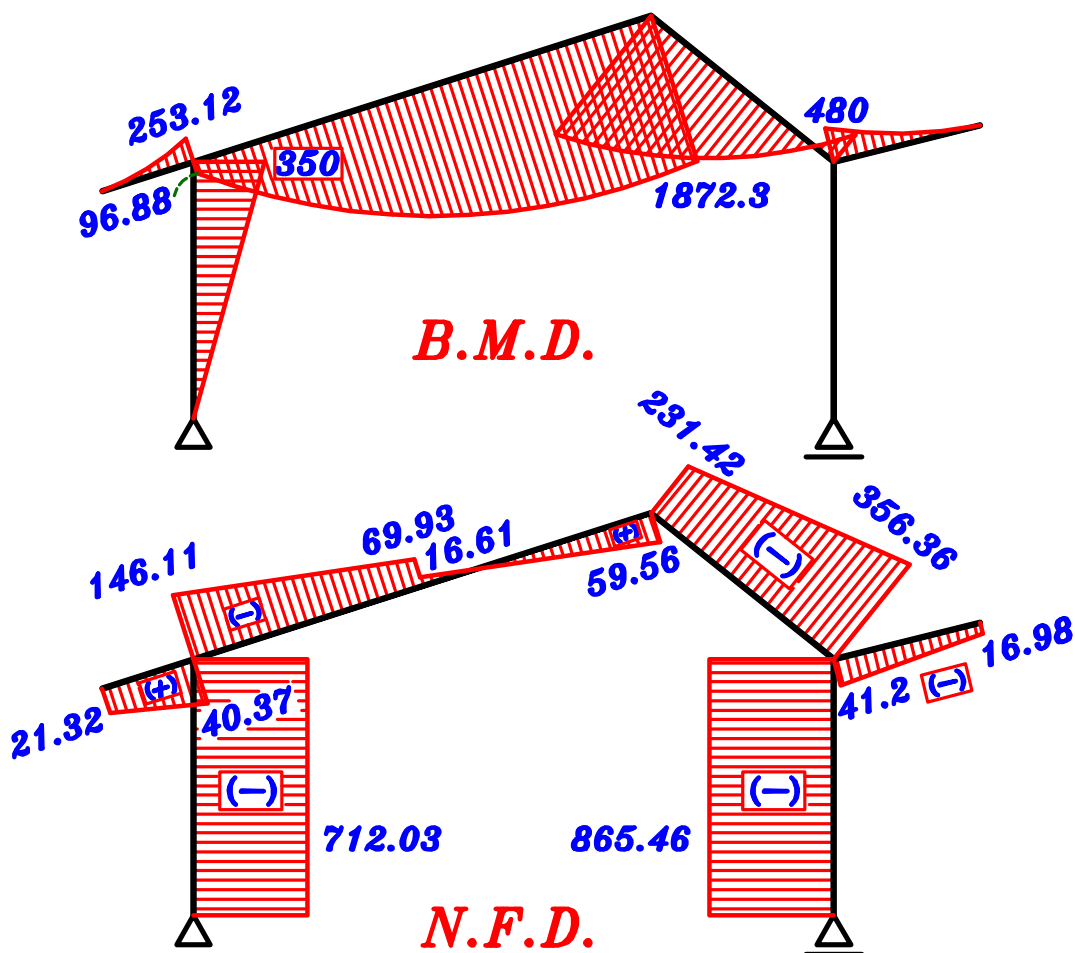
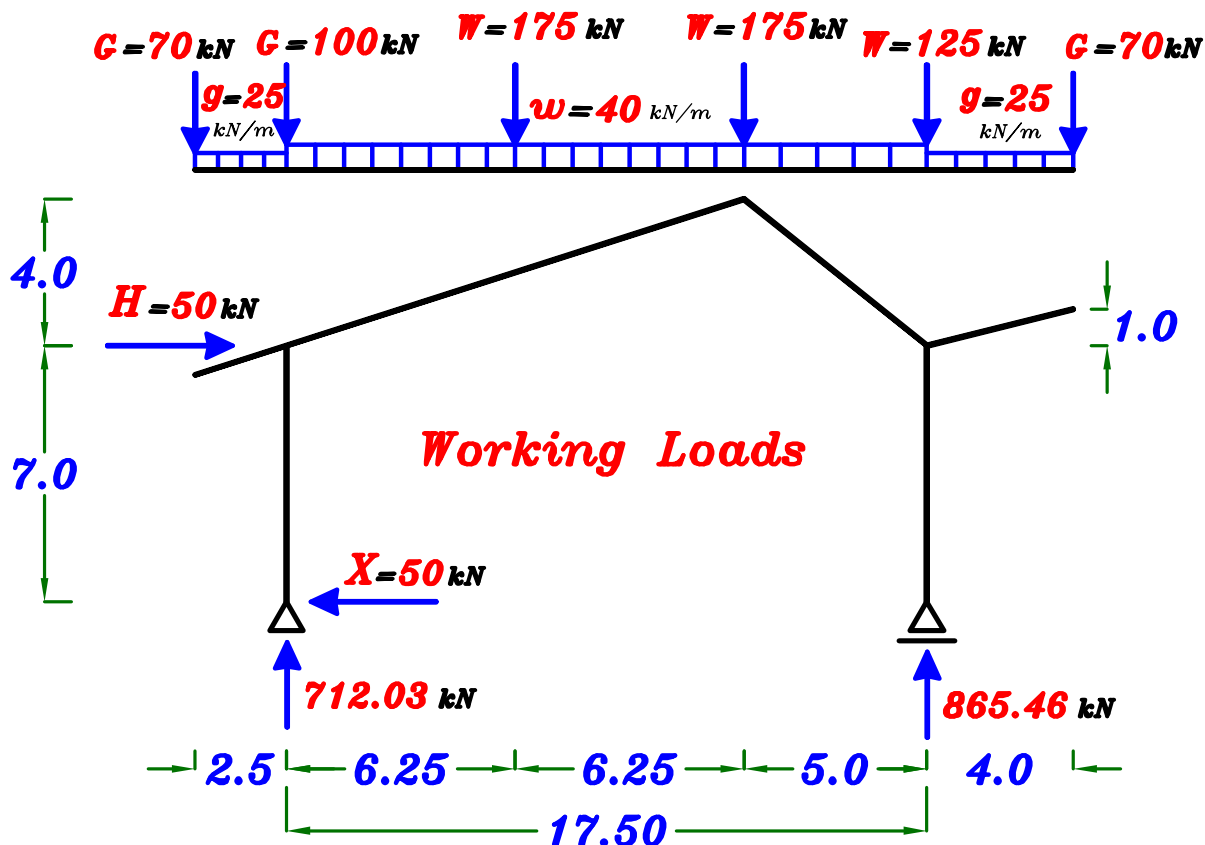
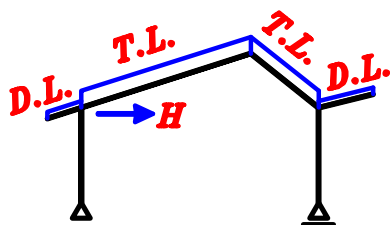


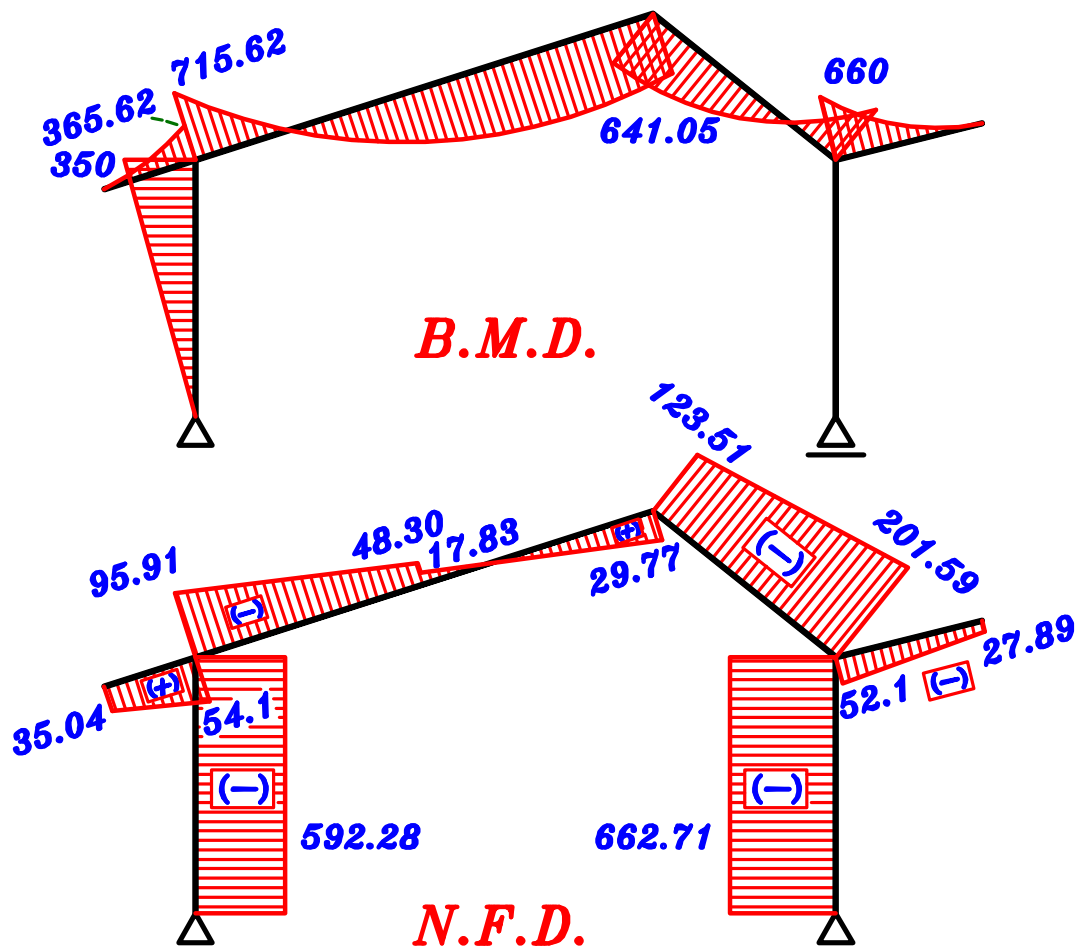
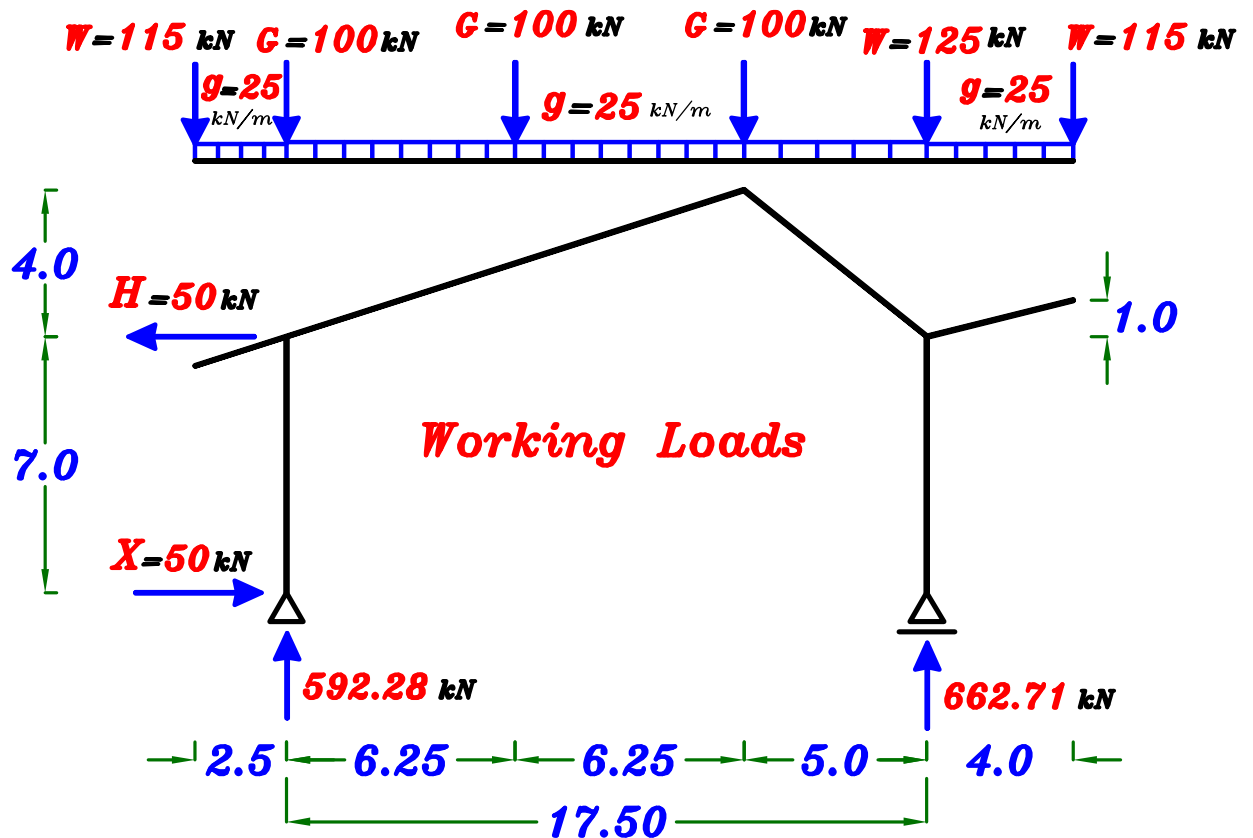
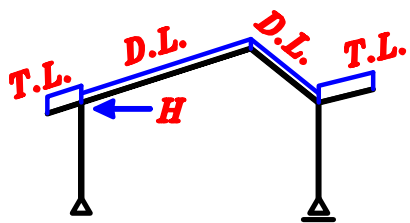
مع وجود القوى الافقيه (**H**) سنحتاج لحالتى تحميل أخريتين



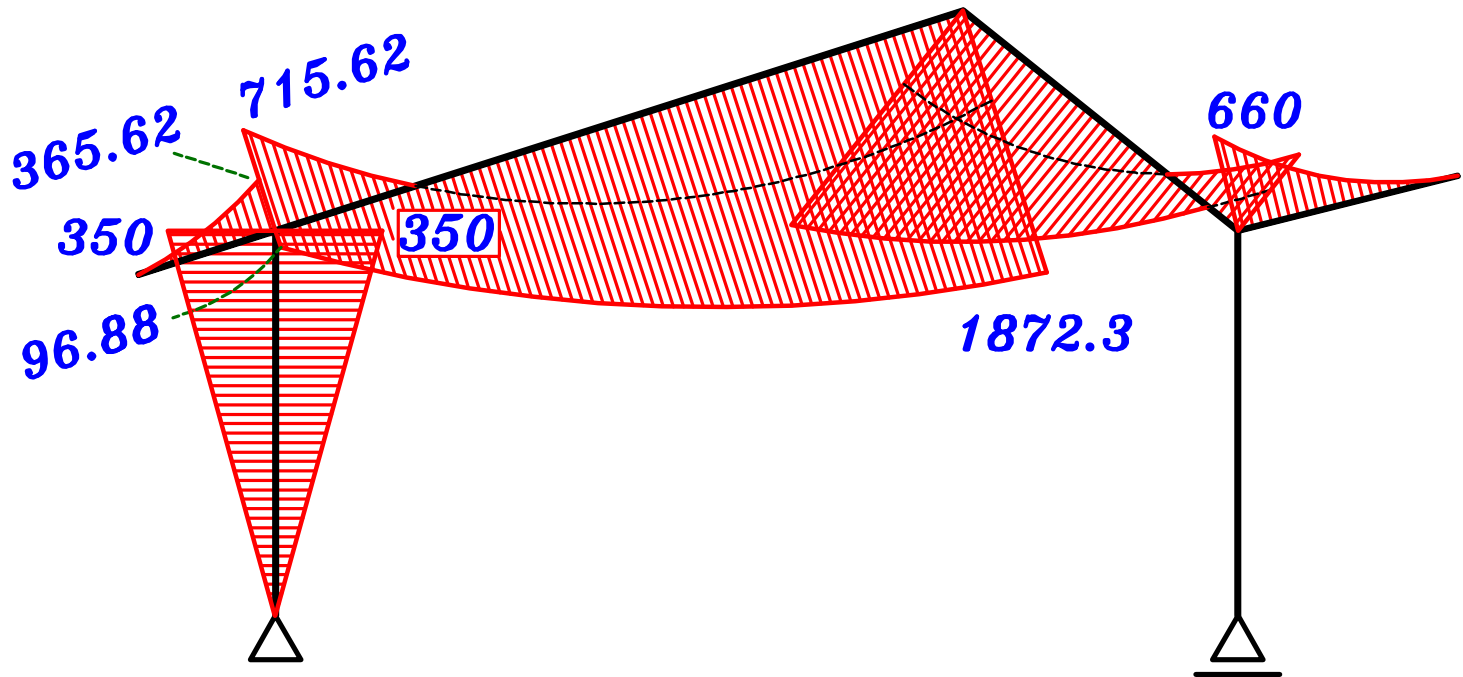
و نظرا لضيق الوقت سنأخذ حالات التحميل الاساسيه مع الاخذ فى الاعتبار القوى الافقيه



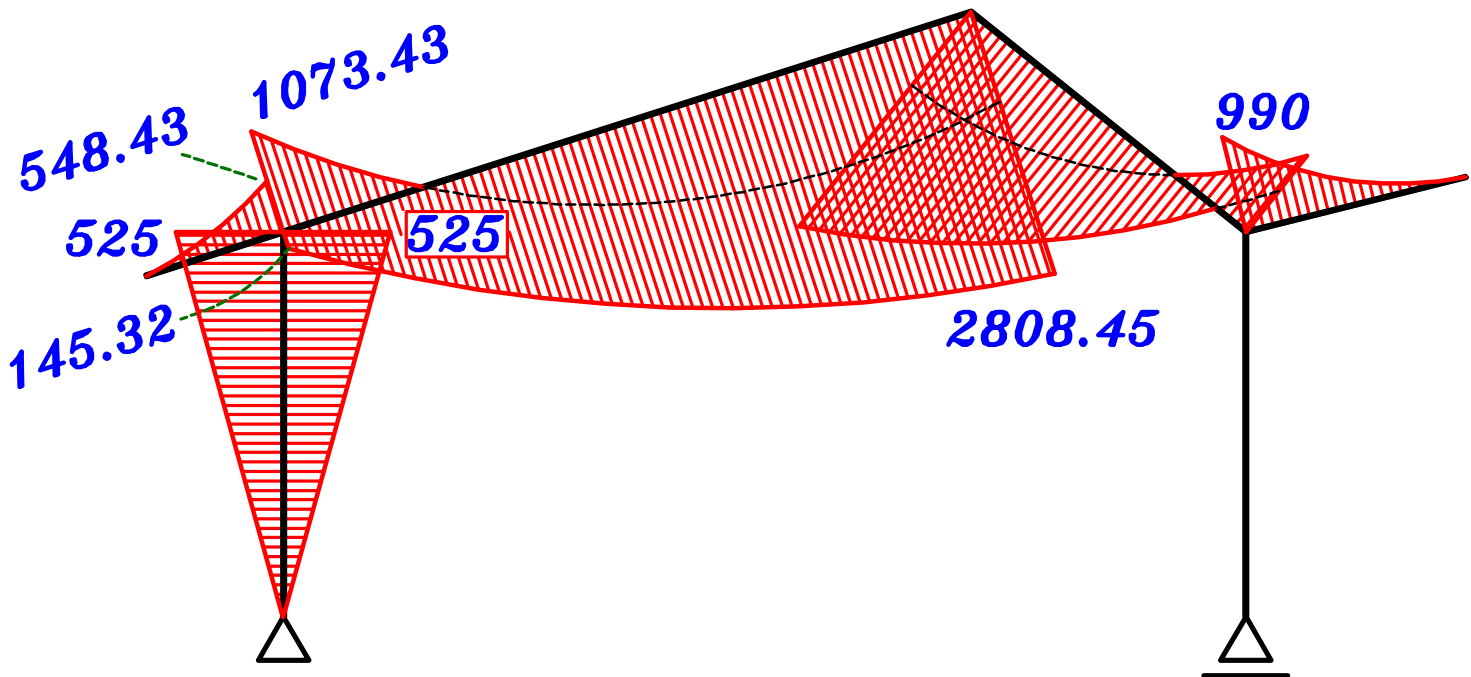




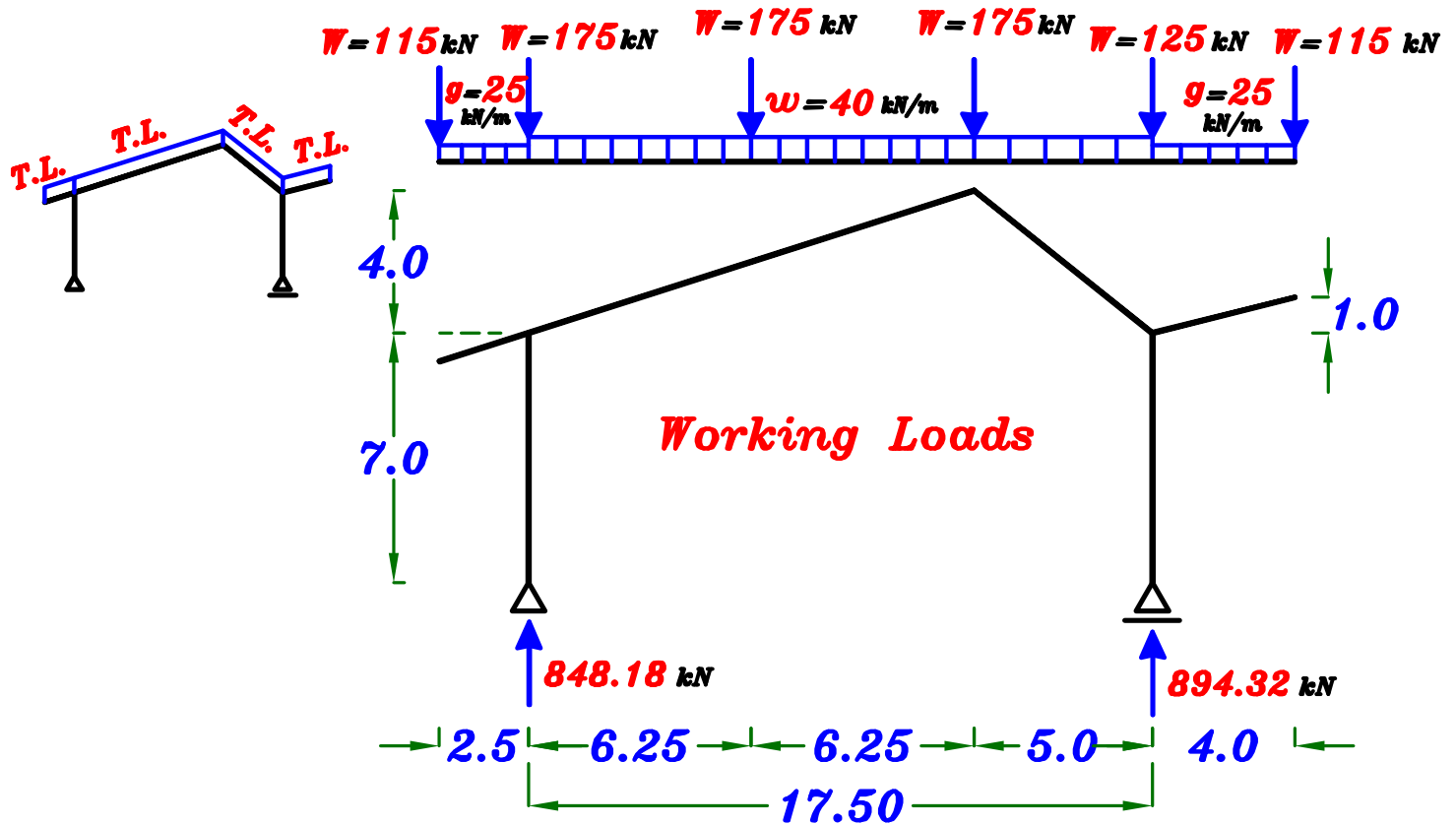
max.-max. B.M.D. working Loads



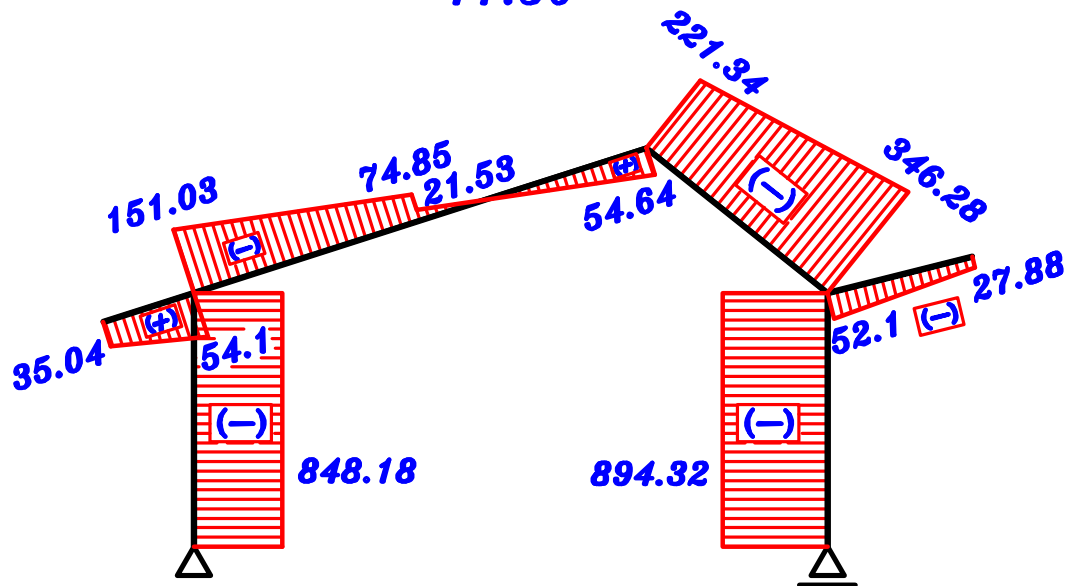
max.-max. B.M.D. U.L.



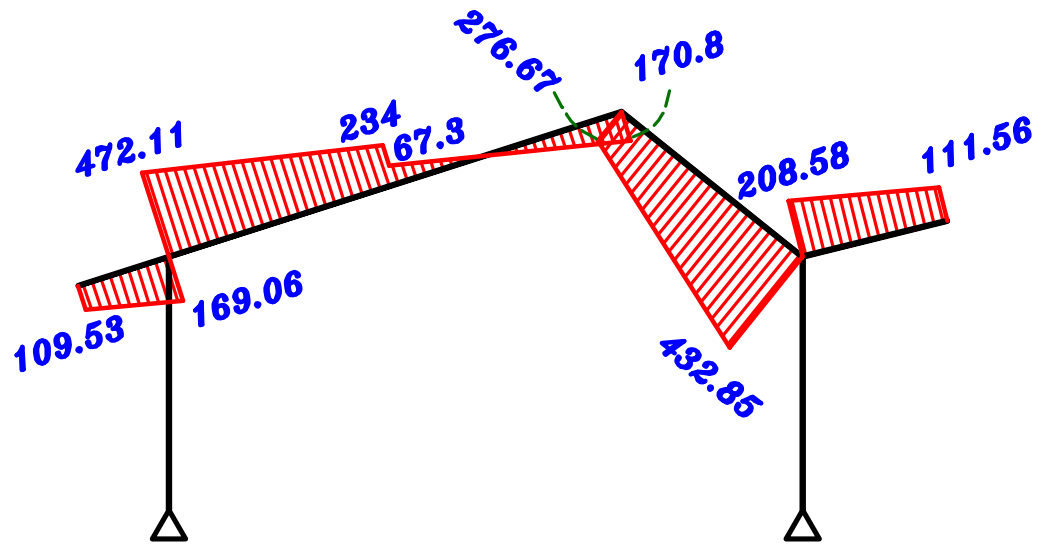
2- Draw the **N.F.D** and **S.F.D** For case of total load only, neglecting the wind load (**H**).



N.F.D.
working

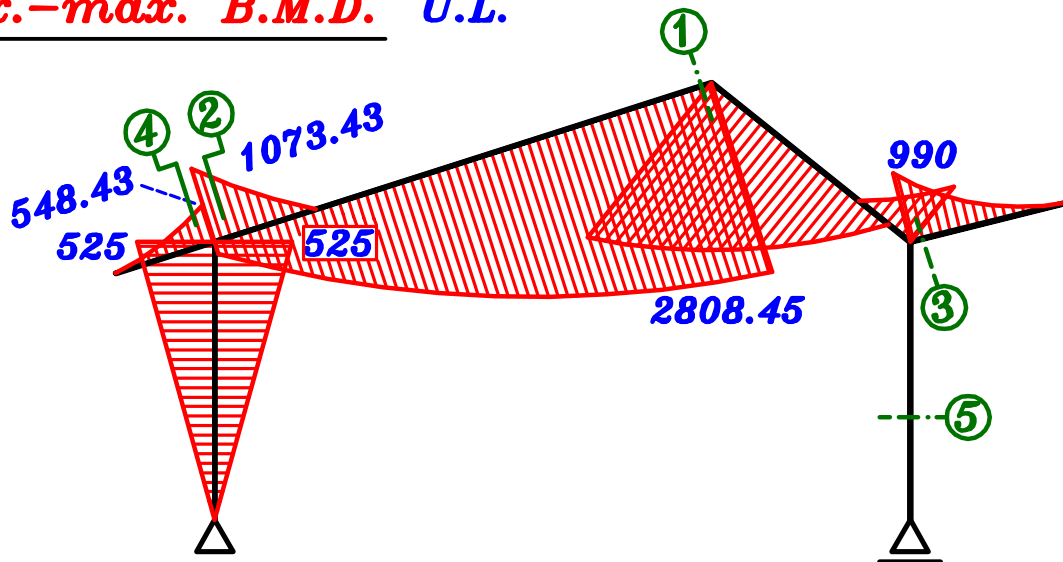


S.F.D.
working



3- Design the critical sections (at least Four sections) For the intermediate Frame (F).
to satisfy both bending moments and normal Forces.

max.-max. B.M.D. U.L.



Sec. ①

$$M = 2808.45 \text{ kN.m} , T = 59.56 * 1.5 = 89.34 \text{ kN} , b = 350 \text{ mm}$$

$$d = 3.5 \sqrt{\frac{2808.45 * 10^6}{30 * 350}} = 1810.1 \text{ mm} \text{ (as R-Sec.)}$$

$$\therefore \text{Take } d = 1900 \text{ mm} , t = 2000 \text{ mm}$$

$$e = \frac{M}{T} = \frac{2808.45}{89.34} = 31.43 \text{ m} \therefore \frac{e}{t} = \frac{31.43}{2.0} = 15.71 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e - \frac{t}{2} + c = 31.43 - \frac{2.0}{2} + 0.10 = 30.53 \text{ m}$$

$$M_s = T * e_s = 89.34 * 30.53 = 2727.55 \text{ kN.m}$$

$$\therefore d = c_1 \sqrt{\frac{M_s}{F_{cu} b}} \therefore 1900 = c_1 \sqrt{\frac{2727.55 * 10^6}{30 * 350}} \rightarrow c_1 = 3.73 \rightarrow J = 0.792$$

$$\begin{aligned} \therefore A_s &= \frac{M_s}{J F_y d} + \frac{T_{U.L.}}{(F_y \setminus \delta_s)} \\ &= \frac{2727.55 * 10^6}{0.792 * 360 * 1900} + \frac{89.34 * 10^3}{(360 \setminus 1.15)} = 5320.3 \text{ mm}^2 \end{aligned}$$

Check $A_{s_{min.}}$

$$A_{s_{req.}} = 5320.3 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1900 = 2276.5 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 5320.3 \text{ mm}^2 \quad (11 \phi 25)$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{25 + 25} = 6.50 = 6.0 \text{ bars}$$

ملحوظه لان قيمه ال *Tension* صغيره بالنسبه لـ *moment*
فاذا اعملنا ال *Tension* فى هذه الحاله و صممنا على ال *moment* فقط
فلن نفرق كثيرا فى كميه الحديد المطلوبه .

Sec. ② $M = 1073.43 \text{ kN.m}$, $P = 95.91 * 1.5 = 143.86 \text{ kN}$

$$, b = 350 \text{ mm} , t = 2000 \text{ mm}$$

Check $\frac{P}{F_{cu} b t} = \frac{143.86 * 10^3}{30 * 350 * 2000} = 0.006 < 0.04 \therefore (\text{neglect } P)$

$$\therefore d = c_1 \sqrt{\frac{M_{u.L.}}{F_{cu} b}} \therefore 1900 = c_1 \sqrt{\frac{1073.43 * 10^6}{30 * 350}} \rightarrow c_1 = 5.94 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{u.L.}}{J F_y d} = \frac{1073.43 * 10^6}{0.826 * 360 * 1900} = 1899.9 \text{ mm}^2$$

Check $A_{s_{min.}}$

$$A_{s_{req.}} = 1899.9 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1900 = 2276.5 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$A_{s_{min.}} = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1900 = 2276.5 \text{ mm}^2 \quad \left. \begin{array}{l} \text{الأقل} \\ 1.3 A_{s_{req.}} = 1.3 * 1899.9 = 2470 \text{ mm}^2 \end{array} \right\} = 2276.5 \text{ mm}^2 \quad (5 \phi 25)$$

Sec. ③

$$M = 990 \text{ kN.m} , P = 52.1 * 1.5 = 78.15 \text{ kN} , b = 350 \text{ mm}$$

$$d_o = 3.5 \sqrt{\frac{990 * 10^6}{30 * 350}} = 1074.71 \text{ mm (as R-Sec.)}$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1074.71) = (1182.18 \rightarrow 1397.12) \text{ mm}$$

$$\text{Take } d = 1200 \text{ mm} , t = 1200 + 100 = 1300 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{78.15 * 10^3}{30 * 350 * 1300} = 0.0057 < 0.04 \therefore (\text{neglect } P)$$

$$\therefore \text{Take } d = d_o = 1074.71 \text{ mm}$$

$$\therefore \text{Take } d = 1100 \text{ mm} , t = 1200 \text{ mm}$$

$$\therefore C_1 = 3.50 \rightarrow J = 0.78$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{990 * 10^6}{0.780 * 360 * 1074.71} = 3280.55 \text{ mm}^2$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 3280.55 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1100 = 1317.9 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 3280.55 \text{ mm}^2 \quad (7 \phi 25)$$

Sec. ④

$$M = 548.43 \text{ kN.m} , T = 54.10 * 1.5 = 81.15 \text{ kN}$$

$$, b = 350 \text{ mm} , t = 1200 \text{ mm} = \text{The same depth of Sec. ③}$$

$$e = \frac{M}{T} = \frac{548.43}{81.15} = 6.758 \text{ m}$$

$$\therefore \frac{e}{t} = \frac{6.758}{1.2} = 5.63 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e - \frac{t}{2} + c = 6.758 - \frac{1.20}{2} + 0.10 = 6.258 \text{ m}$$

$$M_s = T * e_s = 81.15 * 6.258 = 507.83 \text{ kN.m}$$

$$\therefore 1100 = c_1 \sqrt{\frac{M_s}{F_{cu} b}} = c_1 \sqrt{\frac{507.83 * 10^6}{30 * 350}} \rightarrow c_1 = 5.0 \rightarrow J = 0.826$$

$$\begin{aligned} \therefore A_s &= \frac{M_s}{J F_y d} + \frac{T_{u.l.}}{(F_y \setminus \delta_s)} \\ &= \frac{507.83 * 10^6}{0.826 * 360 * 1100} + \frac{81.15 * 10^3}{(360 \setminus 1.15)} = 1811.7 \text{ mm}^2 \end{aligned}$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1811.7 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{360} \right) 350 * 1100 = 1317.9 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1811.7 \text{ mm}^2 \quad (4 \phi 25)$$

Sec. ⑤ (350 * 1000)

Axially Loaded Column. $P = 894.32 * 1.5 = 1341.48 \text{ kN}$

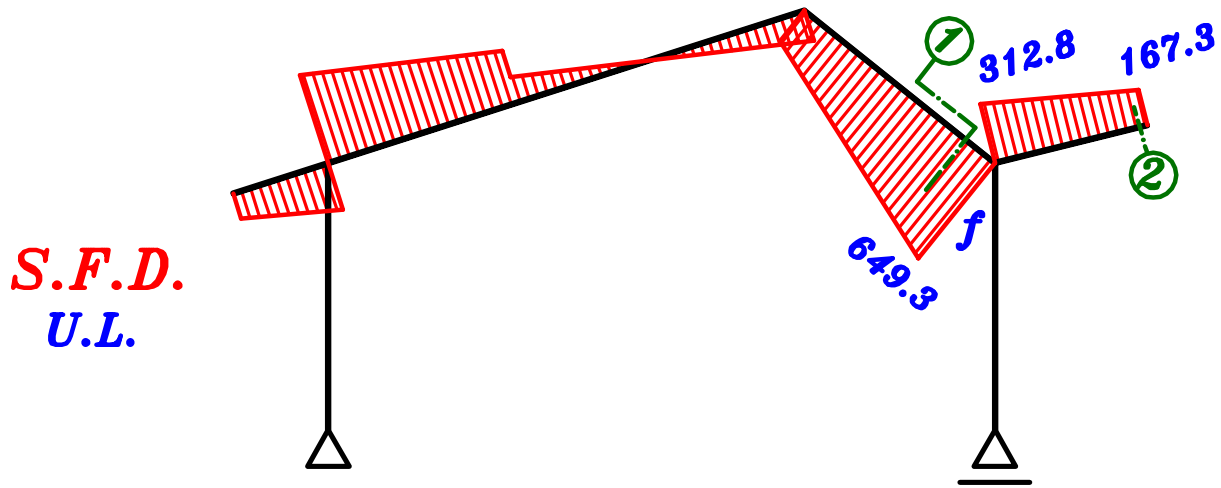
$$\therefore P_{u.l.} = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

$$\therefore 1341.48 * 10^3 = 0.35 (350 * 1000) (30) + 0.67 A_s (360)$$

$$\therefore A_s = -9674 \text{ mm}^2 = (-Ve) \text{ Value}$$

$$\therefore A_s = A_{s_{min.}} = \frac{0.8}{100} * 350 * 1000 = 2800 \text{ mm}^2 \quad (12 \phi 18)$$

4- Check shear stresses at joint (f)



– Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{30}{1.5}} = 3.0 \text{ N/mm}^2$$

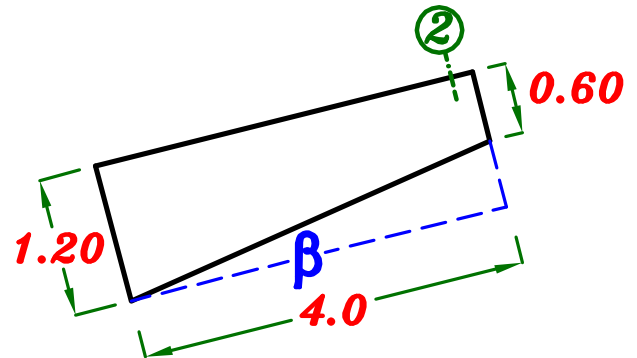
Sec. ① $Q = 649.3 \text{ kN}$ $b = 350 \text{ mm}$, $b = 1900 \text{ mm}$

$$\therefore q_u = \frac{Q}{b d} = \frac{649.3 * 10^3}{350 * 1900} = 0.97 \text{ N/mm}^2$$

$\therefore q_{cu} > q_u$ \therefore Use min. Stirrups $5 \phi 8 \text{ m}^2 2 b$

Sec. ②

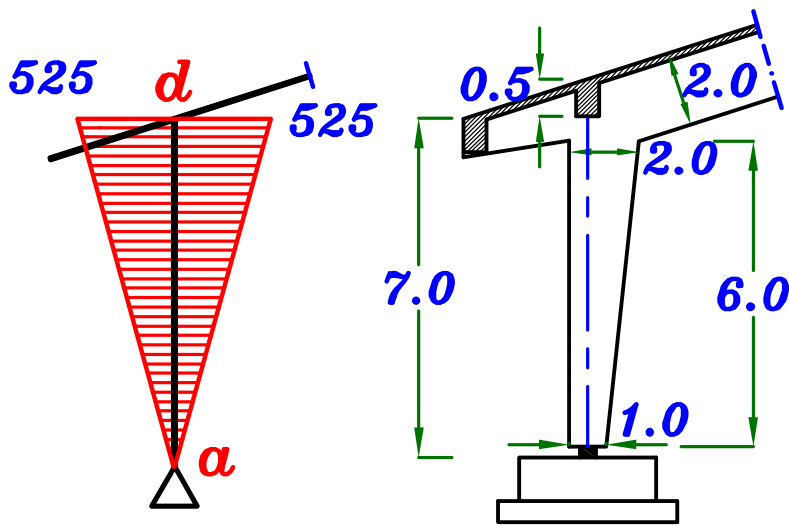
$$q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$



$$q_u = \frac{167.3 * 10^3}{350 * 550} - \text{zero} = 0.87 \text{ N/mm}^2$$

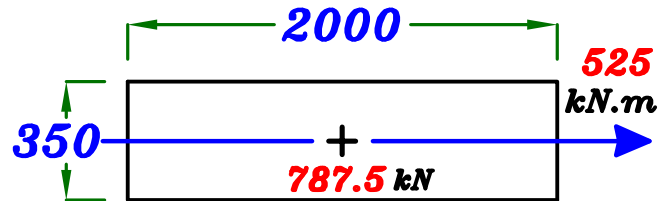
$\therefore q_{cu} > q_u$ \therefore Use min. Stirrups $5 \phi 8 \text{ m}^2 2 b$

5- Consider the effect of buckling condition in the design of column (a-d).



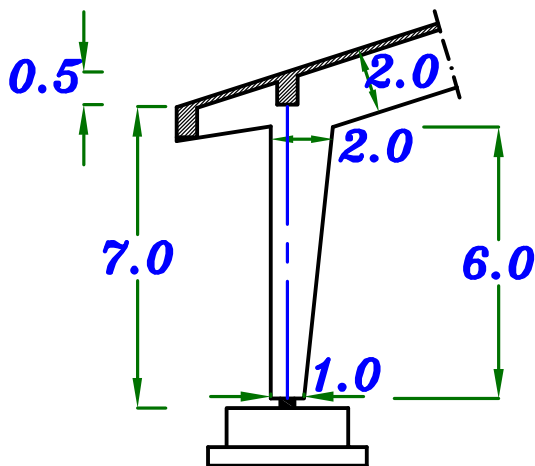
$$M_{ext.} = 525 \text{ kN.m}$$

$$P = 525 * 1.5 = 787.5 \text{ kN}$$



Check Buckling.

① In plane.



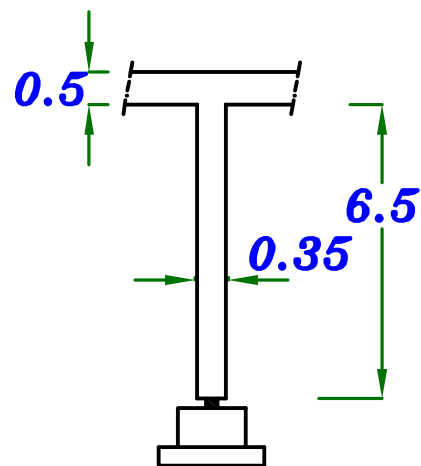
Upper Case ① }
Lower Case ③ } $k = 1.6$

$$H_o = 6.0 \text{ m}$$

$$\lambda_{b_{in}} = \frac{1.6 * 6.0}{2.0} = 4.80 < 10$$

Short Col.

② Out of plane.



Upper Case ① }
Lower Case ③ } $k = 1.6$

$$H_o = 6.50 \text{ m}$$

$$\lambda_{b_{out}} = \frac{1.6 * 6.5}{0.35} = 29.7 > 23$$

Unsafe Buckling

Increase $b \rightarrow b = 0.50 \text{ m}$

$$\lambda_{b_{out}} = \frac{1.6 * 6.5}{0.50} = 20.8 > 10$$

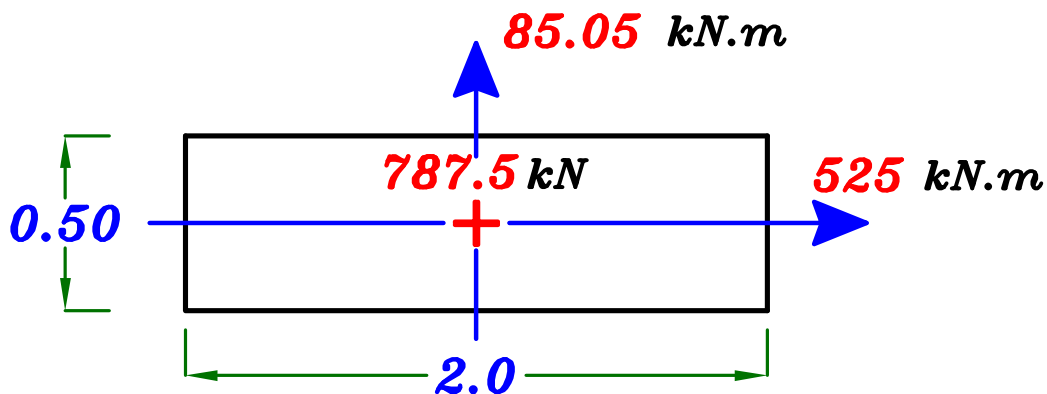
Long Col.

Take the bigger value of $\lambda_b = 20.8$ (Out of plane)

The Buckling Out of plane.

$$\delta = \frac{(\lambda_b)^2 * b}{2000} = \frac{20.8^2 * 0.50}{2000} = 0.108 \text{ m}$$

$$M_{add.} = P * \delta = 787.5 * 0.108 = 85.05 \text{ kN.m}$$



Using Bi-axial I.D.

assume $\zeta = 0.90$ ----- ECCS لا توجد قيمه غيرها فى ال

$$R_b = \frac{P}{F_{cu} b t} = \frac{787.5 * 10^3}{30 * 500 * 2000} = 0.026 \rightarrow R_b = 0.30$$

ECCS Design Aids Page 5-13

$$\left. \begin{aligned} \frac{M_x}{F_{cu} b t^2} &= \frac{85.05 * 10^6}{30 * 2000 * 500^2} = 0.0056 \\ \frac{M_y}{F_{cu} t b^2} &= \frac{525.0 * 10^6}{30 * 500 * 2000^2} = 0.0087 \end{aligned} \right\} \rho < 1.0$$

Take $\rho = 1.0$

$$\mu = \rho * F_{cu} * 10^{-4} = 1.0 * 30 * 10^{-4} = 0.003$$

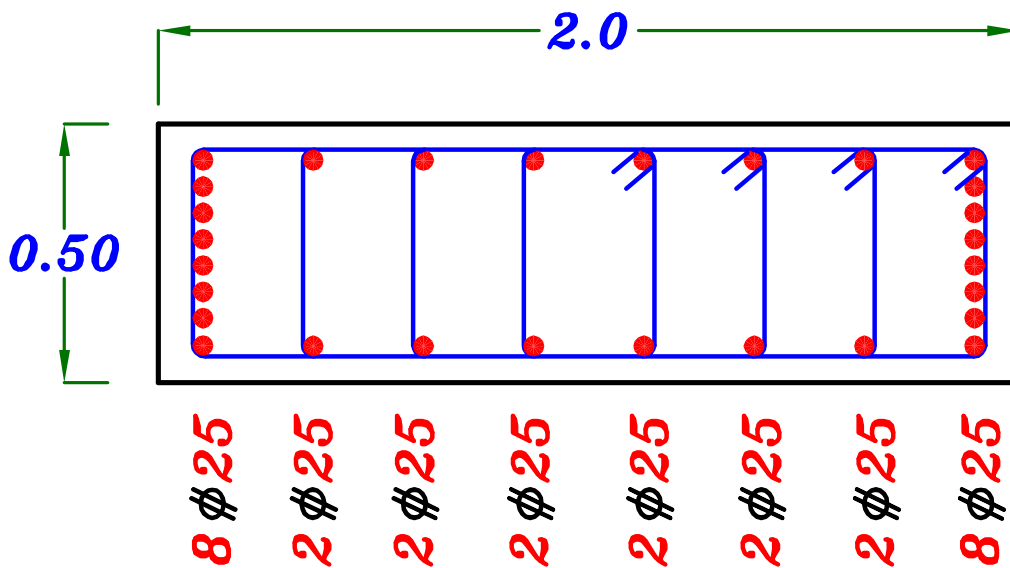
$$A_{total} = \mu * b * t = 0.003 * 500 * 2000 = 3000 \text{ mm}^2$$

$$A_{s_{min}} = \frac{0.25 + 0.052 \lambda_{max}}{100} * b * t$$

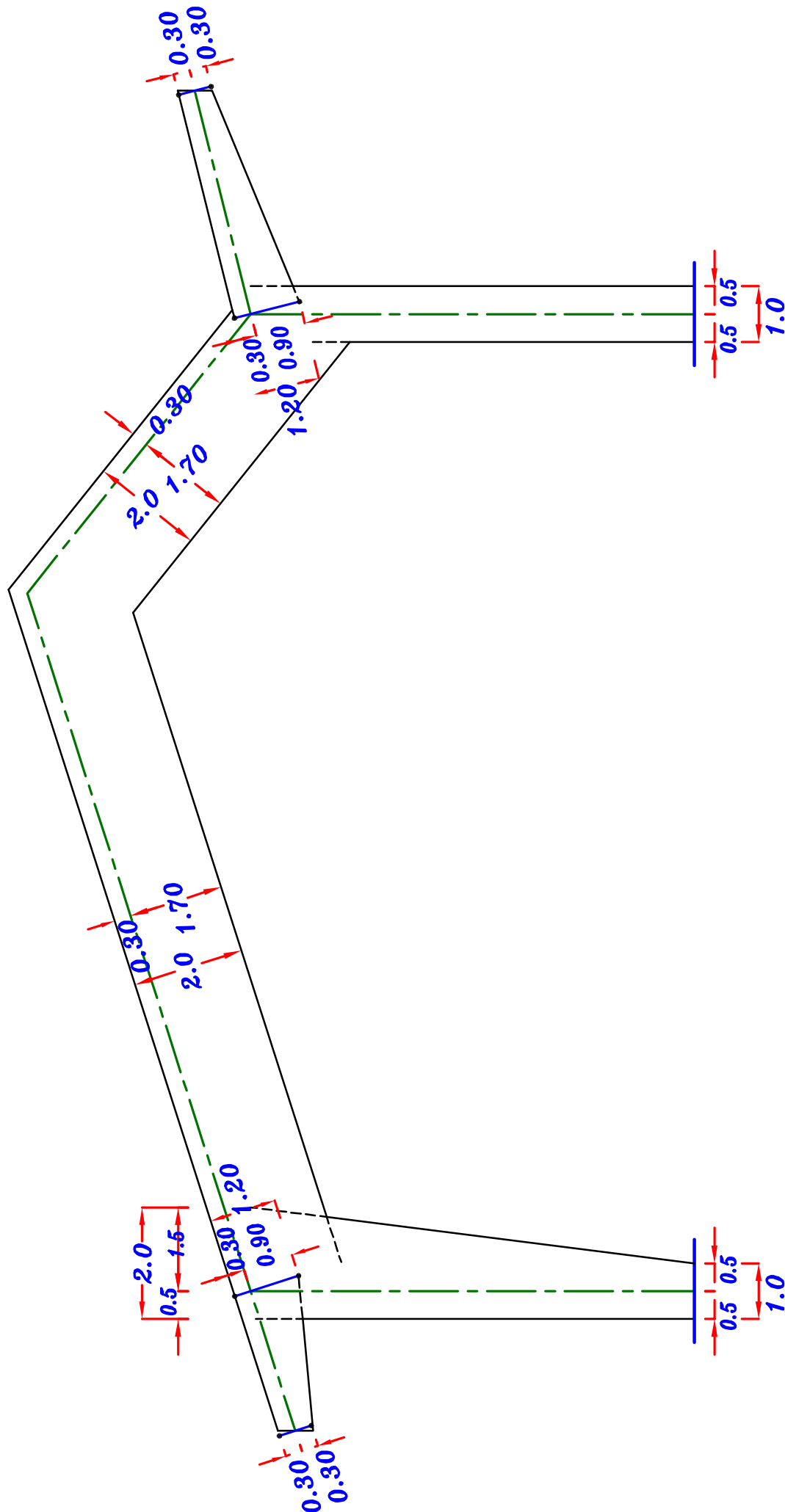
$$= \frac{0.25 + 0.052 (20.8)}{100} * 500 * 2000 = 13316 \text{ mm}^2 > A_{s_{total}}$$

Take $A_s = A_{s_{min}} = 13316 \text{ mm}^2$ **28 ϕ 25**

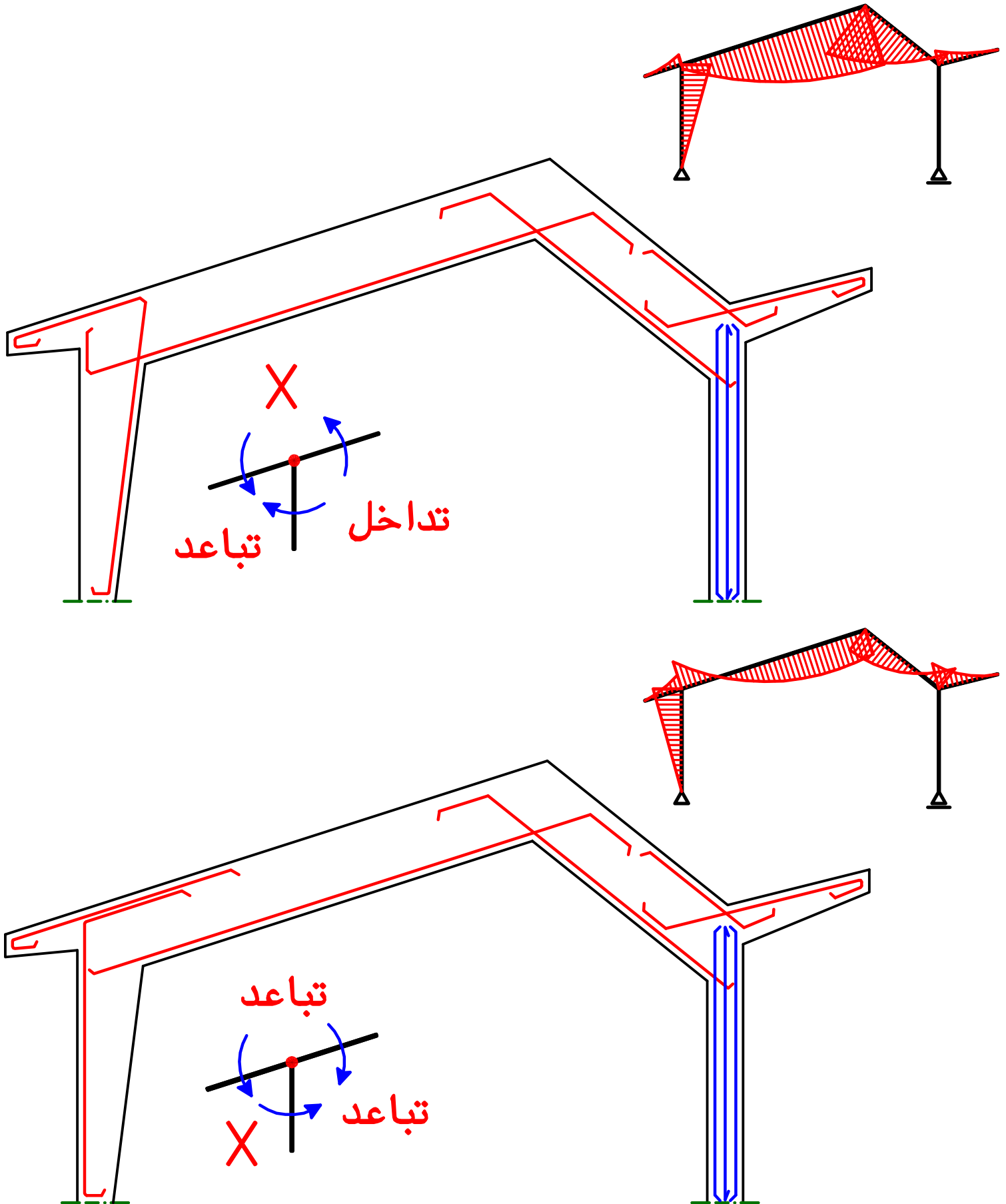
توزع ٤ أسياخ فى الاركان و الباقي يوزع على الاربعه جهات .

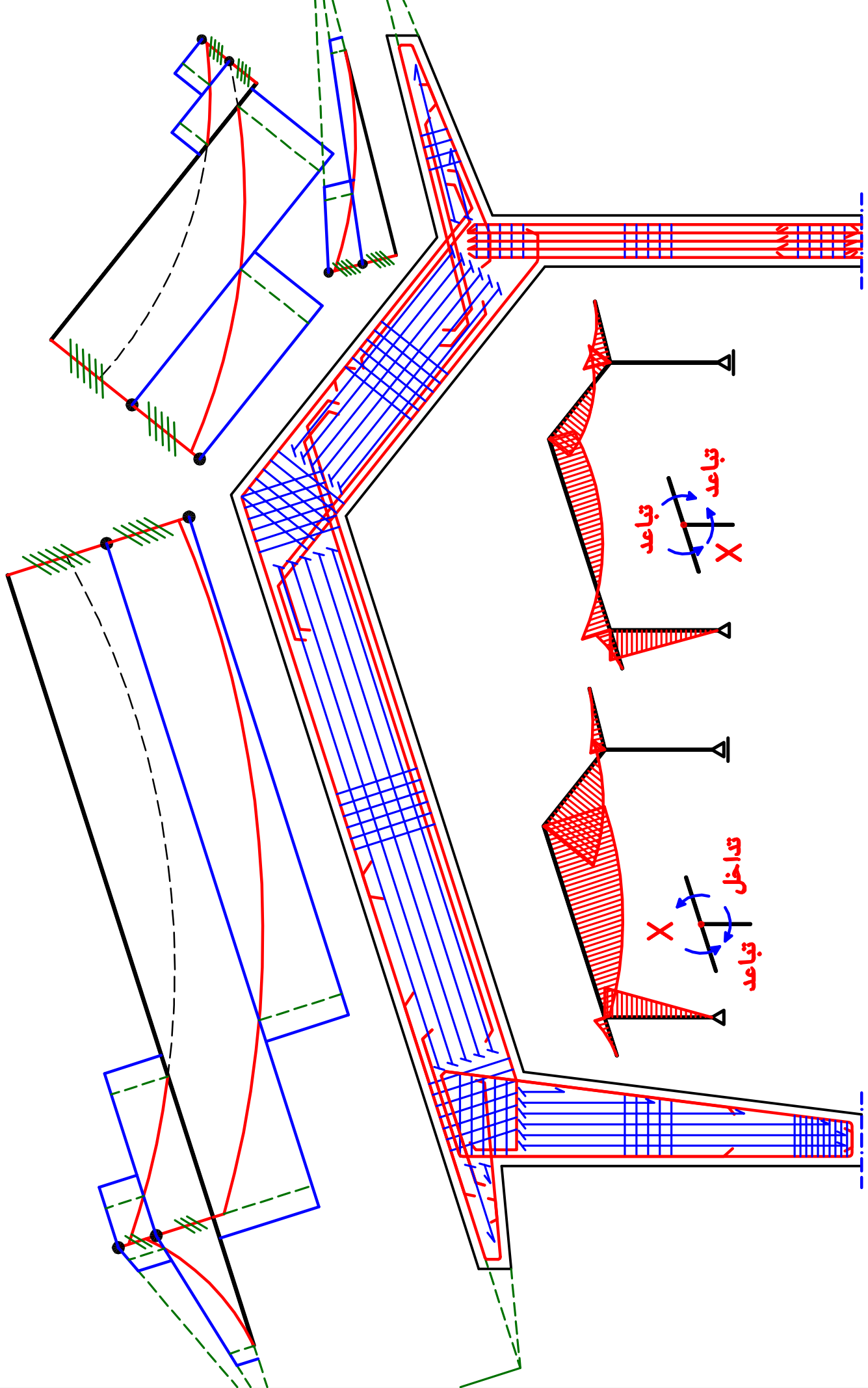


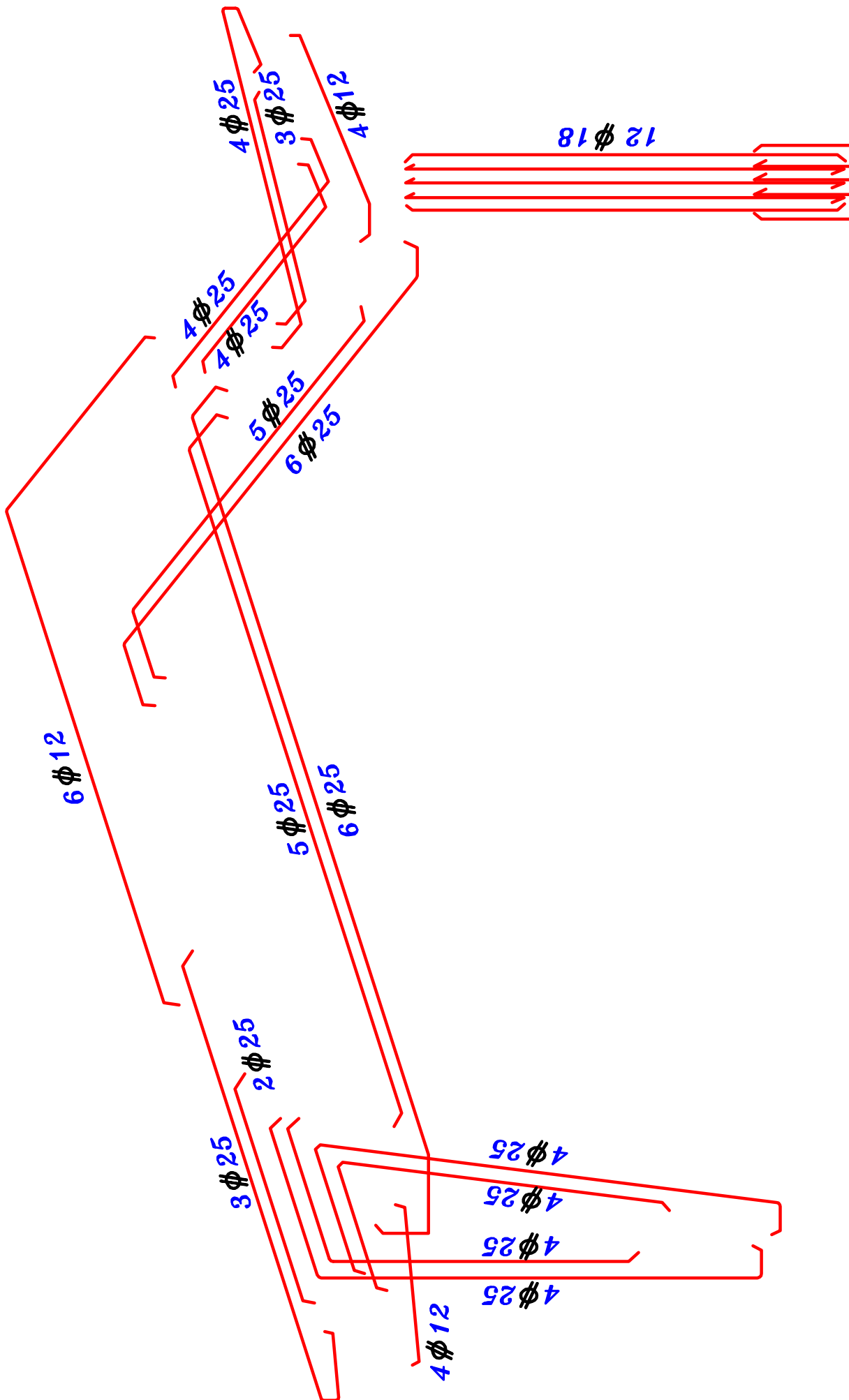
6– Draw the details of reinforcement For the Frame, considering **the moment of resistance principle** For girder part (**c-d-e-f-g**) in elevation (to scale **1:50**) and cross section (to scale **1:20**).



لا نرسم التسليح على شكل الـ *max-max B.M.D.* ولكن نرسم التسليح لاي حالة تحميل أولا ثم نكمل التسليح من حالة التحميل الاخرى







Example.

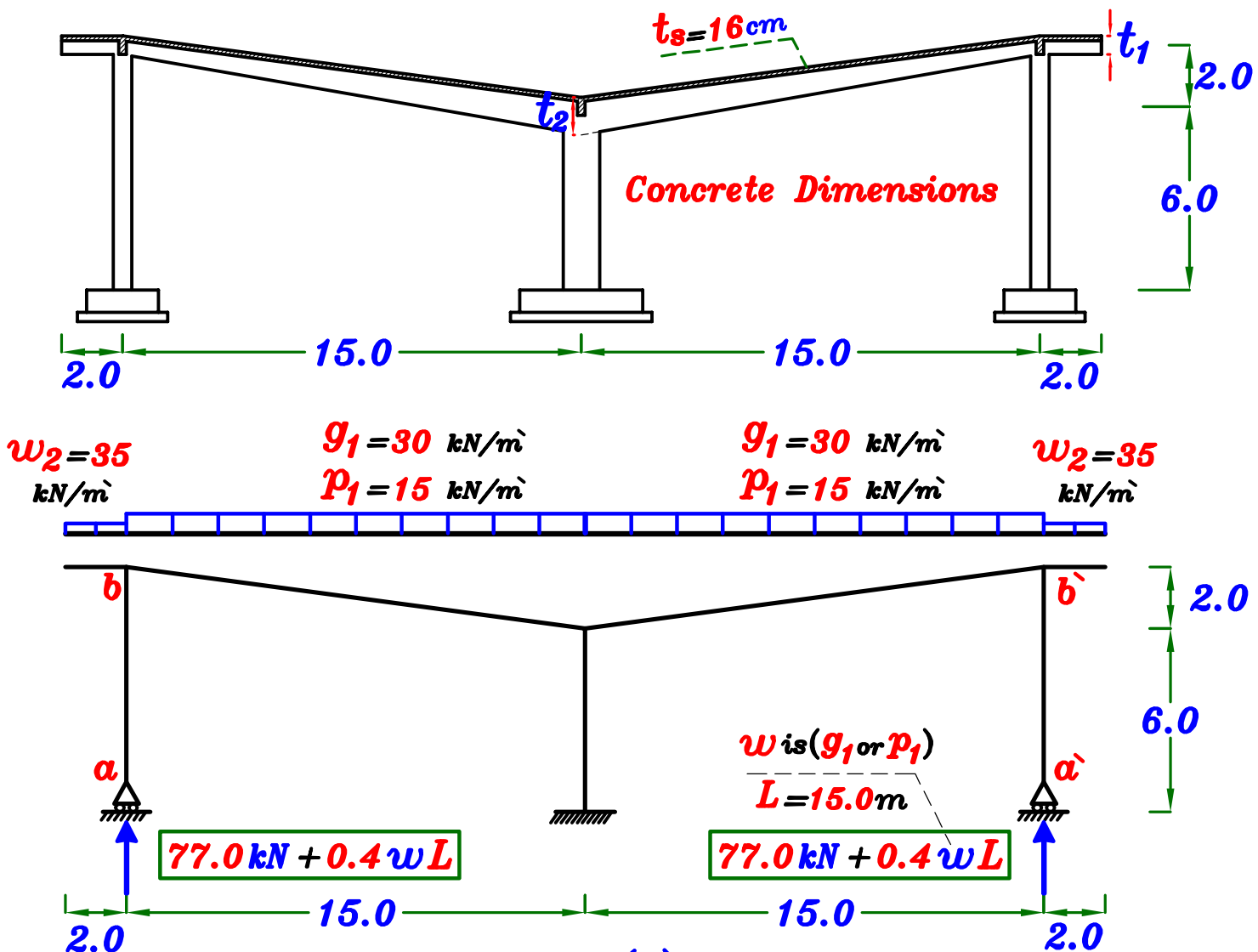
Fig.(1) shows concrete dimensions and statical system of a Frame in an industrial building. The interior spans of the Frame are subjected to dead and live loads equal to **30, 15 kN/m** respectively while the external cantilevers are subjected to total load equal to **35 kN/m**

It is required to :

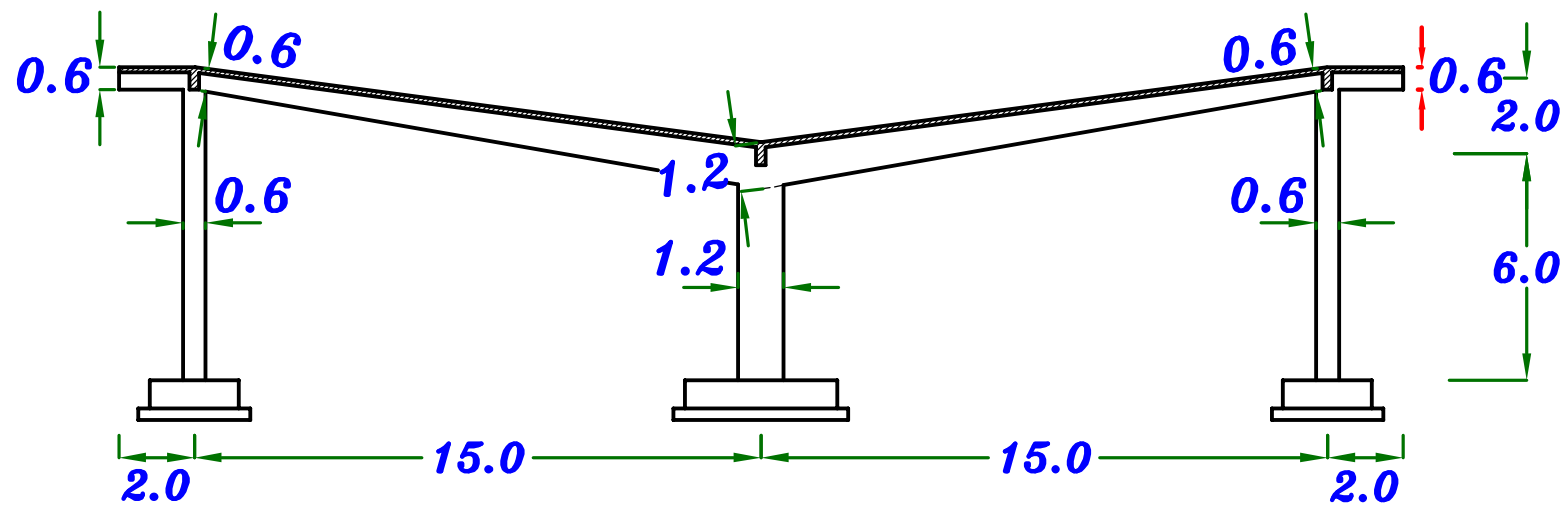
- 1- Estimate the concrete dimensions For all elements of the Frame.
- 2- Draw the absolute (**max-max**) Bending Moment Diagram.
- 3- Draw the Normal Force and Shear Force Diagrams (**Case of total load only**).
- 4- Design the critical sections of the Frame For bending and/or normal Force.
- 5- Check shear stresses at the critical sections.
- 6- Design column (**a-b**) as a braced column.
- 7- Draw the concrete dimensions and the details of reinforcement in elevation and cross-sections to an appropriate scale.

Use: **$F_{cu} = 35 \text{ MPa}$** , **Steel 36/52** , **$b = 350 \text{ mm}$** , **Frame spacing = 5.0 m**

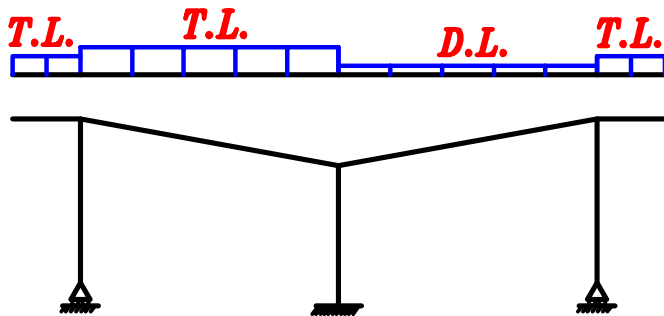
Given Loads are working loads.



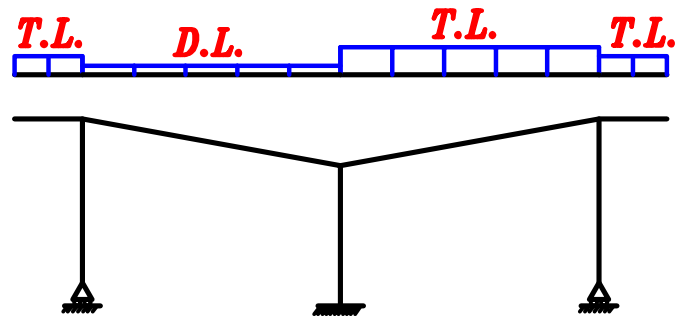
1- Estimate the concrete dimensions For all elements of the Frame.



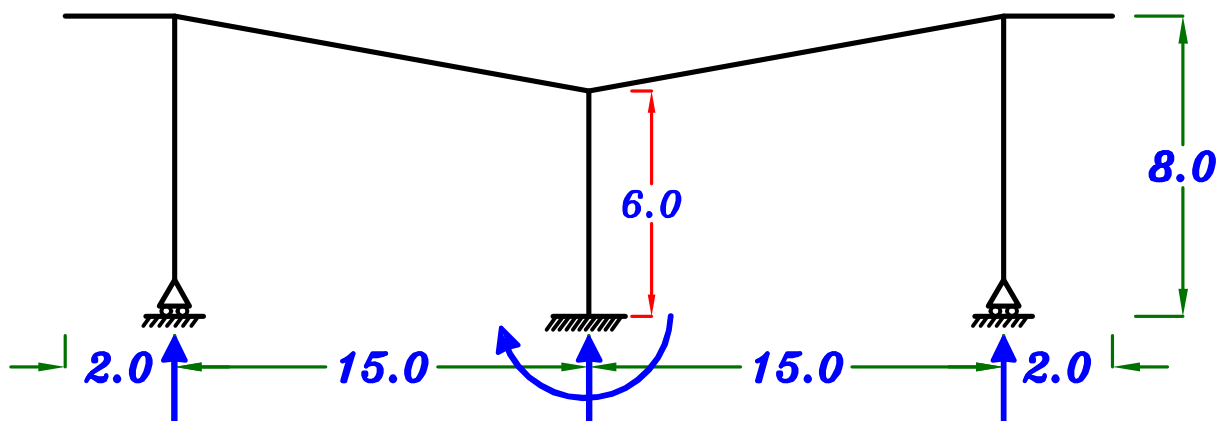
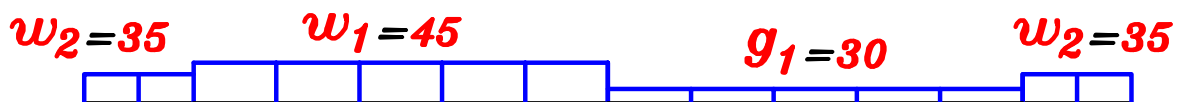
2- Draw the absolute (*max-max*) Bending Moment Diagram.



Case ①



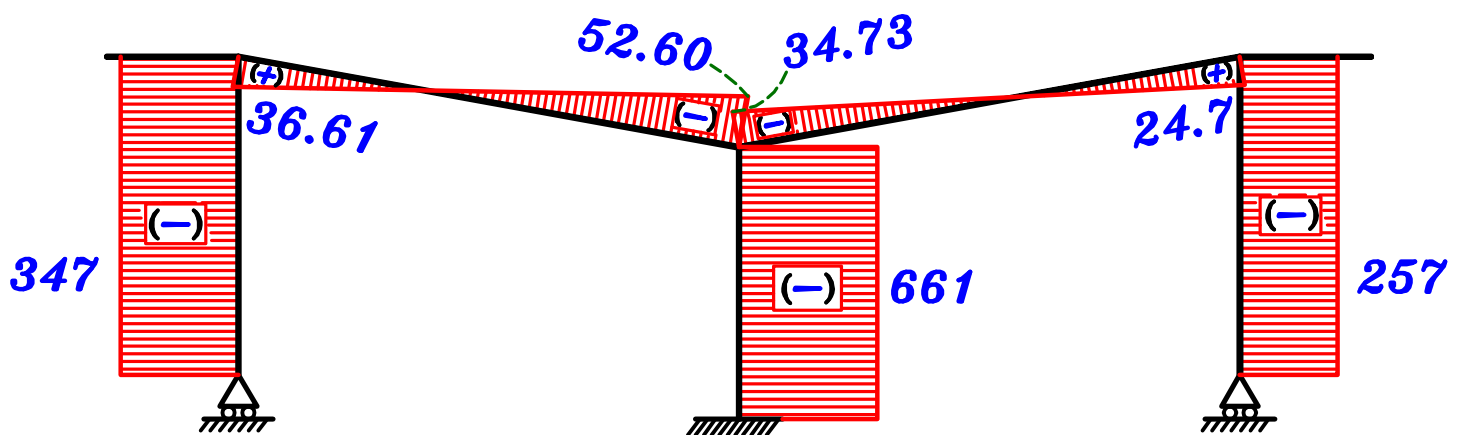
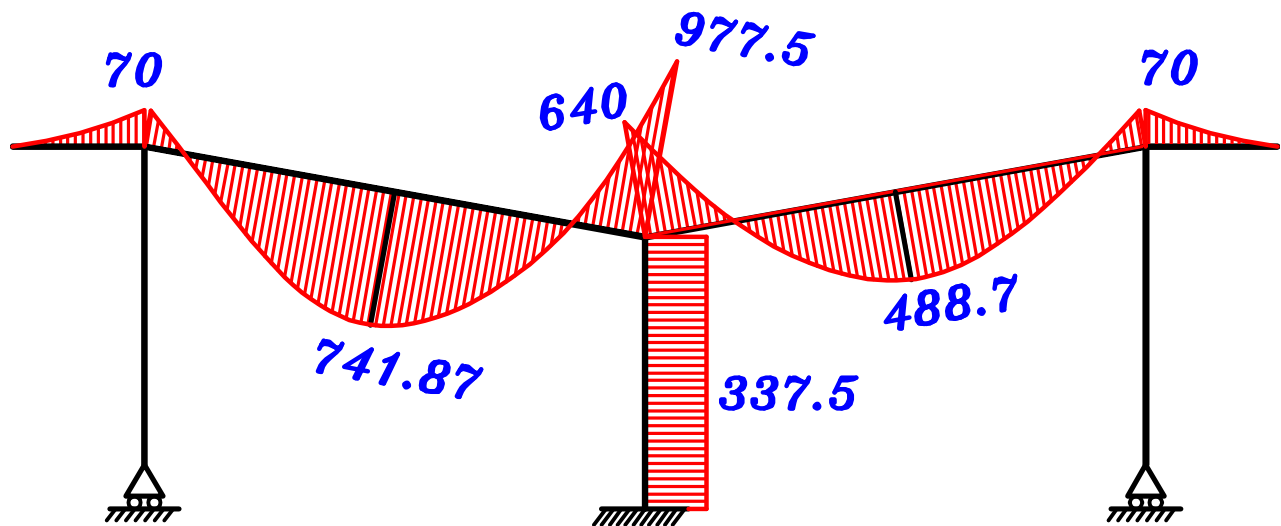
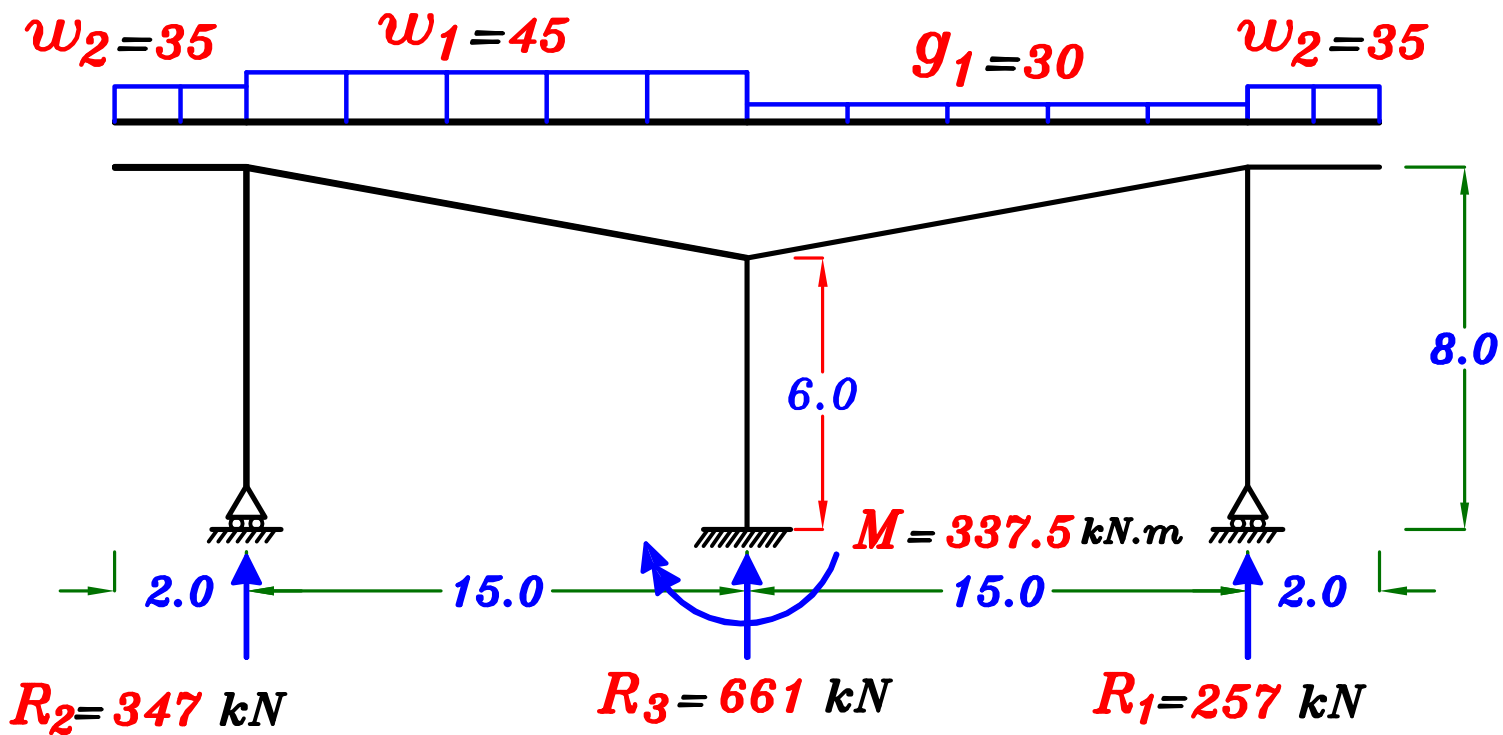
Case ②

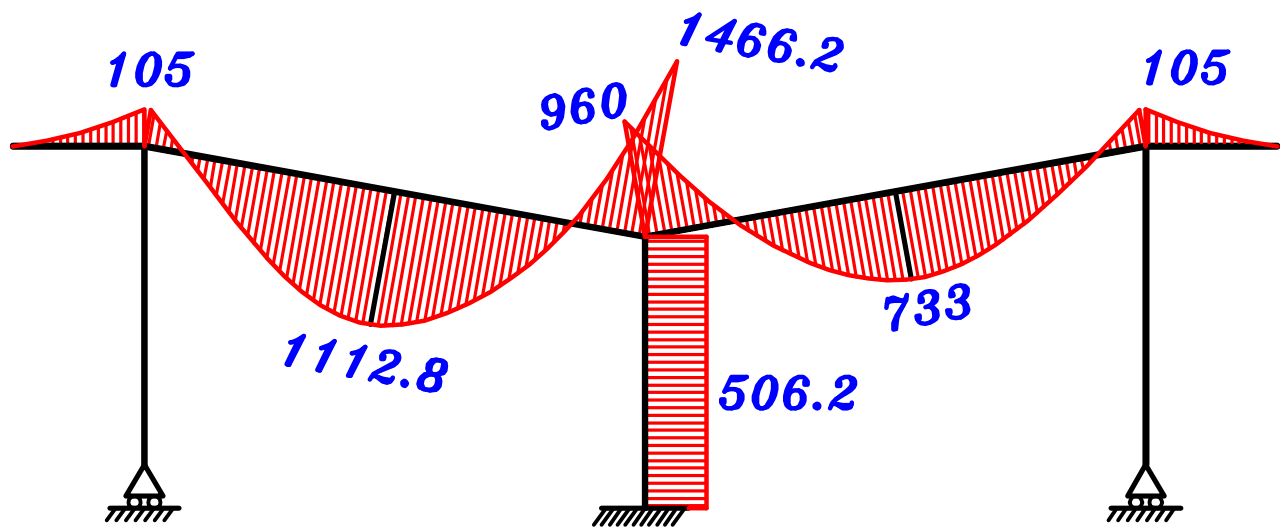


$$\begin{aligned} R_2 &= 77 + 0.4 w_1 L \\ &= 77 + 0.4 (45) (15) \\ &= 347 \text{ kN} \end{aligned}$$

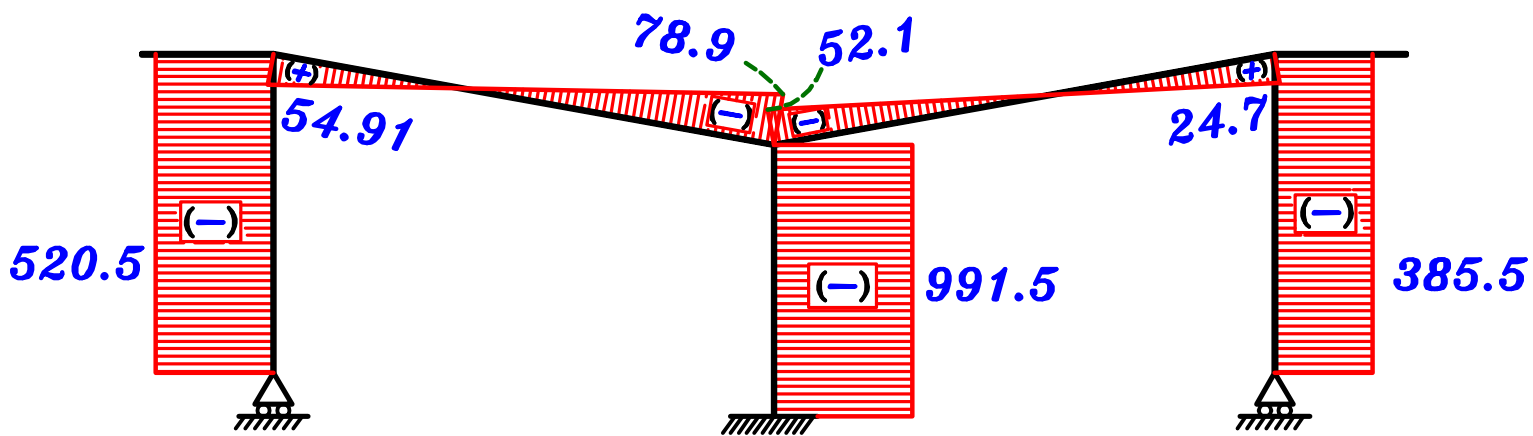
$$\begin{aligned} \sum Y &= \text{Zero} \\ R_3 &= 661 \text{ kN} \end{aligned}$$

$$\begin{aligned} R_1 &= 77 + 0.4 g_1 L \\ &= 77 + 0.4 (30) (15) \\ &= 257 \text{ kN} \end{aligned}$$



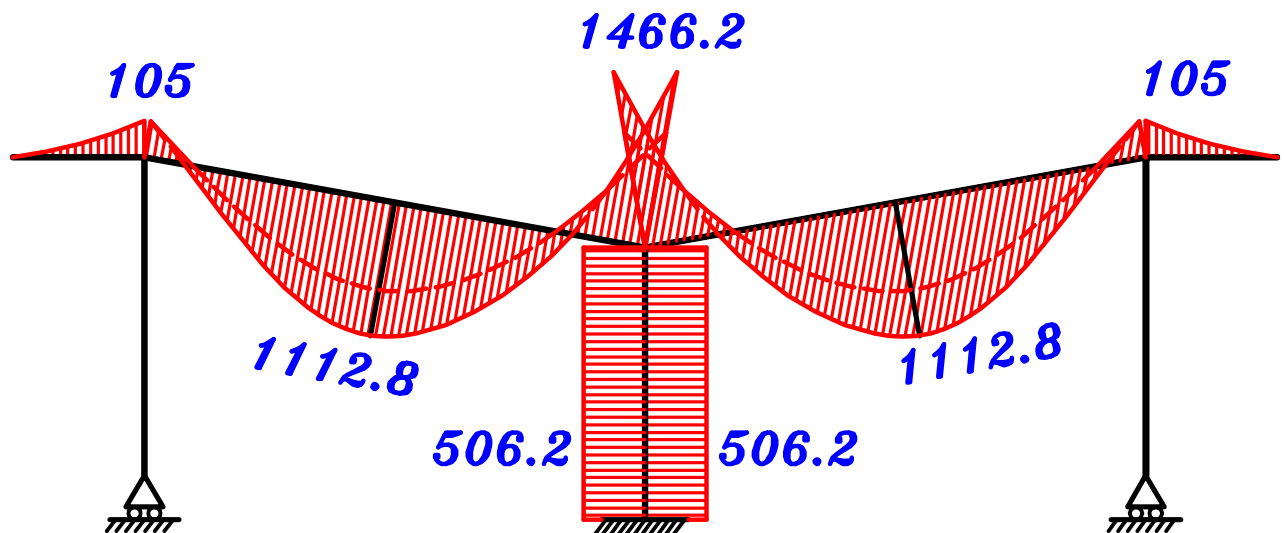


B.M.D. (U.L.)

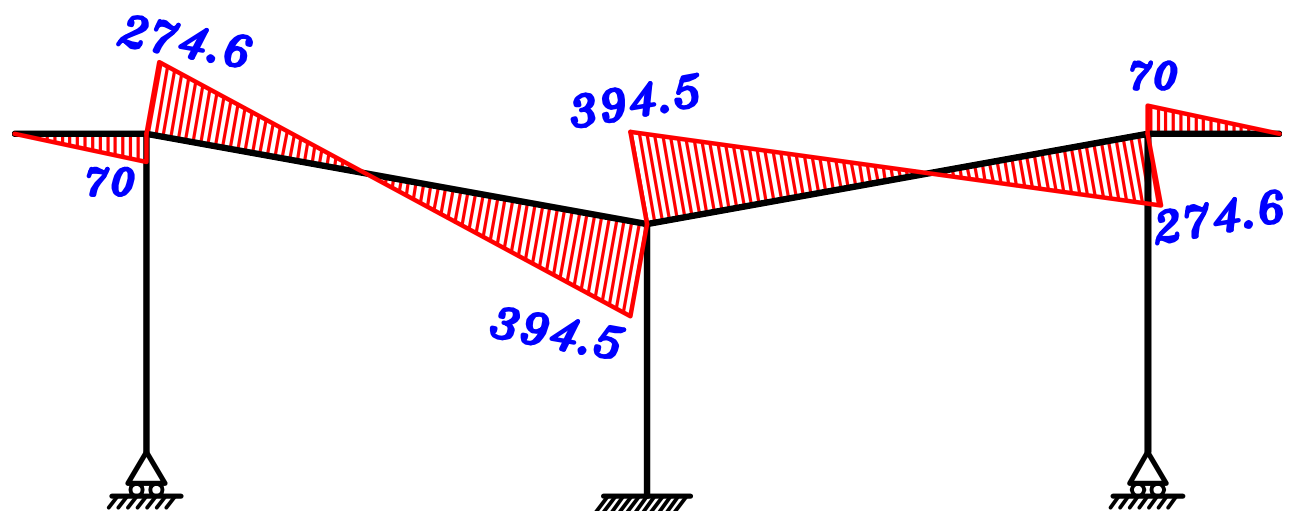
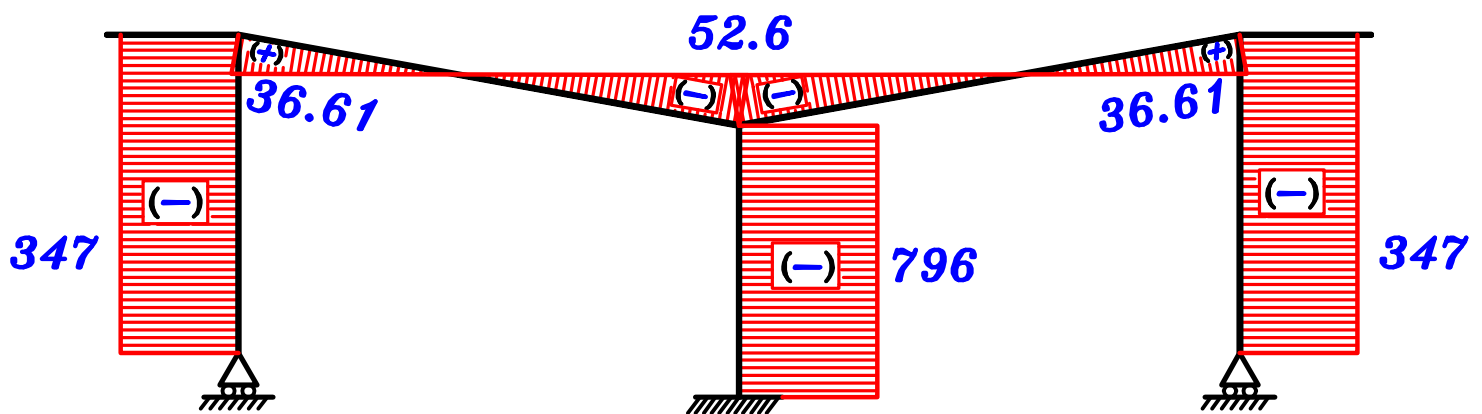
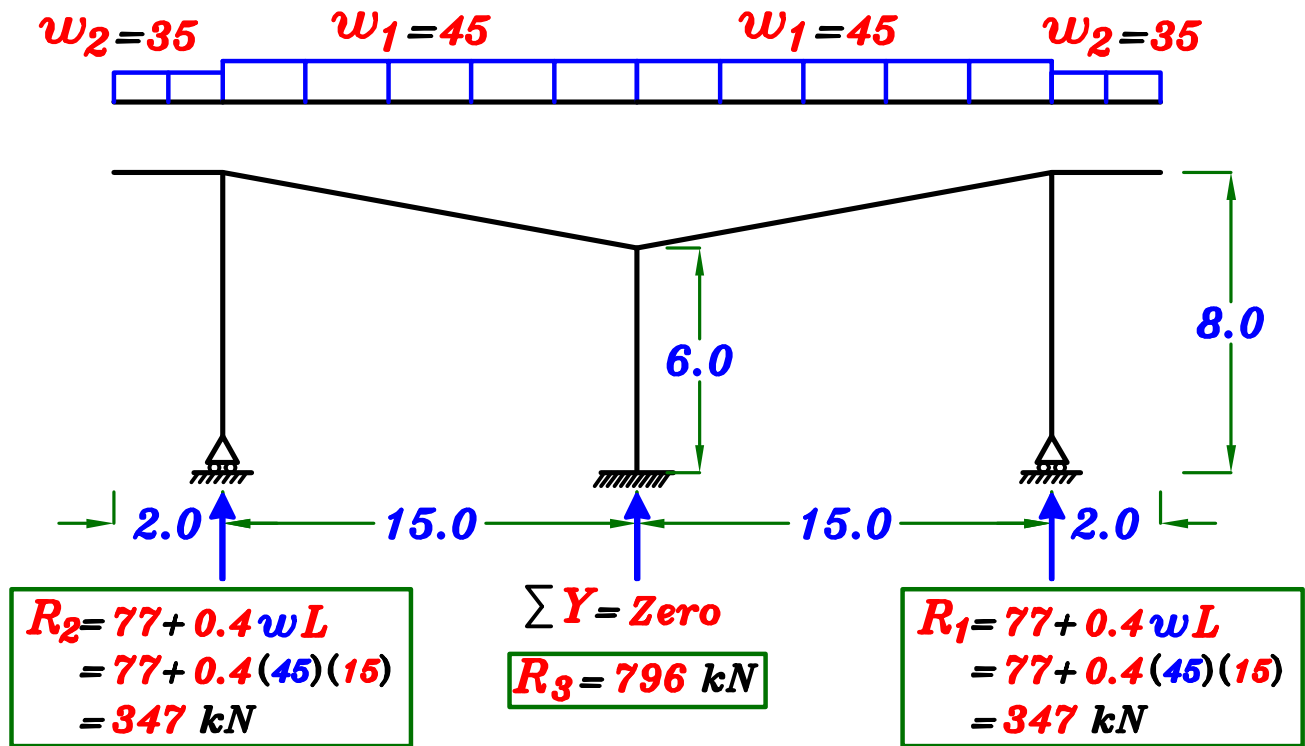


N.F.D. (U.L.)

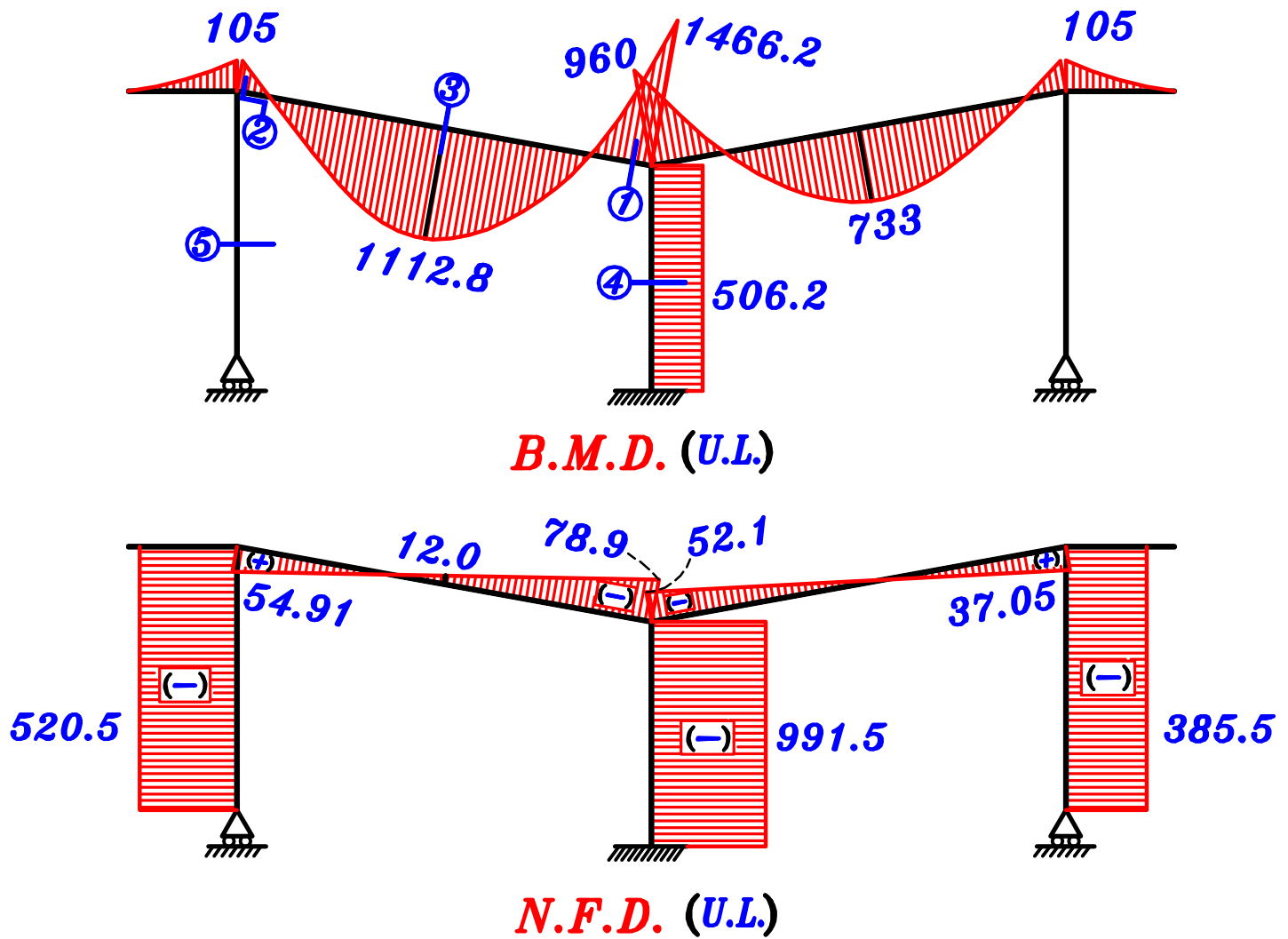
max-max B.M.D. (U.L.)



3- Draw the Normal Force and Shear Force Diagrams (Case of total load only).



4- Design the critical sections of the Frame For bending and/or normal Force.



Sec. ① $M = 1466.2 \text{ kN.m}$, $P = 78.9 \text{ kN}$, $b = 350 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{1466.2 \cdot 10^6}{35 \cdot 350}} = 1210.9 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (1210.9) = (1332 \rightarrow 1574.1) \text{ mm}$$

$$\text{Take } d = 1400 \text{ mm} , \quad t = 1400 + 100 = 1500 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{78.9 \cdot 10^3}{35 \cdot 350 \cdot 1500} = 0.004 < 0.04 \quad \therefore (\text{neglect } P)$$

$$\therefore \text{Take } d = d_o = 1210.9 \text{ mm}$$

$$\therefore \text{Take } \boxed{d = 1300 \text{ mm}} , \quad \boxed{t = 1400 \text{ mm}}$$

$$\therefore C_1 = 3.50 \longrightarrow J = 0.78$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1466.2 * 10^6}{0.780 * 360 * 1210.9} = 4312.1 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 4312.1 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{35}}{360} \right) 350 * 1300 = 1682.3 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 4312.1 \text{ mm}^2 \quad \textcircled{9 \phi 25}$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{350 - 25}{25 + 25} = 6.50 = 6.0 \text{ bars}$$

Sec. ② $M = 105 \text{ kN.m}$, $T = 54.91 \text{ kN}$, $b = 350 \text{ mm}$

$$d_o = 3.5 \sqrt{\frac{105 * 10^6}{35 * 350}} = 324.0 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (0.9 \rightarrow 1.0) d_o = (0.9 \rightarrow 1.0) (324.0) = (291.6 \rightarrow 324.0) \text{ mm} < \frac{t}{2}$$

$$t_1 = \frac{t}{2} = \frac{1400}{2} = 700 \quad \boxed{d = 650 \text{ mm}} , \quad \boxed{t = 700 \text{ mm}}$$

$$e = \frac{M}{T} = \frac{105}{54.91} = 1.91 \text{ m} \therefore \frac{e}{t} = \frac{1.91}{0.7} = 2.73 > 0.5 \xrightarrow{\text{Use}} e_s$$

$$e_s = e - \frac{t}{2} + c = 1.91 - \frac{0.70}{2} + 0.05 = 1.61 \text{ m}$$

$$M_s = T * e_s = 54.91 * 1.61 = 88.40 \text{ kN.m}$$

$$\therefore 650 = C_1 \sqrt{\frac{88.40 * 10^6}{35 * 350}} \longrightarrow C_1 = 7.65 \longrightarrow J = 0.826$$

$$\therefore A_s = \frac{M_s}{J F_y d} + \frac{T_{u.l.}}{(F_y \setminus \delta_s)}$$

$$= \frac{88.40 * 10^6}{0.826 * 360 * 650} + \frac{54.91 * 10^3}{(360 \setminus 1.15)} = 632.76 \text{ mm}^2$$

Check $A_{s_{min}}$ $A_{s_{req.}} = 632.76 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{35}}{360} \right) 350 * 650 = 841.2 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

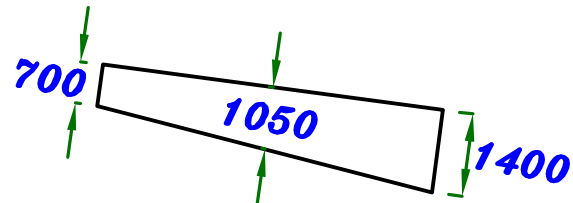
$$A_{s_{min.}} = \left(0.225 * \frac{\sqrt{25}}{360} \right) 350 * 650 = 841.2 \text{ mm}^2$$

$$1.3 A_{s_{req.}} = 1.3 * 632.76 = 822.6 \text{ mm}^2$$

الأقل } = 822.6 \text{ mm}^2 \quad (2 \phi 25)

Sec. ③ $M = 1112.8 \text{ kN.m}$, $P = 12.0 \text{ kN}$

, $b = 350 \text{ mm}$, $t = 1050 \text{ mm}$

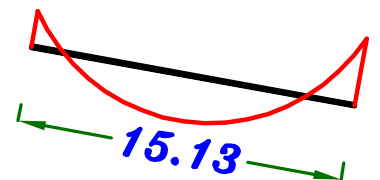


Check $\frac{P}{F_{cu} b t} = \frac{12.0 * 10^3}{35 * 350 * 1050} = 0.0093 < 0.04$ (Neglect P)

The sec. will be T-sec.

$$B = \left\{ \begin{array}{l} \text{C.L. - C.L.} = \text{Spacing} = 5.0 \text{ m} = 5000 \text{ mm} \\ 16 t_s + b = 16 * 160 + 350 = 2910 \text{ mm} \\ K \frac{L}{5} + b = 0.7 * \frac{15130}{5} + 350 = 2468 \text{ mm} \end{array} \right\}$$

$B = 2468 \text{ mm}$



$$\therefore d = c_1 \sqrt{\frac{M_{u.l.}}{F_{cu} B}} \quad \therefore 950 = c_1 \sqrt{\frac{1112.8 * 10^6}{35 * 2468}} \rightarrow c_1 = 8.36 \rightarrow J = 0.826$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1112.8 * 10^6}{0.826 * 360 * 950} = 3939.2 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 3939.2 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{35}}{360} \right) 350 * 950 = 1229.4 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 3939.2 \text{ mm}^2 \quad (9 \phi 25)$$

Sec. ④ R-Sec. $M = 506.2 \text{ kN.m}$, $P = 991.5 \text{ kN}$

$$d_o = 3.5 \sqrt{\frac{506.2 * 10^6}{35 * 350}} = 711.5 \text{ mm} \quad (\text{as R-Sec.})$$

$$d = (1.1 \rightarrow 1.3) d_o = (1.1 \rightarrow 1.3) (711.5) = (782.6 \rightarrow 924.9) \text{ mm}$$

$$\therefore \text{Take } d = 850 \text{ mm} , t = 850 + 50 = 900 \text{ mm}$$

$$\therefore t_{(Column)} < 0.8 t_{(Beam)} \xrightarrow{\text{Take}} t_{(Column)} = t_{(Beam)} = 1400 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{991.5 * 10^3}{35 * 350 * 1400} = 0.057 > 0.04 \therefore (\text{Don't neglect } P)$$

\therefore Design the Sec. on both N.F. & B.M.

$$e = \frac{M}{P} = \frac{506.2}{991.5} = 0.51 \text{ m} \therefore \frac{e}{t} = \frac{0.51}{1.40} = 0.36 < 0.5 \xrightarrow{\text{Use}} \text{I.D.}$$

\therefore Use Interaction Diagram

$$\zeta = \frac{1400 - 200}{1400} = 0.85 = 0.80 \xrightarrow{\text{use}} \text{ECCS Design Aids Page 4-24}$$

$$\left. \begin{aligned} \frac{P_u}{F_{cu} b t} &= \frac{991.5 * 10^3}{35 * 350 * 1400} = 0.057 \\ \frac{M_u}{F_{cu} b t^2} &= \frac{506.2 * 10^6}{35 * 350 * 1400^2} = 0.02 \end{aligned} \right\} \rho < 1.0 \xrightarrow{\text{Take}} \rho = 1.0$$

$$\mu = \rho * F_{cu} * 10^{-4} = 1.0 * 35 * 10^{-4} = 3.5 * 10^{-3}$$

$$A_s = A_{s'} = \mu * b * t = 3.5 * 10^{-3} * 350 * 1400 = 1715 \text{ mm}^2$$

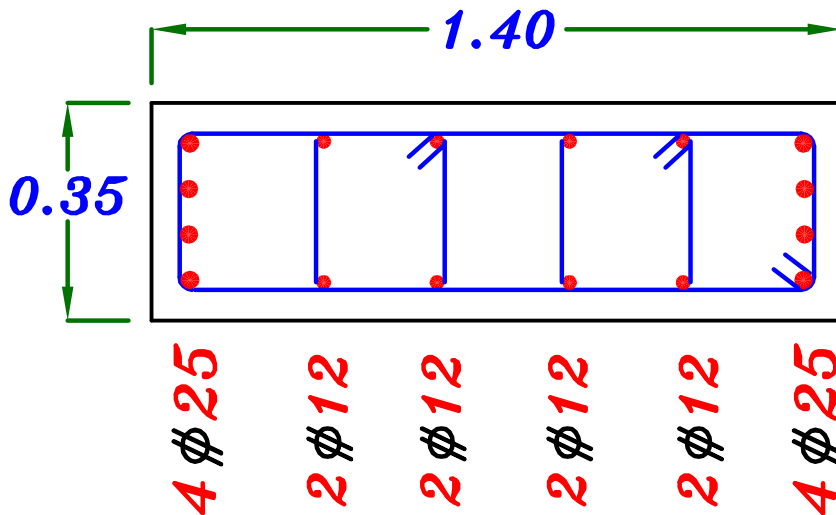
– Check $A_{s_{min.}} = \frac{0.8}{100} * b * t = \frac{0.8}{100} * 350 * 1400 = 3920 \text{ mm}^2$

$$A_{s_{Total}} = A_s + A_{s'} = 2 * 1715 = 3430 \text{ mm}^2 \therefore A_{s_{Total}} > A_{s_{min.}}$$

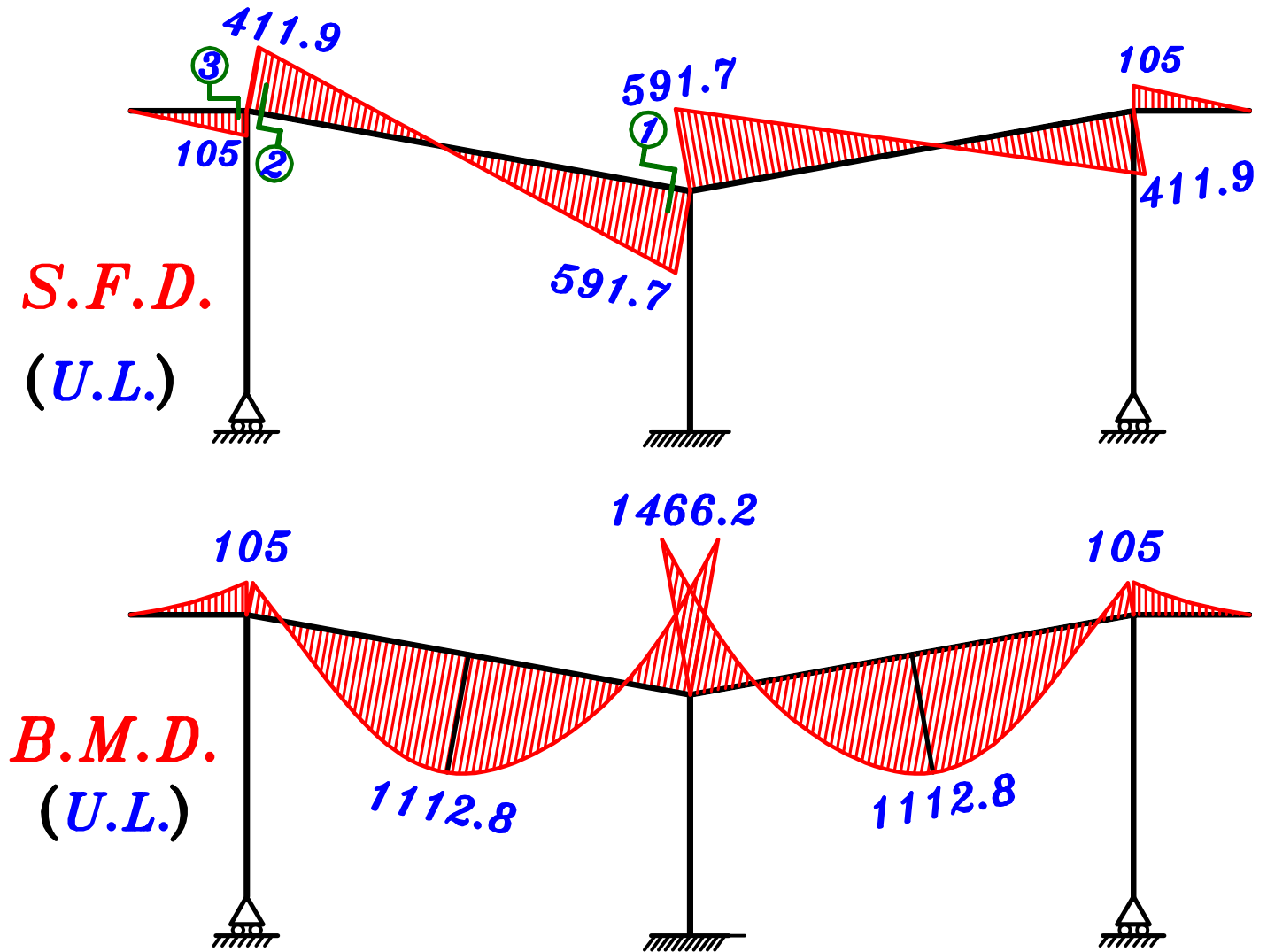
$$\therefore \text{take } A_s = A_{s'} = \frac{A_{s_{min.}}}{2} = \frac{3920}{2} = 1960 \text{ mm}^2$$

4 ϕ 25

يجب أن يكون التسليح متساوى فى الجهتين لان العزم من الممكن ان يكون موجود فى ايا من الجهتين .

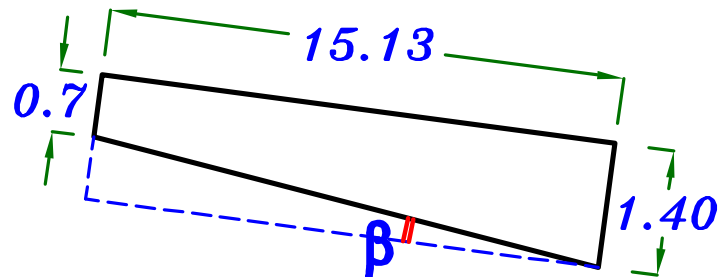


5- Check shear stresses at the critical sections.



Check Shear.

$$q_U = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2}$$



$$\tan \beta = \frac{0.7}{15.13} = 0.046$$

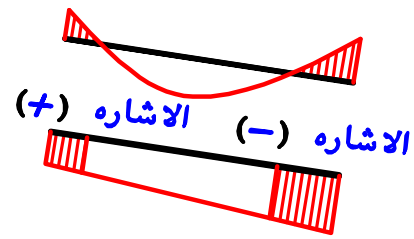
- Allowable shear stress.

$$- q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{35}{1.5}} = 1.16 \text{ N/mm}^2$$

$$- q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{35}{1.5}} = 3.38 \text{ N/mm}^2$$

Sec. ① $Q = 591.7 \text{ kN}$, $M = 1466.2 \text{ kN.m}$

$d = 1300 \text{ mm}$



$$q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2} = \frac{591.7 \cdot 10^3}{350 \cdot 1300} - \frac{1466.2 \cdot 10^6 \cdot 0.046}{350 \cdot 1300^2} = 1.186 \text{ N/mm}^2$$

$\therefore q_{cu} < q_u < q_{max} \therefore$ We need Stirrups more Than $5 \phi 8 \setminus m$

\therefore Use $q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \setminus \gamma_s)}{b S}$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.186 - \frac{1.16}{2} = \frac{2 \cdot 50.3 (240 \setminus 1.15)}{350 \cdot S} \rightarrow S = 98.9 \text{ mm} < 100 \text{ mm}$$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

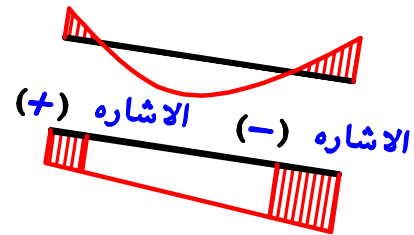
$$1.186 - \frac{1.16}{2} = \frac{2 \cdot 78.5 (240 \setminus 1.15)}{350 \cdot S} \rightarrow S = 154.5 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

\therefore No. of stirrups $\setminus m = \frac{1000}{S} = \frac{1000}{154.5} = 6.47 = 7.0$

\therefore Use Stirrups $7 \phi 10 \setminus m$ 2 branches

Sec. ② $Q = 411.9 \text{ kN}$, $M = 105 \text{ kN.m}$

$d = 650 \text{ mm}$



$$q_u = \frac{Q}{b d} - \frac{M \tan \beta}{b d^2} = \frac{411.9 \cdot 10^3}{350 \cdot 650} - \frac{105 \cdot 10^6 \cdot 0.046}{350 \cdot 650^2} = 1.78 \text{ N/mm}^2$$

$\therefore q_{cu} < q_u < q_{max} \therefore$ We need Stirrups more Than $5 \phi 8 \setminus m$

\therefore Use $q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \setminus \gamma_s)}{b S}$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.78 - \frac{1.16}{2} = \frac{2 * 50.3 (240 \setminus 1.15)}{350 * S} \rightarrow S = 50.0 \text{ mm} < 100 \text{ mm}$$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

$$1.78 - \frac{1.16}{2} = \frac{2 * 78.5 (240 \setminus 1.15)}{350 * S} \rightarrow S = 78.15 \text{ mm} < 100 \text{ mm}$$

* Take $n = 4$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.78 - \frac{1.16}{2} = \frac{4 * 50.3 (240 \setminus 1.15)}{350 * S} \rightarrow S = 100.15 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$$

$$\therefore \text{No. of stirrups} \setminus m = \frac{1000}{S} = \frac{1000}{100.15} = 9.98 = 10.0$$

\therefore Use Stirrups $10\phi 8 \setminus m$ 4 branches

Sec. ③ $Q = 105.0 \text{ kN}$

$$\therefore q_v = \frac{Q}{b d} = \frac{105.0 * 10^3}{350 * 650} = 0.461 \text{ N} \setminus \text{mm}^2$$

$$\therefore q_v < q_{cu} \rightarrow \text{Use min. stirrups } 5\phi 8 \setminus m \text{ 2 branches}$$

6-Design column (a-b) as a braced column.

$$P_{U.L.} = 520.5 \text{ kN}$$

① In plane. $t = 0.70 \text{ m}$

Upper Case ①
Lower Case ① } $k = 0.75$

$$H_o = 7.65 \text{ m}$$

$$\lambda_b = \frac{0.75 * 7.65}{0.70} = 8.19 < 15$$

② Out of plane. $t = 0.35 \text{ m}$

Upper Case ①
Lower Case ① } $k = 0.75$

$$H_o = 7.90 \text{ m}$$

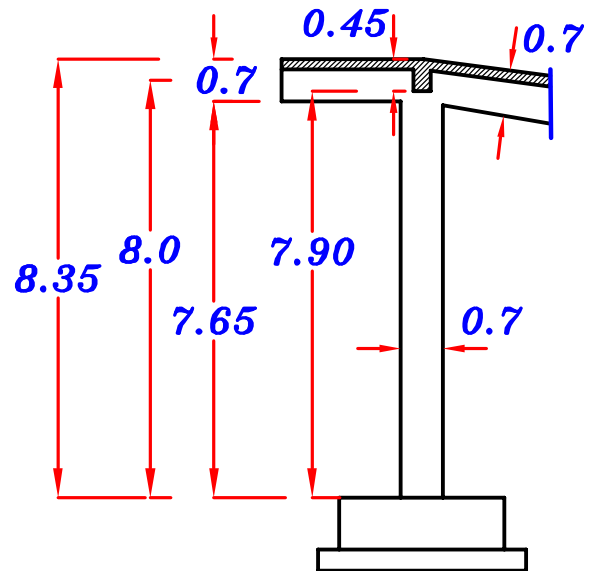
$$\lambda_b = \frac{0.75 * 7.90}{0.35} = 16.92 > 15 \text{ Long column}$$

Take the bigger value of $\lambda_b = 16.92$ (Out of plane)

The Buckling Out of plane.

$$\delta = \frac{(\lambda_b)^2 * b}{2000} = \frac{16.92^2 * 0.35}{2000} = 0.050 \text{ m}$$

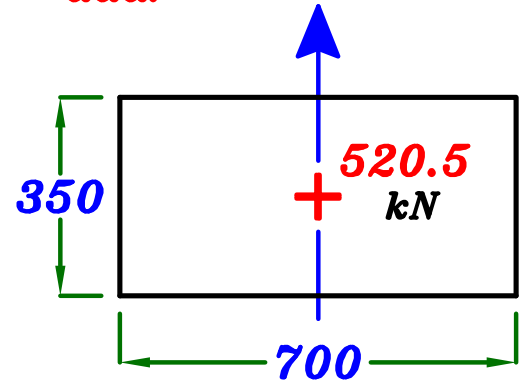
$$M_{add.} = P * \delta = 520.5 * 0.050 = 26.02 \text{ kN.m}$$



$$e = \delta = \frac{M}{P} = \frac{26.02}{520.5} = 0.05 \text{ m}$$

$$M_{add.} = 26.02 \text{ kN.m}$$

$$\frac{e}{t} = \frac{0.05}{0.35} = 0.143 < 0.5 \xrightarrow{\text{use}} I.D.$$



$$\zeta = \frac{0.35 - 0.1}{0.35} = 0.71 \xrightarrow{\text{Take}} \zeta = 0.7 \xrightarrow{\text{Use}} I.D. \quad \boxed{\text{ECCS Page (4-25)}}$$

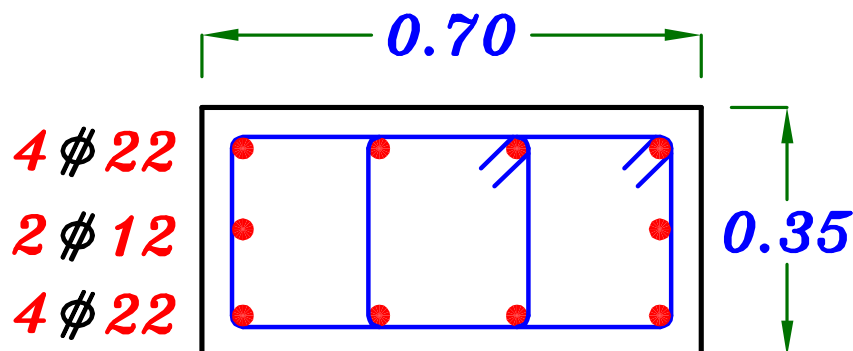
$$\left. \begin{aligned} \frac{P_U}{F_{cu} b t} &= \frac{520.5 * 10^3}{35 * 700 * 350} = 0.060 \\ \frac{M_U}{F_{cu} b t^2} &= \frac{26.02 * 10^6}{35 * 700 * 350^2} = 0.008 \end{aligned} \right\} \rho < 1.0 \xrightarrow{\text{Take}} \rho = 1.0$$

$$A_s = A_{s'} = \mu * b * t = \rho * F_{cu} * 10^{-4} * b * t = 1.0 * 35 * 10^{-4} * 700 * 350 = 857.5 \text{ mm}^2$$

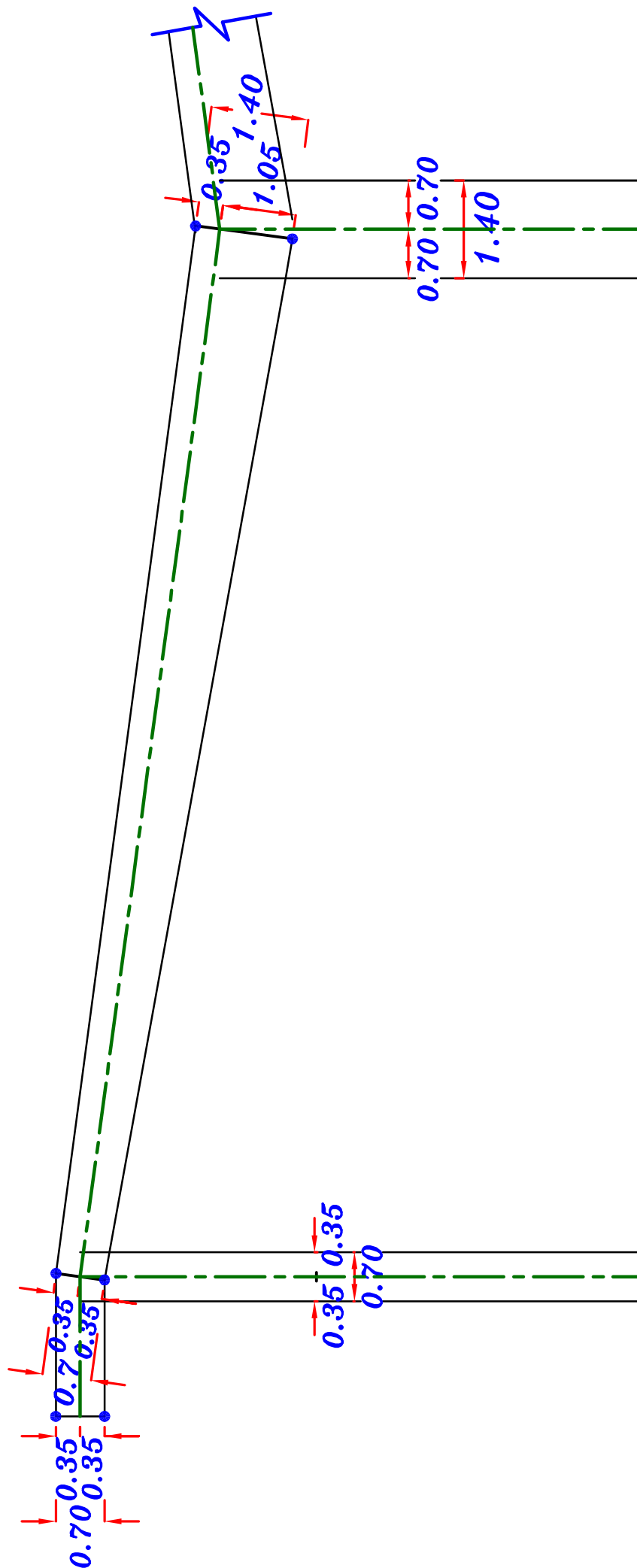
$$A_{s_{total}} = A_s + A_{s'} = 1715 \text{ mm}^2$$

$$\begin{aligned} A_{s_{min}} &= \frac{0.25 + 0.052 \lambda_{max}}{100} * b * t \\ &= \frac{0.25 + 0.052 (16.92)}{100} * 700 * 350 = 2768 \text{ mm}^2 > A_{s_{total}} \end{aligned}$$

$$A_s = A_{s'} = \frac{A_{s_{min}}}{2} = \frac{2768}{2} = 1384 \text{ mm}^2 \quad \textcircled{4 \phi 22}$$

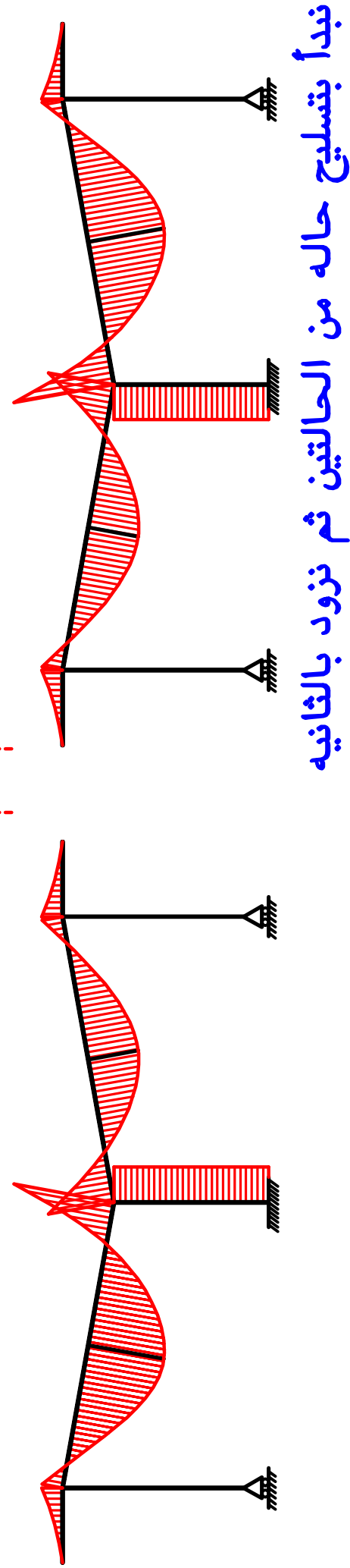
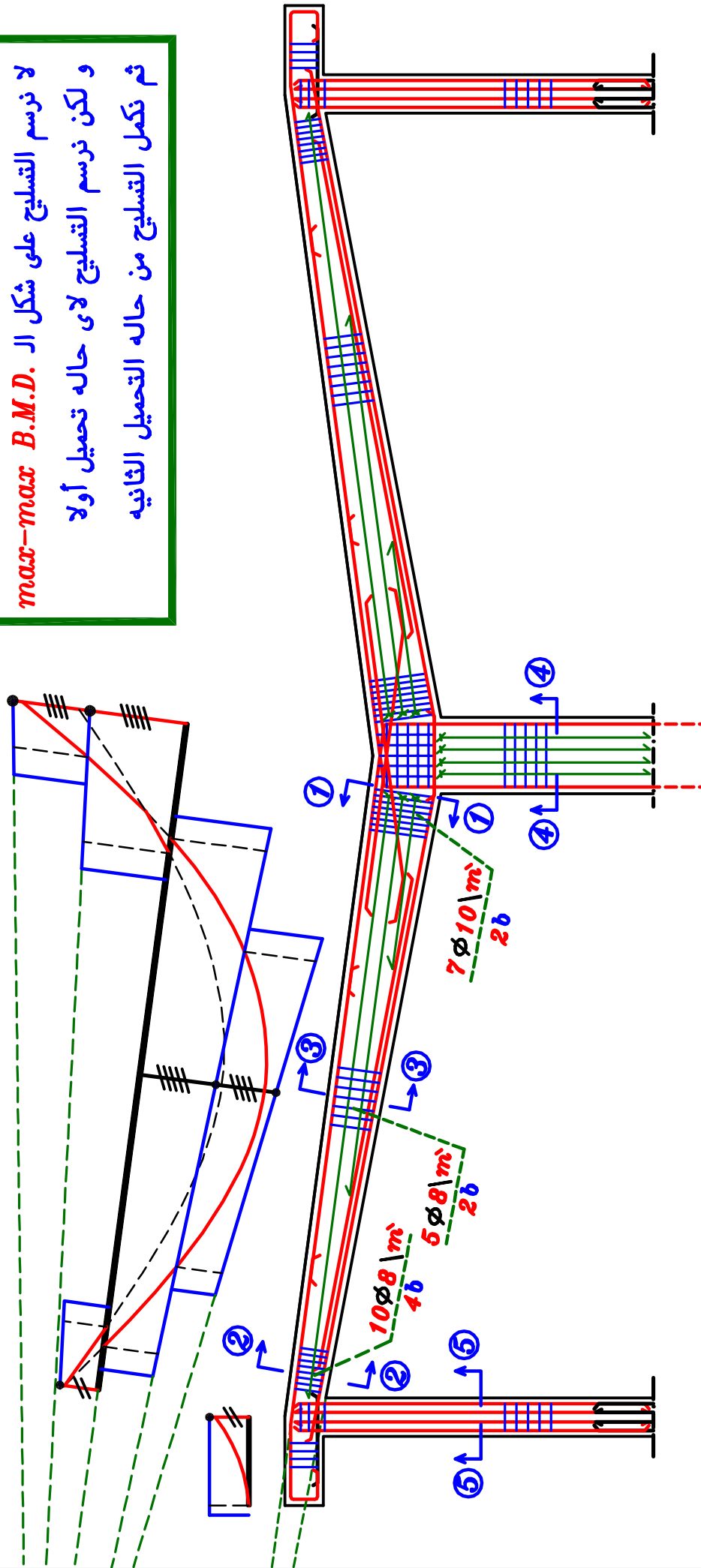


7— Draw the concrete dimensions and the details of reinforcement in elevation and cross-sections to an appropriate scale.



R.F.T. of the Frame.

لا نرسم التسليح على شكل ال *max-max B.M.D.*
و لكن نرسم التسليح لاي حالة تحميل أولا
ثم نكمل التسليح من حالة التحميل الثانيه



نبدأ بتسليح حاله من الحالتين ثم نزود بالثانيه

